

Multi-Stage Hiring in Labor Market Equilibrium

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Disclaimer: My views do not represent those of FRB Philadelphia, the Federal Reserve System, Ben, Piero, or Ronald.

Introduction

- How does a firm hire a worker?
- Empirically, there are **multiple, distinct** stages:

[Van Ours and Ridder 1992;
Davis and Samaniego de la
Parra 2025]

Post job

→ Accept applications

→ Interview selected applicants

→ Make an offer.

Insights from multi-stage model of hiring

Integrating this process into theory adds value:

1] Introduces explicit and measurable margin of recruiting effort.

➤ Prob(interviewing) is a means of responding to policies and shocks.

[Davis et al 2013; Gavazza et al 2018; Leduc & Lui 2020; Forsythe & Weinstein 2025]

Insights from multi-stage model of hiring

Integrating this process into theory adds value:

- 1] Introduces explicit and measurable margin of recruiting effort.
- 2] Connects theory to growing empirical literature on “callbacks”.
 - How does $\text{var}(\text{interview rates})$ shape understanding of $\text{var}(\text{job finding})$?
[Pager 2003; Agan & Starr 2018; Kroft et al 2013; Farber et al 2019; Kline et al 2022]

Insights from multi-stage model of hiring

Integrating this process into theory adds value:

- 1] Introduces explicit and measurable margin of recruiting effort.
- 2] Connects theory to growing empirical literature on “callbacks”.
- 3] Framework for analysis of policies that regulate hiring process.
 - Needed: Equ. model in which interviewing plays allocative role.

[Agan and Starr 2018; Hansen and McNichols 2020; Cortes et al 2022]

What we do

Theory: a SaM framework that includes

1] realistic multi-stage recruiting process. [Wolthoff 2018; Villena-Roldan 2012]

What we do

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- 2] multiple applicants & optimal interviewing using Weitzman [1979].

[See also Choi, Dai, &
Kim 2018]

What we do

Theory: a SaM framework that includes

- 1] realistic multi-stage recruiting process.
- 2] multiple applicants & optimal interviewing using Weitzman [1979].
- 3] **ex ante worker types** and **match-specific productivity**. [Jarosch & Pilossoph 2019; Meier & Obermeier 2025]
 - Realistic heterogeneity enables policy applications.
 - Accommodates *incomplete info.* over worker types.
 - Remains tractable: *analytical* solutions for *distributions* of interviewing and job finding rates.

What we do

Theory: a SaM framework that includes

- 1] realistic multi-stage recruiting process.
- 2] multiple applicants & optimal interviewing using Weitzman [1979].
- 3] ex ante worker types and match-specific productivity.
- 4] job creation decision & tractable aggregate dynamics.
 - Enables *dynamic equilibrium* evaluation of policies.

What we do

Quantitative application: Ban the Box.

- “Hides” criminal record at application stage but not at interview.
 - Highlights roles of interview and imperfect info. → suitable test for the model.
- Potential impact: Exoffender share of job seekers is large in the U.S., especially among black men.
- First equilibrium exploration of policy.

Related (theoretical) literature

- Related lit. has pulled together multiple model ingredients.
[Jarosch & Pilossoph 2019]
- What we offer:
 - (i) Simple ranking of applicants when observable sufficient stat. (e.g., unemployment duration) is not available.
 - (ii) Analytical progress using urn-ball matching.
 - (iii) Endogenous job creation.
 - (iv) Nash bargaining.
- What we lack: (a) application extensive margin [Bradley 2025; Bagga & Mann 2026]
(b) multiple applications [Birinci et al 2025 w/ random search;
Albrecht et al 2006; Galenianos &
Kircher 2009 w/ directed search]

Static model

Actors

- Measure ν of homogeneous vacancies.
- Workers distributed over L discrete *types*.
 - A type is a vector of *attributes*, $\mathbf{x} \equiv (x_1, x_2, \dots)$.
 - Example: $L = 4$ types w/ $x_1 = \{\text{black, white}\}$ & $x_2 = \{\text{no record, conviction}\}$.
 - Type- $\mathbf{x}$ share in the population is $m_{\mathbf{x}}$.
- At start of period, measure of unemployed of type $\mathbf{x}$ is $u_{\mathbf{x}}$.
 - Unemployment *rate* is $u_{\mathbf{x}}/m_{\mathbf{x}}$.

Matching

- Each unemployed worker randomly sends 1 application per period.
- Many searchers and many vacancies $\Rightarrow$ # of applications received by a vacancy from type $\mathbf{x} \sim \text{Poisson}(u_{\mathbf{x}}/v)$ [**urn ball technology**].
- Notation: Let $\lambda_{\mathbf{x}} \equiv u_{\mathbf{x}}/v$ and $\boldsymbol{\lambda} \equiv \{\lambda_{\mathbf{x}}\}$.
- Individual firm treats $\boldsymbol{\lambda}$ as given.

Wage setting

- Alternative A: Firm makes take-it-or-leave-it offer.

⇒ wage = flow value of time = $b_{\mathbf{x}}$. [Jarosch & Pilossoph 2019;
Meier & Obermeier 2025]

- Alternative B: Nash bargaining
 - Prior to bargaining, firm *severs all ties* to other applicants.
 - Endogenizes outside option as a function of $\mathbf{x}$ in dynamic model.

Wage setting

For now • **Alternative A: Firm makes take-it-or-leave-it offer.**

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For later • Alternative B: Nash bargaining

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Firm's payoff (with fixed wage)

Firm's payoff from a filled job, Π , has the structure,

$$\Pi = \underbrace{z_{\mathbf{x}} + \eta + \varepsilon}_{\text{Output}} - b_{\mathbf{x}}.$$

Wage

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- 1] $Z_{\mathbf{x}}$ is a *deterministic* function of type seen at **application** stage.
- 2] η is drawn from *type-specific distribution* at **application** stage.
- 3] ε is drawn from *type-specific distribution* at **interview** stage.

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- 1] $Z_{\mathbf{x}}$ is a *deterministic* function of type seen at **application** stage.
 - Captures permanent heterogeneity in productivity net of $b_{\mathbf{x}}$ (outside option).
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- 2] η is drawn from *type-specific distribution* at **application** stage.
 - Captures differences in how certain skills are valued across matches.
 - Assume η is *discrete*: $\eta \in \{\eta_1, \dots, \eta_M\}$ with p.m.f. $g(\eta \mid \mathbf{x})$.
- 3] ε is drawn from *type-specific distribution* at **interview** stage.

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- 2] η is drawn from *type-specific distribution* at **application** stage.
- 3] ε is drawn from *type-specific distribution* at **interview** stage.
 - Captures idio. “fit” (e.g. how well worker and manager collaborate).
 - Zero mean with c.d.f. $F_{\mathbf{x}}(\varepsilon)$.

Interviewing problem

- Firm sees $Z_{\mathbf{x}}$ and η and decides whom to interview.
 - Offer made to interviewed candidate with highest payoff.
- Each interview costs $c \rightarrow$ do not want to “waste” interviews.
- Challenge: How to order heterogeneous workers?
 - In general, it is not optimal to rank by $Z_{\mathbf{x}} + \eta$ alone.
 - Why? A low $E[\text{value}]$ match may have high “upside” (high $\text{var}(\varepsilon)$).

Interviewing solution [Weitzman 1979]

- If highest payoff of those interviewed *thus far* is Π , should firm interview an(other) applicant with $\boldsymbol{\varsigma} \equiv (\mathbf{x}, \eta) \in \mathbb{R}^{L \times M}$?
- Potential payoff $\pi \sim H(\pi \mid \boldsymbol{\varsigma}) \equiv \Pr(Z_{\mathbf{x}} + \eta + \varepsilon < \pi \mid \boldsymbol{\varsigma})$

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- Marginal value of interview is

$$-c + \Pi H(\Pi \mid \boldsymbol{\varsigma}) + \int_{\Pi} \pi dH(\pi \mid \boldsymbol{\varsigma}) - \Pi.$$

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- This is **decreasing** in $\Pi \rightarrow$ *Reservation policy*: Interview if $\Pi < \Pi^*(\boldsymbol{\varsigma})$.

