Are Ideas Getting Harder to Find?

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July 11, 2017 — Version 0.8

Abstract

In many growth models, economic growth arises from people creating ideas, and the long-run growth rate is the product of two terms: the effective number of researchers and their research productivity. We present a wide range of evidence from various industries, products, and firms showing that research effort is rising substantially while research productivity is declining sharply. A good example is Moore's Law. The number of researchers required today to achieve the famous doubling every two years of the density of computer chips is more than 15 times larger than the number required in the early 1970s. Across a broad range of case studies at various levels of (dis)aggregation, we find that ideas — and in particular the exponential growth they imply — are getting harder and harder to find. Exponential growth results from the large increases in research effort that offset its declining productivity.

^{*}We are grateful to Daron Acemoglu, Ufuk Akcigit, Michele Boldrin, Pete Klenow, Peter Kruse-Andersen, Rachel Ngai, Pietro Peretto, John Seater, Chris Tonetti, and seminar participants at the CEPR Macroeconomics and Growth Conference, George Mason, Harvard, the NBER Macro across Time and Space conference, the Rimini Conference on Economics and Finance, and Stanford for helpful comments and to Antoine Dechezlepretre, Dietmar Harhoff, Wallace Huffman, Keith Fuglie, Unni Pillai, and Greg Traxler for extensive assistance with data. The European Research Council and ESRC have provided financial support.

1. Introduction

This paper applies the growth accounting of Solow (1957) to the production function for new ideas. The basic insight can be explained with a simple equation, highlighting a stylized view of economic growth that emerges from idea-based growth models:

Economic
growthResearch
productivityNumber of
researcherse.g. 2% or 5% \downarrow (falling) \uparrow (rising)

Economic growth arises from people creating ideas. As a matter of accounting, we can decompose the long-run growth rate as the product of two terms: the effective number of researchers and their research productivity. We present a wide range of empirical evidence showing that in many different contexts and at various levels of disaggregation, research effort is rising substantially, while research productivity is declining sharply. Steady growth, when it occurs, results from the offsetting of these two trends.

Perhaps the best example of this finding comes from studying Moore's Law, one of the key drivers of economic growth in recent decades. This "law" refers to the empirical regularity that the number of transistors packed onto a computer chip doubles approximately every two years. Such doubling corresponds to a constant exponential growth rate of around 35% per year, a rate that has been remarkably steady for nearly half a century. As we show in detail below, this growth has been achieved by putting an evergrowing number of researchers to work on pushing Moore's Law forward. In particular, the number of researchers required to achieve the doubling of chip density today is more than 15 times larger than the number required in the early 1970s. At least as far as semiconductors are concerned, ideas are getting harder and harder to find. Research productivity in this case is declining sharply, at a rate that averages about 6.5% per year.

We document qualitatively similar results essentially no matter where we look in the U.S. economy. We consider detailed microeconomic evidence on idea production functions, focusing on places where we can get the best measures of both the output of ideas and the inputs used to produce them. In addition to Moore's Law, our case studies include agricultural productivity (corn, soybeans, cotton, and wheat) and medical innovations. Research productivity for seed yields declines at about 5% per year. We find a similar rate of decline when studying the mortality improvements associated with cancer and heart disease. Finally, we examine firm-level data from Compustat to provide another perspective on research productivity. While the data quality from this sample is not as good as for our industry case studies, the latter suffer from possibly not being representative. We find substantial heterogeneity across firms, but research productivity is declining in more than 85% of the firms in our sample. Averaging across firms, research productivity declines at a rate of around 10% per year.

Perhaps research productivity is declining sharply within every particular case that we look at and yet not declining for the economy as a whole. While existing varieties run into diminishing returns, perhaps new varieties are always being invented to stave this off. We consider this possibility by taking it to the extreme. Suppose each variety has a productivity that cannot be improved at all, and instead aggregate growth proceeds entirely by inventing new varieties. To examine this case, we consider research productivity for the economy as a whole. We once again find that it is declining sharply: aggregate growth rates are relatively stable over time,¹ while the number of researchers has risen enormously. In fact, this is simply another way of looking at the original point of Jones (1995), and for this reason, we present this application first to illustrate our methodology. We find that research productivity for the aggregate U.S. economy has declined by a factor of 41 since the 1930s, an average decrease of more than 5% per year.

Despite these large declines in research productivity, relatively stable exponential growth is common in the cases we study (and in the aggregate U.S. economy). How is this possible? Looking back at the equation that began the introduction, declines in research productivity must be offset by increased research effort, and this is indeed what we find. Moreover, we suggest at the end of the paper that the rapid declines in research productivity that we see in semiconductors, for example, might be precisely due to the fact that research effort is rising so sharply. Because it gets harder to find new ideas as research progresses, a sustained and massive expansion of research like we see in semiconductors (for example, because of the "general purpose technology"

¹There is a debate over whether the slower rates of growth over the last decade are a temporary phenomenon due to the global financial crisis, or a sign of slowing technological progress. Gordon (2016) argues that the strong US productivity growth between 1996 and 2004 was a temporary blip and that productivity growth will, at best, return to the lower growth rates of 1973–1996. Although we do not need to take a stance on this, note that if frontier TFP growth really has slowed down, this only strengthens our argument.

nature of information technology), may lead to a substantial downward trend in research productivity.

Others have also provided evidence suggesting that ideas may be getting harder to find over time. Griliches (1994) provides a summary of the earlier literature exploring the decline in patents per dollar of research spending. Gordon (2016) reports extensive new historical evidence from throughout the 19th and 20th centuries. Cowen (2011) synthesizes earlier work to explicitly make the case. (Ben) Jones (2009) documents a rise in the age at which inventors first patent and a general increase in the size of research teams, arguing that over time more and more learning is required just to get to the point where researchers are capable of pushing the frontier forward. We see our evidence as complementary to these earlier studies but more focused on drawing out the tight connections to growth theory.

The remainder of the paper is organized as follows. Section 2 lays out our conceptual framework and presents the aggregate evidence on research productivity to illustrate our methodology. Section 3 places this framework in the context of growth theory and suggests that applying the framework to micro data is crucial for understanding the nature of economic growth. Sections 4 through 7 consider our applications to Moore's Law, agricultural yields, medical technologies, and Compustat firms. Section 8 then revisits the implications of our findings for growth theory, and Section 9 concludes.

2. Research Productivity and Aggregate Evidence

2.1. The Conceptual Framework

An equation at the heart of many growth models is an idea production function taking a particular form:

$$\frac{\dot{A}_t}{A_t} = \alpha S_t. \tag{1}$$

Classic examples include Romer (1990) and Aghion and Howitt (1992), but many recent papers follow this approach, including Aghion, Akcigit and Howitt (2014), Acemoglu and Restrepo (2016), Akcigit, Celik and Greenwood (2016), and Jones and Kim (2014). In the equation above, \dot{A}_t/A_t is total factor productivity growth in the economy. The variable S_t (think "scientists") is some measure of research input, such as the number of researchers. This equation then says that the growth rate of the economy — through the production of new ideas — is proportional to the number of researchers.

Relating \dot{A}_t/A_t to ideas runs into the familiar problem that ideas are hard to measure. Even as simple a question as "What are the units of ideas?" is troublesome. We follow much of the literature — including Aghion and Howitt (1992), Grossman and Helpman (1991), and Kortum (1997) — and define ideas to be in units so that a constant flow of new ideas leads to constant exponential growth in A. For example, each new idea raises incomes by a constant percentage (on average), rather than by a certain number of dollars. This is the standard approach in the quality ladder literature on growth: ideas are proportional improvements in productivity. The patent statistics for most of the 20th century are consistent with this view; indeed, this was a key piece of evidence motivating Kortum (1997). This definition means that the left hand side of equation (1) corresponds to the flow of new ideas.

We can now define the productivity of the idea production function as the ratio of the output of ideas to the inputs used to make them:

Research productivity :=
$$\frac{\dot{A}_t/A_t}{S_t} = \frac{\# \text{ of new ideas}}{\# \text{ of researchers}}.$$
 (2)

The null hypothesis tested in this paper comes from the relationship assumed in (1). Substituting this equation into the definition of research productivity, we see that (1) implies that research productivity equals α — that is, research productivity is constant over time. This is the standard hypothesis in much of the growth literature. Under this null, a constant number of researchers can generate constant exponential growth.

The reason this is such a common assumption is also easy to see in equation (1). With constant research productivity, a research subsidy that increases the number of researchers permanently will permanently raise the growth rate of the economy. In other words "constant research productivity" and the fact that sustained research subsidies produce "permanent growth effects" are equivalent statements.² This clarifies a claim in the introduction: testing the null hypothesis of constant research produc-

²The careful reader may wonder about this statement in richer models — for example, lab equipment models where research is measured in goods rather than in bodies or models with both horizontal and vertical dimensions to growth. These extensions will be incorporated below in such a way as to maintain the equivalence between "constant research productivity" and "permanent growth effects."

tivity is interesting in its own right but also because it is informative about the kind of models that we use to study economic growth. The finding that research productivity is declining virtually everywhere we look poses problems for a large class of endogenous growth models. Moreover, the way we have defined ideas gives this concept economic relevance: exponential growth (e.g. in semiconductor density or seed yields or living standards) is getting harder to find.

2.2. Aggregate Evidence

The bulk of the evidence presented in this paper concerns the extent to which a constant level of research effort can generate constant exponential growth within a relatively narrow category, such as a firm or a seed type or Moore's Law or a health condition. We provide consistent evidence that the historical answer to this question is no: research productivity is declining at a substantial rate in virtually every place we look.

This finding raises a natural question, however. What if there is sharply declining research productivity *within* each product line, but the main way that growth proceeds is by developing ever-better new product lines? First there was steam power, then electric power, then the internal combustion engine, then the semiconductor, then gene editing, and so on. Maybe there is limited opportunity within each area for productivity improvement and long-run growth occurs through the invention of entirely new areas. Maybe research productivity is declining within every product line, but still not declining for the economy as a whole because we keep inventing new products. An analysis focused on microeconomic case studies would never reveal this to be the case.

