## Climate Change and Growth Risks

Ravi Bansal, Dana Kiku and Marcelo Ochoa<sup>\*</sup>

July 7, 2015

#### Abstract

We use the forward-looking information from global capital markets to estimate the elasticity of equity prices to temperature fluctuations and find that global warming has a significant negative effect on asset valuations. We also find that the negative elasticity of prices has been increasing over time, suggesting that the impact of climate change has been rising. We use our empirical work to calibrate a long-run risks model with temperature-induced disasters that affect future output and growth. The model simultaneously matches the projected temperature path, the observed consumption growth dynamics, discount rates provided by the risk-free rate and equity market returns, and the estimated temperature elasticity of equity prices. We use the calibrated model to quantify the social cost of carbon (SCC) and to frame the optimal climate policy. We show that a preference for early resolution of uncertainty and long-run impact of temperature on growth imply a significant SCC and motivate early actions to abate global warming.

<sup>\*</sup>Ravi Bansal is affiliated with the Fuqua School of Business at Duke University and NBER, Dana Kiku is at the University of Illinois at Urbana-Champaign, and Marcelo Ochoa is at the Federal Reserve Board. The analysis and conclusions set forth are those of the authors and do not indicate concurrence by other members of the research staff or the Board of Governors. We would like to thank Lars Hansen, Christian Traeger, Ricardo Colacito, Tony Smith, Thomas Maurer, Juhani Linnainmaa, and seminar participants at Duke University, the 2nd Macro Finance Workshop, Developing the Next Generation of Economic Models of Climate Change Conference, the 2015 AEA meetings, the 2015 MFA meetings for their helpful comments. The usual disclaimer applies.

### Introduction

Global warming and its potential impact on the macro-economy is a matter of considerable importance. This article makes a contribution towards understanding the interactions between rising temperature, economic growth and risk. To study the potential impact of climate change on the macro-economy, we present a temperature-augmented long-run risks (LRR-T) model that jointly models the path of temperature, consumption, and global-warming induced disasters. We use our model to quantify the social cost of carbon and frame the socially optimal response to climate change. Our model and its calibration are guided by the empirical evidence of the negative economic impact of global warming revealed by forward-looking valuation data from capital markets. We show that in the data, equity valuations have a significantly negative elasticity to temperature fluctuations, particularly to low-frequency variations in temperature that contribute to global warming. This evidence underscores the important interactions between temperature, economic growth and risk that determine equity prices.

Our model builds on the long-run risks framework of Bansal and Yaron (2004) that features recursive preferences of Kreps and Porteus (1978), Epstein and Zin (1989), and Weil (1990) with a preference for early resolution of uncertainty and a persistent expected growth component in consumption. To account for the potentially severe consequences of global warming we introduce temperature-induced natural disasters that affect current and future economic growth, similar in spirit to Rietz (1988) and Barro (2009). Disasters are triggered when temperature breaches a threshold level and capture the idea of tail risk related to global warming as discussed in Pindyck (2012). Our LRR-T model provides a framework, in which temperature rises economic risk and affects aggregate wealth and valuations of long-lived assets. We show that with a preference for early resolution of uncertainty, a rise in temperature, even in the distant future, lowers the current wealth to consumption ratio and that temperature variations carry a positive risk premium. These implications are consistent with the evidence of a negative elasticity of equity prices to long-run temperature risks that we document in the data. In contrast, under power utility, which is the standard assumption in the integrated assessment models, aggregate wealth increases in states of high temperature and high likelihood of disasters. Consequently, as we show, the incentive to abate global warming, and the timing and the scale of abatement efforts depend critically on the attitude towards long-run (climate) risks.

One of the important and well-recognized issues in climate-change economics is uncertainty about the impact of global warming. Pindyck (2007) provides a comprehensive discussion of this and other sources of uncertainty in environmental economics. Micro evidence by Tol (2002a 2002b) offers some guidance regarding temperature-related damages, however, there are essentially no historical records pertaining to tail risks of climate change and the induced catastrophic losses. Significant effects of global warming are expected to unfold in the future and, therefore, are difficult to assess from the past output data. It might, however, be possible to learn about climate-change risks from forwardlooking equity prices — if temperature will have a significant growth or/and discount-rate effects, it should have a measurable impact on current equity valuations. We pursue this idea and use cross-country capital market and temperature data to estimate elasticity of equity valuations to temperature risks. Our panel consists of 39 countries and span the 1970-2012 time period. We find that after controlling for global and local risk factors, temperature has a significantly negative impact on equity valuations — that is, higher temperature lowers valuation ratios. Quantitatively, a one degree Celsius increase in temperature leads to about 5% decline in equity valuations. We also find that temperature elasticity has become more negative over time — its magnitude changes from about -3% in the early pre-2000 sample to -5% over the entire sample period. This suggests that during the period over which global temperature has risen, its impact on the economy has increased. Importantly, we show that the negative impact of temperature on equity valuations is driven by its low-frequency (i.e., trend) fluctuations that correspond to global warming. Earlier empirical works by Dell, Jones, and Olken (2012), and Bansal and Ochoa (2012) examine the effect of temperature variations on income growth. In contrast, we focus on forward-looking equity valuations that reflect both long-term expected growth and risk, which past income growth data do not provide.

We calibrate our LRR-T model to match the projected climate-change and consumption dynamics, our estimates of temperature elasticity of equity valuations and the observed discount rates from capital markets.<sup>1</sup> The latter is important, as willingness to abate climate change and the social cost of carbon are highly sensitive to discount rates as highlighted in Nordhaus (2008) and Gollier (2012). The social cost of carbon (SCC) is an important concept in the economic analysis of global warming. Intuitively, it measures the present value of damages due to a marginal increase in carbon emissions and as such, it allows us to quantify and assess the incentive to curb industrial

<sup>&</sup>lt;sup>1</sup> We focus on the exchange economy to maintain tractability and ensure that the model is able to match the asset market data. This is quantitatively difficult to achieve in a production-based setting.

emissions. We find that with a preference for early resolution of uncertainty, the social cost of carbon is quite significant. In our baseline LRR-T model, SCC is measured at about 100 dollars of world consumption per metric ton of carbon. It declines to a still sizable \$40 when temperature is assumed to affect the level of output but not the long-term growth. Thus, when distant risks matter, carbon emissions and rising temperature carry a significant price. In sharp contrast, in a power-utility setting, climate change is not perceived as sufficiently risky because its impact is deferred to the distant future. Consequently, SCC under power-utility preferences is very small, of merely 1 cent.

To further explore the implications of risk preferences, we solve for the socially optimal abatement policy. To this end, we consider a social planner who may choose to abate a prospective increase in temperature and thus limit future disasters by investing in the development of carbon-free technologies. Abatement policies are costly investments that require resources that otherwise could be consumed. The optimal abatement effort, therefore, is chosen by trading off costs of lower current consumption versus benefits of lower climate-change risks in the future. We show that with a preference for early resolution of uncertainty, the social planner opts for an immediate and a relatively stringent abatement policy that allows to avert large disasters in the future. When the planner is indifferent towards the timing of resolution of uncertainty, as in the case of power utility, there is very little willingness to abate climate change. The power-utility planner postpones abatement for nearly 50 years until after the effects of global warming start unfolding, and lets the economy to be exposed to sizable losses. In essence, preferences for early resolution of uncertainty (which are supported by capital market data) are important to motivate early and significant abatement.

The rest of the paper is organized as follows. In the next section, we set up the LRR-T model. Section 2 provides specifics of our calibration. In Section 3, we present the quantitative solution to the model and discuss its implications. In Section 4, we examine the impact of long-run temperature fluctuations on equity prices in the data. Section 5 concludes.

### 1 LRR–T Model

In this section, we set up a unified general equilibrium model of the world economy and global climate. Our LRR-T model accounts for the interaction between current and future economic growth and climate change in a framework that features elements of Epstein and Zin (1989), Bansal and Yaron (2004), and Hansen and Sargent (2006) models. A unique dimension of our model is that it incorporates temperature-induced natural disasters that are expected to have a long-run effect on future well-being. This feature is consistent with by now the consensus view that global warming will have a long-lasting negative effect on ecological systems and human society (IPCC (2007, 2013)).<sup>2</sup>

#### 1.1 Climate-Change Dynamics

We assume that industrial carbon emissions are driven by technologies that are used to produce consumption or output. Let  $Y_t$  denote the total (gross) amount of consumption goods, then the level of CO<sub>2</sub> emissions is given by:

$$E_t = Y_t^{\lambda_t} \,, \tag{1}$$

where  $\lambda_t \geq 0$  is carbon intensity of consumption. The (log) growth rate of emissions is, therefore,

$$\Delta e_{t+1} = \lambda_{t+1} \Delta y_{t+1} + \Delta \lambda_{t+1} y_t \,, \tag{2}$$

where  $e_t \equiv \log E_t$ ,  $y_t \equiv \log Y_t$ , and  $\Delta$  is the first difference operator.

With no abatement efforts, carbon intensity is assumed to be exogenous and we calibrate it to match the projected path of  $CO_2$  emissions under the business-as-usual (BAU) scenario of Nordhaus (2010). We assume that in the long-run limit, both intensity and emissions decline to zero to capture the eventual replacement of current technologies with carbon-free ones as fossil fuel resources become depleted. We will discuss our calibration in more details below.

The accumulation of greenhouse gasses, of which carbon dioxide is the most significant

 $<sup>^{2}</sup>$ While climate change has a broader meaning, we use it to refer to anthropogenic global warming due to the continuing buildup of carbon dioxide in the atmosphere caused by the combustion of fossil fuels, manufacturing of cement and land use change.

anthropogenic source, leads to global warming due to an increase in radiative forcing. The geophysical equation linking  $CO_2$  emissions and global temperature is a modified version of that in Nordhaus (2008)'s DICE model.<sup>3</sup> In particular, we assume that global temperature relative to its pre-industrial level follows:

$$T_t = \nu_t T_{t-1} + \chi e_t \,, \tag{3}$$

where  $T_t$  is temperature anomaly (i.e., temperature above the pre-industrial level),  $e_t$  is the log of CO<sub>2</sub> emissions,  $\nu_t \in (0, 1)$  is the rate of carbon retention in the atmosphere and, hence, the degree of persistence of temperature variations, and  $\chi > 0$  is temperature sensitivity to CO<sub>2</sub> emissions.<sup>4</sup> Note that, effectively, Equation (3) describes a stock of man-made emissions in the atmosphere (i.e., CO<sub>2</sub> concentration), and temperature anomaly is assumed to be proportional to the level of carbon concentration. These dynamics are also consistent with the conclusions of the Fifth Assessment Report of the Intergovernmental Panel on Climate Change (IPCC) that establishes an unequivocal link between the increase in the atmospheric concentration of greenhouse gasses and the rise in global temperature (IPCC (2013)).

