

Micro and macro cost-price dynamics in normal times and during inflation surges

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Abstract

We develop a unified approach to studying cost-price dynamics in the cross-section of firms in order to explain the time series of aggregate inflation, both during normal times and inflation surges. A key novelty is the use of microdata on firms' prices and production costs to construct an empirical measure of *price gaps*—the deviation between a firm's listed and optimal price. We characterize the mapping between price gaps and the size and frequency of price adjustments and take them to the data to test nonparametrically how firms' pricing strategies align with the predictions of different pricing models, conditional on shocks of different magnitudes. The microdata provide strong evidence of state dependence: the passthrough of costs into inflation increases more than proportionately when the economy is hit by large aggregate shocks. In contrast, in normal times, the frequency of price adjustment is approximately constant, and the microdata conform to the predictions of time-dependent models (e.g., Calvo 1983). Conditional on the path of aggregate cost shocks extracted from the data, a generalized state-dependent pricing model accounts well for both the low and stable inflation of the pre-pandemic period and the nonlinear surge that followed.

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1 Introduction

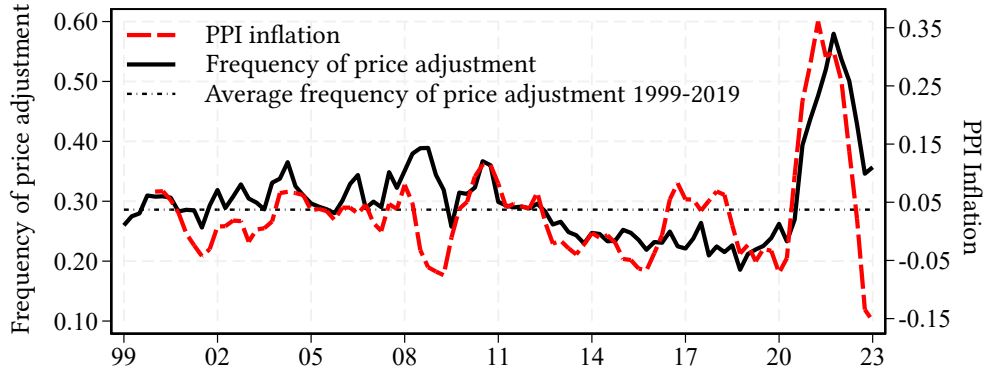
Firms adjust output prices infrequently despite continuously evolving economic conditions, leading their prices to drift temporarily from those that maximize flow profits. In all models featuring nominal rigidities, the deviation between listed and optimal prices—the *price gap*—determines firms’ pricing behavior, as it reflects the evolution of production costs since the last adjustment. What distinguishes different models is how they map price gaps to price changes, with potentially important implications for aggregate inflation. In time-dependent models (e.g., Taylor 1980; Calvo 1983), prices have a fixed duration or adjust with a fixed probability. In these models, expected price changes are a linear function of the price gap, since firms reset prices to their optimum upon adjustment. In contrast, in state-dependent pricing models (e.g. Caballero and Engel 1993, 2007; Golosov and Lucas 2007) expected price changes are a nonlinear function of the price gaps, since both the size of adjustments and the frequency of price changes depend endogenously on the gap. While the distinction between time- and state-dependent pricing is less significant when shocks to desired prices are small, it becomes important and nonlinearities emerge when large aggregate shocks hit the economy.

The recent surge in inflation well illustrates these mechanisms. Figure 1 plots year-over-year changes in the producer price index for the Belgian manufacturing sector alongside the average frequency of price adjustment from 1999:Q1 to 2023:Q4. Before the pandemic, both inflation and the average frequency remained low and relatively stable, consistent with a linear mapping between expected price changes and price gaps. Starting in early 2021, however, both inflation and the frequency rose sharply—hallmarks of state-dependent pricing and, as we show, nonlinear cost-price dynamics.¹

Recent contributions have demonstrated that state-dependent models can rationalize the inflation dynamics during the recent surge (Blanco et al. 2024a, 2024b; Bunn et al. 2024; Cavallo et al. 2024; Morales-Jiménez and Stevens 2024). A common approach in these studies, as well as in the foundational contributions on which they build (Nakamura and Steinsson 2010; Midrigan 2011; Alvarez et al. 2016), is to invert the model in order to discipline its structural parameters by fitting the observed distribution

¹See Blanco et al. (2024b) and Cavallo et al. (2024) for evidence of similar dynamics in the U.S. and other developed economies and Gagliardone and Gertler (2023) and Hazell and Hobler (2024) for a discussion of the drivers of the pandemic-era inflation surge.

Figure 1: Aggregate inflation and frequency of price adjustment



Notes. This figure shows the time series of PPI manufacturing inflation along with the annual frequency of price adjustment. The former is computed as the year-over-year percentage change in the aggregate PPI. The latter is calculated as a rolling average of the quarterly frequency of price adjustment over the previous four quarters.

of price changes. Under some assumptions, it is also possible to recover the implied distribution of price gaps that rationalize the observed price changes (Alvarez et al. 2022). We emphasize that all these papers identify state-dependent behavior using *only* data on prices. In this paper, we follow a different approach, leveraging information on *both* prices and costs to construct an empirical measure of firm-level price gaps—the key object of our analysis—which allows us to study pricing policies in the microdata and their connection to aggregate inflation dynamics.

We assemble a rich micro dataset of administrative records covering output prices, output quantities, and production costs at a quarterly frequency for Belgian manufacturing firms from 1999 to 2023. These data allow us to construct an empirical measure of firm-level price gaps that maps directly to its theoretical counterpart. We analyze the joint empirical distribution of price gaps and price changes through the lens of a tractable, state-dependent model—a menu-cost framework in the spirit of Nakamura and Steinsson (2010) and Auclert et al. (2024)—which nests a time-dependent Calvo (1983) model as a special case.² Using the model, we derive closed-form (algebraic) expressions characterizing price adjustments along both the extensive and intensive margins as a function of the firms’ price gaps. We take these expressions to the data to directly test how the mapping from price gaps—and thus the predictions of alternative models—varies

²Other seminal contributions include the works by Caplin and Spulber (1987), Caplin and Leahy (1991, 1997) and Dotsey et al. (1999) on state-dependent models and monetary neutrality.

with the magnitude of shocks. In addition, the availability of microdata on production costs allows us to construct an aggregate cost index (and a corresponding sequence of aggregate cost shocks), which we feed into our model to account for the time series of aggregate inflation. Our analysis makes the following contributions.

Passthrough in the cross-section—The mapping between price gaps and price changes in the microdata provides direct evidence of the state-dependent nature of firms’ pricing behavior. First, focusing on the extensive margin, we show that the frequency of price adjustment increases with the absolute value of a firm’s price gap and is well approximated by a convex (quadratic) function. This analysis allows us to produce the empirical analog of the generalized hazard function (GHF) postulated by the menu-cost model. Furthermore, by comparing the distribution of price gaps before and during the pandemic, we document how large aggregate shocks shift the entire distribution, pushing many firms to its tails, where the GHF is steeper. This shift results in a sharp rise in the average frequency of price adjustment, consistent with the evidence in Figure 1. Second, studying the intensive margin, we find that the data closely align with the model’s prediction: firms that adjust their prices so as to nearly close the price gap, with an elasticity close to one.