The answer to this concern turns out to be straightforward and is an excellent place to begin. First, consider the extreme case where there is no possibility at all for productivity improvement in a product line and all productivity growth comes from adding new product lines. Of course, this is just the original Romer (1990) model itself, and to generate constant research productivity in that case requires the equation we started the paper with:

$$\frac{A_t}{A_t} = \alpha S_t. \tag{3}$$

In this interpretation, A_t represents the number of product varieties and S_t is the aggregate number of researchers. Even with no ability to improve productivity within each variety, a constant number of researchers can sustain exponential growth if the varietydiscovery function exhibits constant research productivity.

This hypothesis, however, runs into an important well-known problem.³ For the U.S. economy as a whole, exponential growth rates in GDP per person since 1870 or in total factor productivity since the 1930s — which are related to the left side of equation (3) — are relatively stable or even declining. But measures of research effort — the right side of the equation — have grown tremendously. When applied to the aggregate data, our approach of looking at research productivity is just another way of making this same point.

To illustrate the approach, we use the decadal averages of TFP growth to measure the "output" of the idea production function. For the input, we use the NIPA measure of investment in "intellectual property products," a number that is primarily made up of research and development spending but also includes expenditures on creating other nonrival goods like computer software, music, books, and movies. As explained further below, we deflate this input by a measure of the average annual earnings for people with 4 or more years of college so that it measures the "effective" number of researchers that the economy's R&D spending could purchase. These basic data are shown in Figure 1.

Figure 2 shows research productivity and this measure of research effort by decade. Since the 1930s, research effort has risen by a factor of 23 — an average growth rate of 4.3 percent per year. Research productivity has fallen by an even larger amount — by a factor of 41 (or at an average growth rate of -5.1 percent per year). By construction, a factor of 23 of this decline is due to the rise in research effort and so less than a factor of 2 is due to the well-known decline in TFP growth.

The "new economy" of the 1990s exhibited a bounceback of TFP growth that was even larger than the increase in research in that decade, resulting in a slight increase in research productivity between the 1980s and 1990s. But the overall trend is clear. For example, between the 1960s and the 2000s, research productivity fell by a factor of 8.0. And between the 1980s and the 2000s, it fell by a factor of 1.7, with the entire amount due to rising research effort.

This aggregate evidence could be improved on in many ways. One might question the TFP growth numbers — how much of TFP growth is due to innovation versus real-

³For example, see Jones (1995).

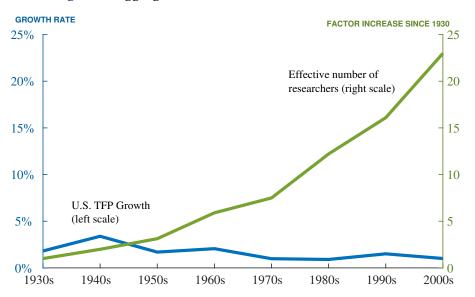


Figure 1: Aggregate Data on Growth and Research Effort

Note: The idea output measure is TFP growth, by decade (and for 2000-2014 for the latest observation). For the years since 1950, this measure is the BLS Private Business Sector multifactor productivity growth series, adding back in the contributions from R&D and IPP. For the 1930s and 1940s, we use the measure from Robert Gordon (2016). The idea input measure is gross domestic investment in intellectual property products from the National Income and Product Accounts, deflated by a measure of the nominal wage for high-skilled workers.

location or declines in misallocation? One might seek to include international research in the input measure. But reasonable variations along these lines would not change the basic point of Figure 2: a model in which economic growth arises from the discovery of newer and better varieties with limited possibilities for productivity growth *within* each variety exhibits sharply-declining research productivity. If one wishes to maintain the hypothesis of constant research productivity, one must look elsewhere. It is for this reason that the literature — and this paper — turns to the micro side of economic growth.

3. Refining the Conceptual Framework

In this section, we further develop the conceptual framework introduced in the previous section. First, we explain why the aggregate evidence just presented can be misleading, motivating our focus on micro data. Second, we consider the measurement

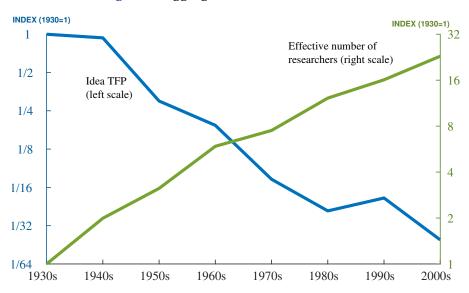
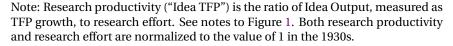


Figure 2: Aggregate Evidence on Idea TFP



of research productivity when the input to research is R&D expenditures (i.e. "goods") rather than just bodies or researchers (i.e. "time"). Finally, we discuss various extensions to our calculation of research productivity.

3.1. The Importance of Micro Data

The null hypothesis that research productivity is constant over time is attractive conceptually in that it leads to models in which changes in policies related to research can permanently affect the growth rate of the economy. Several papers, then, have proposed alternative models in which the calculations using aggregate data can be misleading about research productivity. The insight of Dinopoulos and Thompson (1998), Peretto (1998), Young (1998), and Howitt (1999) is that the aggregate evidence may be masking important heterogeneity, and that research productivity may nevertheless be constant for a significant portion of the economy. Perhaps the idea production function *for individual products* shows constant research productivity. The aggregate numbers may simply capture the fact that every time the economy gets larger we add more products, so the aggregate calculation mismeasures research productivity.⁴

To see the essence of the argument, suppose that the economy produces N_t different products, and each of these products is associated with some quality level A_{it} . Innovation can lead the quality of each product to rise over time according to an idea production function,

$$\frac{A_{it}}{A_{it}} = \alpha S_{it}.$$
(4)

Here, S_{it} is the number of scientists devoted to improving the quality of good *i*, and in a symmetric case, we might have $S_{it} = \frac{S_t}{N_t}$. The key is that the aggregate number of scientists S_t can be growing, but perhaps the number per product S_t/N_t is not growing. This can occur in equilibrium if the number of products itself grows endogenously at the right rate. In this case, the aggregate evidence discussed earlier would not tell us anything about the idea production functions associated with the quality improvements of each variety. Instead, aggregation masks the true constancy of research productivity at the micro level.

This insight provides one of the key motivations for the present paper: to study the idea production function at the micro level. That is, we study equation (4) directly and consider research productivity for individual products:

Research productivity :=
$$\frac{\dot{A}_{it}/A_{it}}{S_{it}}$$
. (5)

By considering micro evidence, we can directly test the key hypothesis underlying a large portion of endogenous growth theory.

3.2. "Lab Equipment" Specifications

In many applications, the input that we measure is R&D expenditures rather than the number of researchers. In fact, one could make the case that this is a more desirable measure, in that it weights the various research inputs according to their relative prices: if expanding research involves employing people of lower talent, this will be properly measured by R&D spending. When the only input into ideas is researchers, then deflating R&D expenditures by an average wage will appropriately recover the effective

⁴This line of research has been further explored by Aghion and Howitt (1998), Li (2000), Laincz and Peretto (2006), Dinopoulos and Syropoulos (2007), Ha and Howitt (2007), Kruse-Andersen (2016), and Peretto (2016a; 2016b).

quantity of researchers. In practice, R&D expenditures also typically involve spending on capital goods and materials. As explained next, deflating by the nominal wage to get an "effective number of researchers" that this research spending could purchase remains a good way to proceed.

In the growth literature, these specifications are called "lab equipment" models, because implicitly both capital and labor are used as inputs to produce ideas. In lab equipment models, the endogenous growth case occurs when the idea production function takes the form

$$\dot{A}_t = \alpha R_t, \tag{6}$$

where R_t is measured in units of a final output good. For the moment, we discuss this issue in the context of a single-good economy; in the next section, we explain how the analysis extends to the case of multiple products.

To see why equation (6) delivers endogenous growth, it is necessary to specify the economic environment more fully. First, suppose there is a final output good that is produced with a standard Cobb-Douglas production function:

$$Y_t = K_t^{\theta} (A_t L)^{1-\theta}.$$
(7)

Next, the resource constraint for this economy is

$$Y_t = C_t + I_t + R_t \tag{8}$$

That is, final output is used for consumption, investment in physical capital, or research.

We can now combine these three equations to get the endogenous growth result. First, notice that dividing both sides of the production function for final output by Y^{θ} and rearranging yields

$$Y_t = \left(\frac{K_t}{Y_t}\right)^{\frac{\theta}{1-\theta}} A_t L.$$
(9)

Then, letting $s_t := R_t/Y_t$ denote the share of the final good spent on research, the idea production function in (6) can be expressed as

$$\dot{A}_t = \alpha R_t = \alpha s_t Y_t = \alpha s_t \left(\frac{K_t}{Y_t}\right)^{\frac{\theta}{1-\theta}} A_t L.$$
(10)

And rearranging gives

$$\frac{\dot{A}_t}{A_t} = \alpha \left(\frac{K_t}{Y_t}\right)^{\frac{\theta}{1-\theta}} \times s_t L$$
research productivity "scientists" (11)

It is now easy to see how this setup generates endogenous growth. Along a balanced growth path, the capital-output ratio K/Y will be constant, as will the research investment share s_t . If we assume there is no population growth, then equation (11) delivers a constant growth rate of total factor productivity in the long-run. Moreover, a permanent increase in the R&D share *s* will permanently raise the growth rate of the economy.