We assume that climate change due to global warming has a damaging effect on the economy. Once temperature crosses a tipping point,  $T_t \ge T^*$ , the economy becomes subject to natural disasters that result in a significant reduction of economic growth. The probability of natural disasters and the loss function are described next.

#### **1.2** Consumption Growth Dynamics

Consumption growth follows the dynamics as in Bansal and Yaron (2004) augmented by the impact of natural disasters caused by global warming. The growth rate of gross consumption  $(y_t \equiv \log Y_t)$ 

<sup>&</sup>lt;sup>3</sup>Nordhaus (2008) models carbon-cycle dynamics using a three-reservoir system that accounts for interactions between the atmosphere, the upper and the lower levels of the ocean. The dynamics of temperature that we use is qualitatively consistent with the implications of his structural specification. Also, quantitatively, our calibration is designed to match temperature dynamics under the BAU policy as predicted by Nordhaus (2010).

<sup>&</sup>lt;sup>4</sup>We assume that  $\nu_t$  is increasing in carbon intensity. This feature implies a more persistent effect of emissions at high levels of CO<sub>2</sub> concentration and temperature and is designed to capture re-inforcing feedbacks of global warming due to melting ice and show that increases absorbtion of sunlight, an increase in water vapor that causes temperature to climb further, a more intensive release of carbon dioxide and other greenhouse gases from soils as temperature rises, a reduced absorbtion of carbon by warmer oceans, etc.

is given by:

$$\Delta y_{t+1} = \mu + x_t + \sigma \eta_{t+1} - D_{t+1}, \qquad (4)$$

$$x_{t+1} = \rho_x x_t + \varphi_x \sigma \epsilon_{t+1} - \phi_x D_{t+1}, \qquad (5)$$

where  $\mu$  is the unconditional mean of gross consumption growth;  $x_t$  is the expected growth component;  $\eta_{t+1}$  and  $\epsilon_{t+1}$  are standard Gaussian innovations that capture short-run and longrun risks, respectively; and  $-D_{t+1}$  is a decline in consumption growth due to temperature-induced disasters. Effectively,  $D_{t+1}$  measures an economic cost of global warming.<sup>5</sup>

Note that in our specification climate-change disasters affect current and future expected consumption growth and, therefore, have a permanent effect on the economy. We focus on potentially catastrophic consequences of climate change that might not be possible to reverse or easily adapt to, and as such they are expected to have a permanent effect on human well-being. These include but not limited to rising sea levels and drowning of currently populated coastlines and islands, intensified heat waves, severe droughts, storms and floods, destruction of ecosystems and wildlife, spreading of contagious tropical diseases, shortages of food and fresh water supply, significant destruction of property and human losses. To incorporate these types of large-scale and permanent effects we assume that disasters affect the growth rate of the economy instead of just the current level of output as is typically assumed in the integrated assessment models.<sup>6</sup> A permanent impact of climate change and its implications for policy decisions are also analyzed in Pindyck (2012). We consider a more general specification in which global warming may affect not only current but also future consumption growth. While uncertainty over adaptation to global warming is well recognized, the assumption that rising temperature will have a negative effect on human welfare and global economy is standard in the climate-change literature (eg., Nordhaus (2010), Weitzman (2010), Anthoff and Tol (2012), Pindyck (2012)).<sup>7</sup>

We assume that natural disasters are triggered when temperature reaches a tipping point  $T^*$ 

<sup>&</sup>lt;sup>5</sup>Our specification of climate-change driven disasters as rare tail events is reminiscent of rare disasters models of Rietz (1988), Barro (2009), Barro and Ursua (2012), Gabaix (2012) and Wachter (2013). As we discuss below, different from the standard disaster specifications, disaster risks in our model account for a relatively modest fraction of the overall risk premia.

<sup>&</sup>lt;sup>6</sup>For example, the DICE/RICE models of Nordhaus (2008, 2010), the FUND model of Tol (2002a, 2002b) and Anthoff and Tol (2013), and the PAGE model of Hope (2011).

<sup>&</sup>lt;sup>7</sup>The implications of tail risks in the presence of uncertainty about climate-change impact are analyzed in Weitzman (2009).

and model their impact using a compensated compound Poisson process,

$$D_{t+1} = \sum_{i=1}^{N_{t+1}} \zeta_{i,t+1} - d_t \pi_t , \qquad (6)$$

where  $N_{t+1}$  is a Poisson random variable with time-varying intensity  $\pi_t$ , and  $\zeta_{i,t+1} \sim \Gamma(1, d_t)$  are gamma distributed jumps with a time-varying mean of  $d_t$ . We assume that both occurrence of natural disasters and their damages are increasing in temperature. In particular, the expected size of disasters is given by:

$$d_t = \begin{cases} q_1 T_t + q_2 T_t^2, & \text{if } T_t \ge T^* \\ 0, & \text{otherwise} \end{cases}$$
(7)

and disaster intensity follows:

$$\pi_t \equiv E_t[N_{t+1}] = \begin{cases} l_0 + l_1 T_t, & \text{if } T_t \ge T^* \\ 0, & \text{otherwise,} \end{cases}$$
(8)

where parameters  $q_1$ ,  $q_2$ ,  $l_0$  and  $l_1$  are greater than zero. Quadratic loss functions are commonly used in the climate-change literature, e.g., Nordhaus (2008), Weitzman (2010), Lemoine and Traeger (2012), Golosov, Hassler, Krusell, and Tsyvinski (2011), and Heutel (2012).

#### **1.3** CO<sub>2</sub> Abatement Policies

The social planner may decide to lower the likelihood of natural disasters and the amount of damages incurred by implementing a policy that limits carbon emissions and, consequently, slows down global warming. The decision of which, if any, abatement action to take depends on its benefits and costs.

We model the benefits of policy intervention as an acceleration in the development and adoption of carbon-free technologies. That is, we focus on abatement actions that reduce carbon emissions not only in the short but also in the long run. Specifically, we assume that:

$$E_t^* = Y_t^{\lambda_t^*}, \qquad (9)$$

$$\Delta \lambda_t^* = \Delta \lambda_t - \theta_t , \qquad (10)$$

where  $E_t^*$  and  $\lambda_t^*$  are CO<sub>2</sub> emissions and carbon intensity under a chosen abatement policy,

respectively;  $\lambda_t$  is intensity under the business-as-usual scenario; and  $\theta_t \geq 0$  is the emission reduction function. Effectively, we assume that the matter-of-course long-run decline in carbon intensity under the BAU policy can be speeded up by  $\theta_t$  if the social planner decides to act. Higher values of  $\theta_t$ represent more stringent policies, and  $\theta_t = 0$  corresponds to the BAU scenario.

Abatement policies are costly investments — they require resources that otherwise could be consumed. We assume that emission reductions cost  $\Lambda_t Y_t$  units of consumption goods, and the abatement cost at time t depends on the targeted reduction level  $(\theta_t)$ :

$$\Lambda_t = \xi_t \theta_t^k \,, \tag{11}$$

where  $\xi_t > 0$  and k > 0 (i.e., at any point in time, more stringent abatement policies cost more), and  $\xi_t = \xi_0 e^{-gt}$  is assumed to decline over time at a rate of g > 0. A deterministic decline in the cost function represents an improvement in cost-efficiency of abatement technologies over time.

#### 1.4 Cost-Benefit Tradeoff

Under the BAU scenario, agents in the economy consume all available goods. Thus, their consumption is given by:  $C_t = Y_t$ . If an abatement policy is adopted, agents have to give up a fraction of consumption goods to finance the policy in place. Consequently, their consumption is reduced by the policy implementation costs:

$$C_t = Y_t (1 - \Lambda_t) \,, \tag{12}$$

and the actual consumption growth (in logs) is given by  $\Delta c_t \approx \Delta y_t - \Delta \Lambda_t$ . The net-of-costs consumption growth, therefore, follows:

$$\Delta c_{t+1} = \mu - \Delta \Lambda_{t+1} + x_t + \sigma \eta_{t+1} - \phi_c D_{t+1}.$$
(13)

In essence, by adopting an abatement policy, the social planner trades off costs of lower current consumption versus benefits of lower risk of natural disasters and lower damages in the future.

#### 1.5 Preferences

Following the long-run risk literature, we define preferences recursively as in Kreps and Porteus (1978), Epstein and Zin (1989), and Weil (1990). We use  $U_t$  to denote the continuation utility at time t, which is given by:

$$U_{t} = \left\{ (1-\delta)C_{t}^{1-\frac{1}{\psi}} + \delta \left( E_{t} \left[ U_{t+1}^{1-\gamma} \right] \right)^{\frac{1-\frac{1}{\psi}}{1-\gamma}} \right\}^{\frac{1}{1-\frac{1}{\psi}}},$$
(14)

where  $\delta$  is the time-discount rate,  $\gamma$  is the coefficient of risk aversion, and  $\psi$  is the intertemporal elasticity of substitution (IES). When  $\gamma = \frac{1}{\psi}$ , than preferences collapse to the power utility specification, in which the timing of the resolution of uncertainty is irrelevant. When risk aversion exceeds the reciprocal of IES,  $\gamma \geq \frac{1}{\psi}$ , early resolution of uncertainty about future consumption path is preferred. Power utility is the standard assumption in the integrated assessment models of climate change. Preferences for early resolution of uncertainty are the benchmark in the longrun risks literature and, as emphasized in Bansal and Yaron (2004), are critical for explaining the dynamics of financial markets. We consider both specifications and highlight the importance of preferences to risks and to temporal resolution of risks for the analysis of global warming and policy decisions.

Note that the maximized life-time utility is proportional to the wealth to consumption ratio,  $Z_t \equiv \frac{W_t}{C_t}$ , and as such is determined by the present value of expected consumption growth from now to infinity. In particular,

$$U_t = \left[ (1-\delta)Z_t \right]^{\frac{\psi}{\psi-1}} C_t \,, \tag{15}$$

and

$$Z_t = E_t \left[ \sum_{j=0}^{\infty} \frac{C_{t+j}/C_t}{R_{j,t+j}} \right],\tag{16}$$

where  $R_{j,t+j}$  is the discount rate of the consumption strip with *j*-time to maturity. Because prices are forward-looking, the current price of the consumption claim (and that of market equity) carries information about the impact of climate change on future economic growth and risk.