Finally, we derive an algebraic expression that combines the adjustments along the extensive and intensive margins and characterizes the passthrough for shocks of varying magnitudes. Our main proposition establishes that expected price changes can be approximated by a third-order (odd) polynomial in price gaps. Consistent with this prediction, we show that the relationship between price gaps and average price changes is S-shaped, allowing us to partition the cross-section of firms into two distinct regions. The first region, which we refer to as the “Calvo region,” includes firm-quarter observations with small price gaps, i.e., those experiencing modest shocks to their desired prices. In this region, the frequency of price adjustment is approximately constant and near its long-run (steady-state) average, and expected price changes increase linearly with the gap. Thus, consistent with the predictions of the time-dependent Calvo model, the elasticity of average price changes with respect to price gaps is constant (roughly equal to the average frequency of adjustment), resulting in linear cost-price dynamics. The second region lies in the tails of the price gap distribution, where large shocks result in substantial deviations from firms’ optimal prices (approximately 20% or more). For these firms, the frequency of price adjustment rises more than proportionally with the size of the gap, capturing the

nonlinearities induced by state-dependent pricing. Accordingly, the elasticity of average price changes with respect to gaps is approximately twice as large as in the Calvo region.

Passthrough in the time series—Our second set of results concerns the role of cost-price dynamics in explaining aggregate inflation over time. Leveraging our microdata, we construct a real marginal cost index for the Belgian manufacturing sector, with strong predictive power for inflation. Intermediate input costs drive most of the variation in the index, with labor costs playing a more limited role.

We use the real cost index to evaluate how well our menu-cost model accounts for inflation dynamics. In doing so, we differ from prior literature in two ways. First, we develop a novel identification strategy to calibrate the key parameters governing nominal rigidities. In contrast to the standard calibration approach—which relies on model inversion and fits only the distribution of price changes—we exploit moments from the joint distribution of price changes and price gaps. Second, whereas prior studies reverse-engineer unobservable shocks to match inflation, we instead condition on an observable series of aggregate shocks and feed it directly into the model to assess fit.

The menu-cost model closely tracks short-run fluctuations in Belgian manufacturing inflation and in the frequency of price adjustment—both during the stable pre-pandemic period and the post-pandemic surge. The model captures not only the stable behavior of adjustment frequencies before the pandemic but also the sharp rise in price adjustments that followed, both in timing and magnitude. By contrast, a Calvo model fed with the same sequence of aggregate cost shocks accounts well for inflation during normal times but explains only about two-thirds of the post-pandemic inflation surge. Taken together, these empirical findings support the conclusions of prior theoretical work, which highlight that the distinction between time- and state-dependent pricing models is modest in the presence of small shocks (Dias et al. 2007; Gertler and Leahy 2008; Alvarez et al. 2017; Auclert et al. 2024), but emphasize that state dependence becomes essential to rationalize inflation dynamics in the wake of large shocks.

Related literature. Prior research has provided robust evidence consistent with state-dependent pricing by studying micro-moments extracted from the empirical distribution of price changes (Klenow and Kryvtsov 2008; Gagnon 2009; Vavra 2014; Gautier and Saout 2015) and has shown that state-dependent pricing models can

rationalize key features of these distributions (see the references cited earlier in this section). Direct empirical evidence of state dependence remains limited. Notable exceptions include Gagnon (2009) and Alvarez et al. (2019), who present evidence of state-dependent pricing by showing how inflation surges in Mexico and Argentina are associated with significant increases in the average frequency of price changes.

Our work advances this literature in three directions. A first key difference lies in our ability to construct a high-frequency, firm-level measure of price gaps based on both costs and competitors' prices data. This allows us to go beyond the distribution of price changes and directly test how pricing decisions relate to deviations from optimal prices. Second, we simultaneously explain both the cross-section and time series of price changes. In doing so, we derive algebraic expressions linking the size and frequency of price adjustment to price gaps, and use them to test how firms' pricing strategies align with different models, conditional on the magnitude of aggregate shocks. Our micro-based approach also yields novel identification results, allowing us to pin down key model parameters using a new moment derived from the distribution of price changes conditional on price gaps. Finally, we construct an observable series of cost shocks constructed directly from the data and feed it into the model to explain inflation dynamics. This provides a sharper validation of the model than the traditional approach of reverse-engineering unobservable shocks to match inflation.

Campbell and Eden (2014), Eichenbaum et al. (2011), Gagnon et al. (2013), and Karadi et al. (2024) provide evidence of state-dependent pricing by showing that the frequency of price adjustment in microdata responds systematically to deviations from a firm's notion of its ideal price. Campbell and Eden (2014) uses scanner data from supermarkets to show that the probability of nominal price adjustment is highest when a store's price substantially deviates from the average price charged by competing stores. Eichenbaum et al. (2011) uses data on retail and wholesale prices from a large food and drug retailer to construct a "reference price" metric. Similarly, Gagnon et al. (2013) and Karadi et al. (2024) define a reset price as the average price at which competing retailers offer the same product. Like our study, these papers document that the likelihood of price adjustment increases with the absolute deviation from the ideal price.

We depart from this literature in two fundamental ways. First, our empirical measure of price gaps captures not only variation in a firm's own cost structure but

also changes in markups arising from competitors’ pricing behavior. This measure is anchored in theory, thereby enabling a direct micro-to-macro mapping, and supported by empirical evidence that highlights cost variation and imperfect competition as key determinants of pass-through (Amiti et al. 2019; Gagliardone et al. Forthcoming). Second, the scope and representativeness of our dataset are substantially broader than previous studies. We can construct firm-level price gaps for a near-complete sample of domestic manufacturing producers in Belgium—covering 80–90 percent of the sector—over a 25-year period that includes both low-inflation regimes and inflationary episodes. This rich time-series variation is important as it allows us to study environments with stable, low adjustment frequencies as well as periods marked by sharp increases in price-changing behavior. Combined with the theoretical consistency of our price gap measure and broad cross-sectional coverage, it enables a systematic characterization of the nonlinearities in the passthrough arising from shocks of varying magnitudes.

Finally, the results in this paper connect to Gagliardone et al. (Forthcoming), which estimates the slope of the cost-based New Keynesian Phillips curve in normal times, i.e. when aggregate cost shocks are small. This paper complements our earlier work by providing a nonparametric characterization of the nonlinearities of the passthrough from cost to prices—which determines the slope of the generalized NKPC (Auclert et al. 2024)—as a function of the magnitude of the cost shocks.

The paper proceeds as follows. Section 2 presents the theoretical framework, and Section 3 derives testable implications based on the model’s predictions. Section 4 describes our dataset and the empirical measures of prices, costs, and price gaps. Section 5 and 6 present empirical results characterizing the mapping from price gaps to price changes in the cross-section of firms and in cost-price dynamics in the time series. In Section 7, we outline the calibration process and provide model simulations, which show how the calibrated model explains the inflation time series and the frequency of price adjustments, including the rise during the pandemic. Section 8 offers concluding remarks.