Looking back at the idea production function in (6), the question is then how to define research productivity there. The answer is both intuitive and simple: we deflate the R&D expenditures R_t by the wage to get a measure of "effective scientists." Letting $w_t = \bar{\theta} Y_t / L_t$ be the wage for labor in this economy, (6) can be written as

$$\frac{\dot{A}_t}{A_t} = \frac{\alpha w_t}{A_t} \times \frac{R_t}{w_t}.$$
(12)

Importantly, the two terms on the right-hand side of this equation will be constant along a balanced growth path in a standard endogenous growth model. It is easy to see that $\tilde{S}_t := \frac{R_t}{w_t} = \frac{R_t}{Y_t} \cdot \frac{Y_t}{w_t} = s_t L/\bar{\theta}$. And of course w_t/A_t is also constant along a BGP.

In other words, if we deflate R&D spending by the economy's wage rate, we get \tilde{S}_t , a measure of the number of researchers the R&D spending could purchase. Of course, research labs spend on other things as well, like lab equipment and materials, but the theory makes clear how \tilde{S}_t is a useful measure for constructing research productivity. Hence we will refer to \tilde{S}_t as "effective scientists" or "research effort."

The idea production function in (12) can then be written as

$$\frac{A_t}{A_t} = \tilde{\alpha}_t \tilde{S}_t \tag{13}$$

where both $\tilde{\alpha}_t$ and \tilde{S}_t will be constant in the long run under the null hypothesis of endogenous growth. We can therefore define research productivity in the lab equipment setup in a way that parallels our earlier treatment:

Research productivity :=
$$\frac{\dot{A}_t/A_t}{\tilde{S}_t}$$
. (14)

The only difference is that we deflate R&D expenditures by a measure of the nominal wage to get \tilde{S} . Under the null hypothesis of endogenous growth, this measure of research productivity should be constant in the long run (and would only vary outside the long-run because of changes in the capital-output ratio).

An easy intuition for (14) is this: endogenous growth requires that a constant population — or a constant number of researchers — be able to generate constant exponential growth. Deflating R&D spending by the wage puts the R&D input in units of "people" so that constant research productivity is equivalent to the null hypothesis of endogenous growth.

Equation (12) above also makes clear why deflating R&D spending by the wage is important. If we did not and instead naively computed research productivity by dividing \dot{A}_t/A_t by R_t , we would find that research productivity would be falling because of the rise in A_t , even in the endogenous growth case. In other words, this naive approach to research productivity would not really correspond to anything economically useful. Economic theory suggests deflating by the research wage in order to get a meaningful concept of research productivity, in this case, one that corresponds to an important hypothesis in the growth literature.

As a measure of the nominal wage in our empirical applications, we use mean personal income from the Current Population Survey for males with a Bachelor's degree or more of education.⁵ This approach means that researchers of heterogeneous quality are combined according to their relative wages. For example, if the best researchers are hired first and subsequent researchers are less talented, the additional researchers will be given a lower weight in our research measure. The potential depletion of research talent is then appropriately incorporated in our empirical approach.

⁵These data are from Census Tables P18 and P19, available at http://www.census.gov/topics/ income-poverty/income/data/tables.html. Prior to 1991, we use the series for "4 or more years of college." For years between 1939 and 1967, we use the series Bc845 from the Historical Statistics for the U.S. Economy, Millennial Edition. Finally, for the aggregate research productivity calculation in Figure 1, we require a deflator from the 1930s. We extrapolate the college earnings series backward into the 1930s using nominal GDP per person for this purpose.

3.3. Heterogeneous Goods and the Lab Equipment Specification

In the previous two subsections, we discussed (i) what happens if research productivity is only constant within each product while the number of products grows and (ii) how to define research productivity when the input to research is measured in goods rather than bodies. Here, we explain how to put these two together.

Among the very first models that used both horizontal and vertical research to neutralize scale effects, only Howitt (1999) used the lab-equipment approach. In that paper, it turns out that the method we have just discussed — deflating R&D expenditures by the economy's average wage — works precisely as explained above. That is, research productivity for each product should be constant if one divides the growth rate by the effective number of researchers working to improve that product.⁶ This is true more generally in these horizontal/vertical models of growth whenever product variety grows at the same rate as the economy's population. Peretto (2016a) cites a large literature suggesting that this is the case: product variety and population scale together over time and across countries.⁷ The two previous subsections then merge together very naturally.

3.4. Stepping on Toes

One other potential modification to the idea production function that has been considered in the literature is a duplication externality. For example, perhaps the idea production function depends on S_t^{λ} , where λ is less than one. Doubling the number of researchers may less than double the production of new ideas because of duplication or because of some other source of diminishing returns.

We could incorporate this effect into our analysis explicitly but choose instead to

⁶The main surprise in confirming this observation is that w_t/A_{it} is constant. In particular, w_t is proportional to output per worker, and one might have expected that output per worker would grow with A_t (an average across varieties) but also with N_t , the number of varieties. However, this turns out not to be the case: Howitt includes a fixed factor of production (like land), and this fixed factor effectively eats up the gains from expanding variety. More precisely, the number of varieties grows with population while the amount of land per person declines with population, and these two effects exactly offset.

⁷Building on the preceding footnote, it is worth also considering Peretto (2016b) in this context. Like Howitt, that paper has a fixed factor and for some parameter values, his setup also leads to constant research productivity. For other parameter values (e.g. if the fixed factor is turned off), the wage w_t grows both because of quality improvements and because of increases in variety. Nevertheless, deflating by the wage is still a good way to test the null hypothesis of endogenous growth: in that case, research productivity *rises* along an endogenous growth path. So the finding below that research productivity is declining is also relevant in this broader framework.

focus on the benchmark case of $\lambda = 1$ for three reasons. First and foremost, our measurement of research effort already incorporates a market-based adjustment for the depletion of talent: R&D spending weights workers according to their wage, and less talented researchers will naturally earn a lower salary. If more of these workers are hired over time, R&D spending will not rise by as much. Second, adjusting for λ only affects the magnitude of the trend in research productivity, but not the overall qualitative fact of whether or not there is a downward trend. It is easy to deflate the growth rate of research effort by whatever value of λ you'd like to get a sense for how this matters; cutting our growth rates in half — an extreme adjustment — would still leave the nature of our results unchanged. Third, one might expect a "short-run" value of λ to differ from its "long-run" value. For example, the duplication and talent depletion effects could certainly apply if we tried to double the amount of research in a given year. However, to the extent that the increase occurs gradually over time, one might expect these effects to be mitigated. Finally, there is no consensus on what value of λ one should use — Kremer (1993) even considers the possibility that it might be larger than one because of network effects. Appendix A shows the robustness of the main results in the paper to this assumption by considering the case of $\lambda = 3/4$, for example.

The remainder of the paper applies this framework in a wide range of different contexts: Moore's Law for semiconductors, agricultural crop yields, pharmaceutical innovation and mortality, and then finally at the firm level using Compustat data. Our consistent finding everywhere we've looked is that research productivity is declining at a substantial rate over long periods of time.

4. Moore's Law

One of the key drivers of economic growth during the last half century is Moore's Law: the empirical regularity that the number of transistors packed onto an integrated circuit serving as the central processing unit for a computer doubles approximately every two years. Figure 3 shows this regularity back to 1971. The log scale of this figure indicates the overall stability of the relationship, dating back nearly fifty years, as well as the tremendous rate of growth that is implied. Related formulations of Moore's Law involving computing performance per watt of electricity or the cost of information

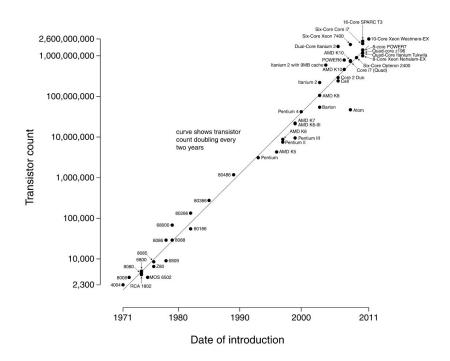


Figure 3: The Steady Exponential Growth of Moore's Law

Source: Wikipedia, https://en.wikipedia.org/wiki/Moores_law.

technology could also be considered, but the transistor count on an integrated circuit is the original and most famous version of the law, so we use that one here.⁸

A doubling time of two years is equivalent to a constant exponential growth rate of 35 percent per year. While there is some discussion of Moore's Law slowing down in recent years (there always seems to be such discussion!), we will take the constant exponential growth rate as corresponding to a constant flow of new ideas back to 1971. That is, we assume the output of the idea production for Moore's Law is a stable 35 percent per year. Other alternatives are possible. For example, we could use decadal growth rates or other averages, and some of these approaches will be employed later in the paper. However, from the standpoint of understanding steady, rapid exponential growth for nearly half a century, the stability implied by the straight line in Figure 3 is a good place to start. And any slowing of Moore's Law would only reinforce the finding we are about to document.⁹

⁸See the Wikipedia entry at https://en.wikipedia.org/wiki/Moores_law.

⁹For example, there is a recent shift away from speed and toward energy-saving features; see Flamm

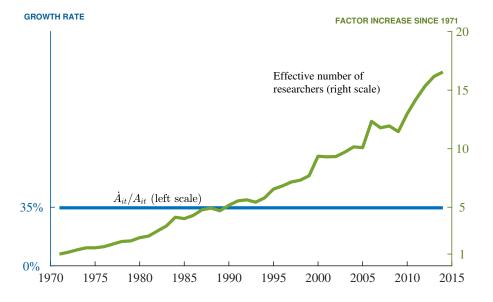


Figure 4: Data on Moore's Law

Note: The effective number of researchers is measured by deflating the nominal semiconductor R&D expenditures of key firms by the average wage of high-skilled workers. The R&D data includes research by Intel, Fairchild, National Semiconductor, Texas Instruments, Motorola, and more than two dozen other semiconductor firms and equipment manufacturers; see Table 1 for more details.