#### 1.6 Dynamic Optimization Problem

Each period, the social planner makes a decision of which abatement policy  $\theta_t$  is optimal to implement by solving utility-maximization problem. Let  $\mathbb{S}_t$  summarize the state of the economy and climate at time t:  $\mathbb{S}_t = \{T_t, Y_t, \lambda_t, \Lambda_t, x_t\}$ . The dynamic optimization problem can be described recursively as:

$$U_t(\mathbb{S}_t) = \max_{\theta_t, C_t} \left\{ (1-\delta) C_t^{1-\frac{1}{\psi}} + \delta \left( E_t \left[ U_{t+1} (\mathbb{S}_{t+1})^{1-\gamma} \right] \right)^{\frac{1-\frac{1}{\psi}}{1-\gamma}} \right\}^{\frac{1}{1-\frac{1}{\psi}}},$$
(17)

s.t. 
$$C_{t+1} = Y_{t+1}(1 - \Lambda_{t+1}),$$
 (18)

$$\mathbb{S}_{t+1} = F(\mathbb{S}_t, \theta_t) \,. \tag{19}$$

Utility maximization is subject to two constraints: the resource allocation constraint in Equation (18), and the state dynamics in Equation (19), where  $F(\cdot, \cdot)$  summarizes the transitional dynamics of the state vector under the chosen policy.

We solve the dynamic programming problem numerically using value function iterations. We start at the "terminal" date at which temperature anomaly disappears and the solution becomes stationary, and work backwards in time. We discretize the state space and use Chebyshev polynomial approximation of the value and abatement policy functions. Expectations at the maximization stage (see Equation (17)) are computed via simulations. Notice that the optimal abatement policy that we derive is dynamically consistent, thus, future abatement decisions will comply with the policies chosen today.

#### 1.7 Social Cost of Carbon

The social cost of carbon (SCC) has become an important concept in the cost-benefit analysis of global warming. SCC measures the present value of damages due to a marginal increase in carbon emissions. Formally, it is defined as marginal utility of carbon emissions:

$$SCC_t = \frac{\partial U_t}{\partial E_t} \Big/ \frac{\partial U_t}{\partial C_t}$$
 (20)

The scaling by marginal utility of consumption allows us to express the cost in units of consumption goods (time-t dollars), which makes SCC easy to interpret. Using Equation (15), we can express the social cost of carbon at time 0 as:

$$SCC_0 = \frac{\psi}{\psi - 1} \frac{\partial Z_0 / \partial E_0}{Z_0} C_0.$$
<sup>(21)</sup>

That is, SCC is equal to the (appropriately scaled) monetized value of a percentage change in wealth due to an additional unit of emissions. Intuitively, the social cost of carbon measures an increase in current consumption that is required to compensate for damages caused by a marginal increase in date-0 emissions.

### 2 Calibration of the BAU Scenario

We calibrate the path of carbon intensity  $(\lambda_t)$  and temperature  $(T_t)$  in the absence of any abatement efforts to match the business-as-usual forecasts of CO<sub>2</sub> emissions and global warming in Nordhaus (2010) and IPCC (2007, 2013). Time in the model is measured in decades and we assume that the steady state in the BAU case will be reached in 60 periods or 600 years from now. The steady state corresponds to the state in which anthropogenic emissions decline to zero and the temperature anomaly disappears due to the ultimate de-carbonization of the economy. The first two panels of Figure 1 show the calibrated path of carbon intensity and the amount of emissions along the transitional path. Under the BAU policy, carbon intensity is expected to remain relatively high over the next two centuries and carbon emissions accelerate since the economy is growing.

As more and more CO<sub>2</sub> emissions are released, the concentration of carbon in the atmosphere increases and temperature anomaly escalates. The projected BAU path of temperature is shown in Panel (c) of Figure 1. Calibration of global warming dynamics and the impact of climate change on consumption growth are presented in Table I.<sup>8</sup> To capture re-enforcing feedback effects of emissions, we allow the retention of carbon in the atmosphere,  $\nu_t$ , to increase in carbon intensity. We assume that about 80% of current CO<sub>2</sub> emissions will remain in the atmosphere for another century, their decay will increase as the rate of emissions slows down. The average value of the retention rate under the BAU scenario is equal to 0.962, which implies that about 70% of CO<sub>2</sub> molecules emitted along

<sup>&</sup>lt;sup>8</sup>To facilitate interpretation of the calibrated parameters, we report and discuss them in annualized terms.

the transitional path are removed from the atmosphere within a century. The precise atmospheric life of carbon dioxide is yet unknown but our calibration is designed to roughly match the available estimates in the geophysical literature (Jacobson (2005), and Archer (eg., 2005, 2009)).

We set the tipping point of global warming disasters to 2°C that according to the Copenhagen accord is internationally recognized as a likely trigger of dangerous changes in the climate system. If the current trend in emissions continues, temperature is expected to cross the disaster threshold in about 30-35 years from now (see Figure 1). This assumption is fairly consistent with the most recent forecast of the IPCC. As reported in the Fifth Assessment Report, the global mean surface temperature anomaly is expected to exceed 2°C in three to four decades from now (IPCC (2013)).

Once the 2°C tipping point is crossed, the global economy faces the risk of natural cataclysms. Both intensity and size of climate-induced disasters are increasing with temperature and their expected paths are presented in Figure 2. Time-varying intensity dynamics are motivated by the evidence in Raddatz (2009) that, worldwide, the number of climatic disasters (such as droughts, floods, and extreme temperature) has increased over the last four decades — the period that has experienced a steep increase in temperature. The initial impact of global warming is assumed to be relatively moderate but it is intensified as temperature keeps rising. In particular, we assume that upon the crossing of the 2°C threshold, the annual probability of disasters is about 1.2% and their average size is -0.7%. As temperature reaches its peak, the disaster probability rises to 2.8% per annum and average losses increase to -6.0%.

Table II summarizes our calibration of preferences and consumption dynamics. Our LRR-T model features preferences for early resolution of uncertainty and incorporates a negative effect of global warming on current and future consumption growth. We choose preference parameters so that the model is able to match key moments of financial data. In particular, we set risk aversion at 5, the intertemporal elasticity of substitution at 1.5, and the subjective time-discount factor at 0.99. We set the unconditional mean of consumption growth at 1.8% and assume that the standard deviation of i.i.d. gaussian shocks is 1.6% per annum. We calibrate the dynamics of the long-run risk component to match persistence of consumption growth in normal times. Consistent with the US consumption data, in our specification the first-order autocorrelation of consumption growth absent climate disasters is equal to 0.44. Exposure of the expected consumption growth to disaster risks is set at 0.05. Note that while the average size of climate disasters in the expected growth component

is assumed to be quite modest, their effect on consumption is propagated due to persistence of long-run risks. That is, upon a disaster, consumption growth does not immediately bounce back to its normal level but is expected to remain low for a relatively long while.

Note that in contrast to the standard integrated assessment models, in which climate change is assumed to cause a deterministic loss in future output or consumption, in our model, global warming affects the economy entirely through a risk channel. Figures 3 and 4 illustrate the implications of global warming for the distribution of consumption growth in our baseline specification. Notice that because temperature-induced disasters are compensated, they have no effect on the ex-ante mean of log consumption growth (see Panel (a) of Figure 3). Thus, similar to gaussian i.i.d. and long-run risks, ex-ante, global warming does not affect the log level of future consumption path but does affect its variation. As Panel (b) of Figure 3 shows, climate-change driven disasters increase the annualized ex-ante volatility of cumulative consumption growth by up to 0.18% (which is more than ten percent increase in volatility relative to a no-disaster case). Also, because global-warming disasters represent tail risks, the distribution of future consumption growth is both negatively skewed and fat-tailed. A side-by-side comparison of the distribution of the normalized consumption growth at the peak of climate-driven disasters and the corresponding distribution absent disasters is presented in Figure 4. To summarize, while ex-ante, global-warming does not alter the future path of consumption, it introduces an additional source of risk in the economy. Thus, ex-post, global warming consequences for consumption can be substantial.

In addition to our LRR-T model, we discuss three alternatives. In all alternative specifications, we shut down the long-run risk channel and assume that global warming affects only realized consumption growth. That is, if a disaster is realized, the level of consumption declines on impact but future consumption growth remains unaffected. We use these simplified dynamics to analyze the implications of risk preferences for policy decisions on climate change. To this end, we consider three preference specifications: (1) preference for early resolution of uncertainty, which we refer to as "KPEZW-Preferences", (2) power utility with high degree of risk aversion — "CRRA-highRA", and (3) power utility with low risk aversion — "CRRA-lowRA". In the KPEZW-case, we maintain the same preference configuration as in our LRR-T model. In the case of power utility, we set either risk aversion or IES at their corresponding baseline values. That is, under CRRA-highRA preferences, risk aversion is set at 5, and in the CRRA-lowRA case, risk aversion is set at 0.67 (the

reciprocal of our baseline IES value of 1.5).

In our set-up, abatement policies are specified as an effort to stimulate the development and adoption of carbon-free technologies and, as such, they lead to a permanent reduction in emissions. Anthoff and Tol (2013) also allow abatement efforts to have a permanent effect, at least in part. Given the similarities in our modeling approaches, we calibrate the abatement cost function to be consistent with mitigation costs implied by their FUND model. More ambitious abatement efforts cost more and we assume that the cost function is convex by setting k at 1.5, the scale parameter  $\xi_0$  is set at 5 (see Equation (11)). Abatement costs decline over time at a rate of 1.5% per annum that is chosen to match the average TFP growth in the post-war US economy.

The dynamics of future climate changes and their economic consequences are highly uncertain and not yet well-understood. While some empirical evidence on the impact of rising temperature and climatic disasters does exist, it is based on human experiences that have not yet been subjected to catastrophic climate changes that we consider. Therefore, we can use it only as a guidance rather than a target. Whenever possible, we calibrate the model parameters to be broadly consistent with assumptions of the standard integrated assessment models and consensus forecasts outlined by the IPCC. With this in mind, we do not intend to claim that our calibrated dynamics represent the future better than others. We consider plausible dynamics and focus on highlighting the channels through which beliefs about climate-change risks and risk preferences affect policy decisions. To discriminate across the LRR-T model and alternative specifications, we confront each with financial market data and empirical evidence on the impact of rising temperature on equity prices.