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- This is **decreasing** in $\Pi \rightarrow$ *Reservation policy*: Interview if $\Pi < \Pi^*(\boldsymbol{\varsigma})$.
 - Π^* is payoff required to *not* interview $\rightarrow$ prices marginal interview
 - Π^* is a function **only** of $\boldsymbol{\varsigma} \equiv (\mathbf{x}, \eta)$!

Interviewing solution [Weitzman 1979]

1] Order reservation values from largest to smallest.

➤ $K \equiv L \times M$ pairs of $\boldsymbol{\varsigma} \equiv (\mathbf{x}, \eta) \rightarrow K$ reservation values, $\Pi_1^* > \dots > \Pi_K^*$.

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Bin 1

Bin K

Interviewing solution [Weitzman 1979]

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2] Interviews conducted in order of Π^* (largest first).

3] If k th bin applicants draw $\pi < \Pi_{k+1}^*$, interview $k + 1$; otherwise, stop interviews & select highest payoff among interviewed apps.

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∴ Multi-dimensional type condensed to a scalar index.

Aggregate outcomes

- Weitzman addresses optimal interviewing *after* matching.
- Now embed interviewing within matching model given $\lambda_{\mathbf{x}} \equiv u_{\mathbf{x}}/v$.
- Characterize outcomes across *bins*, then will map back to type.
- Notation:
 - Each bin “occupied” by a pair of type and $\eta \rightarrow$ pair in bin k is $(\mathbf{x}_k, \eta_k)$
 - Unemployed in bin $k / v = \lambda(\mathbf{x}_k) \times g(\eta_k | \mathbf{x}_k) = \lambda_k$.
 - Similarly, $H_k(\pi) = H(\pi | \mathbf{x}_k, \eta_k)$.

Interview probability

The prob. an applicant of bin k is interviewed is

$$\Gamma_k =$$

Prob. interview *some* bin
 k applicant

×

Prob. interview any one
applicant within bin k

Interview probability

The prob. an applicant of bin k is interviewed is

$$\Gamma_k = \exp \left\{ - \sum_{j=1}^{k-1} \lambda_j \left(1 - H_j(\Pi_k^*) \right) \right\} \times$$

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Corollary: $\Gamma_{\mathbf{x}} \equiv \Pr(\text{interview type } \mathbf{x}) = \sum_{k=1}^K \Gamma_k \times g(\eta_k \mid \mathbf{x})$.

Aggregate outcomes

- Worker flows and p.d.f.(firm payoffs) also solved analytically.
- In summary: Given $\lambda_{\mathbf{x}} \equiv u_{\mathbf{x}}/v$, $H(\pi \mid \mathbf{x}, \eta)$ and $g(\eta \mid \mathbf{x})$,
 - 1] Probability of type $\mathbf{x}$ being interviewed, $\Gamma_{\mathbf{x}}$.
 - 2] Job finding probability of type $\mathbf{x}$, $p_{\mathbf{x}}$.
 - 3] Prob. of filling job using type $\mathbf{x}$, $q_{\mathbf{x}}$.
 - 4] Density of payoffs | hire type $\mathbf{x}$, $\phi(\pi \mid \mathbf{x})$.

Dynamic model

Dynamic model

- Match with type $\mathbf{x}$ dissolves at rate $\delta_{\mathbf{x}}$.
- Output per period is constant within a match.
 - Firm-worker pair draws η and ε once at start of job.
- Firm's discount factor is $\beta \equiv (1 + r)^{-1} \approx 1 - r$.

Present value of filled job

- With take-it-or-leave-it-offers,

$$\Pi = (z_{\mathbf{x}} - b_{\mathbf{x}} + \eta + \varepsilon)/(r + \delta_{\mathbf{x}}).$$

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- Under Nash bargaining,

$$w = \alpha \cdot (z_{\mathbf{x}} + \eta + \varepsilon) + (1 - \alpha) \cdot rU_{\mathbf{x}},$$

where $rU_{\mathbf{x}}$ is the annuity value of search,

$$rU_{\mathbf{x}} = b_{\mathbf{x}} + \frac{\alpha}{1 - \alpha} \cdot p_{\mathbf{x}} \mathbb{E}_{\mathbf{x}}[\pi \mid \text{hired}].$$

Present value of filled job

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└──────── Density of payoffs | hire type $\mathbf{x}$

Present value of filled job

- With take-it-or-leave-it-offers,

$$\Pi = (z_x - b_x + \eta + \varepsilon)/(r + \delta_x).$$

- Under Nash bargaining,

$$\Pi = (1 - \alpha) \cdot (z_x - rU_x + \eta + \varepsilon)/(r + \delta_x).$$

Equilibrium (steady state)

- Given $\lambda_{\mathbf{x}} \equiv u_{\mathbf{x}}/v$ and $rU_{\mathbf{x}}$, solve Weitzman (Π^* s) and compute
 - (a) interviewing ($\Gamma_{\mathbf{x}}$), job finding ($p_{\mathbf{x}}$), & job filling ($q_{\mathbf{x}}$) rates; and
 - (b) density of match payoffs, $\phi(\pi|\mathbf{x})$.
- v , $u_{\mathbf{x}}$, and $rU_{\mathbf{x}}$ then solve
 - (i) Free entry
 - (ii) Beveridge curve for each $\mathbf{x}$.
 - (iii) Bellman equation of job searcher.

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(i) Free entry:

$$\mathbb{E}[y \text{ among hires}] - \mathbb{E}[\text{cost of interviews}] = \text{entry cost}, \chi$$

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(i) Free entry:

$$\sum_{\mathbf{x}} q_{\mathbf{x}} \int_0^{\infty} \pi \phi(\pi|\mathbf{x}) d\pi = \chi + \frac{c \sum_{\mathbf{x}} \Gamma_{\mathbf{x}} u_{\mathbf{x}}}{v}$$

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 - (i) Free entry:
 - (ii) Beveridge curve for each $\mathbf{x}$:

$$\text{Inflows} = \delta_{\mathbf{x}}(m_{\mathbf{x}} - u_{\mathbf{x}}) = p_{\mathbf{x}}u_{\mathbf{x}} = \text{Outflows}$$

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Free Entry:
$$\sum_{\mathbf{x}} q_{\mathbf{x}} \int_0^{\infty} \pi \phi(\pi|\mathbf{x}) d\pi = \chi + c \sum_{\mathbf{x}} \Gamma_{\mathbf{x}} u_{\mathbf{x}}/v$$

Flow balance:
$$\delta_{\mathbf{x}}(m_{\mathbf{x}} - u_{\mathbf{x}}) = p_{\mathbf{x}} u_{\mathbf{x}}$$

Worker Bellman:
$$rU_{\mathbf{x}} = b_{\mathbf{x}} + \frac{\alpha}{1-\alpha} \cdot p_{\mathbf{x}} \int \pi \phi(\pi|\mathbf{x}) d\pi$$

Extension: (Partially) hidden types

- Example: Two attributes—race and criminal record.
Assume record is concealed at application stage.
 - $Z \equiv z - rU$ partially hidden but π learned at interview.
- To choose interviews, evaluate distribution of payoffs | $\boldsymbol{\varsigma} \equiv (\textit{race}, \eta)$.
 - Swap this for original c.d.f. (H), solve for Π^* s, and compute $\Gamma_{\mathbf{x}}$, etc.
- Key point: Reservation values (Π^*) do *not* depend on record.
 - Low prod. type (exoffenders) assigned higher Π^* than before.

