

Growth Viewpoints

# The "Knowledge Production Function"

✤ <u>Question</u>: How do inputs to innovative activity map into innovations and new firms?

$$\frac{dA}{dt} = q(H, K, Z, A)$$

✤ Inputs

- Human capital (H), physical capital (K)
- Institutions (Z)
- Current state of ideas (A)

✤ How do we understand the role of human capital, especially in light of views/models of the creative process? Endogenous Growth Viewpoints: Romer Approach

✤ Romer (1990) et cetera assumed

$$\frac{dA}{dt} = \delta A L_A$$

Inputs are (1) effort  $(L_A)$  and (2) current stock of ideas (A)

 $\clubsuit$  Growth rate in economy (divide through by A) is

 $g_A = \delta L_A$ 

Implication: growth rate follows the level of innovative effort

### Recall Growth Theory's Second Approach

\* C. Jones (1995) showed empirically that a constant growth rate appears consistent with *growing* innovative effort, not with a constant *level* of innovative effort

✤ Led to a generalization

$$\frac{dA}{dt} = \delta A^{\phi} L_A^{\lambda} \quad \Rightarrow \quad g_A = \frac{\lambda}{1 - \phi} g_{L_A}$$

Allows limited increase in idea production *per researcher* along the growth path  $(0 < \phi < 1)$ ; perhaps even declining idea production per researcher  $(\phi < 0)$ .

✤ Now we need to grow labor supply

### Digging Deeper: Three Models of the Creative Process

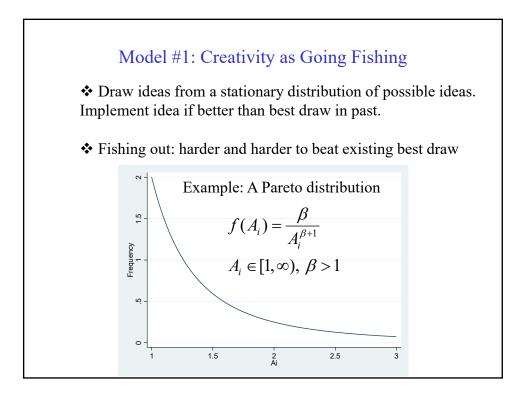
Fishing Out (Kortum 1997)

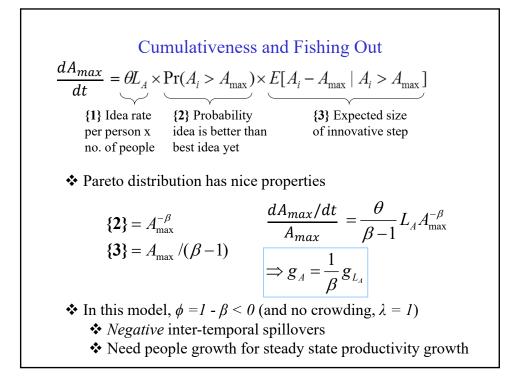
Recombination (Weitzman 1998)

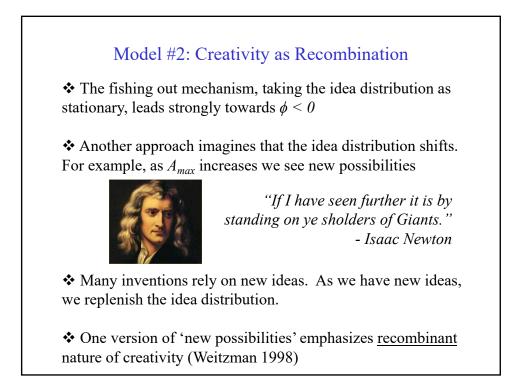
Burden of Knowledge (B. Jones 2009)

Thinking especially about how current stock of ideas influences further idea production, based on particular views of the *underlying creative process*.

This leads to insights (from simple to more complex) about the role of innovative labor supply / human capital.







# Creativity as Combinations

 Darwin: evolution as random mutation (new) + selection (old: animal husbandry)

Edison: Light bulb = candle (old) + electricity (new)

Mullis: DNA replication technology = DNA (new) + polymerase enzyme (new)

#### Cumulativeness as an Improving Distribution

Example: A Pareto distribution where new ideas are always better than current best idea

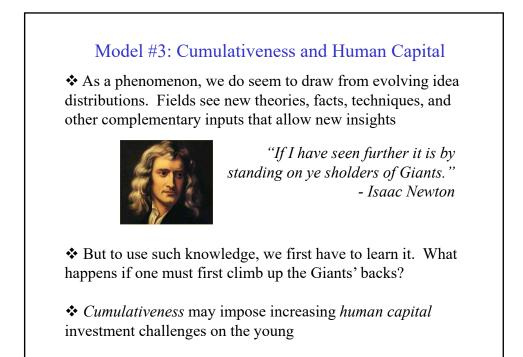
$$f(A_i) = \frac{\beta A_{\max}^{\beta}}{A_i^{\beta+1}}, \ A_i \in [A_{\max}, \infty), \ \beta > 1$$