## 3 Policy Decisions and Welfare Implications

We begin our analysis with the LRR-T model, in which agents have preferences for early resolution of uncertainty and global warming has a permanent effect on the economy through climate-induced disasters in realized and expected consumption growth. Afterwards we consider simplified dynamics for consumption growth and explore the implications of risk preferences for the optimal cost-benefit tradeoff and welfare.

#### 3.1 LRR-T Model

In our model, detailed in Table II, temperature risks have a negative effect on consumption level and future growth and agents care about long-run risks through preferences for early resolution of uncertainty. Solving the maximization problem, we find that the social planner in this environment opts for a stringent mitigation policy from the very beginning despite the fact that earlier efforts are relatively costly. The optimal level of abatement effort ( $\theta_t$ ) and its cost ( $\Lambda_t$ ) are presented in Figure 5. Figure 6 illustrates the policy implications for carbon emissions and temperature. Recall that earlier abatement efforts are valuable as they yield long-term benefits, i.e., an earlier development and adoption of carbon-free technologies implies a progressive increase in emission reductions over time. Panel (a) of Figure 6 shows that industrial carbon emissions under the optimal policy are expected to decline by about 80% in 100 years from now and essentially disappear by 2200. It is optimal to give up about 0.03% of the current output and up to 0.95% later on to mitigate climate risks. And while it is too costly to contain temperature anomaly under the tipping point, the achieved reduction in carbon emissions guarantees that it does not exceed 2.8°C and does not stay above the disaster threshold for too long.

Note that in the BAU scenario, even at the peak of temperature anomaly, climate-induced catastrophes are low-probability events. On average, the highest likelihood of disasters is short of 3% per year. However, if realized, their economic consequences can be highly significant. Panel (a) of Figure 7 shows that the 90%-confidence interval of disaster size under the business-as-usual scenario includes quite substantial losses of as large as 15%–18% of consumption. In our specification, these damages are non-recoverable — they lead to a permanent decline in consumption level and a long-term reduction in growth. Under preferences for early resolution of uncertainty, such low-probability yet sizable and persistent events represent a significant concern that makes the social planner act today to prevent them in the future. Panel (b) of Figure 7 shows that the optimal abatement policy effectively eliminates catastrophic outcomes. The average size of disasters is reduced to under 1% and the 95-percentile of the disaster-size distribution is kept well under 4%. Notice also a significant reduction in duration of global warming disasters under the optimal policy — disaster period starts later and is expected to last for only few decades.

By trading off a fraction of current consumption for limiting the likelihood and size of disasters

in the future, agents are able to achieve a significantly higher level of utility relative to the businessas-usual scenario. The utility gain of the optimal abatement policy is around 11%. The immediate call for action is also reflected in the social cost of carbon, which is quite sizable under the LRR-T specification. As shown in Table III, under the business-as-usual scenario, SCC is estimated at about \$104 per ton of carbon. The social cost of carbon is measured in 2012 dollars of world household final consumption expenditure per metric ton of carbon. In the presence of risks that affect long-term growth, agents' utility is highly sensitive to emissions due to both high potential damages and late resolution of climate risks. The two channels combined lead to the high price of carbon emissions.

Temperature risks aside, our LRR-T specification corresponds to the long-run risks model of Bansal and Yaron (2004). As they show, with preferences for early resolution of uncertainty, risks that matter for the long run carry high risk premia and are able to account for the dynamics of equity prices and asset returns. Our calibration of the gaussian part of consumption dynamics is similar to theirs and, therefore, is consistent with financial market data. As Table IV shows, the average risk-free rate in the LRR-T specification is 0.9%, and the risk premium on consumption claim is about 1.7%. Hence, the implied equity premium, assuming leverage of around 2–3, is about 3.5–5% per annum. It is important to emphasize that most of the risk premium is the compensation for long-run gaussian risks, and only a relatively modest fraction of it is due to temperature risks.

#### **3.2** Welfare Implications of Risk Preferences

To examine the effect of preferences for welfare implications and policy decisions, we consider three alternative specifications. In all of them, we simplify consumption dynamics by shutting off the longrun risk component and assume that the only effect of global warming is through its negative impact on realized consumption growth. Under these dynamics, climate risks continue to have a permanent negative impact on consumption level but are assumed to have no effect on future economic growth. We compute and compare optimal climate policy decisions of three social planners under different risk preferences: preferences for early resolution of uncertainty, power utility with high degree of risk aversion (and low IES) and power utility with low risk aversion (and high IES) as summarized in Table II.

Figure 8 plots the optimal level of abatement cost and the implied path of temperature for each

alternative specification. Consider first the economy with KPEZW-preferences. As Panel (a) shows, the optimal response of the social planner under preferences for early resolution of uncertainty is to promptly set up an abatement policy to slow down global warming and to avert large disasters. Because the amount of temperature risks in the alternative set-up is smaller, the initial scale of abatement is somewhat lower relative to that in the LRR-T model, yet similarly, an abatement policy is set in motion right away and abatement efforts are accelerated at a high rate in the future.

The optimal response to climate risks in a power-utility setting is quite different. A power-utility planner (under the two risk-aversion configurations) chooses to postpone abatement into the future and even then implements a relatively modest level of effort. In fact, as Figure 8 shows, both high- and low-RA power-utility planners find it optimal to do nothing until temperature crosses over the tipping point and the likelihood of economic disasters becomes nontrivial. From their perspective, current abatement costs outweigh future benefits and they do not act until climatechange risks become real. In other words, the optimal response to global warming of power-utility planners is to mitigate it as it unfolds rather than to prevent it. Even at the peak of climate-driven disasters, power-utility planners are willing to spend only a small amount on abatement efforts, letting temperature stay well above the disaster threshold for a very long while. As Panel (b) shows, under the KPEZW-based optimal policy, temperature anomaly is kept under 3.3°C and the disaster period lasts for approximately one hundred years; whereas under the CRRA-based optimal policies, temperature anomaly reaches 5°C and climate-induced disasters stretch out over more than 200 years.

The reluctance to mitigate global warming in the power-utility settings is reflected in the social cost of carbon, which under power utility is quite trivial. As Table III shows, SCC is merely 1 cents per metric ton of carbon in the high risk-aversion configuration and virtually zero in the case of low risk aversion. This suggests that in the power-utility settings, climate-change risks are essentially discounted out as they are expected to realize in a relatively distant future. In contrast, with preferences for early resolution of uncertainty, distant climate risks carry a significant weight and their importance is reflected in a sizable \$42 social cost of carbon. Also, while optimal abatement efforts are welfare improving in all three cases, their quantitative benefits are quite different. The utility gain of the chosen optimal policy under KPEZW-preferences is a significant 4.0%, whereas it is only 0.02% and essentially zero in the power-utility setting with high and low risk aversion,

respectively.

The magnitude of the social discount rate has become a subject of controversy and disagreement in the climate-change literature. The level of the discount rate is certainly important for translating future damages into their present-value terms, particularly in the context of global warming which impact is expected to unfold over the course of centuries and, therefore, entails long-term discounting. However, the magnitude of the discount rate that has attracted so much attention, by itself, is not sufficient for understanding welfare implications of climate-change risks. To illustrate the point, we refer to Table IV that presents asset pricing implications of the alternative specifications. First, compare the implications of KPEZW-preferences and power utility with the low degree of risk aversion. Because the intertemporal elasticity of substitution is the same, the risk-free rates and therefore discount rates in the two specifications are very similar of about 2.2-2.3%. To be precise, the level of discount rates of consumption strips across all maturities is slightly higher in the KPEZW-case compared with CRRA-lowRA preferences. Given that the damage function is identical, the present value of expected global warming damages in the power-utility case is higher than that in the case of KPEZW-preferences. Yet, among the two, it is the planner with KPEZW-preferences who is concerned with climate-change risks and attaches a high price tag to carbon emissions. Further, if we now compare the two power-utility specifications, we find that despite big differences in discount rates (10.3% v.s. 2.2% under high and low risk aversion,respectively), both social planners care equally little about temperature risks and do not consider early or significant abatement efforts worthwhile. That is, in a power-utility economy, whether it is characterized by high or low discount rates, distant temperature risks are not considered a pressing issue and, consequently, current carbon emissions carry an almost zero marginal price. This evidence demonstrates that the optimal response to climate-change risks is not simply a matter of discounting but rather of temporal characteristics of climate risks and risk preferences.

What accounts for differences in optimal climate policies and welfare implications is the elasticity of discount rates and utility to carbon emissions. Hansen and Scheinkman (2012), and Borovička and Hansen (2014) provide a rigorous analysis of cash-flow and price elasticities. We illustrate them graphically in Figure 9. Consider a one-percent increase in carbon emissions at time 0. The additional amount of emissions leads to marginally higher temperature and, hence, a higher probability and a larger size of disasters in the future. Panel (a) of Figure 9 shows the percentage increase in annual expected damages due to the increase in current emissions. This is the negative cash-flow effect of the additional unit of emissions, which is invariant to preferences. The discountrate effect and therefore wealth implications are preference-dependent. As shown in Panel (b), under KPEZW-preferences, an increase in current emissions leads to an increase in risk premia and a fall in asset prices. In particular, the current wealth to consumption ratio of KPEZW-agents declines by 0.003% and their utility decreases by 0.009%. In contrast, in the CRRA-highRA economy, discount rates fall significantly in response to higher emissions due to a fall in the risk-free rates. The negative discount-rate effect dominates the negative cash-flow effect resulting in an increase in current prices. That is, under power utility, the wealth to consumption ratio is actually higher if disaster losses are expected to be bigger. The power-utility agents are still worse off since their utility is inversely related to wealth, but because both the elasticity of wealth to emissions and the elasticity of utility to wealth are quite low, the decline in utility is very tiny, more than three orders of magnitude smaller than the corresponding decline under recursive preferences. As the figure also shows, the elasticity of discount rates and, consequently, utility in the case of power utility with low risk aversion is virtually zero. To summarize, with preferences for early resolution of uncertainty, the planner is wary of risks that are going to be realized in the distant future and does not disregard them as easily as the power-utility planners. Consequently, the life-time utility of KPEZW-agents is more sensitive to emissions compared with power-utility preferences, which is reflected in the higher social cost of carbon.