Quantitative illustration

Roadmap

- Apply model to study a labor market policy: **Ban the Box (BtB)**.
- Modeled as unforeseen, permanent policy.
 - Illegal to view criminal record at application stage: z partially hidden.
 - Legal to pull criminal record at interview stage: Firm sees π if interview.
- Plan: calibrate to *pre*-ban environment; then solve for dynamic response to BtB.

Parameters

- 1] Separation rates, $\delta_{\mathbf{x}}$, and population shares, $m_{\mathbf{x}}$
- 2] Frictions: Interview cost, c , and job creation cost, χ .
- 3] Payoff parameters: α , $b_{\mathbf{x}}$, $z_{\mathbf{x}}$, and distributions of η and ε .

Parameters

1] Separation rates, $\delta_{\mathbf{x}}$

- By race: CPS 2015-19, men ages 18-34 not in school.
- By record: Modest differences $\Rightarrow$ same δ *within* race.

[Minor et al 2018]

Race	Emp.-to-NonEmp. Transition Prob. (mo.)
Black	0.0418
White	0.0199

Parameters

1] Population shares, $m_{\mathbf{x}}$

- No consensus on exoffender shares by race.
- Our baseline: NLSY + admin. data on prisoner releases.

Race	Felon share
Black	0.195— 0.325
White	0.098

Parameters

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2] Frictions: Interview cost, c , and job creation cost, χ .

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} Calibrated
internally
(mostly)

Parameters

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Today: $\alpha = 0$. Model with Nash bargain not ready for prime time.

Parameters

- 1] Separation rates, $\delta_{\mathbf{x}}$, and population shares, $m_{\mathbf{x}}$
- 2] Frictions: Interview cost, c , and job creation cost, χ .
- 3] Payoff parameters: $b_{\mathbf{x}}$, $z_{\mathbf{x}}$, and distributions of η and ε .

Other restrictions: (i) $b_{\mathbf{x}} = b \forall \mathbf{x}$.

(ii) $\varepsilon \sim \mathcal{N}$ and σ_{ε} differs by race, not record.

(iii) ID *differences* in $\text{Var}(\eta)$ w.r.t. white nonoffenders

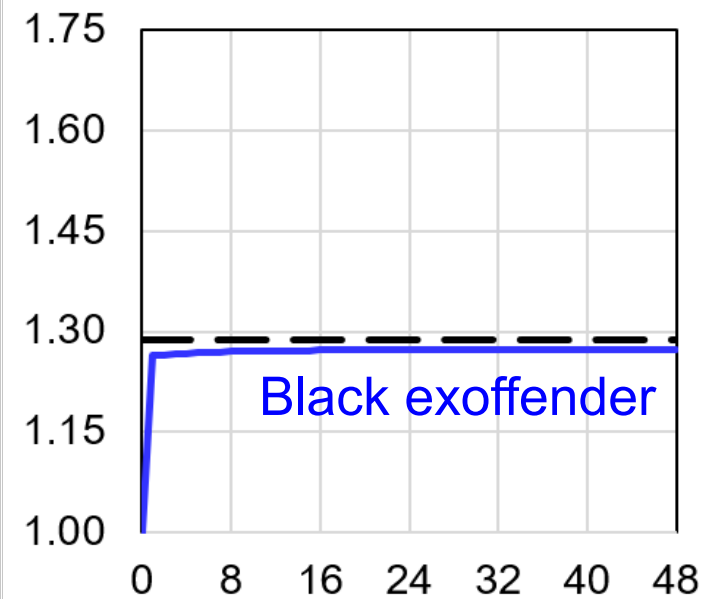
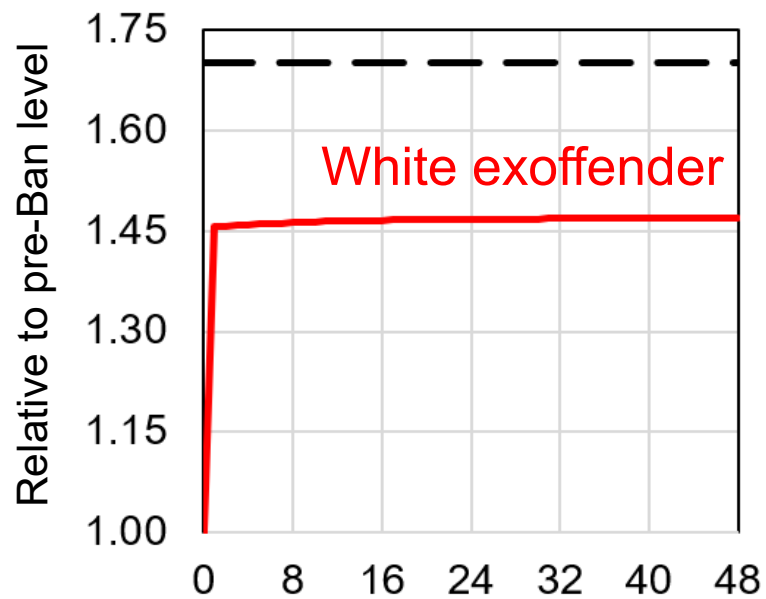
[Level for white nonoff. informed by ongoing work w/ Nash]

Source	Moment	Value	Relevant parameter
Barron et al [1997]	Pr(interview)	0.373	std(ε)
Agan & Starr [2018]	Pr(interview x)	WH exoff. = 0.593	z(WH exoff.),
	Pr(interview white exoff.)	BL exoff. = 0.614	z(BL exoff.),
		BL nonoff. = 0.936	std(ε BL)

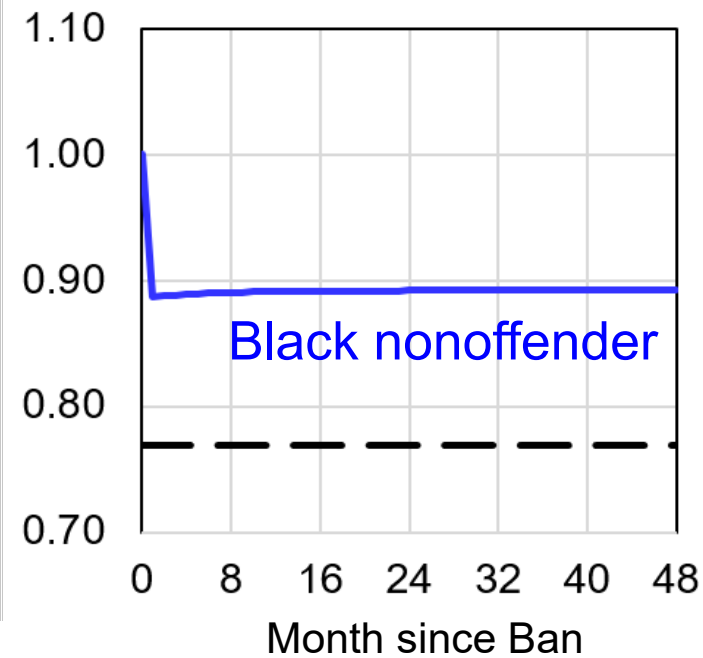
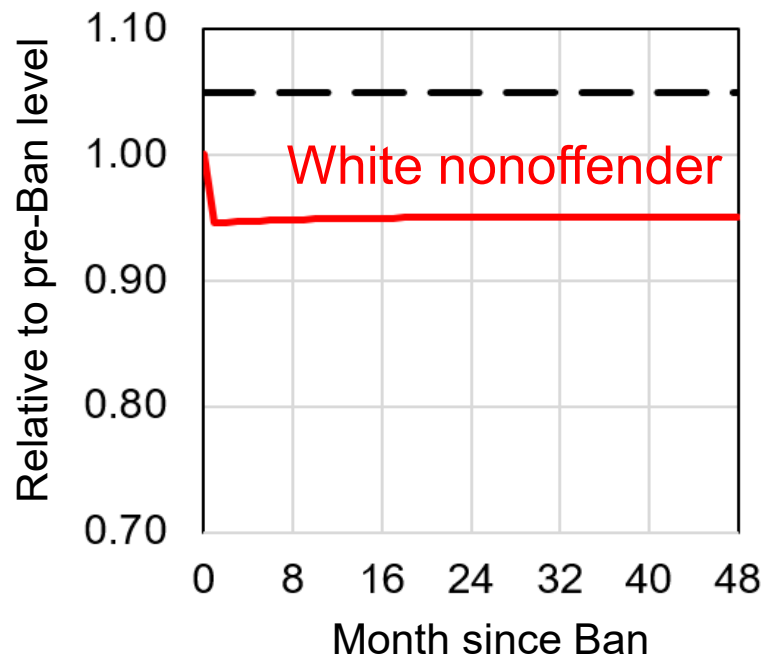
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Agan & Starr [2018]	$\frac{\text{Pr}(\text{interview } \mathbf{x})}{\text{Pr}(\text{interview white exoff.})}$	WH exoff. = 0.593 BL exoff. = 0.614 BL nonoff. = 0.936	$z(\text{WH exoff.}),$ $z(\text{BL exoff.}),$ $\text{std}(\varepsilon \mid \text{BL})$
Current Pop. Survey	Nonemp. (NE) rate	0.137	χ
Current Pop. Survey	$\frac{\text{Black NE rate}}{\text{White NE rate}}$	2.045	$\text{std}(\eta \mid \text{BL})$
Shem-Tov & Rose [2025]	Exoff. NE less nonoff. NE	0.120	$\text{std}(\eta \mid \text{exoff.})$