2 Theoretical framework

Our baseline framework is a variation of a standard discrete-time menu-cost model. To fit the data, we allow for both random menu costs as in Caballero and Engel (2007)

and random opportunities of free price adjustment, as in the “CalvoPlus” model of Nakamura and Steinsson (2010).³ As in Alvarez et al. (2023), we work with a quadratic approximation of the firm’s profit function and permanent idiosyncratic shocks. In addition, motivated by our previous work (Gagliardone et al. Forthcoming), we allow for strategic complementarities in price setting. This framework nests Calvo (1983) as a special case.

2.1 Model setup

In each period t , the economy is populated by a continuum of heterogeneous firms $f \in [0, 1]$ selling a single differentiated product under monopolistic competition facing a demand function à la Kimball (1995). Let lowercase letters denote the logarithms of the corresponding uppercase variables. We denote by $p_t(f)$ the firm’s price and by p_t the aggregate price index. Up to a first-order approximation around the symmetric steady state, the latter is given by:

$$p_t \approx \int_{[0,1]} \left(p_t(f) - \varphi_t(f) \right) df, \quad (1)$$

where $\varphi_t(f)$ denotes a firm-specific mean-zero log-taste shock, i.i.d. over firms and time.

Technology. Each firm uses a composite input $l_t(f)$ and a constant return to scale production technology to produce one unit of output, $y_t(f) = z_t(f) + l_t(f)$, where $z_t(f)$ denotes total factor productivity.⁴ We assume that the latter evolves as a random walk, $z_t(f) = z_{t-1}(f) + \zeta_t(f)$, where $\zeta_t(f)$ denotes an idiosyncratic shock that is mean zero and i.i.d. over time and across firms. In this setting, firms’ nominal marginal cost is given by:

$$mc_t^n(f) = mc_t^n - z_t(f). \quad (2)$$

The term mc_t^n captures an aggregate nominal cost shifter. Consistent with the empirical evidence, we assume that mc_t^n obeys a random walk $mc_t^n = mc_{t-1}^n + g_t$, where g_t is an aggregate shock, that is i.i.d. over time with mean μ_g , drawn from a unimodal, symmetric, and smooth distribution. For analytical tractability, we assume no trend inflation ($\mu_g = 0$)

³See also Dotsey et al. (1999) for a treatment of random menu-cost models with idiosyncratic shocks.

⁴In our empirical analysis, we relax the constant-return-to-scale assumption and account for variation in short-run variable costs driven by both labor and intermediate inputs.

in what follows.⁵ We relax this assumption in the quantitative exercises of Section 7.

Profit maximization. Firms choose prices to maximize the present value of profits, subject to nominal rigidities. Each firm pays a fixed cost $\chi_t(f)$ upon changing its price. As in Caballero and Engel (2007), the fixed cost $\chi_t(f)$ is the realization of a random variable, i.i.d. between firms and time, and uniformly distributed on the $[0, \bar{\chi}]$ interval. As in the CalvoPlus model, with probability $(1 - \theta^o)$ the fixed cost is zero, which implies that the firm can adjust its price for free.

We denote by $p_t^o(f)$ the firm's *static target price*, that is, the price it would choose absent nominal rigidities. Under Kimball preferences, a firm's price elasticity of demand increases with its relative price $(p_t(f) - p_t)$, which makes the desired markup decrease in relative prices. As we show in Appendix A.2, this implies that $p_t^o(f)$ is given by the sum of the steady-state (log) markup, $\mu(f)$, and a convex combination of the firm's nominal marginal cost and the price index:

$$p_t^o(f) = (1 - \Omega) \left(\mu(f) + mc_t^n(f) \right) + \Omega \left(p_t + \varphi_t(f) \right), \quad (3)$$

where the scalar $\Omega \in [0, 1)$ captures the strength of strategic complementarities in price setting. The taste shock $\varphi_t(f)$ shows up in the target price as noise.

Following Alvarez et al. (2023), we take a quadratic approximation of the per-period profit function around the static optimum $p_f(f) = p_t^o(f)$ and normalize it by steady-state profits. This yields the following loss function measuring the cost of deviations of the price from the target:

$$\Pi_t(f) \approx -\frac{\sigma(\sigma - 1)}{2(1 - \Omega)} (p_t(f) - p_t^o(f))^2,$$

where σ is the steady-state price elasticity of demand and steady-state profits are equal to $1/\sigma$. Note that the weight on the loss function increases with the complementarity parameter Ω . This is due to the fact that strategic complementarities increase the curvature of the profit function, and therefore raise the firm's desire to keep the price close to the target relative to the cost of adjustment.

Let $\mathbb{I}_t(f)$ be an indicator function that equals one if the firm adjusts its price and zero otherwise. Then, the value of the firm normalized by steady-state profits is given by:

⁵As Nakamura et al. (2018), Alvarez et al. (2019), and Alvarez et al. (2022) show, an economy with zero inflation provides an accurate approximation for economies where inflation is low, as the effect of low trend inflation on firms' decision rules is of second order.

$$V_t(f) = \max_{\{p_t(f), \mathbb{I}_t(f)\}_{t=0}^{\infty}} \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \left\{ \Pi_t(f) - \chi_t(f) \cdot \mathbb{I}_t(f) \right\}. \quad (4)$$

2.2 Characterization of firms' pricing policies

As is standard in state-dependent models, the solution of the firm problem has an “Ss flavor.” The optimal pricing policy reduces to determining an optimal probability of price adjustment and, conditional on adjustment, an optimal reset gap:

$$x_t^{\star} \equiv p_t^o(f) - p_t^{\star}(f),$$

which captures the difference between the static target price and p_t^{\star} , the (*dynamic*) *reset price* set by a firm that decides to adjust its price.⁶

To characterize firms' optimal pricing policies, we define the (ex-ante) *price gap*:

$$x_{t-1}(f) \equiv p_t^o(f) - p_{t-1}(f). \quad (5)$$

The price gap captures the percentage difference between the static target price and the price set by the firm in the previous period. It serves as a state variable because it is measurable before the firm decides whether to adjust its price (hence, “ex-ante”), yet incorporates the realization of all time t shocks through their impact on $p_t^o(f)$. To see this, we substitute $p_t^o(f)$ from Equation (3) and $mc_t^n(f)$ from Equation (2) into Equation (5), and then use the expressions describing the processes for the aggregate and idiosyncratic components of $mc_t^n(f)$ to obtain:

$$x_{t-1}(f) = \left(p_{t-1}^o(f) + (1 - \Omega)(g_t + \varepsilon_t(f)) + \Omega(p_t - p_{t-1}) \right) - p_{t-1}(f),$$

where $\varepsilon_t(f) \equiv \frac{\Omega}{1-\Omega} \varphi_t(f) - \zeta_t(f)$ denotes a composite idiosyncratic shock, which combines idiosyncratic technology and taste shocks. We assume that $\varepsilon_t(f)$ is drawn from a unimodal, symmetric, and smooth distribution with mean zero and variance σ_{ε}^2 .