If the output side of Moore's Law is constant exponential growth, what is happening on the input side? Many commentators note that Moore's Law is not a law of nature but instead results from intense research effort: doubling the transistor density is often viewed as a goal or target for research programs. We measure research effort by deflating the nominal semiconductor R&D expenditures of key firms by the nominal wage of high-skilled workers, as discussed above. Our semiconductor R&D series includes research spending by Intel, Fairchild, National Semiconductor, Motorola, Texas Instruments, and more than two dozen other semiconductor firms and equipment manufacturers. More details are provided in the notes to Table 1 below.

The striking fact, shown in Figure 4, is that research effort has risen by a factor of 17 since 1971. This massive increase occurs while the growth rate of chip density is more or less stable: the constant exponential growth implied by Moore's Law has been achieved only by a staggering increase in the amount of resources devoted to pushing the frontier forward.

⁽forthcoming) and Pillai (2016). However, our analysis still applies historically.

Assuming a constant growth rate for Moore's Law, the implication is that research productivity has fallen by this same factor of 17, an average rate of 6.5 percent per year. If the null hypothesis of constant research productivity were correct, the growth rate underlying Moore's Law should have increased by a factor of 17 as well. Instead, it was remarkably stable. Put differently, because of declining research productivity, it is *around 17 times* harder today to generate the exponential growth behind Moore's Law than it was in 1971.

Table 1 reports the robustness of this result to various assumptions about which R&D expenditures should be counted. No matter how we measure R&D spending, we see a large increase in effective research and a corresponding large decline in research productivity. Even by the most conservative measure in the table, research productivity falls by a factor of 7 between 1971 and 2014.

The null hypothesis at the heart of many endogenous growth models — the constancy of research productivity — is resoundingly rejected in the case of Moore's Law. The rise of information technology is an integral part of economic growth in recent decades. One might have expected this rapidly-growing sector to be one of the more natural places to find support for this aspect of endogenous growth theory. Instead, it provides one of the sharpest critiques.

4.1. Caveats

Now is a good time to consider what could go wrong in our research productivity calculation at the micro level. Mismeasurement on both the output and input sides are clearly a cause for concern in general. However, there are two specific measurement problems that are worth considering in more detail. First, suppose there are "spillovers" from other sectors into the production of new ideas related to semiconductors. For example, progress in a completely different branch of materials science may lead to a new idea that improves computer chips. Such positive spillovers are not a problem for our analysis since they would show up as an *increase* in research productivity rather than as the declines that we document in this paper.¹⁰

A type of measurement error that could cause our findings to be misleading is if

¹⁰If such spillovers were larger at the start of our time period than at the end, we could be underestimating the impact of semiconductor R&D on productivity growth. We do not know of evidence suggesting this.

Factor decrease	Average growth	Implied half- life (years)
17	-6.5%	10.6
7	-4.6%	15.0
11	-5.6%	12.4
25	-7.5%	9.2
347	-13.6%	5.1
352	-13.6%	5.1
	decrease 17 7 11 25 347	decreasegrowth17-6.5%7-4.6%11-5.6%25-7.5%347-13.6%

Table 1: Research Productivity for Moore's Law, 1971–2014

Note: The R&D measures are based on Compustat data and PATSTAT data, assembled with assistance from Unni Pillai and Antoine Dechezlepretre. We start with the R&D spending data on 26 semiconductor firms plus an additional 11 semiconductor equipment manufacturers from all over the world. Next, we gathered data from PATSTAT on patents from the U.S. patent office. The different rows in this table differ in how we add up the data across firms. There are two basic ways we treat the R&D data. In the "Narrow" treatment, we recognize that firms engage in different kinds of R&D, only some of which may be relevant for Moore's Law. We therefore weight a firm's R&D according to a (moving average) of the share of its patents that are in semiconductors (IPC group "H01L"). For example, in 1970, 75% of Intel's patents were for semiconductors, but by 2010 this number had fallen to just 8%. In the "Broad" category, we include all R&D by semiconductor firms like Intel and National Semiconductor but use the patent data to infer semiconductor R&D for conglomerates like IBM, RCA, Texas Instruments, Toshiba, and Samsung. The "downweight conglomerates" label means that we further downweight the R&D spending of conglomerates by a factor of 1/2, reflecting the possibility that even their semiconductor patenting data may be broader than Moore's Law. Finally the last two rows show results when we consider the "Narrow" measure of R&D but focus on only one or two firms.

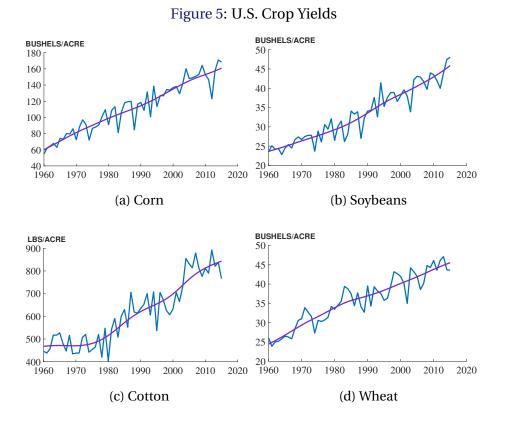
we systematically understate R&D in early years and this bias gets corrected over time. In the case of Moore's Law, we are careful to include research spending by firms that are no longer household names, like Fairchild Camera and Instrument (later Fairchild Semiconductor) and National Semiconductor so as to minimize this bias: for example, in 1971, Intel's R&D was just 0.4 percent of our estimate for semiconductor R&D in that year. Throughout the paper, we try to be as careful as we can with measurement issues, but this type of problem must be acknowledged.

5. Agricultural Crop Yields

Our next application for measuring research productivity examines the evolution of crop yields for various crops over time. Due partly to the historical importance of agriculture in the economy, crop yields and agricultural R&D spending are relatively well-measured for various crops. For each of corn, soybeans, cotton, and wheat, we measure ideas as crop yields, and research inputs as R&D expenditure directed at improving those yields. Crop R&D is generally broken down into research on biological efficiency (cross-breeding and bioengineering), mechanization, management, protection and maintenance, and post-harvest (see, for example, Huffman and Evenson (2006)). We count research on biological efficiency and protection and maintenance as the portion devoted to improving crop yields. Figure 5 shows these measures for our four crops back to the 1960s.¹¹

The figure show yields for each crop, measured in bushels or pounds harvested per acre planted. These correspond to average yields realized on U.S. farms. They are therefore subject to many influences, including choice of inputs and random shocks. These shocks, especially adverse weather and pest events, tend to have asymmetric effects: adverse events cause much larger reductions in yields than favorable events increase them, as indicated by the many large one-year reductions followed by recoveries in the

¹¹ For our measure of ideas, we use the national realized yields series for each crop available from the U.S. Department of Agriculture National Agricultural Statistics Service (2016). Our measure of R&D inputs consists of the sum of R&D spending by the public and private sectors in the U.S. Data on private sector biological efficiency and crop protection R&D expenditures are from an updated USDA series based on Fuglie et al. (2011), with the distribution of expenditure by crop taken from Perrin et al. (1983), Fernandez-Cornejo et al. (2004), Traxler et al. (2005), Huffman and Evenson (2006), and University of York (2016). Data on U.S. public sector R&D expenditure by crop are from the U.S. Department of Agriculture National Institute of Food and Agriculture Current Research Information System (2016) and Huffman and Evenson (2006), with the distribution of expenditure by research focus taken from Huffman and Evenson (2006).



Note: Smoothed yields are computed using an HP filter with a smoothing parameter of 400.

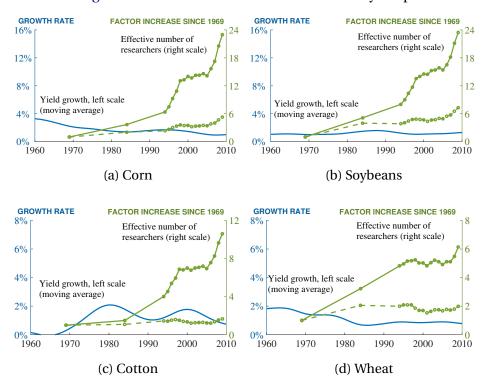


Figure 6: Yield Growth and Research Effort by Crop

Note: The blue line is the annual growth rate of the smoothed yields over the following 5 years, from Figure 5. The two green lines report "Effective Research": the solid line is based on R&D targeting seed efficiency only; the dashed line additionally includes research on crop protection. Both are normalized to one in 1969. See footnote 11 for data sources.

figure (see Huffman, Jin and Xu (2016)). Nevertheless, yields across these four crops roughly doubled between 1960 and 2015.

Figure 6 shows the annualized average 5-year growth rate of yields (after smoothing to remove shocks mostly due to weather). Yield growth has averaged around 1.5 percent per year since 1960 for these four crops, but with ample heterogeneity. These 5-year growth rates serve as our measure of idea output in studying the idea production function for seed yields.

The green lines in Figure 6 show measures of the "effective" number of researchers working on each crop, measured as the sum of public and private R&D spending deflated by the wage of high-skilled workers. Two measures are presented. The fasterrising number corresponds to research targeted only at so-called biological efficiency. This includes cross-breeding (hybridization) and genetic modification directed at in-

Сгор	— Effective research — Factor Average increase growth		Research P Factor decrease	Productivity Average growth
Research on seed efficiency only				
Corn	23.0	7.8%	52.2	-9.9%
Soybeans	23.4	7.9%	18.7	-7.3%
Cotton	10.6	5.9%	3.8	-3.4%
Wheat	6.1	4.5%	11.7	-6.1%
Research includes crop protection				
Corn	5.3	4.2%	12.0	-6.2%
Soybeans	7.3	5.0%	5.8	-4.4%
Cotton	1.7	1.3%	0.6	+1.3%
Wheat	2.0	1.7%	3.8	-3.3%

Table 2: Research Productivity by Crop, 1969–2009

Note: In the first panel of results, the research input is based on R&D expenditures for seed efficiency only. The second panel additionally includes research on crop protection. R&D expenditures are deflated by a measure of the nominal wage for high-skilled workers.

creasing yields, both directly and indirectly via improving insect resistance, herbicide tolerance, and efficency of nutrient uptake, for example. The slower-growing number additionally includes research on crop protection and maintenance, which includes the development of herbicides and pesticides. The effective number of researchers has grown sharply since 1969, rising by a factor that ranges from 3 to more than 25, depending on the crop and the research measure.