### 4 Temperature Risks and Asset Prices

In our model, rising temperature has a negative effect on the macro-economy — it lowers future growth and raises economic risk. Further, with a preference for early resolution of uncertainty, higher temperature leads to a decline in aggregate wealth to consumption ratio. The empirical research on the impact of global warming on the macro-economy has primarily focused on the effect of temperature on growth. For example, Dell, Jones, and Olken (2012) analyze the impact of rising temperature on output and find evidence that current output and short-term future growth tend to decrease with temperature, although the negative effect seems to be entirely concentrated in low-income countries. In our empirical work, we take a different approach and measure the impact of temperature on the macro-economy using forward-looking equity prices rather than past growth rates. Long-horizon equity prices reflect information about future expected growth rates and future risks. Hence, if temperature is expected to affect future growth and/or risk, these expectations ought to be reflected in capital markets provided that agents care about the future. This is the idea that we pursue in our empirical analysis of equity prices and temperature fluctuations. To preview our findings, our empirical evidence suggests that temperature risks are likely to have a persistent negative effect on the global economy and points towards preferences for early resolution of uncertainty.

#### 4.1 Data

To measure the economic impact of temperature, we use country-level panel data that cover 39 countries and span the time period from 1970 and 2012. Country-level temperature that correspond to land-surface temperature anomaly are taken from the Berkeley Earth open database. Temperature anomaly is measured in degrees Celsius and is defined relative to the 1951-1980 average. The price-dividend data come from the Global Financial Data and provide a market proxy for the wealth-to-consumption ratio for each country. Country-specific macro data (such as gross domestic product, inflation, unemployment, real interest rates) are taken from the World Bank database. To control for income-heterogeneity, we divide countries into three income groups (lower middle, upper middle and high income) according to the World Bank income classification.<sup>9</sup> The list of 39 countries is provided in Table V. This is the most exhaustive set with reliable equity market data that we could find, as such, it is tilted towards developed economies as they are more likely to have a history of equity markets.

In our sample, 38 out of 39 countries have experienced a significant increase in temperature over the sample period. The median temperature anomaly across countries is about 0.38°C and over the last decade, between 2003 and 2012, the anomaly averages 0.73°C. Figure 10 shows the histogram of the temperature anomaly in the most recent decade in our sample. We find that local temperature series have a strong common component that is highly correlated with variation in global temperature. The first principal component of annual temperature series accounts for about 53% of the total variation in temperature across countries and has a 71% correlation with

<sup>&</sup>lt;sup>9</sup>Due to the unavailability of asset price data, our sample does not include countries in the low income category.

global temperature anomaly. At low frequencies, the co-movement in local temperature becomes much stronger — 81% and 92% of the overall variation in the five- and ten-year averages of local temperature, respectively, are captured by the corresponding first principal components. As illustrated in Figure 11, the low-frequency component of local temperature essentially corresponds to the trend in global warming.

Our analysis of equity prices reveals a strong low dimensional factor structure in price-dividend ratios. We find that the first principal component extracted from the cross-section of price-dividend ratios accounts for about 69% of the total variation in prices across countries and the second component explains an additional 10%. This suggests that the cross-country variation in equity valuations is dominated by few common macro-economic factors. Jagannathan and Marakani (2015) show that the first two price-dividend ratio factors provide robust proxies for future economic growth and variation in macro-economic uncertainty. Guided by their evidence, we use the first two principal components to control for global macro-economic risks in our regression analysis.

#### 4.2 Impact of Temperature on Equity Valuations

To estimate the effect of temperature risks on asset prices, we run the following panel regression:

$$v_{i,t} = \bar{v}_i + \phi_K \,\overline{T}_{i,t}^K + \alpha'_c C_{i,t} + \alpha_v v_{i,t-1} + \varepsilon_{i,t}$$

$$\tag{22}$$

where  $v_{i,t}$  is the log of the equity price-dividend ratio of country *i* at date *t*,  $\bar{v}_i$  is the countryspecific fixed effect,  $\overline{T}_{i,t}^K$  is a *K*-year moving-average of local temperature, and  $C_{i,t}$  is a set of controls that captures the effect of global (and local) risks on asset prices, i.e., macro-economic risks that are distinct from temperature. To analyze the impact of temperature fluctuations at different frequencies, short and long, we consider different *K*'s ranging from one to eight years (note that when K = 1,  $\overline{T}_{i,t}^K$  corresponds to annual temperature anomaly). In our baseline specification that we refer to as Specification I, we control for common global macro-economic variation using two price-dividend ratio factors.<sup>10</sup> To confirm the robustness of our evidence, in Specification II we

<sup>&</sup>lt;sup>10</sup>To allow global macro risks to have differential effect across countries, we also include the interaction of the two principal components with country-income dummies. While the estimates on the interaction terms are mostly significant, their inclusion has virtually no effect on the estimated elasticity of equity prices to temperature risks and its significance. Therefore, for parsimony, we report evidence based on the specification with no interaction terms.

consider a richer set of controls that in addition to global factors includes country-specific variables. The set of local controls comprises inflation, real interest rate, expected growth in gross domestic product (gdp), and change in the unemployment rate.<sup>11</sup> The remaining persistence in asset prices is absorbed by the lagged country-specific price-dividend ratio.

Our focus is on parameter  $\phi_K$  that measures sensitivity of equity prices to local temperature variations. The estimates of temperature elasticities are reported in Table VI. For brevity, we present and discuss the weighted least-squares estimates; the point estimates and inference based on the ordinary least-squares are quite similar. We find that at both short and long horizons, temperature risks have a significant negative effect on equity valuations. In Specification I, the estimated elasticities vary between -0.057 (t-stat = -4.4) at the short horizon and -0.125 (t-stat = -4.2) at the long horizon. To interpret the magnitude of the estimates, note that  $\phi_K$  measures semi-elasticity of asset prices to temperature fluctuations. Hence, controlling for country fixed effects and global macro-economic risks, a one standard-deviation increase in annual temperature anomaly of around  $0.53^{\circ}$ C leads to about 3% decline in equity valuations. The impact of low-frequency temperature risks is similar — for example, a one standard-deviation increase in the five-year temperature trend lowers equity valuations by about 3.4%. The evidence is robust to the inclusion of local controls. In Specification II, the estimated elasticities are all significantly negative and the magnitude of temperature risks on equity valuations varies from -2.5% at the one-year horizon to -2.9% at the five-year horizon.<sup>12</sup>

To insure that our evidence is not spuriously driven by a relatively high degree of persistence of temperature series especially at long horizons, we replace the level of temperature trend in Equation (22) with its innovation. We extract temperature shocks for a given horizon K by fitting a first-order auto-regression (AR(1)) to the K-year moving-average trend in local temperature. The estimated responses of equity prices to temperature innovations, presented in Table VII, are all negative and statistically significant. On average across different horizons, the price impact of a one standard-deviation innovation in temperature implied by the estimates is around -1.6% and -1.7% under

<sup>&</sup>lt;sup>11</sup>We use simple AR(1) dynamics to construct expected gdp growth. We include expected growth because it has a much stronger significance for prices compared with realized growth, but our evidence on temperature elasticities is robust if instead we use realized gdp growth as a control variable.

 $<sup>^{12}</sup>$ The magnitude of t-statistics in Specification II is somewhat smaller compared with Specification I, which we find is mostly due to a shorter panel of data rather than the inclusion of the local controls. Note that in Specification I, the panel consists of 39 countries and spans the period from 1970 to 2012. In Specification II, the panel is reduced to 35 countries over the 1980-2009 period due to the lack of the country-level controls.

Specifications I and II, respectively.

In Table VIII we explore if the effect of temperature on the economy has changed across time. Ideally, to uncover such changes, we would want to compare temperature elasticities measured over earlier and more recent sample periods. This, however, is not entirely feasible given the fairly short span of the available data. Therefore, to explore time-variation in elasticities we estimate them using overlapping samples. In our baseline specification, we start with the early 1970-2000 sample and then progressively increase the sample end to 2005 and 2012 by adding more recent data. In Specification II, the sample starts in 1980 and the sample end varies between 2000 and 2009. Our estimates reported in Table VIII show that the effect of temperature on equity valuations has risen considerably over time. At the one-year horizon, the point estimates change from -0.025 and -0.035in the early sample to -0.057 and -0.050 in the full sample in Specifications I and II, respectively. Similarly, the price impact of temperature risks measured at lower frequencies (i.e., for K > 1) almost doubles when more recent data are incorporated in estimation. This evidence suggests that as temperature rises, global warming imposes higher risks on the economy and, therefore, leads to a larger decline in wealth. As we discuss below, our model is consistent with this evidence — in the model, rising temperature increases the size and the probability of disasters over time, leading to a steeper decline in aggregate wealth.

To measure the economic impact of temperature risks we exploit both time-series and crosssectional variation in temperature. As mentioned above, local temperature series, especially their low-frequency fluctuations, feature a strong common (global) component. In Table IX we explore to what extend global temperature risks affect capital markets. The table shows the response of equity valuations to global temperature estimated by running a panel regression as in Equation (22) but using global temperature anomaly instead of local temperature series. We find that global temperature risks have a negative (and mostly significant) effect of equity prices. This evidence suggests that, to a large extent, common time-series variation in temperature across countries accounts for the negative elasticity of equity valuations to local temperature risks. That is, common time-series dynamics are highly informative but so is the cross-sectional variation in local temperature trends. In unreported results, we run a horse race between local and global temperature series by including them both in our regression specifications and find that although the estimates of both slope coefficients are negative, the estimate on local temperature risks is always statistically significant while the estimate on global temperature is typically not.

#### 4.3 Long-Run vs. Short-Run Temperature Risks

As shown in Tables VI–IX, long-run temperature risks represented by variations in three-, five- and eight-year moving-average trends as well as short-run annual temperature risks have a significant negative effect on equity valuations. Note that year-to-year changes in temperature capture two types of risks: short-run or weather-type risks and low-frequency temperature variations associated with global warming. To understand which risks matter more, we consider the following panel regression:

$$v_{i,t} = \bar{v}_i + \phi_{LR} LRshock_{i,t}^K + \phi_{SR} SRshock_{i,t} + \alpha'_c C_{i,t} + \alpha_v v_{i,t-1} + \varepsilon_{i,t} , \qquad (23)$$

where  $LRshock_{i,t}^{K}$  proxies for low-frequency temperature risks and is measured by an AR(1)innovation in the K-year moving-average of local temperature, for  $K = \{3, 5, 8\}$ , and  $SRshock_{i,t}$ is the annual change in local temperature orthogonalized with respect to long-run shocks. We orthogonalize short- and long-run temperature fluctuations in order to identify their separate effects. The estimates of long- and short-run elasticities,  $\hat{\phi}_{LR}$  and  $\hat{\phi}_{SR}$ , are presented in Table X.