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Shem-Tov & Rose [2025]	Exoff. NE less nonoff. NE	0.120	$\text{std}(\eta \mid \text{exoff.})$
Villena-Roldan [2012]	Interview cost per hire (in mo. wages)	1.3	c
Shimer [2005], Hall & Milgrom [2008]	Value of time/Labor prod.	0.4—0.7	b

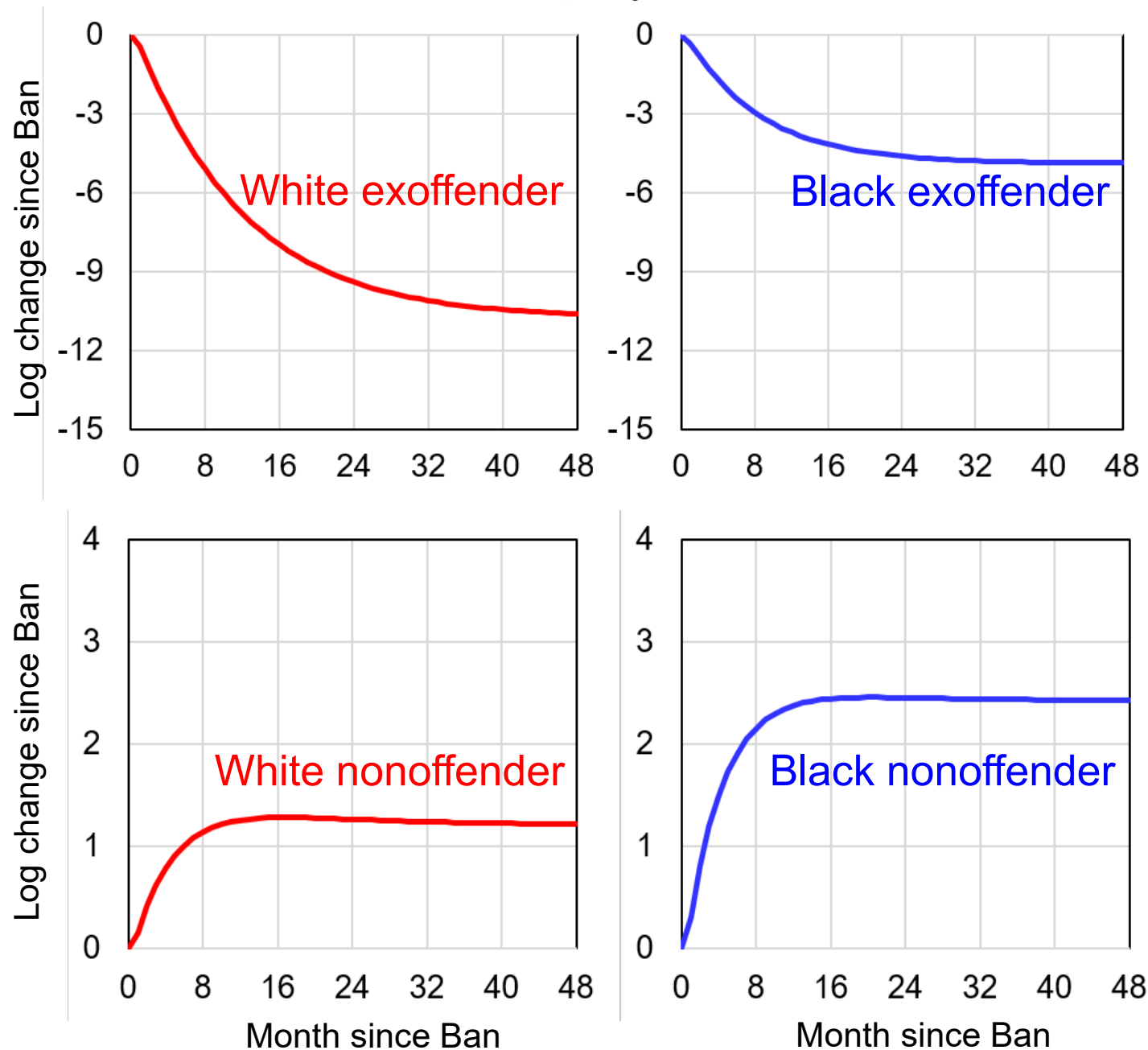
Callback probability



Dash lines from Agan
& Starr [Table II, 2018]