It is immediately evident from comparing Figures 6 that research productivity has fallen sharply for agricultural yields: yield growth is relatively stable or even declining, while the effective research that has driven this yield growth has risen tremendously. Research productivity is simply the ratio of average yield growth divided by the number of researchers.

Table 2 summarizes the research productivity calculation for seed yields. As already noted, the effective number of researchers working to improve seed yields rose enor-

mously between 1969 and 2009. For example, the increase was more than a factor of 23 for both corn and soybeans if we restrict attention to seed-yield research narrowlydefined. If yield growth were constant (which is not a bad approximation across the four crops as shown in Figure 6), then research productivity would on average decline by this same factor. The last 2 columns of Table 2 show this to be the case. On average, research productivity declines for crop yields by about 6 percent per year using the narrow definition of research and by about 4 percent per year using the broader definition.

6. Mortality and Life Expectancy

Health expenditures account for around 18 percent of U.S. GDP, and a healthy life is one of the most important goods we purchase. Our third collection of industry case studies examines the productivity of medical research.

Figure 7 shows U.S. life expectancy at birth and at age 65. This graph makes the important point that life expectancy is one of the few economic goods that does not exhibit exponential growth. Instead, arithmetic growth provides a better description of the time path of life expectancy. Since 1950, U.S. life expectancy at birth has increased at a relatively stable rate of 1.8 years each decade, and life expectancy at age 65 has risen at 0.9 years per decade (see Deaton, 2013).

Also shown in the graph is the well-known fact that overall life expectancy grew even more rapidly during the first half of the 20th century, at around 3.8 years per decade. This raises the question of whether even arithmetic growth is an appropriate characterization. We believe that it is for two reasons. First, there is no sign of a slowdown in the years gained per decade since 1950, either in life expectancy at birth or in life expectancy at age 65. The second reason is a fascinating empirical regularity documented by Oeppen and Vaupel (2002). That paper shows that "record female life expectancy" — the life expectancy of women in the country for which they live the longest — has risen at a remarkably steady rate of 2.4 years per decade ever since 1840. Steady linear increases in life expectancy, not exponential ones, seem to be the norm.

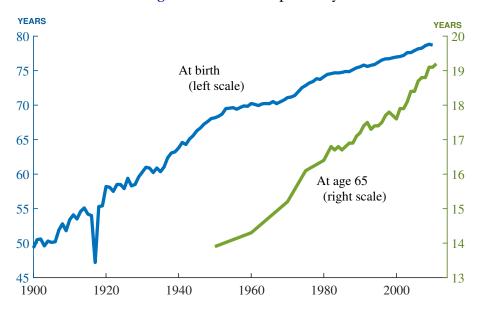


Figure 7: U.S. Life Expectancy

Source: Health, United States 2013 and https://www.clio-infra.eu.

6.1. New Molecular Entities

Our first example from the medical sector is a fact that is well-known in the literature, recast in terms of research productivity. Figure 8 shows the number of new molecular entities ("NMEs") approved by the Food and Drug Administration. NMEs are new drugs, including both chemical and biological products, that have been approved by the FDA. Virtually all pharmaceutical advances in the last 50 years show up in these counts (Zambrowicz and Sands, 2003). Famous examples that became commercial blockbuster drugs are Zocor (for cholesterol), Prilosec (for gastroesophagal reflux), Claritin (for allergies), Celebrex (for arthritis), and Taxol (for treating various types of cancer). Only two or three of the NMEs in any given year become commercial successes. Among famous drugs, only morphine and aspirin do not show up in these counts, because their discovery pre-dates the FDA. The flow of NMEs is well-known to show very little trend, although 2014 and 2015 are two of the years with the most approvals.

We obtain data on pharmaceutical R&D spending from the Pharmaceutical Research and Manufacturers of America (Phrma), which has conducted an annual survey of its members back to 1970 and includes R&D performed both domestically and abroad

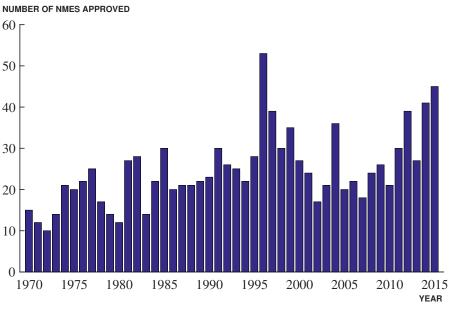


Figure 8: New Molecular Entities Approved by the FDA

by these companies.¹² Using the procedures described earlier, we get the research productivity and effective research numbers shown in Figure 9. Research effort rises by a factor of 9, while research productivity falls by a factor of 11 by 2007 before rising in recent years so that the overall decline by 2014 is a factor of 5. Over the entire period, research effort rises at an annual rate of 6.0 percent, while research productivity falls at an annual rate of 3.5 percent.

Of course, it is far from obvious that simple counts of NMEs appropriately measure the output of ideas; we'd really like to know how important each innovation is. In addition, the NMEs still suffer from an important aggregation issue, adding up across a wide range of health conditions. These limitations motivate the approach described next.

Note: Historical data on NME approvals are from Food and Administration (2013). Data for recent years are taken from Pharmaceutical Research and Manufacturers of America (2016).

¹²A limitation is that it does not include R&D done by foreign companies that is performed abroad. However, Figure 1 of Congressional Budget Office (2006) suggests that this is still a very useful measure.

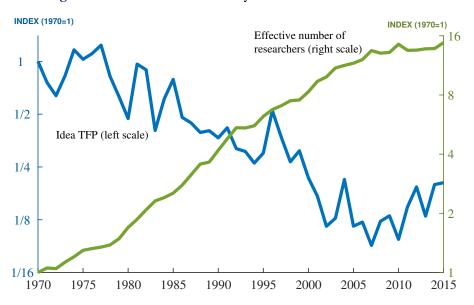


Figure 9: Research Productivity for New Molecular Entities

Note: Historical data on NME approvals are from Food and Administration (2013). Data on research spending by the pharmaceutical industry are from the 2010, 2013, and 2016 editions of Pharmaceutical Research and Manufacturers of America (2016).

6.2. Mortality

Consider a person who faces two age-invariant Poisson processes for dying, with arrival rates δ_1 and δ_2 . We think of δ_1 as reflecting a particular disease we are studying, such as cancer or heart disease, and δ_2 as capturing all other sources of mortality. The probability a person lives for at least x years before succumbing to type i mortality is the survival rate $S_i(x) = e^{-\delta_i x}$, and the probability the person lives for at least x years before dying from any cause is $S(x) = S_1(x)S_2(x) = e^{-(\delta_1 + \delta_2)x}$. Life expectancy at age a, LE(a) is then well known to equal

$$LE(a) = \int_0^\infty S(x)dx = \int_0^\infty e^{-(\delta_1 + \delta_2)x} dx = \frac{1}{\delta_1 + \delta_2}.$$
 (15)

Now consider how life expectancy changes if the type *i* mortality rate changes slightly. It is easy to show that the expected years of life saved by the mortality change is

$$dLE(a) = \frac{\delta_i}{\delta_1 + \delta_2} \cdot LE(a) \cdot \left(-\frac{d\delta_i}{\delta_i}\right).$$
(16)

That is, the expected years of life saved from a decline in, say, cancer mortality is the product of three terms. First is the fraction of deaths that result from cancer. Second is the average years of life lost if someone dies from cancer at age *a*, and finally is the percentage decline in cancer mortality.

Vaupel and Canudas-Romo (2003) show that this expression generalizes to a much richer setting. In particular, the expected years of life saved is the product of three terms with the same interpretation. For example, they allow for an arbitrary number of causes of death each of which has a mortality rate that varies arbitrarily with age.¹³

As discussed at the start of this section, life expectancy tends to rise linearly. Therefore, constant exponential growth in income per person is associated with constant arithmetic increases in life expectancy, which in the aggregate average 1.8 years per decade in the U.S. We therefore take the quantity described in equation (16) as our measure of the output of ideas associated with declines in mortality for a given disease.¹⁴

The research input aimed at reducing mortality from a given disease is at first blush harder to measure. For example, it is difficult to get research spending broken down into spending on various diseases. Nevertheless, we think we have a useful solution to this problem: we measure the number of scientific publications in PUBMED that have "Neoplasms," for example, as a MESH (Medical Subject Heading) term. MESH is the National Library of Medicine's controlled vocabulary thesaurus.¹⁵ We do this in two ways. Our broader approach ("publications") uses all publications with the appropriate MESH keyword as our input measure. Our narrower approach ("trials") further restricts our measure to those publications that according to MESH correspond to a clinical trial. Rather than using scientific publications as an *output* measure, as other studies

¹³Their formula involves an extra covariance term as well. In particular, the covariance between the agespecific percentage decline in mortality associated with cancer and the years of life saved at age *a* when cancer is averted. When the percentage decline in mortality rates is the same across ages, this covariance is zero. More generally, it can differ from zero, but in many of the calculations in their paper, the covariance is small.

¹⁴Our measures of life expectancy and mortality from all sources by age come from the Human Mortality Database at http://mortality.org. To measure the percentage declines in mortality rates from cancer, we use the age-adjusted mortality rates for U.S. women ages 50 and over computed from 5-year survival rates, taken from the National Cancer Institute's Surveillance, Epidemiology, and End Results program at http://seer.cancer.gov/.