We can characterize the solution to the firm's problem as a function of the price

⁶Note that the optimal reset gap x_t^{\star} varies over time due to aggregate shocks but it does not have an f subscript. This is because, to a first-order approximation, the idiosyncratic shocks, $\zeta_t(f)$ and $\varphi_t(f)$, enter both prices in an identical way and therefore cancel out once we take the difference. Important for this result is the assumption that idiosyncratic shocks evolve as a random walk.

gap:⁷

$$p_t^o(f) - p_t(f) = \begin{cases} x_t^* & \text{w. p. } h_t(x_{t-1}) \\ x_{t-1}(f) & \text{w. p. } 1 - h_t(x_{t-1}). \end{cases} \quad (6)$$

Here $h_t(x_{t-1})$ denotes the probability that a firm adjusts its price at t . Upon adjustment, they set their price to $p_t^*(f)$. If they do not adjust their price, they keep their gap at $x_{t-1}(f)$.

Optimal probability of price adjustment. Unlike in time-dependent models, in state-dependent models the optimal adjustment probability is an endogenous variable that ultimately depends on the realization of the price gap $x_{t-1}(f)$.

We denote by $V_t(x_{t-1}(f))$ the value of a firm that decides not to revise its price and by V_t^a the value of a firm that decides to do so. The former is a function of current profits Π_t evaluated at the price gap $x_{t-1}(f)$ and of the discounted expected continuation value:

$$V_t(x_{t-1}) = \Pi_t(x_{t-1}) + \beta \mathbb{E}_t \{ h_{t+1}(x_t) \cdot V_{t+1}^a + (1 - h_{t+1}(x_t)) \cdot V_{t+1}(x_t) \}.$$

The latter is a function of the optimal reset gap, $V^a(x_t^*)$, as we show below. The probability that a firm adjusts its price increases with the distance between the two value functions.

Dropping the firm index to ease notation, given the random menu cost and the random possibility of a free price adjustment, $h_t(x_{t-1})$ —also known as the generalized hazard function (GHF)—is given by:

$$\begin{aligned} h_t(x_{t-1}) &= (1 - \theta^o) + \theta^o \cdot \Pr(V_t^a - \chi_t(f) \geq V_t(x_{t-1})) \\ &= (1 - \theta^o) + \theta^o \cdot \min \left\{ \frac{V_t^a - V_t(x_{t-1})}{\bar{\chi}}, 1 \right\}, \end{aligned} \quad (7)$$

where the second line uses the assumption that the distribution of the menu cost is uniform. The expression above shows that the probability of price adjustment in a given period, $h_t(x_{t-1})$, depends, among other factors, on its price gap $x_{t-1}(f)$. With no trend inflation (and symmetric profit function), the minimum of the GHF is achieved when $x_{t-1} = 0$ and $h_t(0) = (1 - \theta^o)$, the probability of a free price adjustment. Also, observe that, as the upper bound for the menu cost $\bar{\chi}$ approaches infinity, the adjustment frequency becomes exogenous and converges to $(1 - \theta^o)$. Thus, as a limiting case, the model nests a time-dependent Calvo model parameterized by θ^o .

⁷All derivations are provided in Appendix A.

The following lemma shows that the GHF can be accurately approximated in a neighborhood of the zero gap by a quadratic function of the price gap.

Lemma 1. *Assume stationarity of the value function, $V_t(x) = V(x)$. Up to a second-order approximation around $x_t^* = 0$, the GHF is given by:*

$$h(x_{t-1}(f)) = (1 - \theta^0) + \phi \cdot ((x_{t-1}(f))^2 + o((x_{t-1}(f))^2)), \quad (8)$$

where $o((x(f))^2)$ is an approximation error and $\phi \equiv -\frac{\theta^0}{2\bar{\chi}} \frac{\partial^2 V(x)}{\partial x^2} \Big|_{x=0}$.

Proof. See Appendix A.3. □

Lemma 1 states that, under a quadratic approximation, the GHF is U-shaped and symmetric around the point where the price gap is zero. At this point, the adjustment probability is at its global minimum, corresponding to the probability of a free price adjustment $(1 - \theta^0)$. As price gaps widen, the adjustment probability monotonically increases. The parameter ϕ controls the sensitivity of the GHF to changes in gaps, i.e., the “steepness” of the parabola.

Optimal reset gap. The value of the firm conditional on adjusting is the optimized value of V in Equation (4) with respect to the reset price p_t^* :

$$V_t^a = \max_{p_t^*} V_t(x_t^*).$$

Equivalently, the optimal reset gap x_t^* solves the first-order condition $V_t(x_t^*) = 0$. Under low trend inflation, a quadratic approximation of the profit function, and assuming that the firm’s marginal cost follows a random walk, the static optimal price provides a good approximation of the dynamic optimal price ($p_t^*(f) \approx p_t^0(f)$), implying that $x_t^* \approx 0$ (Alvarez et al. 2016). In Section 5, we provide micro-level evidence indicating that this approximation is broadly supported in the data.⁸

2.3 Aggregate inflation

Given the solution of the firm’s problem in Equation (6) and using the formula for the price index in Equation (1), we can express aggregate inflation π_t as:

⁸Appendix B present quantitative exercises analyzing the response of static and dynamic reset prices to shocks of varying magnitudes.

$$\begin{aligned}\pi_t &= \int \left(p_t(f) - p_{t-1}(f) \right) df = \int h_t(x_{t-1}(f)) \cdot (p_t^*(f) - p_{t-1}(f)) df \\ &= \int h_t(x_{t-1}(f)) df \cdot \int \left(p_t^*(f) - p_{t-1}(f) \right) df + Cov\left(h_t(x_{t-1}(f)), (p_t^*(f) - p_{t-1}(f))\right) \quad (9)\end{aligned}$$

The first line shows that aggregate inflation—the average of firm-level price adjustments—can be expressed, to a first-order approximation, as the product of a firm’s adjustment probability and its price change conditional on adjustment. The second line decomposes inflation into (i) the product of the average frequency of price adjustment and the average distance between the ideal reset price and the previous period price and (ii) the covariance between the variables.

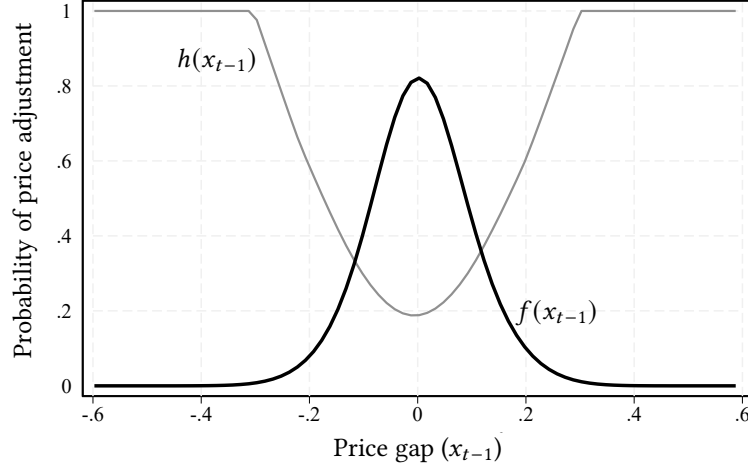
With state-dependent pricing, the adjustment frequency is an endogenous object that, as we will see, increases nonlinearly with the absolute value of the price gap. With Calvo pricing, the adjustment frequency is orthogonal to the price gap and therefore uniform across firms and independent of the size of shocks; the price adjustment is a linear function of the price gap, and inflation is equal to the product of the constant adjustment frequency and the average price gap.