Consistent with the evidence discussed above, we find a negative and statistically significant response of asset prices to low-frequency variations in temperature. Further, the comparison of Tables VII and X reveals that adding short-run temperature series has virtually no effect on the point estimates of long-run temperature elasticities and their significance. We also find that once we control for long-run fluctuations in temperature, short-run temperature risks have no significant effect on equity prices. That is, the negative impact of temperature on the economy is driven by its low-frequency (i.e., trend) risks that correspond to global warming. As Table X shows, our results are robust if alternatively we measure long-run temperature risks using the Hodrick and Prescott (1997) filter.

To further examine the impact of long- and short-run temperature risks on equity prices, we estimate their joint dynamics using a first-order vector-autoregression (VAR). Specifically, we exploit

the following panel VAR specification:

$$X_{i,t} = \bar{a}_i + A X_{i,t-1} + b C_t + u_{i,t}$$
(24)

where  $X_{i,t} = (\overline{T}_{i,t}^8, T_{i,t}, v_{i,t})'$  is a vector of the eight-year moving-average of local temperature, the annual temperature series and the price-dividend ratio of country *i*. We include country fixed effects  $(\overline{a}_i)$  and use the two price-dividend ratio factors to control for global risks ( $C_t$  denotes the vector of global controls). The VAR-regression output is reported in Table XI, and in Figure 12 we plot the implied impulse responses of equity prices to a one-standard deviation shock in temperature trend  $(\overline{T}_{i,t}^8)$  and a one-standard deviation innovation in annual temperature ( $T_{i,t}$ ). The shaded area around the estimated responses represents the two standard-error band. As Panel (a) shows, the VAR-based response of equity prices to low-frequency temperature risks is significantly negative. Notice also that the effect of trend shocks is quite persistent – an increase in temperature trend leads to a decline in equity prices on impact and in the long run. Similar to the evidence presented above, short-run temperature fluctuations do not seem to have any sizable effect. In all, our empirical suggests that a persistent increase in temperature that contributes to global warming has a significant negative impact on the world economies.

#### 4.4 Model-Implied Impact of Temperature

In Table XII we report the model-implied response of the price to consumption ratio to temperature risks under various specifications of preferences and time-series dynamics. For each specification that we discussed above, we simulate 50,000 paths of emissions, temperature and consumption and solve for the price of the consumption claim. Then, similarly to the data, we regress the log of the price-consumption ratio (valuation ratio) on temperature controlling for the relevant state variables. Note that in our model, all temperature fluctuations reflect long-run temperature risks because our model abstracts from any short-run weather-type variations. Hence, our model-based estimates measure elasticities of consumption claim prices to long-run temperature risks.

As the table shows, under recursive preferences, valuations fall in response to an increase in temperature. In particular, in out baseline LRR-T model, a 0.53°C increase in temperature, which corresponds to one standard deviation of the empirical distribution, lowers the price of the

consumption claim by about 0.92%. While this magnitude seems lower than the empirical estimates, it is important to recognize that inside the model we consider the consumption-paying asset whereas in the data we measure the response of the market equity. If we account for market leverage of about 2–3, the response of equity prices to temperature shocks implied by our LRR-T specification would be between -2.8% and -1.8%, which is very similar to our empirical estimates. Also, consistent with the empirical evidence presented in Table VIII, the model-implied sensitivity of asset prices to temperature risks increases as the economy approaches the disaster threshold. In particular, ten and twenty years from now, the price response rises in magnitude from the current -0.0174 to -0.019and -0.021, respectively.

The power-utility implied response of prices to permanent temperature risks is very different compared with recursive preferences. As Table XII shows, in the power-utility case, asset prices rise with temperature. This is the discount-rate or, more precisely, the risk-free rate effect that we discussed above. In the power-utility setting, an increase in temperature leads to a decline in discount rates due to a significant decline in risk-free rates and this effect dominates the negative cash-flow effect of temperature. Consequently, the wealth of the agent and the price of the consumption claim increase. For example, under CRRA-highRA utility, the price-consumption ratio increases by about 0.024% in response to a 0.53°C increase in temperature. This evidence speaks strongly against power utility specification as it fails to match a robustly negative elasticity of asset prices to temperature risks documented in the data.

### 5 Conclusion

We exploit forward-looking information incorporated in equity prices to learn about the impact of global warming on the macro-economy and find that rising temperature has a significant negative effect on aggregate wealth. We also find that the temperature elasticity of equity valuations has become more negative over time, which suggests that the impact of climate change on the global economy has been rising. We use our empirical work to calibrate a long-run risks model with temperature-induced natural disasters that are expected to affect future economic growth and risk. Our model simultaneously matches the projected temperature path, consumption growth dynamics, discount rates provided by risk-free and equity market returns, and our estimated temperature

elasticity of asset prices. We use the calibrated model to compute the social cost of carbon and solve for the optimal policy response to risks imposed by global warming. We find that concerns for the long run represented by preferences for early resolution of uncertainty and long-run impact of temperature on economic growth yield a significant SCC and a considerable utility loss and, therefore, call for an immediate and sustained reduction in carbon emissions.

### References

- Anthoff, David, and Richard S.J. Tol, 2012, The Climate Framework for Uncertainty, Negotiation and Distribution (FUND), Working paper, Technical Description, Version 3.6.
- Anthoff, David, and Richard S.J. Tol, 2013, The Uncertainty about the Social Cost of Carbon: A Decomposition Analysis using FUND, *Climatic Change* 117, 515–530.
- Archer, David, 2005, Fate of Fossil Fuel CO<sub>2</sub> in Geologic Time, Journal of Geophysical Research: Oceans 110, C09S05.
- Archer, David, 2009, Atmospheric Lifetime of Fossil Fuel Carbon Dioxide, Annual Review of Earth and Planetary Sciences 37, 117–134.
- Bansal, Ravi, and Marcelo Ochoa, 2012, Temperature, Aggregate Risk, and Expected Returns, Working paper, Duke University.
- Bansal, Ravi, and Amir Yaron, 2004, Risks for the Long Run: A Potential Resolution of Asset Pricing Puzzles, *Journal of Finance* 59, 1481–1509.
- Barro, Robert J., 2009, Rare Disasters, Asset Prices, and Welfare Costs, American Economic Review 99, 243–264.
- Barro, Robert J., and José F. Ursua, 2012, Rare Macroeconomic Disasters, Annual Review of Economics 4, 83–109.
- Borovička, Jaroslav, and Lars P. Hansen, 2014, Examining Macroeconomic Models through the Lens of Asset Pricing, *Journal of Econometrics* 183, 67–90.
- Dell, Melissa, Benjamin F. Jones, and Benjamin A. Olken, 2012, Temperature Shocks and Economic Growth: Evidence from the Last Half Century, American Economic Journal: Macroeconomics 4(3), 66–95.
- Epstein, Larry G., and Stanley E. Zin, 1989, Substitution, Risk Aversion, and the Intertemporal Behavior of Consumption and Asset Returns: A Theoretical Framework, *Econometrica* 57, 937– 969.

- Gabaix, Xavier, 2012, Variable Rare Disasters: An Exactly Solved Framework for Ten Puzzles in Macro-Finance, Quarterly Journal of Economics 127, 645–700.
- Gollier, Christian, 2012, Pricing the Planet's Future: The Economics of Discounting in an Uncertain World. (Princeton University Press).
- Golosov, Mikhail, John Hassler, Per Krusell, and Aleh Tsyvinski, 2011, Optimal Taxes on Fossil Fuel in General Equilibrium, Working paper, National Bureau of Economic Research, #17348.
- Hansen, Lars P., and Thomas J. Sargent, 2006, Robust Control and Model Misspecification, Journal of Economic Theory 128, 45–90.
- Hansen, Lars P., and José A. Scheinkman, 2012, Pricing Growth-Rate Risk, Finance and Stochastics 16, 1–15.
- Heutel, Garth, 2012, How Should Environmental Policy Respond to Business Cycles? Optimal Policy Under Persistent Productivity Shocks, *Review of Economic Dynamics* 15, 244–264.
- Hodrick, Robert J., and Edward C. Prescott, 1997, Postwar U.S. Business Cycles: An Empirical Investigation Journal of Money, Credit, and Banking, Journal of Money, Credit, and Banking 29, 1–16.
- Hope, Chris, 2011, The PAGE09 Integrated Assessment Model: A Technical Description, Working paper, Cambridge Judge Business School.
- IPCC, 2007, Climate Change 2007: Synthesis Report. (Geneva, Switzerland).
- IPCC, 2013, Working Group I Contribution to the IPCC Fifth Assessment Report. Climate Change 2013: The Physical Science Basis. (Geneva, Switzerland).
- Jacobson, Mark Z., 2005, Correction to "Control of Fossil-Fuel Particulate Black Carbon and Organic Matter, Possibly the Most Effective Method of Slowing Global Warming", Journal of Geophysical Research: Atmospheres 110, D14105.
- Jagannathan, Ravi, and Srikant Marakani, 2015, Price Dividend Ratio Factor Proxies for Long Run Risks, *Review of Asset Pricing Studies, forthcoming.*

- Kreps, David M., and Evon L. Porteus, 1978, Temporal Resolution of Uncertainty and Dynamic Choice, *Econometrica* 46, 185–200.
- Lemoine, Derek M., and Christian Traeger, 2012, Tipping Points and Ambiguity in the Integrated Assessment of Climate Change, Working paper, National Bureau of Economic Research, #18230.
- Nordhaus, William D., 2008, A Question of Balance: Weighing the Options on Global Warming Policies. (Yale University Press).
- Nordhaus, William D., 2010, Economic Aspects of Global Warming in a Post-Copenhagen Environment, *Proceedings of the National Academy of Sciences* 107, 11721–11726.
- Pindyck, Robert S., 2007, Review of Environmental Economics and Policy, Uncertainty in Environmental Economics 1, 45–65.
- Pindyck, Robert S., 2012, Uncertain Outcomes and Climate Change Policy, Journal of Environmental Economics and Management 63, 289–303.
- Raddatz, Claudio, 2009, The Wrath of God: Macroeconomic Costs of Natural Disasters, Working paper, World Bank Policy Research.
- Rietz, Thomas A., 1988, The Equity Risk Premium: A Solution, Journal of Monetary Economics 22, 117131.
- Tol, Richard S.J., 2002a, New Estimates of the Damage Costs of Climate Change, Part I: Benchmark Estimates, *Environmental and Resource Economics* 21, 47–73.
- Tol, Richard S.J., 2002b, New Estimates of the Damage Costs of Climate Change, Part II: Dynamic Estimates, *Environmental and Resource Economics* 21, 135–160.
- Wachter, Jessica A., 2013, Can Time-Varying Risk of Rare Disasters Explain Aggregate Stock Market Volatility?, Journal of Finance 68, 987–1035.
- Weil, Philippe, 1990, Nonexpected Utility in Macroeconomics, Quarterly Journal of Economics 105, 29–42.
- Weitzman, Martin L., 2009, On Modeling and Interpreting the Economics of Catastrophic Climate Change, Review of Economics and Statistics 91, 1–19.