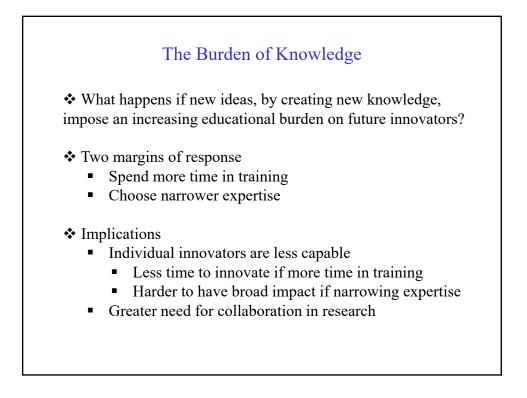
So idea production function is now

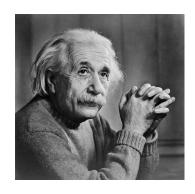
$$\frac{dA_{max}}{dt} = \theta L_A \times \underbrace{\Pr(A_i > A_{max})}_{\{2\}=1 \text{ now}} \times \underbrace{E[A_i - A_{max} \mid A_i > A_{max}]}_{\{3\}=A_{max}/(\beta-1)}$$

$$\frac{dA_{max}/dt}{A_{max}} = \frac{\theta}{\beta - 1} L_A$$

We return to initial Romer world: growth follows effort *level*. But of course this does not appear valid empirically...

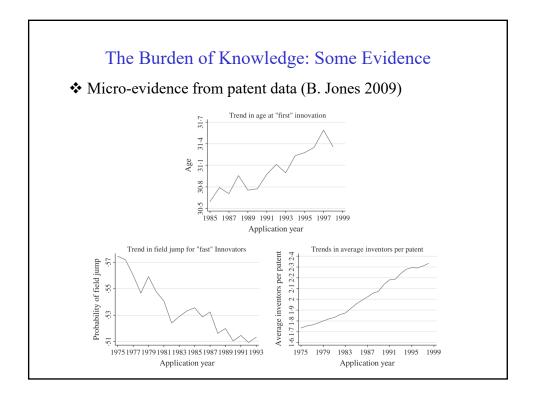


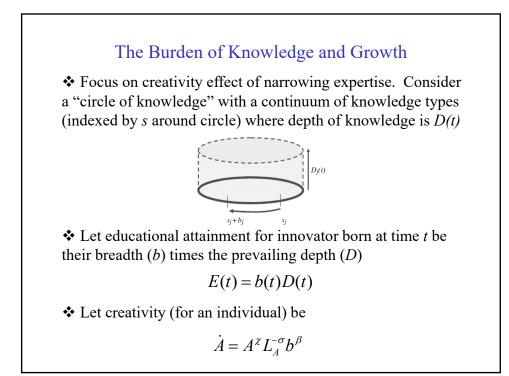




"...knowledge has become vastly more profound in every department of science. But the assimilative power of the human intellect is and remains strictly limited. Hence it was inevitable that the activity of the individual investigator should be confined to a smaller and smaller section..."

-- Albert Einstein (1932)





### The Burden of Knowledge and Growth

✤ Let the depth of knowledge follow the stock of existing ideas

$$D = A^{\circ} \Longrightarrow g_D = \delta g_A$$

★ In equilibrium, individuals choose educational expenditure as a constant fraction of lifetime income, E(t)/y(t) = c, implying

$$g_E = g_y = g_A$$

Thus individual educational attainment grows along the growth path at the same growth rate as the economy

✤ From educational attainment equation we then have

$$E(t) = b(t)D(t) \Longrightarrow g_b = g_E - g_D \Longrightarrow$$
$$g_b = (1 - \delta)g_A$$

#### The Burden of Knowledge and Growth

 $\clubsuit$  Growth rate of economy is

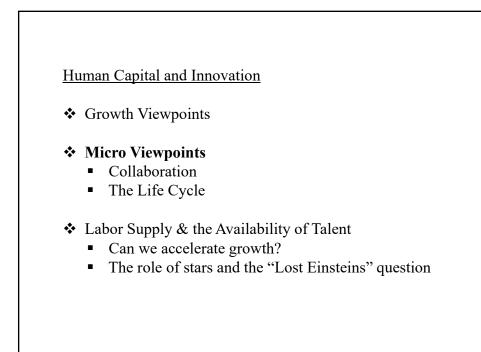
 $\dot{A} = A^{\chi} L_A^{1-\sigma} b^{\beta} \implies \dot{A} / A = A^{\chi-1} L_A^{1-\sigma} b^{\beta}$ 