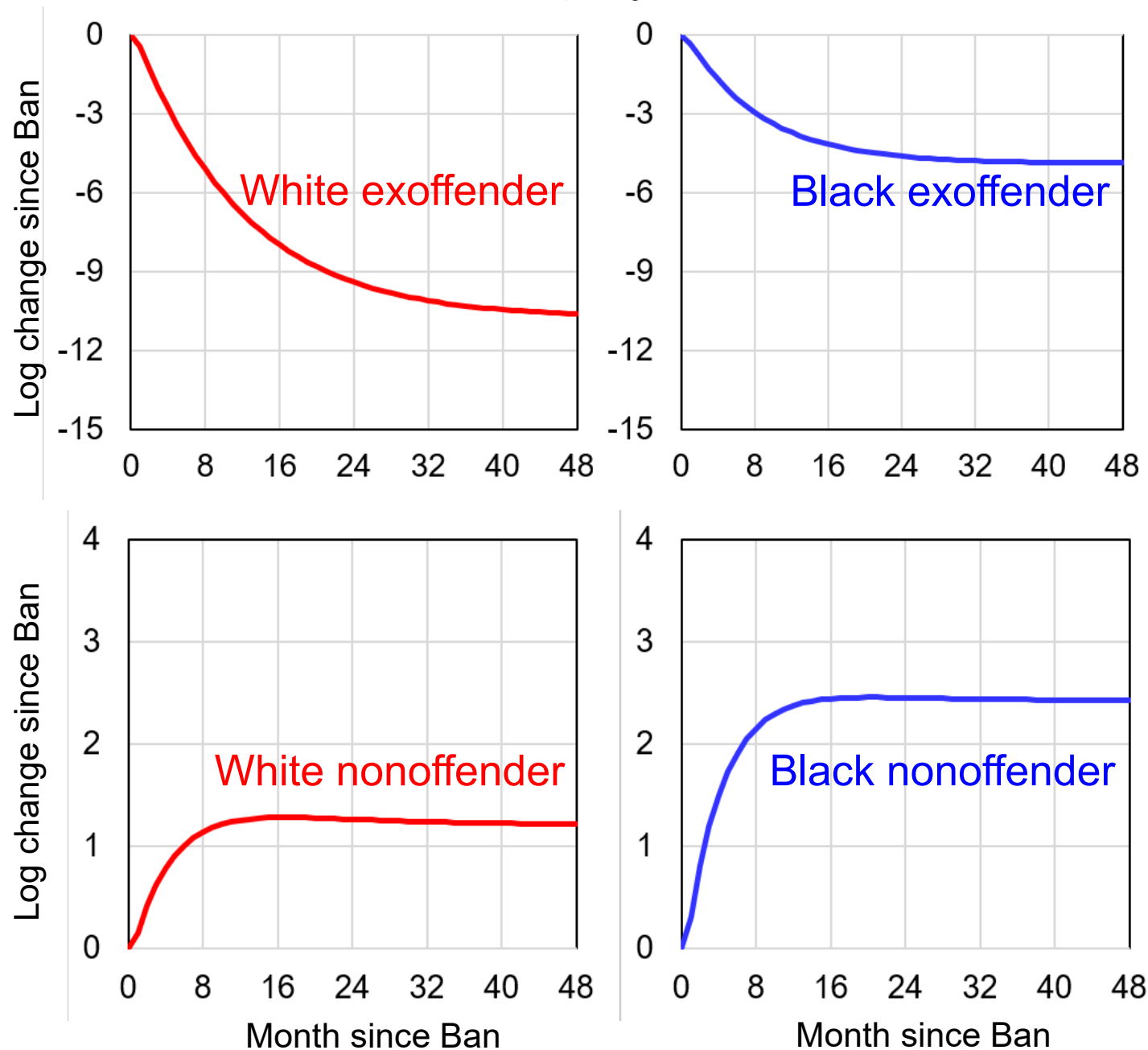


Nonemployment rate



Exoff. Interviews $\uparrow \approx 35\%$
but
Exoff. Employment $\uparrow \approx 7\%$

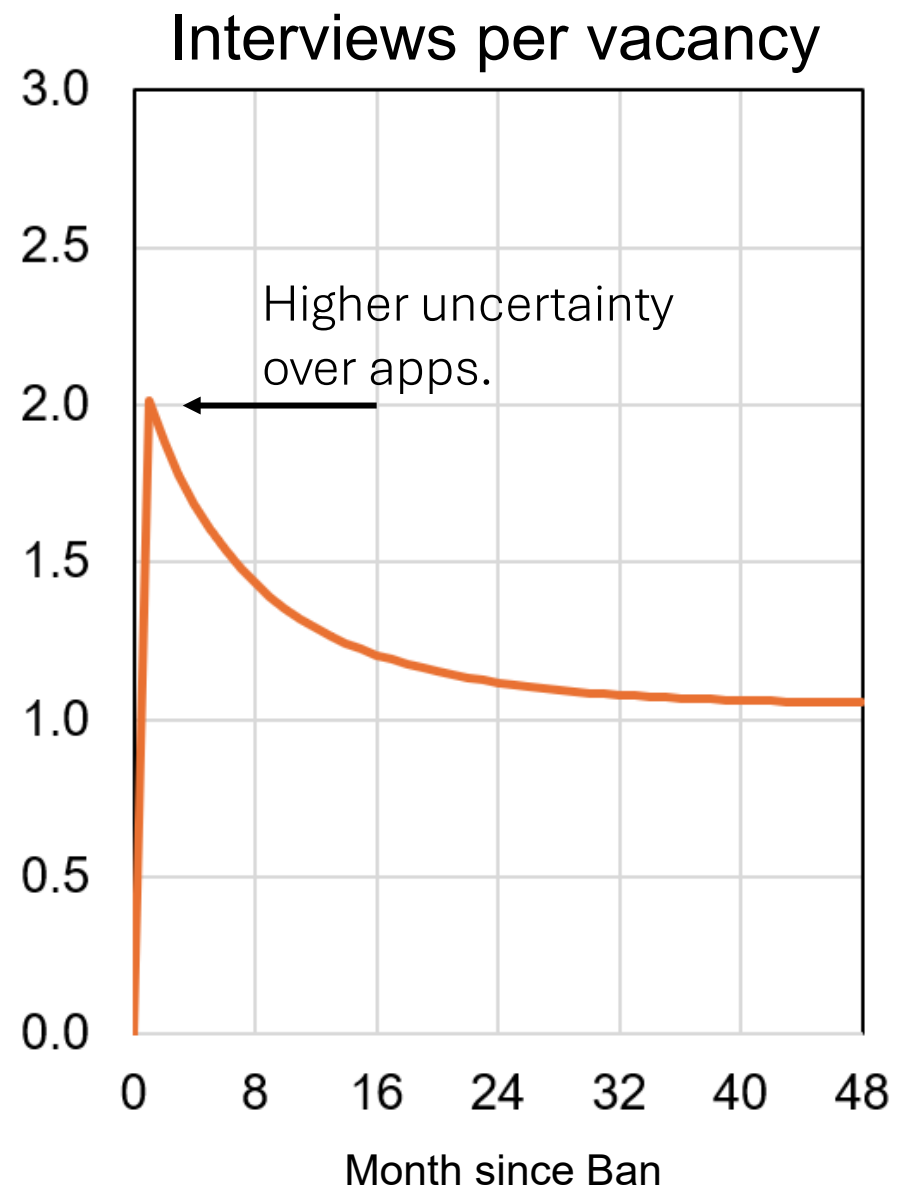
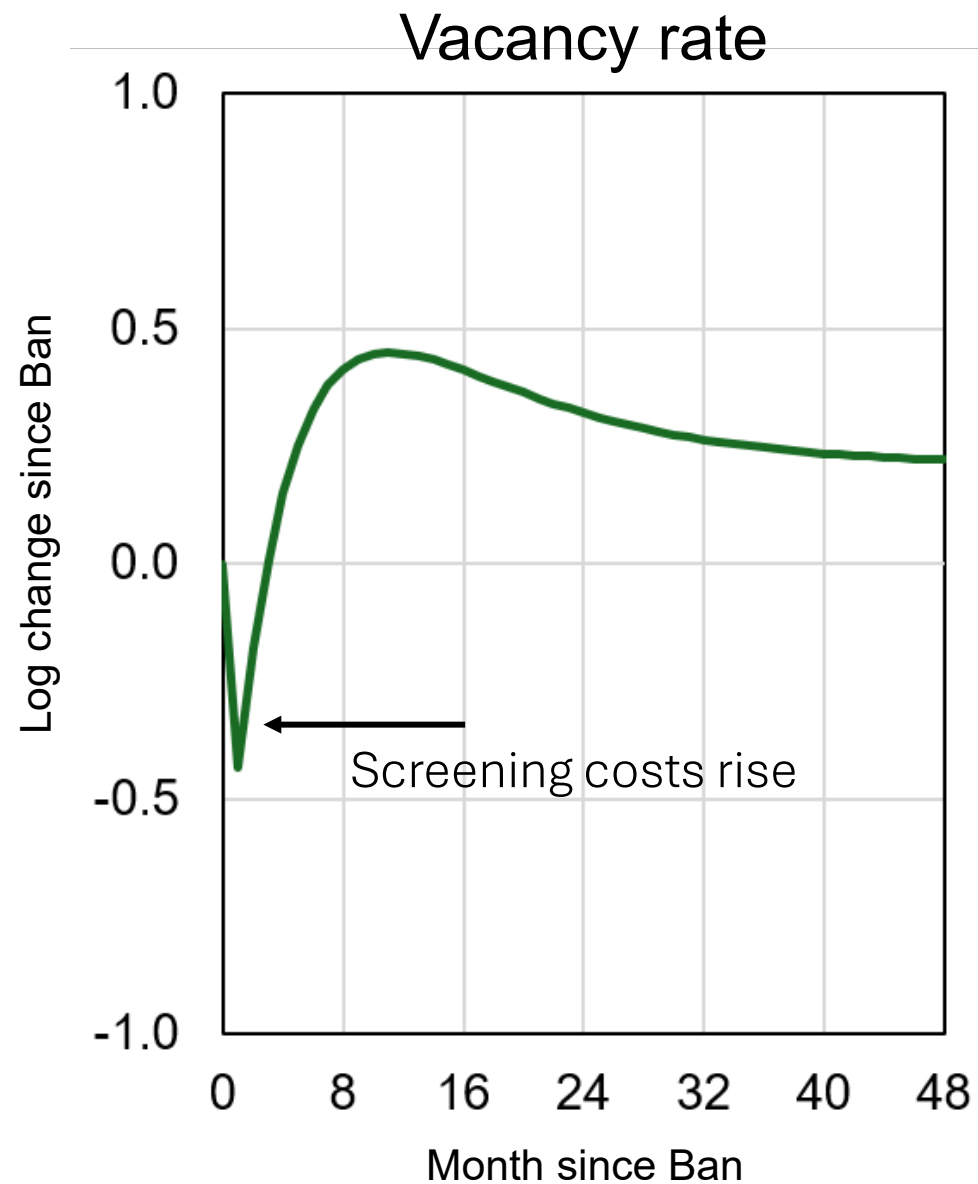
Nonemployment rate