As in Caballero and Engel (2007), Golosov and Lucas (2007) and, more recently, Karadi et al. (2024), a “selection effect” increases the degree of monetary neutrality in an economy with large shocks. This force is captured by the covariance term in Equation (9). Firms that are more likely to adjust are also those that change their prices the most (conditional on adjustment). That is, the gap between $p_t^*(f)$ and $p_{t-1}(f)$ positively co-moves with x_{t-1} and therefore with $h_t(x_{t-1})$. Thus, the selection effect amplifies aggregate inflation.

3 Testable implications and identification results

We now derive algebraic expressions that nonparametrically characterize the mapping from price gaps to firms’ pricing decisions at the extensive and intensive margins, and their interaction. This framework yields testable implications that validate the model and its underlying assumptions (Section 5) and inform the calibration of structural parameters (Section 7).

Figure 2: Generalized hazard function and distribution of price gaps



Notes. This figure shows the generalized hazard function (GHF), $h(x_{t-1})$ as a function of the underlying distribution of price gaps $f(x_{t-1})$.

3.1 The generalized hazard function

Figure 2 illustrates the relationship between price gaps and the extensive margin of price adjustments in the stationary equilibrium. The horizontal axis depicts the steady-state probability density function of price gaps, denoted by $f(x_{t-1})$, which is unimodal and bell-shaped. The vertical axis shows the GHF, $h_t(x_{t-1})$, the probability of price adjustment at different points in the price gap distribution. Under our assumptions, it is U-shaped and centered around $x_{t-1} = 0$. As discussed above, the GHF reaches its minimum precisely at this point, $h(0) = (1 - \theta^0)$, matching the free adjustment probability. Given the realization of the shocks affecting $p_t^o(f)$, firms in the right (left) tail operate with a suboptimally low (high) markup and are thus more likely to increase (decrease) their price relative to the last adjusted price.

We derive an expression relating the frequency of price adjustment—the measurable counterpart of the GHF—to a second-order (even) polynomial in the price gaps. Formally, we partition the price gap distribution into a finite number of quantiles, with the lowest quantiles containing firms with the most negative gaps. We refer to these quantiles as “bins” and denote them by $b \in \mathcal{B}$. Within each bin, we compute the average price gap, $x_b \equiv \int_{f \in b} x_{t-1}(f) df$, and the dispersion of gaps within the bin, $\sigma_b^2 \equiv \int_{f \in b} (x_{t-1}(f))^2 df - x_b^2$. We work under the assumption bins are sufficiently narrow so that the variance within a

bin is smaller than the squared mean ($\sigma_b^2 \leq x_b^2$ for all $b \in \mathcal{B}$). Appendix A.6 verifies that this assumption holds under our bin definition. The next proposition derives the average frequency of price adjustment for a bin and shows how to use it to identify the frequency of free price changes using microdata.

Proposition 1. *The average frequency of price adjustment in bin b is given by:*

$$h_b \equiv \int_{f \in b} h(x_{t-1}(f)) df = (1 - \theta^o) + \phi(x_b^2 + \sigma_b^2) + o(x_b^2). \quad (10)$$

Restricting the estimation sample to bins in a sufficiently small neighborhood around $x_b = 0$, the estimator \hat{a}_0 of the following cross-sectional regression model recovers the probability of free price adjustment $(1 - \theta^o)$:

$$h_b = a_0 + a_1 \cdot x_b^2 + u_b, \quad (11)$$

where $u_b \equiv \phi\sigma_b^2 + o(x_b^2)$ denotes the error term.

Proof. See Appendix A.4. □

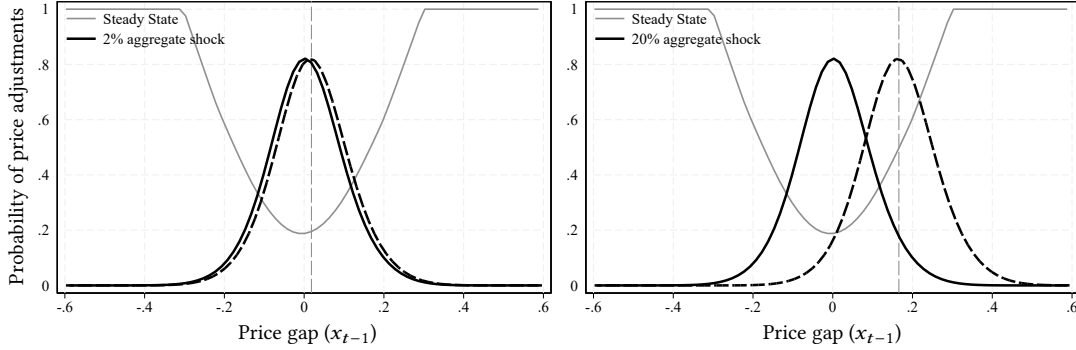
Conditional on the GHF being well approximated by a U-shaped function of price gaps, Proposition 1 offers a robust method for estimating θ^o using microdata on the average frequency of adjustment and average price gaps. In Section 7.1, we will rely on this identification result for model calibration.

3.2 The impact of large aggregate shocks

Aggregate cost shocks—i.e., shocks that do not average out across firms—affect the reset prices of all firms in the economy. When such shocks are large, they shift the entire distribution of price gaps, pushing a substantial share of firms into regions where the generalized hazard function is steep. This displacement raises the frequency of price adjustment and attenuates monetary non-neutrality.

Figure 3 illustrates this mechanism. In the spirit of the exercise in Cavallo et al. (2024), we start from an economy in its stationary equilibrium and shock it with an unexpected cost shock of size $g_t > 0$. The left panel shows the effect of a small shock; the right panel displays the response to a large shock. In both panels, the solid lines depict the stationary generalized hazard function (GHF), while the dashed lines represent the distribution of price gaps after the shock.

Figure 3: Large versus small aggregate cost shocks



Notes. This figure reports the price gap distribution in steady state (black solid line) and after a small and a large aggregate cost shock (black dashed lines).

A small aggregate shock induces only a modest shift in the price gap distribution, resulting in little or no change in the average frequency of price adjustment. In contrast, a large shock pushes a significant number of firms away from their target prices, increasing the average gap in the economy. This displacement leads to a substantial rise in adjustment frequency: more firms raise prices, while fewer reduce them. Under these conditions, the quadratic term in Equation (8) becomes quantitatively relevant, driving aggregate inflation beyond what would be predicted by the change in the average gap alone.

3.3 Price adjustment along the intensive margin

Under our assumptions, the dynamic reset price is approximately equal to the static target, $p_t^*(f) \approx p_t^0(f)$ and $x_t^* = 0$. It follows that, for firms that choose to adjust their prices, the optimal price change is approximately equal to their current price gap:

$$\Delta p_{t-1}(f) \equiv p_t^*(f) - p_{t-1}(f) \approx x_{t-1}(f) \quad \text{if } \mathbb{I}_t(f) = 1. \quad (12)$$

Equation (12) provides a testable implication for the mapping from price gaps to price changes along the intensive margin.