¹⁵For more information on MESH, see https://www.nlm.nih.gov/mesh/. Our queries of the PUBMED data use the webtool created by the Institute for Biostatistics and Medical Informatics (IBMI) Medical Faculty, University of Ljubljana, Slovenia available at http://webtools.mf.uni-lj.si/.

have done, we use publications and clinical trials as *input* measures to capture research effort aimed at reducing mortality for a particular disease.¹⁶

Figure 10 shows our basic "idea output" measures for mortality from all cancers, from breast cancer, and from heart disease. Heart disease and cancer are the top two leading causes of death in the United States, and in the spirit of looking as narrowly as possible, we also chose to look at breast cancer mortality. For the two cancer types, we use the 5-year mortality rate conditional on being diagnosed with either type of cancer and see an S-shaped decline since 1975. This translates into a hump-shaped "Years of life saved per 1000 people" — the empirical analog of equation (16) — as the mortality rate first rises and then slows. For example, for all cancers, the years of life saved series peaks around 1990 at more than 100 years of life saved per 1000 people before declining to around 60 years in the 2000s. For heart disease, a substantial part of the decline in deaths comes from people not contracting the disease in the first place, so we focus on the (smoothed) crude death rate for people aged 55 to 64. The death rate declines at different rates in different periods, leading to a series of humps in years of life saved, but overall there is no large trend in this measure of idea output.

Figure 11 shows our research input measure based on PUBMED publication statistics. Total publications for all cancers increased by a factor of 3.5 between 1975 and 2006 (the years for which we'll be able to compute research productivity), while publications restricted to clinical trials increased by a factor of 17.1 during this same period. A similar pattern is seen for research on breast cancer and heart disease.

Research productivity for our medical research applications is computed as the ratio of years of life saved to the number of publications. Figure 12 shows our research productivity measures. The hump-shape present in the years-of-life-saved measure carries over here. Research productivity rises until the mid 1980s and then falls. Overall, between 1975 and 2006, research productivity for all cancers declines by a factor of 1.2 using all publications and a factor of 4.8 using clinical trials. The declines for breast cancer and heart disease are even larger, as shown in Table 3.

Several general comments about research productivity for medical research deserve mention. First, for this application, the units of research productivity are different

¹⁶Lichtenberg (2017) takes a similar approach in an econometric framework for the years 1999–2013. He uses a difference-in-differences specification to document an economically-significant correlation between research publications related to various cancer sites and subsequent mortality and years of life saved.

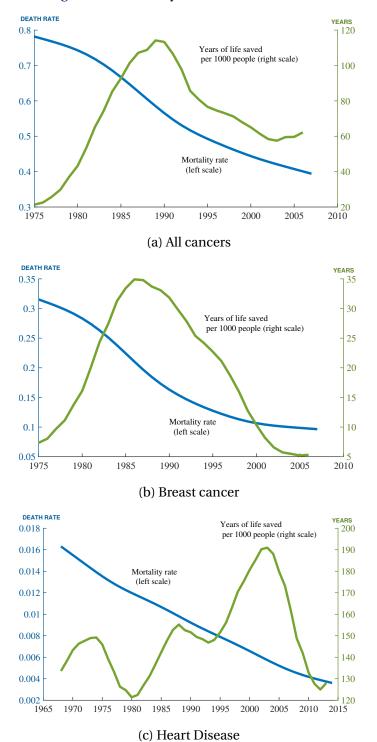
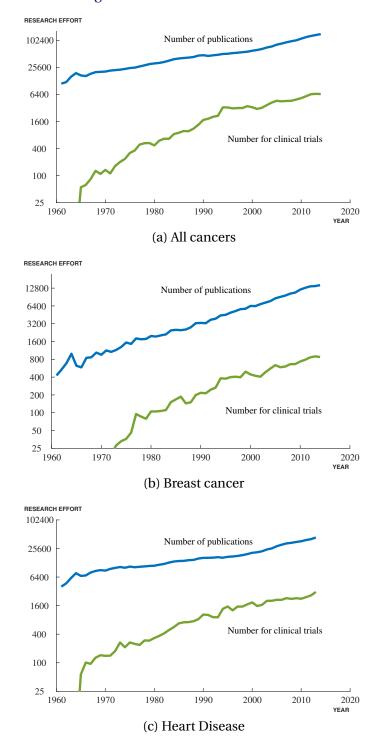
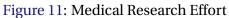


Figure 10: Mortality and Years of Life Saved

Note: For the two cancer figures, the mortality rate is computed as negative the log of the (smoothed) five-year survival rate for cancer for people ages 50 and higher, from the National Cancer Institute's Surveillance, Epidemiology, and End Results program at http://seer.cancer.gov/. For heart disease, we report the crude death rate in each year for people aged 55–64. The "Years of life saved per 1000 people" is computed using equation (16), as described in the text.





Note: The number of publications and clinical trials are taken from the PUBMED publications database. For "publications," the research input is based on all publications in PUBMED with "Neoplasms" or "Breast Neoplasms" or "Heart Diseases" as a MESH keyword. The lines for "clinical trials" restrict further to publications involving clinical trials.

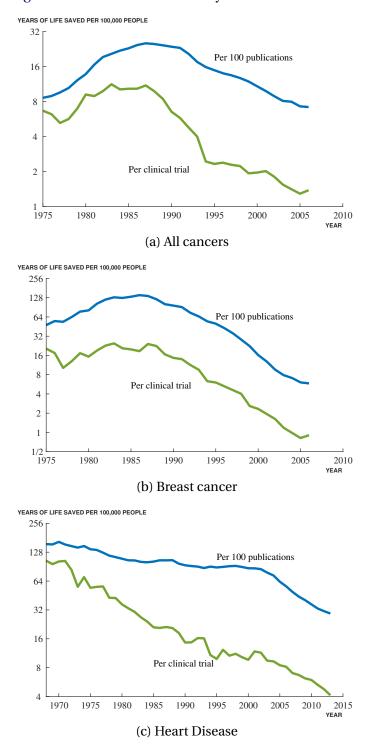


Figure 12: Research Productivity for Medical Research

Note: Research productivity is computed as the ratio of years of life saved to the number of publications.

Disease	— Effective Factor increase	e research — Average growth	Research P Factor decrease	roductivity Average growth
	mercuse	growin	uccicuse	growin
All publications				
Cancer, all types	3.5	4.0%	1.2	-0.6%
Breast cancer	5.9	5.7%	8.2	-6.8%
Heart disease	5.1	3.6%	5.3	-3.7%
Clinical trials only				
Cancer, all types	14.1	8.5%	4.8	-5.1%
Breast cancer	16.3	9.0%	22.6	-10.1%
Heart disease	24.2	7.1%	25.3	-7.2%

Table 3: Research Productivity for Medical Research

Note: In the first panel, the research input is based on all publications in PUBMED with "Neoplasms" or "Breast Neoplasms" or "Heart Diseases" as a MESH keyword. The second panel restricts to only publications involving clinical trials. Results for cancer and breast cancer cover the years 1975–2006, while those for heart disease apply to 1968–2011.

than what we've seen so far. For example, between 1985 and 2006, declining research productivity means that the number of years of life saved per 100,000 people in the population by each publication of a clinical trial related to cancer declined from more than 8 years to just over one year. For breast cancer, the changes are even starker: from around 16 years per clinical trial in the mid 1980s to less than one year by 2006.

Next, however, notice that the changes were not monotonic if we go back to 1975. Between 1975 and the mid-1980s, research productivity for these two cancer research categories increased quite substantially. The production function for new ideas is obviously complicated and heterogeneous. These cases suggest that it may get easier to find new ideas at first before getting harder, at least in some areas.

7. Research Productivity in Firm-Level Data

The case studies considered so far are useful for many reasons already explained. However, at the end of the day, they are just case studies, and one naturally wonders how representative they are of the broader economy. In addition, some growth models associate each firm with a different variety: perhaps the number of firms making corn or semiconductor chips is rising sharply, so that research effort per firm is actually constant, as is research productivity at the firm level. Declining research productivity for corn or semiconductors could in this view simply reflect a further composition bias.¹⁷

To help address these concerns, we turn to Compustat data on US publicly-traded firms. The strength of these data is that they are more representative than the case studies, but of course they too have limitations. Publicly-traded firms are still a select sample, and our measures of "ideas" and research inputs are likely less precise. However, as a complement to the case studies, we find this evidence helpful.

As a measure of the output of the idea production function, we use decadal averages of annual growth in sales revenue, market capitalization, employment, and revenue labor productivity within each firm. We take the decade as our period of observation to smooth out fluctuations.

¹⁷For example, Peretto (1998) and Peretto (2016b) emphasize this perspective on varieties, while Aghion and Howitt (1992) take the alternative view that different firms may be involved in producing the same variety. Klette and Kortum (2004) allow the number of varieties produced by each firm to be heterogeneous and to evolve over time.

Why would growth in sales revenue, market cap, or employment be informative about a firm's production of ideas? This approach follows a recent literature emphasizing precisely these links. Many papers have shown that news of patent grants for a firm has a large immediate effect on the firm's stock market capitalization (e.g. Blundell, Griffith and Van Reenen, 1999; Kogan, Papanikolaou, Seru and Stoffman (2015)). Patents are also positively correlated with the firm's subsequent growth in employment and sales.

More generally, in models in the tradition of Lucas (1978), Hopenhayn (1992), and Melitz (2003), increases in the fundamental productivity of a firm show up in the long run as increases in sales and firm size, but *not* as increases in sales revenue per worker.¹⁸ This motivates our use of sales revenue or employment to measure fundamental productivity. Hsieh and Klenow (2009) and Garcia-Macia, Hsieh and Klenow (2016) are recent examples of papers that follow a related approach. Of course, in more general models with fixed overhead labor costs, revenue labor productivity (i.e. sales revenue per worker) and TFPR can be related to fundamental productivity (e.g. Bartelsman, Haltiwanger and Scarpetta, 2013). And sales revenue and employment can change for reasons other than the discovery of new ideas. We try to address these issues by also looking at revenue productivity and through various sample selection procedures, discussed below. These problems also motivate the earlier approach of looking at case studies.