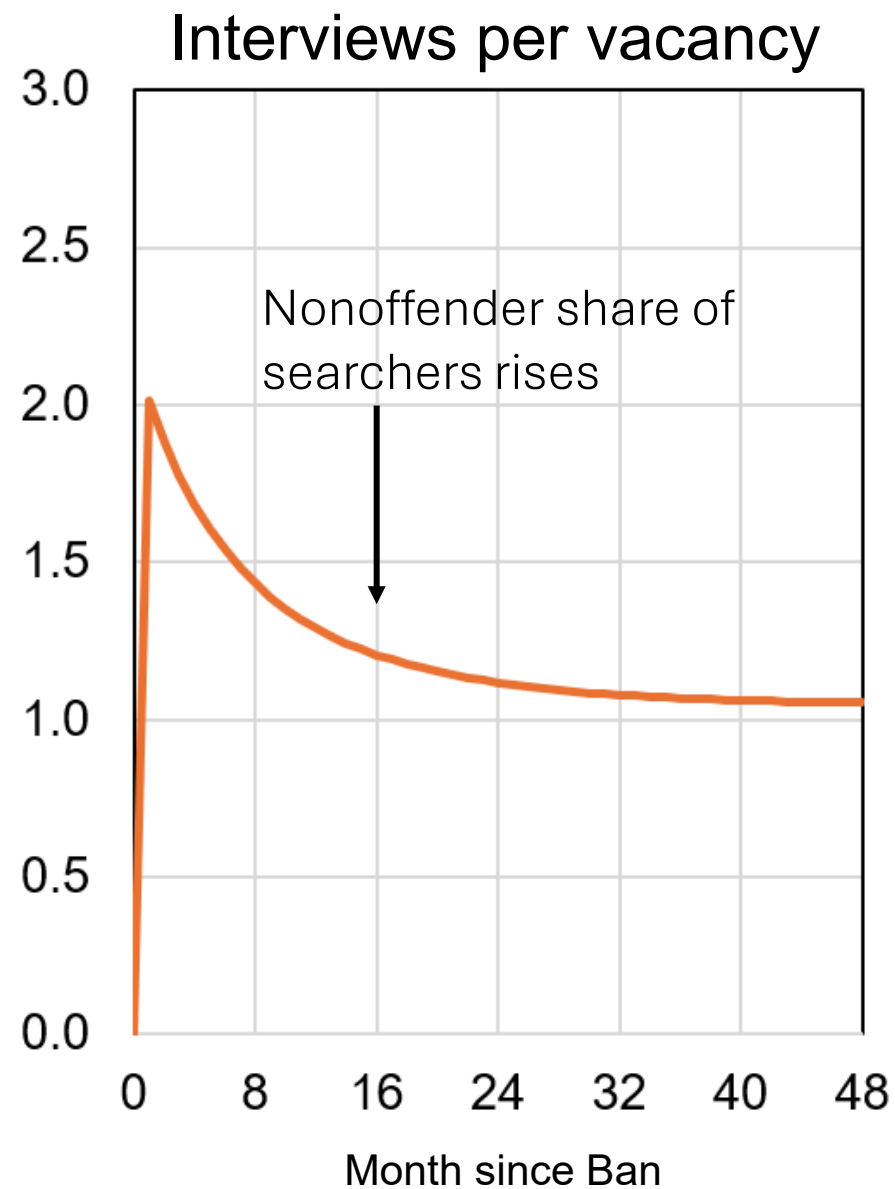
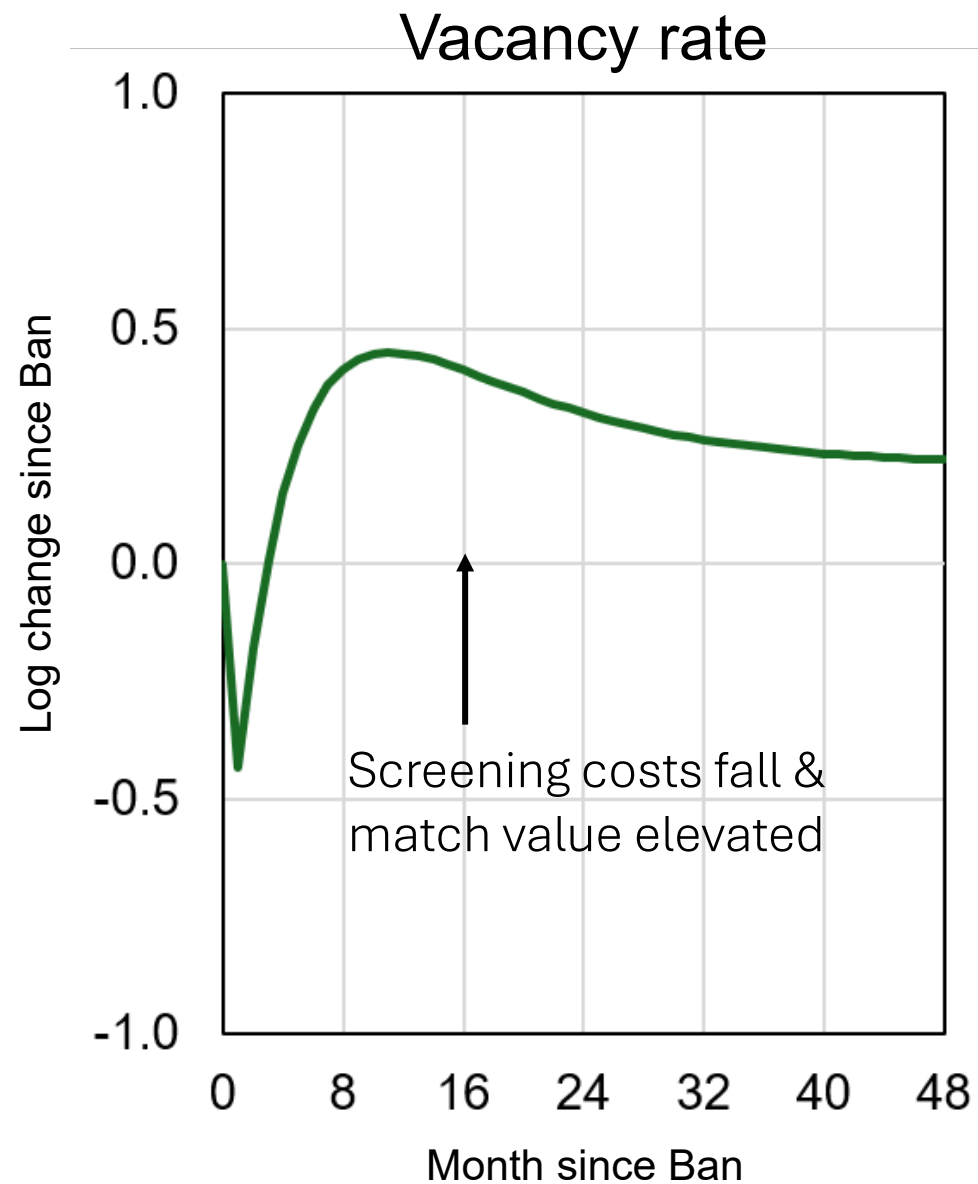


Exoff. Interviews $\uparrow \approx 35\%$
but
Exoff. Employment $\uparrow \approx 7\%$

Exoff. employment in line
with Pyle [2025] but at
upper end of lit. range.