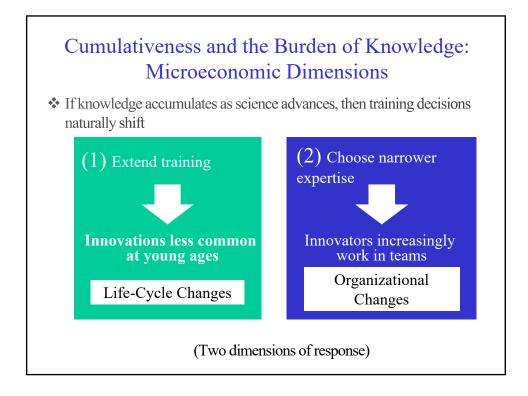
★ For steady-state growth, take logs, differentiate with respect to time, plug in  $g_b = -(\delta - l)g_A$  and rearrange:

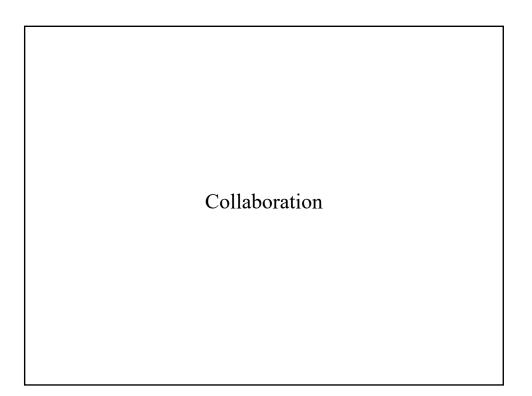
$$g_{A} = \frac{1-\sigma}{1-\chi+\beta(\delta-1)}g_{L_{A}}$$

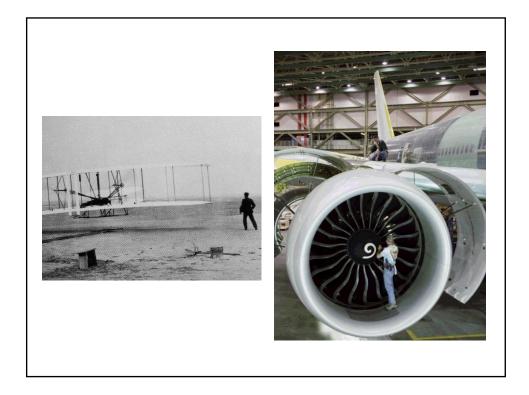
Relating to prior models, the crowding term is  $\lambda = 1 - \sigma$ , and the inter-temporal spillover term is  $\phi = \chi - \beta(\delta - 1)$ 

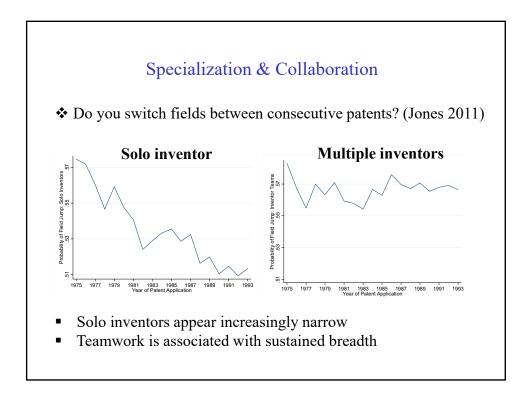
• With increasing specialization  $(\delta > 1)$ , we can now have rich idea possibilities (large  $\chi$ ) and yet still explain macro facts ( $\phi < 1$ ) because individual innovators see narrowing share