Two observations follow. First, in our setting, the approximation is exact in the absence of strategic complementarities in price setting. Under our assumptions, the combined shock—comprising both aggregate and idiosyncratic components—that drives firms' pricing decisions follows a random walk. In turn, the expected present value of

future costs coincides with the current realization. When strategic complementarities influence firm pricing, the optimal dynamic price is more volatile than the static one. This is because it reflects variation in expected future inflation, which may deviate from a random walk. However, with small trend inflation, the additional volatility is negligible, and the approximation remains accurate.⁹

Second, regardless of the process for marginal cost, Equation (12) becomes more accurate after large shocks when firms adjust their prices in a state-dependent manner. As discussed by Dotsey and King (2005), when the probability of a price adjustment in the near future is high, profit flows beyond that horizon have a low weight on today's pricing decisions. Consequently, during periods of large aggregate shocks—when price adjustments become more likely—the wedge between the static and dynamic targets tends to shrink.

3.4 The mapping from price gaps to price changes in the cross-section of firms

We now derive a proposition that combines the effects of price adjustments along both the extensive and intensive margins to characterize the nonlinear passthrough as a function of the shock magnitude.

We again partition the distribution of price gaps into equal-frequency bins (quantiles). Denote by $\gamma_b \equiv \int_{f \in b} ((x(f) - x_b)/\sigma_b)^3 df$ the skewness of price gaps within a bin b and define bins sufficiently small so that $|\gamma_b| \leq 1$ for all $b \in \mathcal{B}$.¹⁰

Proposition 2. *The inflation rate within a bin is given by:*

$$\begin{aligned} \pi_b &\equiv \int_{f \in b} (p_t(f) - p_{t-1}(f)) df \approx \int_{f \in b} (h_t(f) \cdot x_{t-1}(f)) df \\ &= \phi_b^0 \cdot x_b + \phi \cdot x_b^3 + \omega_b. \end{aligned} \tag{13}$$

where $\phi_b^0 \equiv 1 - \theta^o + 3\phi\sigma_b^2$ is a bin-specific coefficient and $\omega_b \equiv \gamma_b\sigma_b^3 + o(x_b^3)$ is small when the bins are sufficiently narrowly defined.

Proof. See Appendix A.5. □

⁹See Alvarez et al. (2023) for a treatment of menu-cost models with strategic complementarities in continuous time.

¹⁰We show that this condition is met given our definition of bins in Appendix A.6.

Proposition 2 states that the inflation rate within a bin (i.e., the average within-bin price change) can be approximated by a third-order (odd) polynomial in the average price gap of the bin. The intuition is as follows. Inflation reflects the average of individual firms' price adjustments, which arise from the interaction between the extensive margin (the frequency of adjustment) and the intensive margin (the size of adjustment, conditional on adjusting). As discussed above, the extensive margin can be approximated by a second-order polynomial in the price gap, while the intensive margin is approximately linear. Their interaction yields a cubic approximation of the mapping from price gaps to average price changes.

It is straightforward to derive the analog of Equation (13) for a time-dependent Calvo model. Under the assumption of a constant exogenous hazard rate $h^c := (1 - \theta^c)$, we obtain:¹¹

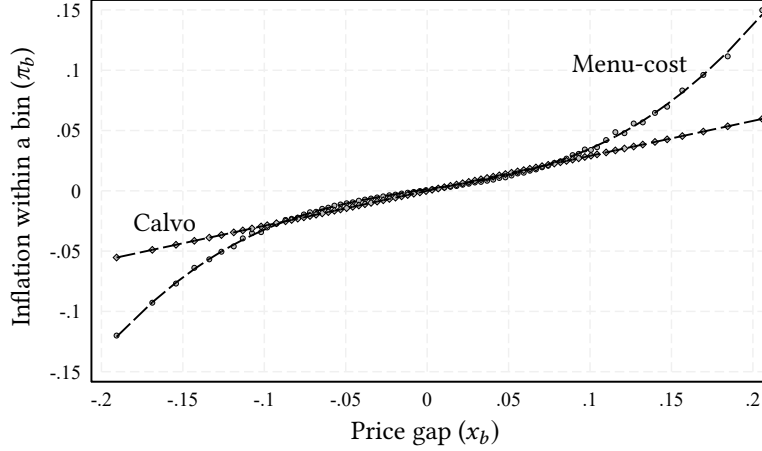
$$\pi_b = (1 - \theta^c) \cdot x_b. \quad (14)$$

The binned scatterplot in Figure 4 visually represents the mapping from price gaps to price changes in the menu-cost model (gray circles) and the Calvo model (gray diamonds). The dashed lines show fitted values from regressions of bin-level inflation on either a third-order polynomial in the average gap (Equation 13) or a first-order polynomial (Equation 14). The graph shows that when price gaps are close to zero, the third-order term becomes negligible, and inflation within a bin is approximately proportional to the average price gap. As a result, firms operating near their optimal prices exhibit near-linear pricing dynamics in both state- and time-dependent models. This result explains the near-equivalence of the two pricing models when shocks are small (Gertler and Leahy 2008; Alvarez et al. 2017; Auclert et al. 2024).

The mapping between price gaps and average price changes becomes nonlinear at the tails of the price gap distribution. Firms in these regions experience large shocks that move them substantially away from their optimal prices. As a result, the frequency of price adjustment increases more than proportionally with the size of the gap (Proposition 1). Consequently, the data-generating process for inflation can be approximated by the cubic expression in Equation (13), which captures the nonlinearities inherent in state-dependent pricing policies when shocks are large.

¹¹In a Calvo model, $\mathbb{E}[p_t(f) \mid \mathcal{I}_t(f)] = \mathbb{E}[p_t(f) \mid p_t^*(f), p_{t-1}(f)] = (1 - \theta^c)p_t^*(f) + \theta^c p_{t-1}(f)$, where $\mathcal{I}_t(f)$ denotes the information set of a firm entering period t . Using the approximation $p_t^*(f) \approx p_t^o(f)$ and rearranging, we obtain the equation in the text.

Figure 4: Nonlinear price dynamics



Notes. In this figure, we partition the distribution of price gaps into quantiles (b) and plot the average price gap of each bin, x_b , against the average logarithmic price change for observations in the same bin, π_b . The gray dots represent simulations of our menu-cost model, while the gray diamonds correspond to simulations from a Calvo model calibrated to the same average frequency of price adjustment. The dashed lines depict: (i) the fitted values of a regression of bin-level inflation on a polynomial in the first and third orders of the average gap, as specified by Equation (13) for the menu-cost model; and (ii) the fitted values from a regression of bin-level inflation on a first-order polynomial in the average gap, as specified by Equation (14) for the Calvo model.