Weitzman, Martin L., 2010, What is the "Damages Function" for Global Warming – And What Difference Might It Make?, *Climate Change Economics* 1, 57–69.

Parameter	Description	Value
Climate D	)ynamics	
$\bar{ u}$	Atmospheric retention of carbon	0.962
$\chi$	Temperature sensitivity to emissions	0.0045
Natural D	Disasters	
$T^*$	Tipping point	$2.0^{\circ}\mathrm{C}$
$\ell_0$	Disaster intensity parameters	0.0050
$\ell_1$	Disaster intensity parameters	0.0033
$q_1$	Damage function parameter	0.0011
$q_2$	Damage function parameter	0.0011

Table ICalibration of Global Warming

Table I presents calibration of global warming under the business-as-usual scenario. The parameter values are annualized.

	LRR-T	Alter	native Specificatio	ons
	Model	KPEZW-Preferences	CRRA-highRA	CRRA-lowRA
Preferences				
eta	0.99	0.99	0.99	0.99
$\gamma$	5	5	5	0.67
$\psi$	1.5	1.5	0.2	1.5
Consumption				
$\mu$	0.018	0.018	0.018	0.018
$\sigma$	0.016	0.016	0.016	0.016
$ ho_x$	0.96			
$arphi_x$	0.25			
$\phi_x$	0.05			

## Table II Calibration of Preferences and Consumption Dynamics

Table II presents calibration of preferences and consumption dynamics under the business-as-usual scenario. Our LRR-T model features preference for early resolution of uncertainty and incorporates a negative impact of global warming on consumption level and expected consumption growth. Under Alternative Specifications, the conditional mean of consumption growth is constant and climate change is assumed to only affect the level of consumption. We consider three specifications of preferences under the alternative dynamics: preferences for early resolution of uncertainty (KPEZW-Preferences), power utility with high degree of risk aversion (CRRA-highRA) and power utility with low level of risk aversion (CRRA-lowRA). Empty entries in the table correspond to zeros. The parameter values are annualized.

	BAU	Optimal
LRR-T Model	103.6	4.32
Alternatives:		
KPEZW-Preferences	39.01	1.18
CRRA-highRA	0.01	0.01
CRRA-lowRA	0.00	0.00

## Table IIISocial Cost of Carbon

Table III reports the social cost of carbon in the business-as-usual (BAU) scenario and under the optimal abatement policy (Optimal) in the LRR-T Model that features the long-run risk component and preferences for early resolution of uncertainty, and alternative specifications with constant expected growth and three types of risk preferences: preferences for early resolution of uncertainty (KPEZW-Preferences), power utility with high degree of risk aversion (CRRA-highRA) and power utility with low level of risk aversion (CRRA-lowRA). The social cost of carbon is measured in 2012 dollars of world consumption per metric ton of carbon.

	LRR-T	Alternative Specifications			
	Model	KPEZW-Preferences	CRRA-highRA	CRRA-lowRA	
Risk-Free Rate	0.91	2.11	10.08	2.22	
Risk Premia	1.70	0.16	0.17	0.02	
Discount Rates:					
10yr Strip	1.51	2.28	10.33	2.24	
100yr Strip	2.41	2.29	10.31	2.24	

## Table IV Asset Pricing Implications under BAU scenario

Table IV presents asset pricing implications of the LRR-T Model that features the long-run risk component and preferences for early resolution of uncertainty, and alternative specifications with constant expected growth and three types of risk preferences: preferences for early resolution of uncertainty (KPEZW-Preferences), power utility with high degree of risk aversion (CRRA-highRA) and power utility with low level of risk aversion (CRRA-lowRA). The moments are computed under the business-as-usual scenario. The table reports the risk-free rate and risk premia on consumption claim averaged over the transitional path, and discount rates on consumption strips with 10- and 100-year maturities. Returns and premia are expressed in annualized percentage terms.

Argentina	Spain	Netherlands
Australia	Finland	Norway
Austria	France	New Zealand
Belgium	U.K.	Peru
Brazil	Greece	Philippines
Canada	Indonesia	Portugal
Switzerland	India	Russia
Chile	Italy	Sweden
China	Japan	Turkey
Colombia	Korea, rep.	Taiwan
Germany	Sri lanka	U.S.A.
Denmark	Mexico	Venezuela
Egypt	Malaysia	South Africa

# Table VList of Countries

Table V provides a list of countries in our data set.

	Specific	Specification I		Specific	ation II
K	$\hat{\phi}_K$	t-stat		$\hat{\phi}_K$	t-stat
1yr	-0.057	-4.44		-0.050	-3.56
3yr	-0.088	-3.93		-0.090	-3.28
5yr	-0.094	-3.78		-0.090	-2.74
8yr	-0.125	-4.20		-0.136	-3.10
Country FE	$\checkmark$			$\checkmark$	
Global Controls	$\checkmark$			$\checkmark$	
Local Controls				$\checkmark$	

## Table VIElasticity of Equity Prices to Temperature Variations

Table VI reports the response of equity prices to temperature risks estimated in the following panel regression:

$$v_{i,t} = \bar{v}_i + \phi_K \,\overline{T}_{i,t}^K + \alpha'_c C_{i,t} + \alpha_v v_{i,t-1} + \varepsilon_{i,t} ,$$

where  $v_{i,t}$  is the log of the price-dividend ratio of country i,  $\bar{v}_i$  is the country-specific fixed effect,  $\overline{T}_{i,t}^K$  is a K-year moving-average of local temperature, and  $C_{i,t}$  is a set of controls. In Specification I, we control for common global variation using two price-dividend ratio factors. In Specification II, the set of controls also includes country-specific inflation, real interest rate, expected gdp growth, and change in the unemployment rate. The table present the weighted least-squares estimates of the slope coefficient,  $\phi_K$ , and the corresponding t-statistics based on standard errors clustered by country. In Specification I, the panel consists of 39 countries and spans the 1970-2012 period; in Specification II, the panel comprises 35 countries over the 1980-2009 period.

	Specification I		Specifica	ation II
K	$\hat{\phi}_K$	t-stat	$\hat{\phi}_K$	t-stat
$1 { m yr}$	-0.042	-4.41	-0.033	-3.33
3yr	-0.099	-4.10	-0.106	-3.20
5yr	-0.108	-2.99	-0.135	-2.78
8yr	-0.191	-2.29	-0.242	-2.26
Country FE	$\checkmark$		$\checkmark$	
Global Controls	$\checkmark$		$\checkmark$	
Local Controls			$\checkmark$	

## Table VIIEquity Price Response to Temperature Shocks

Table VII reports the response of equity prices to temperature risks estimated in the following panel regression:

$$v_{i,t} = \bar{v}_i + \phi_K \,\overline{T} shock_{i,t}^K + \alpha'_c C_{i,t} + \alpha_v v_{i,t-1} + \varepsilon_{i,t} ,$$

where  $v_{i,t}$  is the log of the price-dividend ratio of country i,  $\bar{v}_i$  is the country-specific fixed effect,  $\overline{T}shock_{i,t}^K$  is an AR(1)-innovation in the K-year moving-average of local temperature, and  $C_{i,t}$  is a set of controls. In Specification I, we control for common global variation using two price-dividend ratio factors. In Specification II, the set of controls also includes country-specific inflation, real interest rate, expected gdp growth, and change in the unemployment rate. The table present the weighted least-squares estimates of the slope coefficient,  $\phi_K$ , and the corresponding t-statistics based on standard errors clustered by country. In Specification I, the panel consists of 39 countries and spans the 1970-2012 period; in Specification II, the panel comprises 35 countries over the 1980-2009 period.

Specific	cation I		Specific	ation II	
$K = 1 \mathrm{yr}$	$\hat{\phi}_1$	t-stat	K = 1yr	$\hat{\phi}_1$	t-stat
1970 - 2000	-0.025	-2.03	1980 - 2000	-0.035	-1.96
1970 - 2005	-0.029	-2.41	$1980\!-\!2005$	-0.043	-3.14
$1970\!-\!2012$	-0.057	-4.44	$1980\!-\!2009$	-0.050	-3.56
$K = 5 \mathrm{yr}$	$\hat{\phi}_5$	t-stat	$K = 5 \mathrm{yr}$	$\hat{\phi}_5$	t-stat
1970 - 2000	-0.041	-1.29	1980 - 2000	-0.066	-1.51
1970 - 2005	-0.046	-1.74	$1980\!-\!2005$	-0.077	-2.51
1970 - 2012	-0.094	-3.78	$1980\!-\!2009$	-0.090	-2.74
Country FE	$\checkmark$	/	Country FE	$\checkmark$	,
Global Controls	$\checkmark$	/	Global Controls	$\checkmark$	
Local Controls			Local Controls	$\checkmark$	

Table VIIIEquity Valuations and Temperature: Sub-Sample Evidence

Table VIII reports the response of equity prices to temperature risks estimated in the following panel regression:

$$v_{i,t} = \bar{v}_i + \phi_K \,\overline{T}_{i,t}^K + \alpha'_c C_{i,t} + \alpha_v v_{i,t-1} + \varepsilon_{i,t} \,,$$

where  $v_{i,t}$  is the log of the price-dividend ratio of country i,  $\bar{v}_i$  is the country-specific fixed effect,  $\overline{T}_{i,t}^K$  is a K-year moving-average of local temperature, and  $C_{i,t}$  is a set of controls. In Specification I, we control for common global variation using two price-dividend ratio factors. In Specification II, the set of controls also includes country-specific inflation, real interest rate, expected gdp growth, and change in the unemployment rate. The table present the weighted least-squares estimates of the slope coefficient,  $\phi_{K=\{1,5\}}$ , and the corresponding t-statistics based on standard errors clustered by country. In Specification I, the panel consists of 39 countries; in Specification II, the panel comprises 35 countries.