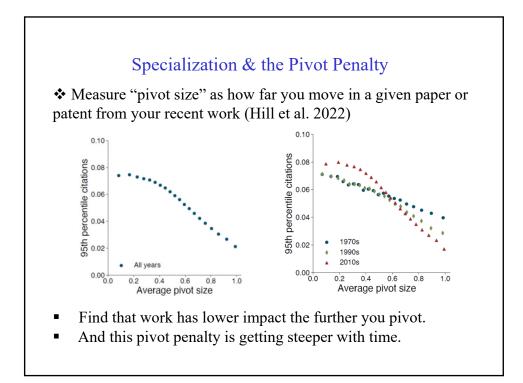


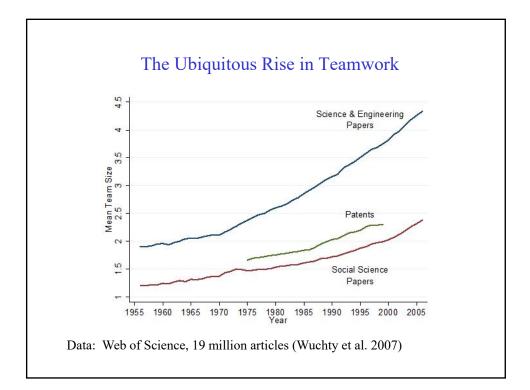


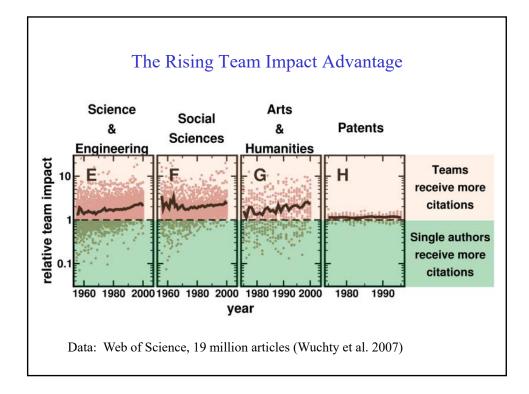


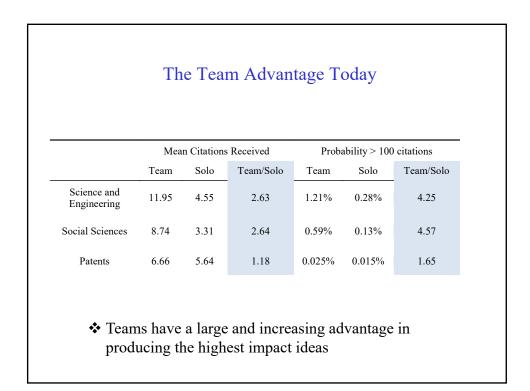


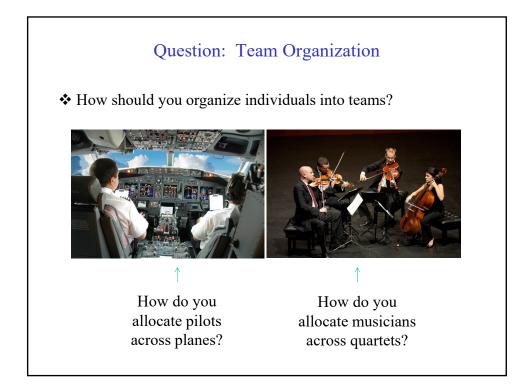


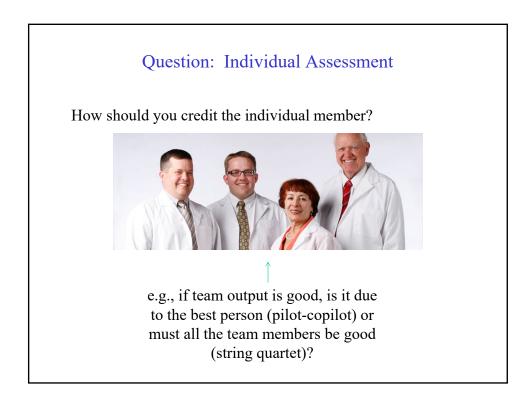


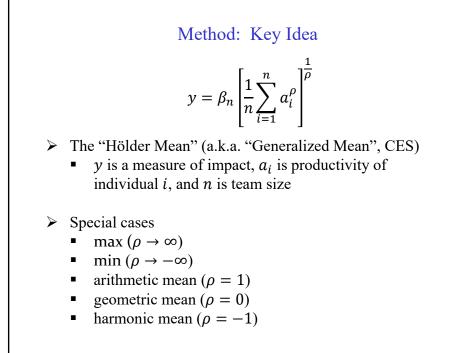


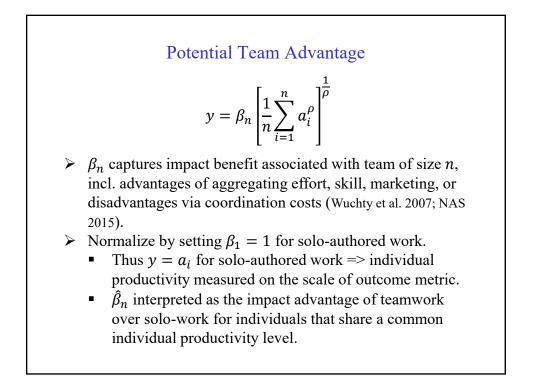






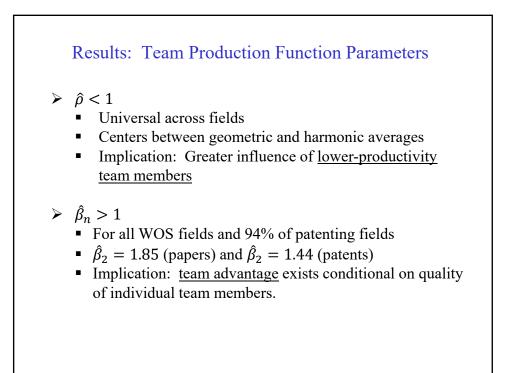


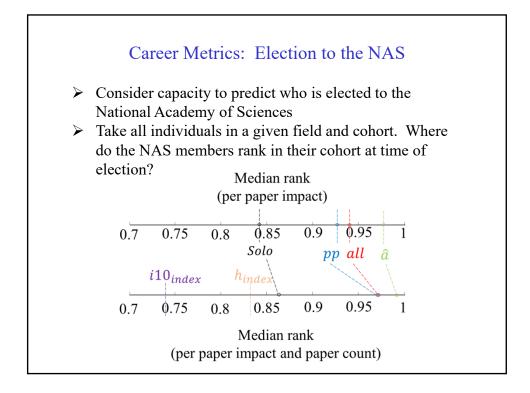


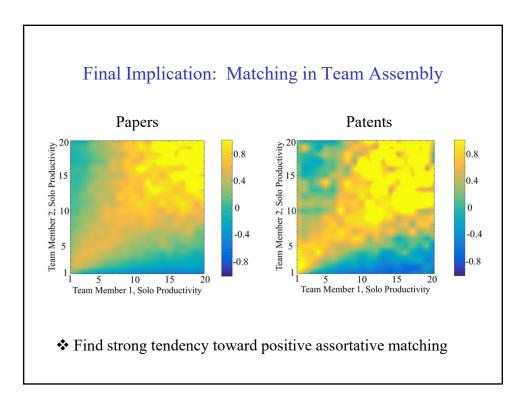


### Data Sets

- ➢ Web of Science, 1945-2005
  - All 185 science & engineering and social science fields with ≥ 500 papers
  - Author name disambiguation from WOS (Bai 2016)
- ▶ USPTO, 1975-2006
  - All 384 tech classes with  $\geq$  500 patents
  - Inventor name disambiguation from Li et al. (2014)
- ➤ Restrict to papers/patents with <= 8 team members
  - 97% of papers and 99% of patents