4 Data and measurement

We construct a micro-level dataset covering the Belgian manufacturing sector from 1999 to 2023. Compiled from administrative sources, the dataset includes information on firms' pricing and production decisions at the business cycle (quarterly) frequency, including detailed data on variable costs such as labor and intermediate inputs. The dataset extends and enriches that used in our prior work (Gagliardone et al. Forthcoming) along two key dimensions.¹² First, the data in Gagliardone et al. (Forthcoming) cover a period characterized by low and stable inflation (1999:Q1 to 2021:Q1). Here we extend the time series to include the recent inflation surge and its subsequent decline (2021:Q2 to 2023:Q4). Second, we incorporate new microdata that allow for a precise measurement of price adjustment frequency.

¹²We refer to Gagliardone et al. (Forthcoming) for details about the data sources and variable definitions.

4.1 Measurement of prices, costs, and price gaps

The unit of observation in our analysis is a firm-industry pair. Our final dataset tracks 5,348 domestic firm-industry pairs, denoted by a subscript f , across 169 narrowly defined manufacturing industries (4-digit NACE rev.2 product codes), denoted by lower-script i .

Price indices. For each domestic firm, we use PRODCOM data on product-level domestic unit values (sales over quantity sold) to construct a firm-industry price index that aggregates domestic price changes across the products sold by firm f in industry i :¹³

$$\frac{P_{ft}}{P_{ft-1}} = \prod_{p \in \mathcal{P}_{ft}} \left(\frac{P_{pt}}{P_{pt-1}} \right)^{\bar{s}_{pt}}, \quad (15)$$

where \mathcal{P}_{ft} represents the set of 8-digit products manufactured by the firm, P_{pt} is the unit value of product p in \mathcal{P}_{ft} , and \bar{s}_{pt} is a Törnqvist weight given by the average within-firm sales share of the product between t and $t-1$, $\bar{s}_{pt} \equiv \frac{s_{pt} + s_{pt-1}}{2}$.

Using PRODCOM and customs declarations data, we construct firm f competitors' price index by aggregating the domestic price changes of products sold by domestic and international competitors selling in the same industry as f (\mathcal{F}_i):

$$\frac{P_{it}^{-f}}{P_{it-1}^{-f}} = \prod_{k \in \mathcal{F}_i \setminus f} \left(\frac{P_{kt}}{P_{kt-1}} \right)^{\bar{s}_{kt}^{-f}}, \quad (16)$$

where $\bar{s}_{kt}^{-f} \equiv \frac{1}{2} \left(\frac{s_{kt}}{1-s_{ft}} + \frac{s_{kt-1}}{1-s_{ft-1}} \right)$ represents the Törnqvist weight assigned to competitor k given by the average residual revenue share of competitor k in the industry (excluding firm f 's revenues).

Finally, we recover the time series of firms' prices (in levels) by concatenating the price indices in Equation (15), $P_{ft} = P_{f0} \prod_{\tau=t_f^0+1}^t (P_{f\tau}/P_{f\tau-1})$, where t_f^0 denotes the first quarter when f appears in our data. We set the base period P_{f0} to one for all firms. As discussed in the following section, this normalization is one rationale for removing firm-fixed effects from our empirical measures of price gaps. The series of competitors' prices, P_{it}^{-f} , is constructed similarly, concatenating the price indices in Equation (16).

Let the log-change in firm's price be defined as $\Delta p_{ft} \equiv \ln(P_{ft}/P_{ft-1})$. We apply

¹³PRODCOM's sampling scheme is designed to survey all Belgian manufacturing firms with more than 10 employees with the goal of accounting for at least 90% of output in each NACE 4-digit industry. We recover domestic values and quantities sold by merging the product-level information from PRODCOM with firms' product-level export quantities and sales from the Belgian customs declarations.

the standard data-cleaning and harmonization procedures to address measurement error and unobserved cross-sectional heterogeneity, which can bias the distributional moments of price changes.¹⁴ We recode all price changes smaller than 1 percent in absolute value as zero and exclude observations in the top and bottom 1.5 percent of the price change distribution. This helps address mismeasurement due to the use of unit values (Eichenbaum et al. 2011). Second, we demean price changes by removing firm-industry intercepts to account for trend inflation (approximately 0.6 quarterly before the surge) and address issues related to unobserved heterogeneity, which can inflate the measured moments (standard deviation and kurtosis) of the price change distribution (Klenow and Kryvtsov 2008; Alvarez et al. 2016). Finally, to account for seasonality in costs, we remove industry-specific seasonal intercepts.

Frequency of price adjustment. We use micro-level records from the National Bank of Belgium Business Survey (NBB-BS) to accurately measure the frequency of price adjustment. This survey regularly interviews a representative sample of firms across manufacturing industries about their pricing decisions. Similar to the official Producer Price Index (PPI) data collection, the NBB-BS asks firms whether they increased, decreased, or maintained the price of a specific product in their portfolio. Using this information, we define a binary variable that equals one if a firm reports adjusting prices at least once within a given quarter relative to the previous month. Averaging this variable across firms and industries in each quarter, we compute the manufacturing sector’s average frequency of price adjustment (h_t).

Information on firms’ price adjustments from the NBB-BS also helps filter out spurious price changes in the microdata. As discussed, our price measure is derived from product-level unit values, which tend to overstate the frequency of small price changes due to minor measurement errors, as shown by Eichenbaum et al. (2014) and Cavallo and Rigobon (2016). To address this issue, we combine firm-level price changes with information on price adjustment frequency from the NBB-BS to define firm-specific thresholds, κ^+ and κ^- , such that small price variations within these bounds are treated as no price update:

$$\mathbb{I}_{ft}^+ = 0 \iff \Delta p_{ft} < \kappa^+ \cdot \text{Var}_f(\Delta p_{ft}) \quad \text{if } \Delta p_{ft} > 0$$

¹⁴See, Klenow and Kryvtsov (2008) and Alvarez et al. (2016) for discussion of these issues and proposed solutions.

$$\mathbb{I}_{f_t}^- = 0 \iff \Delta p_{f_t} > -\kappa^- \cdot \text{Var}_f(\Delta p_{f_t}) \quad \text{if } \Delta p_{f_t} < 0$$

To account for different degrees of upward and downward nominal rigidity in the data, we set the thresholds $\kappa^+ = 0.75$ and $\kappa^- = 0.87$ to separately match the average frequency of upward and downward price changes measured using the NBB-BS microdata: $\frac{\sum_t \sum_f \mathbb{I}_{f_t}^+}{\sum_t (\sum_f \mathbb{I}_{f_t}^+ + \sum_f 1 - \mathbb{I}_{f_t}^+)} = h^+$ and $\frac{\sum_t \sum_f \mathbb{I}_{f_t}^-}{\sum_t (\sum_f \mathbb{I}_{f_t}^- + \sum_f 1 - \mathbb{I}_{f_t}^-)} = h^-$, where $h^+ + h^- = h$.¹⁵

Marginal cost indices. To derive a firm-level marginal cost index, we assume a cost structure in which the nominal marginal cost of a firm is proportional to its average variable costs: $MC_{f_t}^n = (1 + v_f)AVC_{f_t}$. Relaxing the constant-return-to-scale assumption made in the theoretical framework, the coefficient v_f captures the curvature of the short-run cost function, and it is inversely related to the firm's short-run returns to scale in production ($v_f \equiv 1/RS_f - 1$). Using the definition of average variable costs (total variable costs over output, $TVC_{f_t}^n/Y_{f_t}$) and applying a logarithmic transformation, we have that firm-level log-nominal marginal cost is given by:

$$mc_{f_t}^n = (tvc_{f_t}^n - y_{f_t}) + \ln(1 + v_f). \quad (17)$$

We measure total variable costs as the sum of intermediate costs (materials and services purchased) and labor costs (wage bill), sourced from firms' quarterly VAT and social security declarations. To construct a firm-level quantity index, we divide domestic revenues by the firm-specific domestic price index.¹⁶ Short-run returns to scale enter our measure of log-marginal costs as an additive firm-specific constant. Mirroring the cleaning procedure for price changes, we remove this variation by demeaning at the firm-industry level. We also remove industry-specific seasonal intercepts to account for seasonality in costs.