To measure the research input, we use a firm's spending on research and development from Compustat. This means we are restricted to firms that report formal R&D, and such firms are well-known to be a select sample (e.g. disproportionately in manufacturing and large). We look at firms since 1980 that report non-zero R&D, and this restricts us to an initial sample of 15,128 firms. Our additional requirements for sample selection in our baseline sample are

1. We observe at least 3 annual growth observations for the firm in a given decade.

¹⁸This is obvious when one thinks about the equilibrium condition for the allocation of labor across firms in simple settings: in equilibrium, a worker must be indifferent between working in two different firms, which equalizes wages. But wages are typically proportional to output per worker. Moreover, with Cobb-Douglas production and a common exponent on labor, sales revenue per worker would be precisely equated across firms even if they had different underlying productivities. In a Lucas (1978) span of control setting, more productive firms just hire more workers, which drives down the marginal product until it is equated across firms. In alternative settings with monopolistic competition, it is the price of a particular variety that declines as the firm expands. Regardless, higher fundamental productivity shows up as higher employment or sales revenue, but not in higher sales per employee.

These growth rates are averaged to form the idea output growth measure for that firm in that decade.

- 2. We only consider decades in which our idea output growth measure for the firm is positive (negative growth is clearly not the result of the firm innovating, and our framework cannot make sense of negative research productivity).
- 3. We require the firm to be observed (for both the output growth measure and the research input measure) for two consecutive decades. Our decades are the 1980s, the 1990s, the 2000s (which refers to the 2000-2007 period), and the 2010s (which refers to the 2010-2015 period); we drop the years 2008 and 2009 because of the financial crisis.

We relax many of these conditions in our robustness checks.

Table 4 shows our research productivity calculation for various cuts of the Compustat data: using sales revenue, market cap, employment, and revenue labor productivity as our idea output measure and following firms that we observe for two, three, and four decades. In all samples, there is substantial growth in the average number of effective number of researchers within each firm, with growth rates averaging between 2.4% and 8.8% per year. Under our null hypothesis, this rapid growth in research should translate into higher growth rates of firm-level sales and employment with a constant level of research productivity. Instead, what we see in Table 4 are steady, rapid declines in firmlevel research productivity across all samples, at growth rates that range from -4.2% to -14.5% per year for multiple decades.

Put differently, and reporting the results using sales revenue as a baseline, research productivity declines by an average factor of 3.9 for firms that we can compare across only two decades, by a factor of 9.2 across firms we can compare across three decades, and by a factor of 40.3 across firms that we can compare across our entire 4 decade sample, between 1980 and 2015.¹⁹

Averaging across all our samples, research productivity falls at a rate of about 9% per year, cumulating to a 2.5-fold decline every decade. At this rate, research productivity declines by a factor of about 15 over three decades of changes; put differently, it requires 15 times more researchers today than it did 30 years ago to produce the same rate of

¹⁹The averages we report throughout are weighted averages, using the effective number of researchers in each firm as weights.

	— Effective research —		Research Productivity	
Comula	Factor	Average	Factor	Average
Sample	increase	growth	decrease	growth
Sales Revenue				
2 decades (1712 firms)	2.0	6.8%	3.9	-13.6%
3 decades (469 firms)	3.8	6.7%	9.2	-11.1%
4 decades (149 firms)	13.7	8.7%	40.3	-12.3%
Market Cap				
2 decades (1124 firms)	2.2	8.0%	3.4	-12.2%
3 decades (335 firms)	3.1	5.6%	6.3	- 9.2%
4 decades (125 firms)	7.9	6.9%	14.0	-8.8%
Employment				
2 decades (1395 firms)	2.2	8.0%	2.8	-10.3%
3 decades (319 firms)	4.0	6.9%	18.2	-14.5%
4 decades (101 firms)	13.9	8.8%	31.5	-11.5%
Revenue Labor Productivity				
2 decades (1444 firms)	1.9	6.4%	2.2	-7.9%
3 decades (337 firms)	1.6	2.4%	2.5	-4.5%
4 decades (109 firms)	2.5	3.1%	3.5	-4.2%

Table 4: Research Productivity in Compustat Firm-Level Data

Note: The table shows averages of firm-level outcomes for effective research and research productivity. Sales Revenue and Market Cap are deflated by the GDP implicit price deflator. Revenue Labor Productivity is deflated Sales Revenue divided by Employment. R&D expenditures are deflated by a measure of the nominal wage for high-skilled workers. The average growth rate across 2 decades is computed by dividing by 10 years (e.g. between 1985 and 1995); others follow this same approach. Averages are computed by weighting firms by the median number of effective researchers in each firm across the decades.

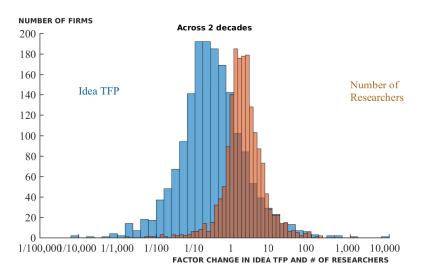


Figure 13: Compustat Distributions, Sales Revenue (2 Decades)

Note: Based on 1712 firms. 22.1% of firms have increasing research productivity ("idea TFP"). Only 3.0% have research productivity that is roughly constant, defined as a growth rate whose absolute value is less than 1% per year.

economic growth.

The next three figures characterize the heterogeneity across firms in our Compustat sample by showing the distribution of the factor changes in effective research and research productivity across all the firms; to keep things manageable, we focus on the results for sales revenue, but the results with other output measures are similar. Figure 13 shows this distribution for the firms we observe for only two decades, while Figures 14 and 15 shows the distributions for the firms observed for three and four decades.

The heterogeneity across firms is impressive and somewhat reminiscent of the heterogeneity we see in our case studies. Nevertheless, it is clear from these histograms that there is essentially no evidence that constant research productivity is a good characterization of the firm-level data. The average, median, and modal firms experience large declines in research productivity. There is a long tail of firms experiencing even larger declines but also a small minority of firms that see increases in research productivity. The fraction of firms that exhibit something like constant research productivity is tiny. For example, less than 5% of firms in any of the histograms have research productivity changing (either rising or falling) by less than 1% per year on average.

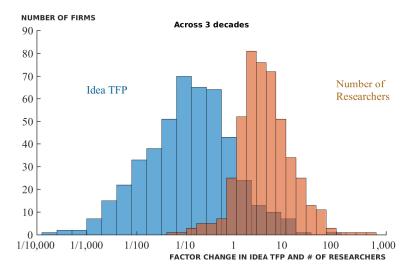


Figure 14: Compustat Distributions, Sales Revenue (3 Decades)

Note: Based on 469 firms. 11.9% of firms have increasing research productivity ("idea TFP"). Only 4.3% have research productivity that is roughly constant, defined as a growth rate whose absolute value is less than 1% per year.

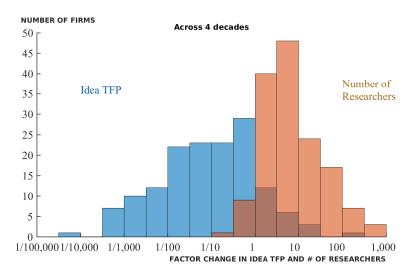


Figure 15: Compustat Distributions, Sales Revenue (4 Decades)

Note: Based on 149 firms. 14.8% of firms have increasing research productivity ("idea TFP"). 4.7% firms in this sample have research productivity that is roughly constant, defined as a growth rate whose absolute value is less than 1% per year.

Table 5 provides additional evidence of the robustness of these results. In the interests of brevity, we report these results for the sales revenue output measure for firms that we observe across three decades, but the results for our other output measures and time frames are similar. The first row of the table repeats the benchmark results described earlier. The second and third rows relax the requirement that sales growth is positive. In the second row, we replace all growth rates less than 1% with 1%, while in the third row we additionally windsorize an equal number of firms at the top of the growth rate distribution. This increases the sample size considerably and brings the R&D growth numbers down substantially. In both cases, research productivity falls sharply, reassuring us that this sample selection criteria is not driving the results. The fourth row imposes the restriction that research is increasing across the observed decades. The fifth row tightens our restrictions and drops firm in which sales revenue declines on average in any decade. The sixth row uses median sales growth in each decade rather than mean sales growth as our output measure. And the last row reports unweighted averages rather than weighting the firms by the effective number of researchers. The general finding of substantial declines in research productivity is robust.

8. Discussion

The evidence presented in this paper concerns the extent to which a constant level of research effort can generate constant exponential growth, either in the economy as a whole or within relatively narrow categories, such as a firm or a seed type or a health condition. We provide consistent evidence that the historical answer to this question is no: as summarized in Table 6, research productivity is declining at a substantial rate in virtually every place we look. The table also provides a way to quantify the magnitude of the declines in research productivity by reporting the half-life in each case. Taking the aggregate economy number as a representative example, research productivity declines at an average rate of 5.3 percent per year, meaning that it takes around 13 years for research productivity to fall by half. Or put another way, the economy has to double its research efforts every 13 years just to maintain the same overall rate of economic growth.

A natural question is whether or not these empirical patterns can be reproduced in

	— Effectiv	e research —	Research F	roductivity
Case	Factor increase	Average growth	Factor decrease	Average growth
Benchmark (469 firms)	3.8	6.7%	9.2	-11.1%
Windsorize $g < .01$ (986 firms)	2.3	4.1%	7.9	10.3%
Windsorize top/bottom (986 firms)	2.3	4.1%	6.0	-8.9%
Research must increase (356 firms)	5.1	8.1%	11.6	-12.3%
Drop if <i>any</i> negative growth (367 firms)	5.6	8.6%	17.9	-14.4%
Median sales growth (586 firms)	3.8	6.6%	6.3	-9.2%
Unweighted averages (469 firms)	3.8	6.7%	9.2	-11.1%

Table 5: Compustat Sales Data across 3 Decades: Robustness

Note: Robustness results reported for the sample of changes across 3 decades. "Winsorize g < .01" means we replace any idea output measure that is less than 1% annually with a value of 1%. "Windsorize top/bottom" does this same thing but windsorizes an equal number of firms at the top of the idea output distribution. "Research must increase" means we require that the research measure be rising across the decades. "Drop if any negative growth" means we drop firms that have any decade (across our 1980–2015 period) in which average market cap growth is negative. "Median sales growth" uses the median of sales revenue growth in each decade rather than the mean. "Unweighted averages" gives each firm equal weight in computing summary statistics, rather than weighting each firm by its effective number of researchers.