  - 24 million journal articles, 13 million authors (WOS)
  - 3.9 million patents, 2.6 million inventors (USPTO)

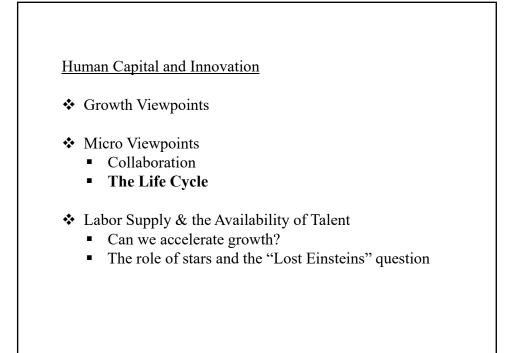


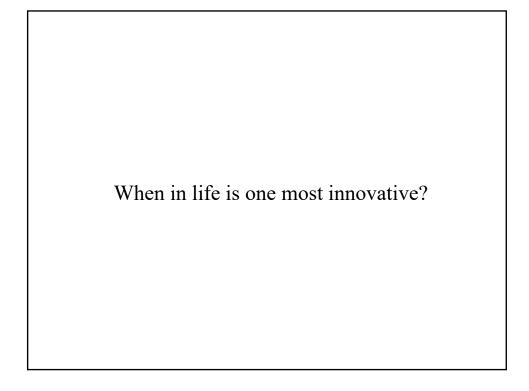


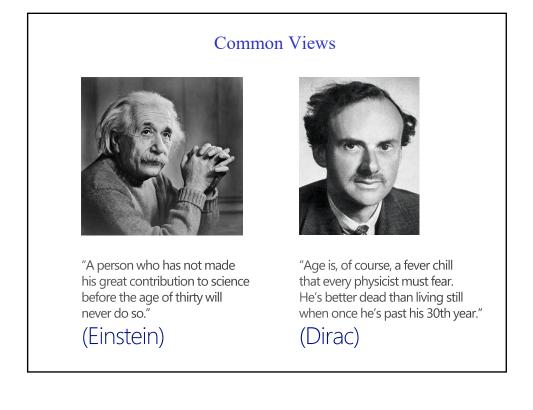


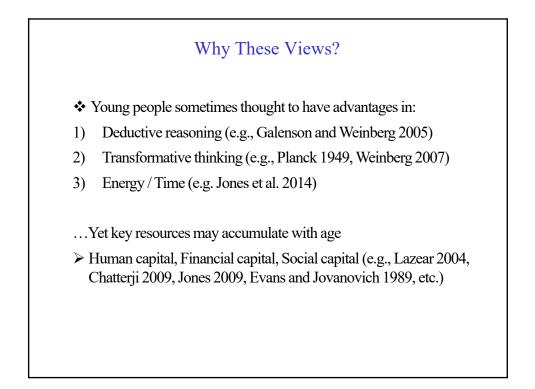
### Summary: Collaboration

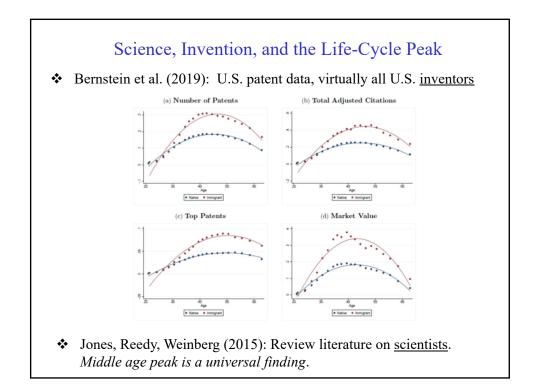
- ➢ Big dynamics
  - People increasingly work in teams in all fields
  - Highest impact ideas increasingly come from teams
  - Researchers experience increasing impact penalties when moving into new areas
    - (Burden of knowledge reasoning may explain patterns)
- Team production: Innovation teams appear like "string quartets." Consistent with "specialist" teams.
  - Positive assortative matching
- Individual assessment: How we credit individuals is essential to career progression, incentives, etc.
  - "Decoding teams" method to confront teamwork challenge