	Specification I		Specifica	ation II
K	$\hat{\phi}_K$	t-stat	$\hat{\phi}_K$	t-stat
1yr	-0.136	-4.57	-0.118	-2.79
3yr	-0.143	-3.77	-0.105	-1.31
5yr	-0.160	-3.97	-0.198	-2.19
8yr	-0.166	-4.18	-0.190	-1.82
Country FE	$\checkmark$		$\checkmark$	
Global Controls	$\checkmark$		$\checkmark$	
Local Controls			$\checkmark$	

## Table IXElasticity of Equity Prices to Global Temperature

Table IX reports the response of equity prices to global temperature risks estimated in the following panel regression:

$$v_{i,t} = \bar{v}_i + \phi_K \,\overline{T}_{G,t}^K + \alpha'_c C_{i,t} + \alpha_v v_{i,t-1} + \varepsilon_{i,t} ,$$

where  $v_{i,t}$  is the log of the price-dividend ratio of country i,  $\bar{v}_i$  is the country-specific fixed effect,  $\overline{T}_{G,t}^K$  is a Kyear moving-average of global temperature, and  $C_{i,t}$  is a set of controls. In Specification I, we control for common macro-economic variation using two price-dividend ratio factors. In Specification II, the set of controls also includes country-specific inflation, real interest rate, expected gdp growth, and change in the unemployment rate. The table present the weighted least-squares estimates of the slope coefficient,  $\phi_K$ , and the corresponding t-statistics based on standard errors clustered by country. In Specification I, the panel consists of 39 countries and spans the 1970-2012 period; in Specification II, the panel comprises 35 countries over the 1980-2009 period.

	Specification I		Specification II		
	Estimate	t-stat		Estimate	t-stat
$K = 3 \mathrm{yr}$					
$\phi_{LR}$	-0.099	-4.10		-0.105	-3.21
$\phi_{SR}$	0.009	1.17		0.012	1.36
$K = 5 \mathrm{yr}$					
$\phi_{LR}$	-0.108	-2.99		-0.133	-2.78
$\phi_{SR}$	-0.002	-0.28		0.007	0.85
$K = 8 \mathrm{yr}$					
$\phi_{LR}$	-0.192	-2.30		-0.244	-2.31
$\phi_{SR}$	0.000	0.03		0.010	1.06
HP-trend					
$\phi_{LR}$	-0.187	-5.17		-0.200	-4.42
$\phi_{SR}$	0.007	1.18		0.003	0.38
Country FE	$\checkmark$			$\checkmark$	
Global Controls	$\checkmark$			$\checkmark$	
Local Controls				$\checkmark$	

Table X				
Equity Respon	nse to Long-	- and Short-Run	Temperature	Risks

Table X reports the response of equity prices to low- and high-frequency temperature risks estimated in the following panel regression:  $K = \frac{1}{2} \frac{1}{2}$ 

$$v_{i,t} = \bar{v}_i + \phi_{LR} LRshock_{i,t}^{R} + \phi_{SR} SRshock_{i,t} + \alpha'_c C_{i,t} + \alpha_v v_{i,t-1} + \varepsilon_{i,t}$$

where  $v_{i,t}$  is the log of the price-dividend ratio of country *i*,  $\bar{v}_i$  is the country-specific fixed effect,  $LRshock_{i,t}^K$  is an AR(1)-innovation in the K-year moving-average of local temperature,  $SRshock_{i,t}$  is the annual change in local temperature orthogonalized with respect to long-run shock, and  $C_{i,t}$  is a set of controls. In the lower panel,  $LRshock_{i,t}^K$ is replaced with the Hodrick-Prescott trend. In Specification I, we control for common global variation using two pricedividend ratio factors. In Specification II, the set of controls also includes country-specific inflation, real interest rate, expected gdp growth, and change in the unemployment rate. The table present the weighted least-squares estimates of the slope coefficients,  $\phi_{LR}$  and  $\phi_{SR}$ , and the corresponding t-statistics based on standard errors clustered by country. In Specification I, the panel consists of 39 countries and spans the 1970-2012 period; in Specification II, the panel comprises 35 countries over the 1980-2009 period.

	$\overline{T}_{i,t}^8$	$T_{i,t}$	$v_{i,t}$
$\overline{T}_{i,t-1}^{8}$	0.921	0.385	-0.093
	[107.1]	[7.06]	$\left[-2.29\right]$
$T_{i,t-1}$	0.026	0.158	-0.017
	[5.44]	$\left[5.19 ight]$	$\left[-0.73\right]$
$v_{i,t-1}$	0.014	0.076	0.520
	$\left[3.15\right]$	$\left[2.65\right]$	$\left[24.41\right]$
$\bar{R}^2$	0.96	0.31	0.67

 Table XI

 VAR Dynamics of Equity Prices and Temperature

Table XI shows the estimates of the first-order panel VAR for equity prices and temperature.  $\overline{T}_{i,t}^8$  denotes the eightyear moving-average of local temperature,  $T_{i,t}$  is annual temperature series, and  $v_{i,t}$  is the log of the price-dividend ratio of country *i*. The exogenous variables included in the VAR comprise two price-dividend ratio factors that control for common macro-economic risks and country-specific fixed effects. T-statistics are reported in brackets. The panel consists of 39 countries over the 1970-2012 period.

Table XII	
Model-Implied Price Response to Temperature	Risks

	Response
LRR-T Model	-0.0174
Alternatives:	
KPEZW-Preferences	-0.0063
CRRA-highRA	0.0002
CRRA-lowRA	0.0000

Table XII reports the response of the price-consumption ratio to temperature risks for the LRR-T model that features the long-run risk component and preferences for early resolution of uncertainty, and alternative specifications with constant expected growth and three types of risk preferences: preferences for early resolution of uncertainty (KPEZW-Preferences), power utility with high degree of risk aversion (CRRA-highRA) and power utility with low level of risk aversion (CRRA-lowRA). For each specification, we simulate the data and compute the model-implied response by regressing the price-consumption ratio on temperature controlling for the relevant state variables. The simulated data consist of 50,000 draws.



(c) Expected Path of Temperature Anomaly

Figure 1. Dynamics under the BAU Scenario

Figure 1 illustrates the business-as-usual scenario. Panel (a) shows the evolution of carbon intensity; Panel (b) presents the projected path of carbon emissions; Panel (c) shows the projected path of temperature anomaly (temperature relative to its pre-industrial level). Emissions are measured in millions of metric ton of carbon per annum, and temperature is in degrees Celsius. The dotted line in Panel (c) represents the tipping point of global warming. The horizontal axis is the time-line measured in years from today.



Figure 2. Global Warming Disasters under the BAU policy

Figure 2 shows the consequences of global warming in the business-as-usual case. Panel (a) plots the expected intensity of climate change disasters per annum; Panel (b) shows the average annual size of disasters  $(-d_t)$ . The horizontal axis is the time-line measured in years from today.



Figure 3. Change in Ex-Ante Consumption Moments due to Disasters

Figure 3 shows the change in the conditional mean and volatility of future consumption due to global-warming disasters. Panel (a) plots the difference between ex-ante mean of cumulative log consumption growth under the business-asusual scenario and the conditional mean absent temperature disasters. Panel (b) presents the corresponding difference in volatility of cumulative consumption growth. Volatility is annualized and expressed in percentage terms. The horizontal axis is the time-line measured in years from today.



Figure 4. Distribution of Consumption Growth

Figure 4 shows the implications of global-warming disasters for consumption growth. The plot presents the distribution of normalized consumption growth at time-0 (when disasters are absent) and 210 years from now (at the peak of global-warming disasters).



(b) Abatement Cost

Figure 5. Optimal Abatement Policy

Figure 5 shows the optimal abatement policy in the LRR-T model that features long-run risks and preferences for early resolution of uncertainty. Panel (a) presents the optimal abatement effort, Panel (b) shows the cost of optimal policy. Abatement effort represents the reduction in carbon intensity, cost is expressed as a fraction of consumption goods. The horizontal axis is the time-line measured in years from today.



(b) Temperature

Figure 6. Implications of Optimal Abatement Policies

Figure 6 shows the implications of the optimal abatement policy in the LRR-T model that features long-run risks and preferences for early resolution of uncertainty. Panel (a) presents the optimal level of carbon emissions, Panel (b) shows the implied evolution of temperature. Emissions are measured in millions of metric ton of carbon per annum, and temperature is in degrees Celsius. The horizontal axis is the time-line measured in years from today.



Figure 7. Distribution of Disaster Size

Figure 7 shows the benefits of the optimal abatement policy in the LRR-T model that features long-run risks and preferences for early resolution of uncertainty. Panel (a) shows the distribution of disaster size in the business-as-usual scenario; Panel (b) present the corresponding distribution under the optimal climate policy. The thick line is the average disaster size and the shaded area represents the 5–95 percentile band. The horizontal axis is the time-line measured in years from today.



(b) Temperature

Figure 8. Policy Decisions under Alternative Specifications

Figure 8 shows the cost of the optimal abatement policy (Panel (a)) and the implied temperature path (Panel (b)) under three alternative specifications of risk preferences. Time-series dynamics of consumption and climate impact across the three specifications are kept the same: consumption is assumed to follow a random walk subject to climate-induced disasters. The cost is expressed as a fraction of consumption and temperature is in degrees Celsius. The horizontal axis is the time-line measured in years from today.



(b) Sensitivity of Wealth-Consumption Ratio

#### Figure 9. Sensitivity to Emissions

Figure 9 shows the impact of an increase in current emissions on future damages and the wealth-consumption ratio. Panel (a) shows the percentage increase in annual expected damages if time-0 emissions are raised by 1%, Panel (b) presents the corresponding elasticity of the wealth-consumption ratio. Both panels are constructed under the businessas-usual scenario for three alternative specifications of preferences. The horizontal axis is the time-line measured in years from today.



Figure 10. Histogram of the Trend in Local Temperature

Figure 10 shows the histogram of the trend in local temperature measured by the change in average temperature over the 2003-2012 period relative to the 1951-1980 average. The cross-sectional data comprise 39 countries; temperature is measured in degrees Celsius.



Figure 11. Trend in Local and Global Temperature

Figure 11 shows the first principal component of the ten-year moving-average of local temperature series (solid line) and the ten-year moving-average of global temperature (dashed line). The two time-series are normalized. The panel data comprise 39 countries over the 1970-2012 period.



(b) Response to Short-Run Shock

Figure 12. Impulse Responses of Equity Prices to Long- and Short-Run Temperature Risks

Figure 12 presents impulse responses of the price-dividend ratio to long- and short-run temperature risks implied by a first-order VAR. The estimated responses are represented by the solid lines, the shaded areas show the two standard-error bands. Time-horizon on the horizontal axes is measured in years.