Scope	Time Period	Average annual growth rate	Half-life (years)	Extent of Diminishing Returns, β
Aggregate economy	1930–2015	-5.3%	13	3.4
Moore's law	1971–2014	-6.5%	11	0.19
Corn, version 1	1969–2009	-9.9%	7	7.2
Corn, version 2	1969–2009	-6.2%	11	4.5
Soybeans, version 1	1969–2009	-7.3%	9	6.3
Soybeans, version 2	1969–2009	-4.4%	16	3.8
Cotton, version 1	1969–2009	-3.4%	21	2.5
Cotton, version 2	1969–2009	+1.3%	-55	-0.9
Wheat, version 1	1969–2009	-6.1%	11	6.8
Wheat, version 2	1969–2009	-3.3%	21	3.7
New molecular entities	1970–2015	-3.5%	20	
Cancer (all), publications	1975-2006	-0.6%	116	
Cancer (all), trials	1975-2006	-5.7%	12	
Breast cancer, publications	1975–2006	-6.1%	11	
Breast cancer, trials	1975-2006	-10.1%	7	
Heart disease, publications	1968–2011	-3.7%	19	
Heart disease, trials	1968–2011	-7.2%	10	
Compustat, sales	3 decades	-11.1%	6	1.1
Compustat, market cap	3 decades	-9.2%	8	0.9
Compustat, employment	3 decades	-14.5%	5	1.8
Compustat, RLP	3 decades	-4.5%	15	1.1

Table 6: Summary of the Evidence on Research Productivity

Note: The growth rates of research productivity are taken from other tables in this paper. The half life is the number of years it takes for research productivity to fall in half at this growth rate. The last column reports the extent of diminishing returns in producing exponential growth, according to equation (17). This measure is only reported for cases in which the idea output measure is an exponential growth rate (i.e. not for the health technologies, where units would matter).

a general equilibrium model of growth. One class of models that is broadly consistent with this evidence is the semi-endogenous growth approach of Jones (1995), Kortum (1997), and Segerstrom (1998).²⁰ These models propose that the idea production function takes the form

$$\frac{A_t}{A_t} = \alpha \frac{S_t}{A_t^\beta} \implies iTFP_t = \frac{\alpha}{A_t^\beta}.$$
(17)

Research productivity declines as A_t rises, so that it gets harder and harder to generate constant exponential growth. The elasticity β governs this process. That is, it measures the extent of dynamic diminishing returns in idea production, with a higher β meaning that research productivity declines more rapidly as A_t increases.

Comparing both sides of the first equation in (17), one can see that constant exponential growth requires a growing number of researchers S_t . In fact, if \dot{A}_t/A_t is constant over time, it must be that the numerator and denominator of the right-hand side of that equation grow at the same rate. This means that constant exponential growth requires

$$g_A = \frac{g_S}{\beta} \tag{18}$$

where g_x denotes the constant growth rate of any variable x. The growth rate of the economy equals the growth rate of research effort deflated by the extent of diminishing returns in idea production. Rising research effort and declining research productivity offset — endogenously in this framework — to deliver constant exponential growth.

Finally, this analysis can be applied across different firms, goods, or industries, following the insights of Ngai and Samaniego (2011), who develop a semi-endogenous growth model with heterogeneity in the dynamic spillover parameters of the idea production functions. Some goods, like semiconductors, can have rapid productivity growth because their β is small, while other goods like the speed of airplanes or perhaps the education industry itself could have slow rates of innovation because their β is large. Nevertheless, all of these products could exhibit constant exponential growth if the amount of research effort put toward innovation is itself growing exponentially.

This framework helps us to address a phenomenon that might at first have appeared puzzling: research productivity is declining very rapidly in the fastest growing sector in the economy, semiconductors. Why? In particular, why are we throwing so many

²⁰Jones (2005) provides a broad overview of this class of models.

resources at a sector that has such sharp declines in research productivity?

The last column of Table 6 reports estimates of β for each of our case studies, according to equation (17), and the results speak to the semiconductor puzzle we just highlighted. In particular, semiconductors is the application with the smallest value of β , coming in at 0.19, suggesting that it is the sector with the *least* degree of diminishing returns in idea production: *A* is growing at 35% per year, while research productivity is falling at 6% per year. From (17), this implies a value of β of $6/35 \approx 0.19$. In contrast, economy-wide TFP growth averages about 1.5% per year, while research productivity is declining at a rate of about 5% per year, yielding a β of more than 3! So in fact, semiconductors shows much *less* diminishing returns than the economy as a whole.

Research productivity for semiconductors falls so rapidly, not because that sector has the sharpest diminishing returns — the opposite is true. It is instead because research in that sector is growing more rapidly than in any other part of the economy, pushing research productivity down. A plausible explanation for the rapid research growth in this sector is the "general purpose" nature of information technology. Demand for better computer chips is growing so fast that it is worth suffering the declines in research productivity there in order to achieve the gains associated with Moore's Law.

One way in which the overall interpretation of the evidence in this paper could be wrong is if there is indeed declining research productivity in every sector, but the entire increase in aggregate R&D occurs in making quality/productivity improvements for individual varieties. The separate idea production function for producing new varieties could then exhibit constant research productivity if in fact the research going to create new varieties is not increasing over time. While this is conceptually possible, it seems unlikely. We do not have any growth models in the literature that suggest this could occur in an equilibrium in which there is population growth. Why, despite a growing population and constant research productivity, would the equilibrium allocation feature a constant number of researchers creating new varieties? Nevertheless, this loophole is one that future research may wish to consider.

9. Conclusion

A key assumption of many endogenous growth models is that a constant number of researchers can generate constant exponential growth. We show that this assumption corresponds to the hypothesis that the total factor productivity of the idea production function is constant, and we proceed to measure research productivity in many different contexts.

Our robust finding is that research productivity is falling sharply everywhere we look. Taking the U.S. aggregate number as representative, research productivity falls in half every 13 years — ideas are getting harder and harder to find. Put differently, just to sustain constant growth in GDP per person, the U.S. must double the amount of research effort searching for new ideas every 13 years to offset the increased difficulty of finding new ideas.

This analysis also has implications for the growth models that economists use in our own research, like those cited in the introduction. The standard approach in recent years is to use models that assume constant research productivity, in part because it is convenient and in part because the earlier literature has been interpreted as being inconclusive on the extent to which this is problematic. We believe the empirical work we've presented speaks clearly against this assumption. A first order fact of growth empirics is that research productivity is falling sharply.

That this particular aspect of endogenous growth theory should be reconsidered does not diminish the contribution of that literature. Quite the contrary. The only reason models with declining research productivity can sustain exponential growth in living standards is because of the key insight from that literature: ideas are nonrival. And if research productivity were constant, sustained growth would actually not require that ideas be nonrival; Akcigit, Celik and Greenwood (2016) show that fully rivalrous ideas in a model with perfect competition can generate sustained exponential growth in this case. Our paper therefore clarifies that the fundamental contribution of endogenous growth theory is not that research productivity is constant or that subsidies to research can permanently raise growth. Rather it is that ideas are different from all other goods in that they do not get depleted when used by more and more people. Exponential growth in research leads to exponential growth in A_t . And because of nonrivalry, this leads to exponential growth in per capita income.

A Robustness Results: Allowing $\lambda < 1$

Table A1 shows the robustness of our results to the baseline assumption that there is no diminishing returns to research in the idea production function. See the discussion in Section 3.4. for more details. For this set of results, we assume the input into the idea production function is S^{λ} where $\lambda = 3/4$. As expected, the growth rates of research productivity are about three-fourths as large as in the baseline case, reported in the main text in Table 6, but they are substantially negative nearly everywhere we look.

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Scope	Time Period	Average annual growth rate	Half-life (years)
Aggregate economy	1930–2015	-4.1%	17
Moore's law	1971–2014	-4.9%	14
Corn, version 1	1969–2009	-7.9%	9
Corn, version 2	1969–2009	-5.2%	13
Soybeans, version 1	1969–2009	-5.4%	13
Soybeans, version 2	1969–2009	-3.2%	22
Cotton, version 1	1969–2009	-1.9%	37
Cotton, version 2	1969–2009	+1.6%	-44
Wheat, version 1	1969–2009	-5.0%	14
Wheat, version 2	1969–2009	-2.9%	24
New molecular entities	1970–2015	-2.0%	34
Cancer (all), publications	1975–2006	+0.4%	-166
Cancer (all), trials	1975–2006	-3.4%	20
Breast cancer, publications	1975–2006	-4.7%	15
Breast cancer, trials	1975–2006	-7.7%	9
Heart disease, publications	1968–2011	-2.8%	25
Heart disease, trials	1968–2011	-5.4%	13
Compustat, sales	3 decades	-9.4%	7
Compustat, market cap	3 decades	-7.8%	9
Compustat, employment	3 decades	-12.8%	5
Compustat, RLP	3 decades	-3.9%	18

Table A1: Robustness Results for Research Productivity: $\lambda=0.75$

Note: This table shows results paralleling those in Table 6 when we allow for diminishing returns to research. In particular, we assume the input into the idea production function is S^{λ} where $\lambda = 3/4$, as opposed to our baseline case of $\lambda = 1$.

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