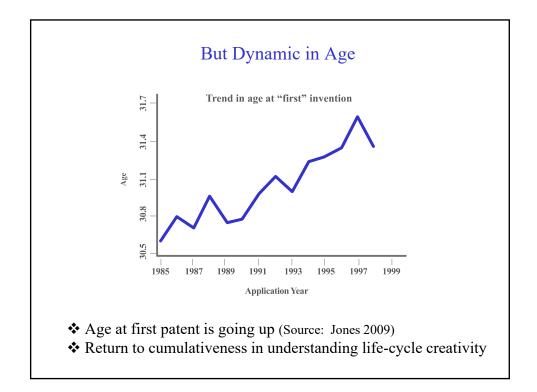


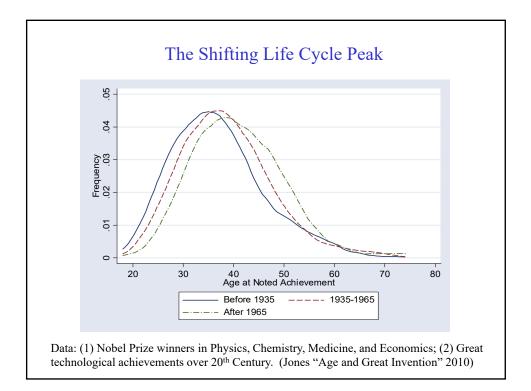


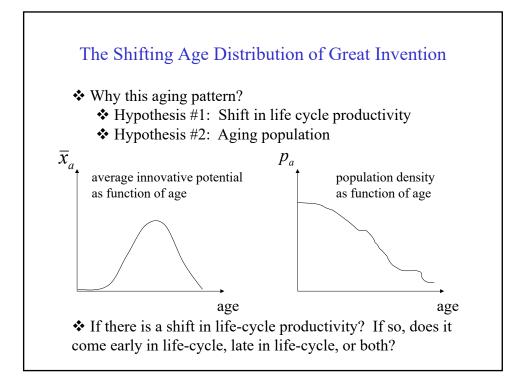


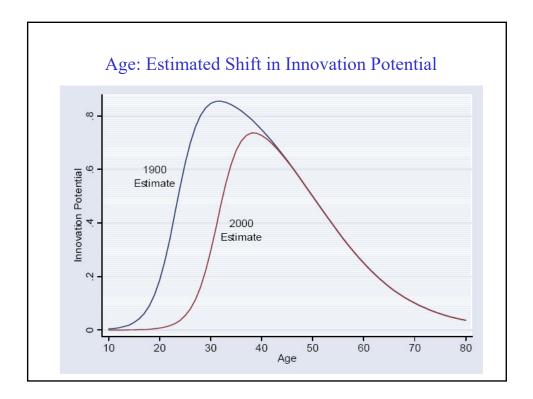


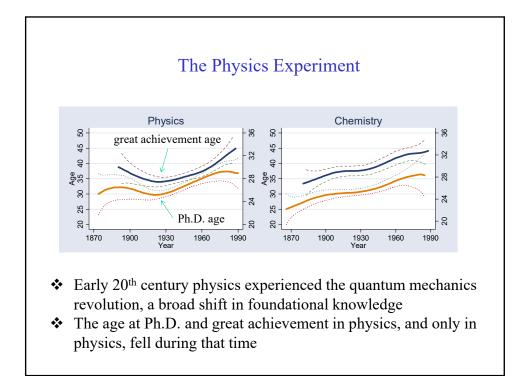


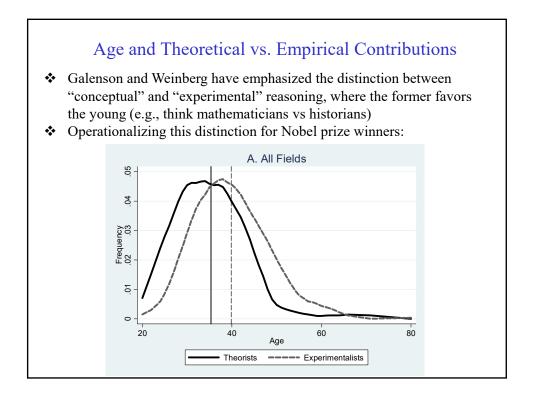


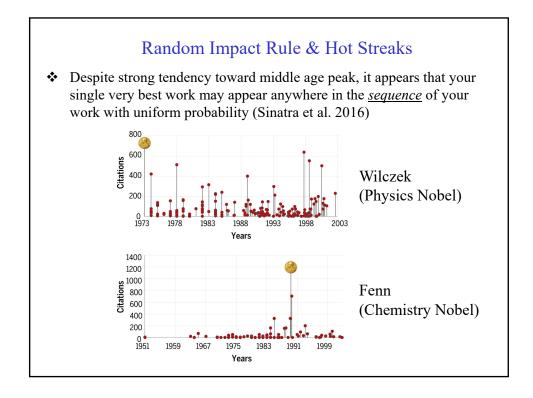


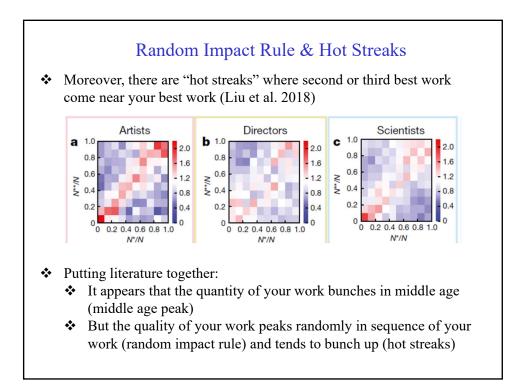












The Life Cycle: Entrepreneurship

# Beyond Technical Knowledge: Kline and Rosenberg (1986)

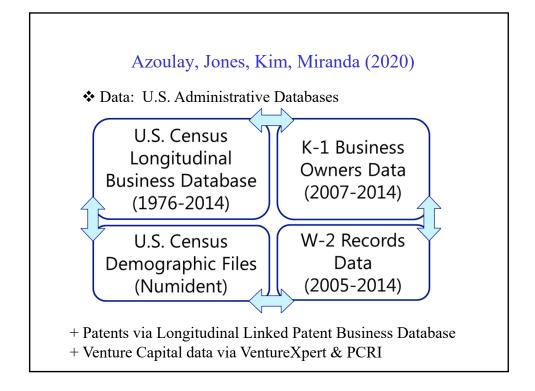
✤ "But technical success (or any purely mechanical measure of performance) is only a necessary and not a sufficient condition in establishing economic usefulness. Indeed, it is obvious from a casual examination of the proceedings in our bankruptcy courts that an excessive or exclusive preoccupation with purely technical measures of performance can be disastrous."

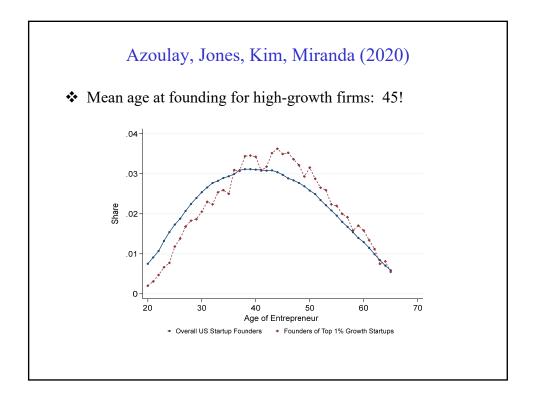