Small impact on **black
employment** consistent w/
Kaestner and Wang [2024],
at odds w/ Doleac and
Hansen [2020].





Conclusion

- Theory: Tractable equilibrium dynamic search model with interview margin and rich specification of heterogeneity.
- Quant. illustration: First equilibrium exploration of Ban the Box.
- More to come:
 - 1] Non-Bayesian firms: Why are white nonoffenders interviewed more? [Agan & Starr 2018]
 - 2] Implications of Nash: High outside options compress diff. in payoffs.
 - 3] Policy analysis: Are there nonBtB policies that would aid exoffenders?

BONUS

Productivity parameters

Type, $\mathbf{x}$	$z(\mathbf{x})^*$	$\sigma_{\eta}(\mathbf{x})$	$\sigma_{\varepsilon}(\mathbf{x})$
white exoffender	0.9086	0.0014	0.0036
black exoffender	0.8286	0.0042	0.0066
white nonoffender	1	0.0027	0.0036
black nonoffender	1	0.0055	0.0066

* Expressed relative to z of white nonoffender

Wage parameters and labor mkt. frictions

Flow value of nonmkt. time, b	0.0120		
Cost of an interview, c	0.0066	$\Rightarrow$	Interview cost per filled job = 0.0332
Cost of entry, χ	0.5375		

Productivity parameters^{**}

Type, $\mathbf{x}$	$z(\mathbf{x})$	$\sigma_{\eta}(\mathbf{x})$	$\sigma_{\varepsilon}(\mathbf{x})$
white exoffender	0.9086	0.1172	0.3039
black exoffender	0.4303	0.1843	0.2891
white nonoffender	1	0.2305	0.3039
black nonoffender	0.5193	0.2431	0.2891

^{**} Expressed on present value basis.

Wage parameters and labor mkt. frictions

Flow value of nonmkt. time, b	1.0145 ^{**}	$\Rightarrow$	Interview cost per filled job = 0.0332
Cost of an interview, c	0.0066		
Cost of entry, χ	0.5375		

Match quality parameters

- Variance of η differs *within* race *and within* record $\Rightarrow$

$$\sigma_{\eta} = \bar{\sigma}_{\eta} + \sigma_{\eta}(\text{exoff.})\mathbf{1}[\text{exoff.}] + \sigma_{\eta}(\text{black})\mathbf{1}[\text{black}]$$

- Variance of ε differs by race (only) $\Rightarrow$

$$\sigma_{\varepsilon} = \bar{\sigma}_{\varepsilon} + \sigma_{\varepsilon}(\text{black})\mathbf{1}[\text{black}]$$

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↑
baseline
dispersion

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$\Rightarrow$ (unconditional) Pr(interview)

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↑
baseline
dispersion $\Rightarrow ??$

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↑
baseline
dispersion

$\Rightarrow$

In model w/ wage dispersion, this
controls contribution of “match
effects” [Woodcock 2008]

- Variance of ε differs by race (only) $\Rightarrow$

$$\sigma_{\varepsilon} = \bar{\sigma}_{\varepsilon} + \sigma_{\varepsilon}(\text{black})\mathbf{1}[\text{black}]$$

↑
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dispersion

$\Rightarrow$ (unconditional) Pr(interview)

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$$\sigma_{\eta} = \bar{\sigma}_{\eta} + \sigma_{\eta}(\text{exoff.})\mathbf{1}[\text{exoff.}] + \sigma_{\eta}(\text{black})\mathbf{1}[\text{black}]$$

baseline
dispersion $\Rightarrow$ Carry over preliminary estimate of $\bar{\sigma}_{\eta} \approx 0.23$ from model with Nash bargaining.

- Variance of ε differs by race (only) $\Rightarrow$

$$\sigma_{\varepsilon} = \bar{\sigma}_{\varepsilon} + \sigma_{\varepsilon}(\text{black})\mathbf{1}[\text{black}]$$

baseline
dispersion $\Rightarrow$ (unconditional) Pr(interview)

Density of hires over π

- Helpful to start with a related object: The prob. a firm hires bin k applicant w/ payoff **greater than y** , $\Phi_k(\pi)$ [survivor function]
- This can be decomposed as ...

$\Pr(\text{hire bin } k \text{ with payoff } \geq \pi)$

$\Phi_k(\pi) =$

$\Pr(\text{bins } 1, \dots, k-1 \text{ draw } < \Pi_k^* \text{ \& bin } k \text{ draws } \pi' \geq \max\{\pi, \Pi_k^*\})$

Pr(hire bin k with payoff $\geq \pi$)

$$\Phi_k(\pi \mid \boldsymbol{\lambda}) =$$

$$e^{-\sum_{j=1}^{k-1} \lambda_j (1 - H_j(\Pi_k^*))} \times$$

Pr(All higher ranked bins
draw payoff $< \Pi_k^*$)

= Pr(bin k
interviewed)

Pr(hire bin k with payoff $\geq \pi$)

$\Phi_k(\pi \mid \boldsymbol{\lambda}) =$

$$e^{-\sum_{j=1}^{k-1} \lambda_j (1 - H_j(\Pi_k^*))} \times \left(1 - e^{-\lambda_k (1 - H_k(\Pi_k^*))} \right) \times \frac{1 - H_k(\max\{\pi, \Pi_k^*\})}{1 - H_k(\Pi_k^*)}$$

Pr(All higher ranked bins
draw payoff $< \Pi_k^*$)

Pr(bin k draws
payoff $> \Pi_k^*$)

Pr(payoff $\geq \pi$
given payoff $\geq \Pi_k^*$)

= Pr(bin k
interviewed)

Pr(hire bin k with payoff $\geq \pi$)

$\Phi_k(\pi \mid \boldsymbol{\lambda}) =$

$$e^{-\sum_{j=1}^{k-1} \lambda_j (1 - H_j(\Pi_k^*))} \times \left(1 - e^{-\lambda_k (1 - H_k(\Pi_k^*))} \right) \times \frac{1 - H_k(\max\{\pi, \Pi_k^*\})}{1 - H_k(\Pi_k^*)}$$

+ Pr(bin k draws *below* Π_k^* but *above* π and
higher than other interviewed bins)

Pr(hire bin k with payoff $\geq \pi$)

$$\Phi_k(\pi \mid \boldsymbol{\lambda}) =$$

$$e^{-\sum_{j=1}^{k-1} \lambda_j (1 - H_j(\Pi_k^*))} \times \left(1 - e^{-\lambda_k (1 - H_k(\Pi_k^*))} \right) \times \frac{1 - H_k(\max\{\pi, \Pi_k^*\})}{1 - H_k(\Pi_k^*)}$$

Case 1: $\pi \in [\Pi_{k+1}^*, \Pi_k^*]$

$$+ \Pr(\text{bin } k \text{ draws } \pi' \text{ s.t. } \Pi_k^* > \pi' > \pi > \Pi_{k+1}^* \\ \& \text{ bins } 1, \dots, k-1 \text{ draw } < \pi')$$