✤ "Successful innovation requires the coupling of the technical and the economic in ways that can be accommodated by the organization while also meeting market needs, and this implies close coupling and cooperation among many activities in the marketing, R&D, and production functions."

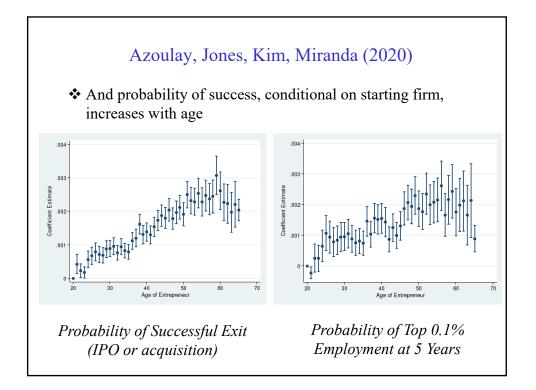


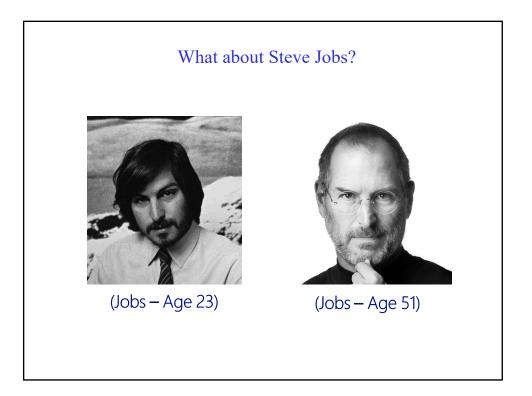
Perception: A Youth Advantage onsider media focus, and VC focus				
	TechCrunch Awards	Inc. and Entrepreneur Magazines	Sequoia	Matrix Partners
Mean	31.0	29.1	33.9	36.5
Median	30	27	33	36
(St. Dev.)	(7.1)	(7.0)	(8.7)	(8.6)
Observations	232	51	415	246
Period	2008-2016	2015	1969-2014	1948-2014
Sectoral Focus (top 5)	Education, Software, Social Media, Consumer Electronics, e-Commerce	Technology, Retail, Media, Consumer Goods, Food Delivery	Semiconductors, Networks, Task Mgmt Apps, Website Compilers, Cloud	Networks, Applications, Commerce, Platform/ Infrastructure, Semiconductors/ Materials