Pr(hire bin k with payoff $\geq \pi$)

$$\Phi_k(\pi \mid \boldsymbol{\lambda}) =$$

$$e^{-\sum_{j=1}^{k-1} \lambda_j (1 - H_j(\Pi_k^*))} \times \left(1 - e^{-\lambda_k (1 - H_k(\Pi_k^*))} \right) \times \frac{1 - H_k(\max\{\pi, \Pi_k^*\})}{1 - H_k(\Pi_k^*)}$$

Case 2: $\pi \in [\Pi_{k+2}^*, \Pi_{k+1}^*]$

+ Pr(bin k draws $\Pi_{k+1}^* > \pi' > \pi > \Pi_{k+2}^*$
& $1, \dots, k-1$ and $k+1$ draw $< \pi'$)

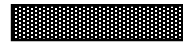
Pr(hire bin k with payoff $\geq \pi$)

$\Phi_k(\pi \mid \lambda) =$

$$e^{-\sum_{j=1}^{k-1} \lambda_j (1 - H_j(\Pi_k^*))} \times \left(1 - e^{-\lambda_k (1 - H_k(\Pi_k^*))} \right) \times \frac{1 - H_k(\max\{\pi, \Pi_k^*\})}{1 - H_k(\Pi_k^*)}$$

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+ Pr(bin k draws $\Pi_{k+1}^* > \pi' > \pi > \Pi_{k+2}^*$
& $1, \dots, k-1$ and $\mathbf{k+1}$ draw $< \pi'$)



A high ranked
bin may end up
in competition
w/ lower ranks

Pr(hire bin k with payoff $\geq \pi$)

$$\Phi_k(\pi \mid \boldsymbol{\lambda}) =$$

$$e^{-\sum_{j=1}^{k-1} \lambda_j (1-H_j(\Pi_k^*))} \times \left(1 - e^{-\lambda_k (1-H_k(\Pi_k^*))}\right) \times \frac{1 - H_k(\max\{\pi, \Pi_k^*\})}{1 - H_k(\Pi_k^*)}$$

$$+ \sum_{\ell=k}^{\min \ell \text{ s.t. } \Pi_{\ell+1}^* \leq \pi} \int_{\max\{\pi, \Pi_{\ell+1}^*\}}^{\Pi_{\ell}^*} e^{-\sum_{j=1}^{\ell} \lambda_j (1-H_j(\pi'))} \lambda_k dH_k(\pi')$$

Pr(hire bin k with payoff $\geq \pi$)

$$\Phi_k(\pi | \boldsymbol{\lambda}) =$$

$$e^{-\sum_{j=1}^{k-1} \lambda_j (1 - H_j(\Pi_k^*))} \times \left(1 - e^{-\lambda_k (1 - H_k(\Pi_k^*))} \right) \times \frac{1 - H_k(\max\{\pi, \Pi_k^*\})}{1 - H_k(\Pi_k^*)}$$

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➤ Pr(hire *any* app. w/ payoff $> \pi$) is $\Phi(\pi | \boldsymbol{\lambda}) = \sum_{k=1}^K \Phi_k(\pi | \boldsymbol{\lambda})$.

➤ Define $\phi_k(\pi) \equiv -\partial \Phi_k(\pi | \boldsymbol{\lambda}) / \partial \pi$ and $\phi(\pi) \equiv -\partial \Phi(\pi | \boldsymbol{\lambda}) / \partial \pi$.

Beveridge curve

- Unemployment by type evolves according to

$$\Delta u_{\mathbf{x}}(t + 1) = \delta_{\mathbf{x}}(\pi_{\mathbf{x}} - u_{\mathbf{x}}(t)) - \mathbf{p}_{\mathbf{x}}(\mathbf{t})u_{\mathbf{x}}(t),$$

where $\mathbf{p}_{\mathbf{x}}(\mathbf{t})$ is the job finding probability of type $\mathbf{x}$.

- Brief derivation: job finding prob. of *rank* k ,

$$p_k = \frac{\text{hires of rank } k}{\text{searchers of rank } k}$$

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where $\mathbf{p}_{\mathbf{x}}(t)$ is the **job finding probability** of type $\mathbf{x}$.

- Brief derivation: job finding prob. of *type* $\mathbf{x}$,

$$p_{\mathbf{x}} = \sum_{k=1}^K p_k \times \Pr(\text{rank} = k | \mathbf{x})$$

Beliefs

- Share of job seekers of race r w/ criminal history s is $\Pr(s | r)$.
- Firm observes η and updates belief about s by Bayes rule,

$$\Pr(s | r, \eta) = \Pr(s | r) \cdot \frac{\Pr(\eta | r, s)}{\Pr(\eta | r)}.$$

Beliefs

- Share of job seekers of race $\mathcal{r}$ w/ criminal history $\mathcal{s}$ is $\Pr(\mathcal{s} | \mathcal{r})$.
- Firm observes η and updates belief about $\mathcal{s}$ by Bayes rule,

$$\Pr(\mathcal{s} | \mathcal{r}, \eta) = \Pr(\mathcal{s} | \mathcal{r}) \cdot \frac{g(\eta | \mathcal{r}, \mathcal{s})}{\sum_{\mathcal{s}} \Pr(\mathcal{s} | \mathcal{r}) g(\eta | \mathcal{r}, \mathcal{s})}.$$

Extension: (Partially) hidden types

- Example: Two attributes—race (WH, BL) and criminal record (Exoff., Nonoff.). Assume record is concealed at application stage.
 - $Z \equiv z - rU$ partially hidden but π learned at interview stage.
- What changes: Distribution of payoffs | application is a weighted avg.,
$$\begin{aligned}\overline{H}(\pi \mid \text{BL}, \eta) &= \text{Pr}(\text{Exoff.} \mid \text{BL}, \eta) \times H(\pi \mid \mathbf{x} = \text{BL Exoff.}, \eta) \\ &\quad + \text{Pr}(\text{Nonoff.} \mid \text{BL}, \eta) \times H(\pi \mid \mathbf{x} = \text{BL Nonoff.}, \eta)\end{aligned}$$
- Swap this for original (H) $\Rightarrow$ analytical results under perfect info. apply.

Parameters

1] Population shares, m_x

- No consensus on exoffender shares by race.
- Our baseline: NLSY + admin. data on imprisonment.

Race	Felon share
Black	0.325
White	0.100

[From NLSY]

- Main idea: $\text{Pr}(\text{ever imprisoned}) = \text{Pr}(\text{ever imprisoned} \mid \text{felony record}) \times \text{Pr}(\text{felony record})$
[From prisoner flow data]

Source	Moment	Value	Relevant parameter
Barron et al [1997]	Pr(interview)	0.373	$\text{std}(\varepsilon)$
Agan & Starr [2018]	$\frac{\text{Pr}(\text{interview } \mathbf{x})}{\text{Pr}(\text{interview white exoff.})}$	WH exoff. = 0.593 BL exoff. = 0.614 BL nonoff. = 0.936	$z(\text{WH exoff.}),$ $z(\text{BL exoff.}),$ $\text{std}(\varepsilon \mid \text{BL})$
Current Pop. Survey	Nonemp. (NE) rate	0.137	χ
Current Pop. Survey	$\frac{\text{Black NE rate}}{\text{White NE rate}}$	2.045	$\text{std}(\eta \mid \text{BL})$
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Villena-Roldan [2012]	Interview cost per hire (in mo. wages)	1.3	c

Source	Moment	Value	Relevant parameter
Barth et al [2016]	$\frac{\text{dln(wage)}}{\text{dln(avg. product)}}$	0.163—0.386	α
Woodcock [2008]	$\frac{\text{Share of var(wage) due to match effects}}{\text{to match effects}}$	0.039—0.157	$\text{std}(\eta)$
Shem-Tov & Rose [2025]	Exoff. relative wage	-0.364	b