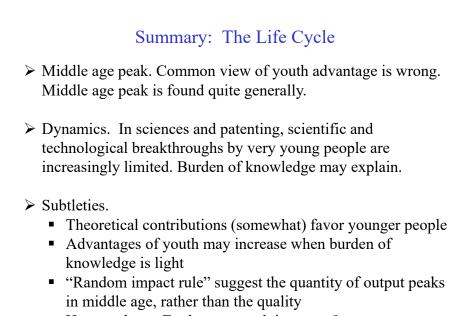
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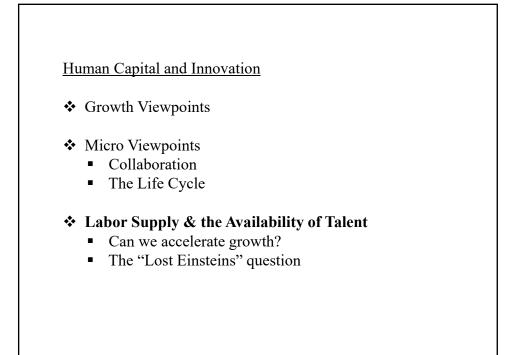


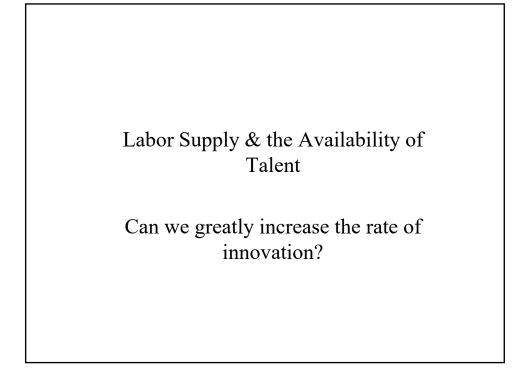


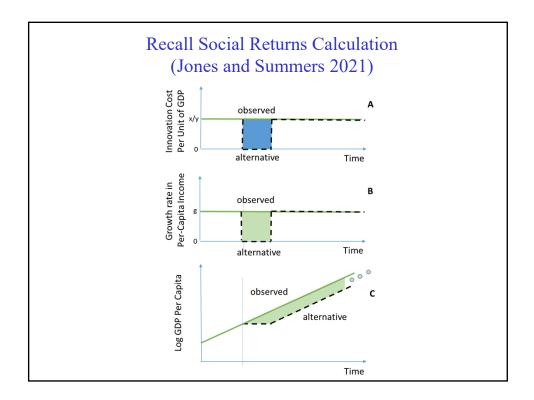




• Hot streaks.... Explore vs. exploit pattern?







#### **Baseline** Calculation

The average social return (benefit cost ratio) is then

$$\rho = \frac{g/r}{x/y} \approx \mathbf{10}?$$

This calculation suggests that the average social returns to innovation investments are really, really high.

But policy is interested in the marginal return. Would we achieve a high return for *additional* effort at innovation?

#### The Average vs. the Margin: Growth Model #1

Consider initial class of endogenous growth models (Romer 1990, Aghion and Howitt 1992)

$$g_A = \gamma L_R \tag{1}$$

.

*Lemma 1*: For the knowledge production function, (1), the marginal social rate of return to R&D is

$$\rho_{marginal} = \frac{g/r}{x/y}$$

Here there are no diminishing returns to R&D effort and large intertemporal spillovers. The average and social returns are the same! But this model leads to the "scale effects" problem.

#### The Average vs. the Margin: Growth Model #2

Consider endogenous growth models where growing effort is need to drive steady-state growth (Jones 1995, Kortum 1997, Jones 2009, Bloom et al. 2020)

$$g_A = \delta A(t)^{\theta - 1} L_R(t)^{\sigma} \tag{2}$$

*Lemma 2*: For the knowledge production function, (2), the marginal social rate of return to R&D is

$$\rho_{marginal} = \frac{\sigma}{1 - (\theta - \sigma)(g/r)} \frac{g/r}{x/y}$$

Here we can have diminishing returns to R&D effort ( $\sigma$ ) and various degrees of intertemporal spillovers ( $\theta$ ).

#### The Average vs. the Margin: Growth Model #2

So, in principle, marginal return to more innovative effort could be quite low. One reason would be that talent is limited, giving steep diminishing marginal returns to increasing  $L_R(t)$ .

Where does the talent come from? Are there steep diminishing returns?

Channels for more "innovative human capital"

- Immigration
- Domestic creation

Counter view

High end talent essential, and this is fundamentally limited