¹⁵See Karadi et al. (2024) and Luo and Villar (2021) for evidence of asymmetric upward and downward rigidity.

¹⁶Specifically, we compute $Y_{f_t} = (PY)_{f_t}/\bar{P}_{f_t}$, where \bar{P}_{f_t} denotes the firm-quarter domestic price index. For single-industry firms, \bar{P}_{f_t} coincides with the firm-industry price index P_{f_t} . For multi-industry firms, we construct \bar{P}_{f_t} as an average of the different firm-industry price indices using as weights the firm-specific revenue shares of each industry. As discussed in Gagliardone et al. (Forthcoming), the vast majority of firms in our sample operate in only one industry, and the main industry accounts for the lion's share of sales of multi-industry firms.

Price gaps. The availability of high-frequency firm-level price and cost data allows us to construct an empirical counterpart of the (ex-ante) price gaps defined in our model:

$$x_{ft-1} = p_{ft}^o - p_{ft-1}.$$

As discussed in Section 2, when p_{ft}^o and p_{ft}^* are sufficiently close, x_{ft-1} captures inefficiencies driven by nominal rigidities and influences firms' pricing policies. Thus, as in the theory, a positive price gap implies that a firm is pricing with a market below its profit-maximizing level and, absent nominal rigidities, would adjust its price upwards.

Guided by our theoretical framework, we construct a measurable proxy for firms' target prices as a convex combination of the firm's own marginal cost and its competitors' price index, $p_{ft}^o = (1 - \Omega)mc_{ft}^n + \Omega p_t^{-f}$, calibrating Ω to 0.5 to match the micro estimate in Gagliardone et al. (Forthcoming). This empirical measure of firms' target prices differs from the theoretical one (Equation (3)) in three dimensions. First, it does not capture variation in firms' steady-state markups. Second, it does not directly account for potential curvature in firms' short-run cost functions. The harmonization of the data discussed below helps address these two limitations. Third, we cannot directly measure the realized idiosyncratic taste shocks (ϕ_{ft}). While such shocks are likely transitory and average out in the cross-section, they are a source of measurement error that possibly weakens the connection between our empirical measures of price gaps and price changes at the firm level.¹⁷

4.2 The empirical distribution of price changes and price gaps

Table 1 presents summary statistics of the distribution of firm-level log price changes and price gaps. The first four columns report moments describing the distribution of price changes. Panel a focuses on the pre-pandemic period (1999–2019), characterized by low and stable inflation and—apart from the global financial crisis—the absence of large aggregate shocks. Drawing an analogy with our model, we view this period as representing the economy in its steady-state distribution. During this period, the (harmonized) average price change is close to zero, which implies that inflation is generally aligned with the long-term industry trend. In addition, the standard deviation of price changes is 0.11 and the average frequency of price adjustment is $h = 0.29$. The

¹⁷See the evidence in Gagliardone et al. (Forthcoming).

Table 1: Summary statistics of price changes and price gaps

Price changes ($p_{ft} - p_{ft-1}$)				Price gaps (x_{ft-1})		
<i>Panel a: Time period 2000-2019</i>						
Mean	Std.	Freq. Adj.	Kurt.	Mean	Std.	Kurt.
0.00	0.12	0.29	3.26	-0.00	0.13	2.86
<i>Panel b: Time period 2020-2023</i>						
Mean	Std.	Freq. Adj.	Kurt.	Mean	Std.	Kurt.
0.02	0.11	0.44	3.56	0.01	0.14	2.83
Number of observations:			118,308			
Number of firm-industry pairs:			4,974			
Number of firms:			4,488			

Notes. This table reports summary statistics for the distributions of price changes ($p_{ft-1} - p_{ft}$) and price gaps (x_{ft-1}) before (Panel a) and after the inflation surge (Panel b).

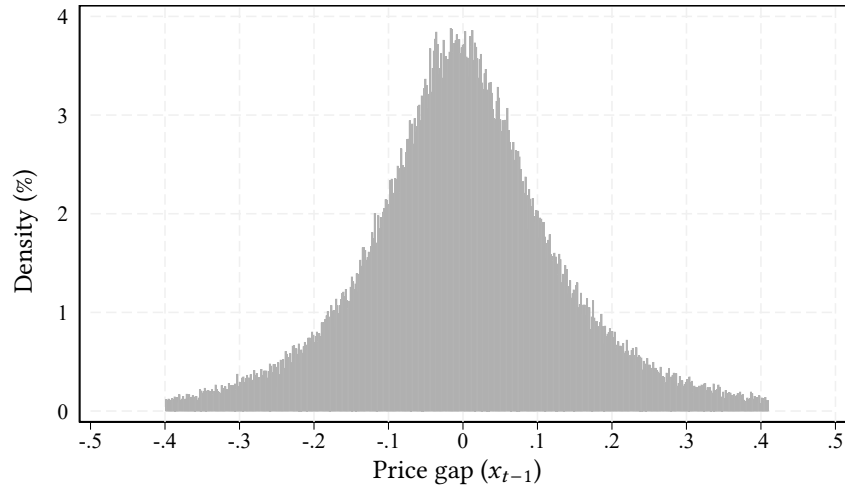
latter implies that, in a low inflation environment, firms adjust their prices every 3 to 4 quarters, on average (Gagliardone et al. Forthcoming).

Panel b reports the same statistics for the pandemic and post-pandemic period (2020–2023), which was marked by high inflationary pressures followed by a gradual tapering. During this period, the PPI quarterly inflation rate was, on average, 1 percentage point above the long-run trend. At the same time, the frequency of price changes increased by 10 percentage points, on average.

The fourth column reports the kurtosis of price changes, calculated following the approach in Klenow and Kryvtsov (2008). The measured kurtosis is 3.26—consistent with values commonly found in the literature (typically ranging between 3 and 5)—indicating that the distribution of price changes is more peaked (a higher frequency of small adjustments) and exhibits fatter tails (a greater frequency of large adjustments) than a normal distribution (kurtosis = 3). These features are consistent with empirical patterns associated with state-dependent price-setting behavior and become even more pronounced during the inflation surge, with kurtosis rising to 3.56 over the 2000–2023 period.

The last three columns of Table 1 report summary statistics for the empirical

Figure 5: Empirical distribution of price gaps



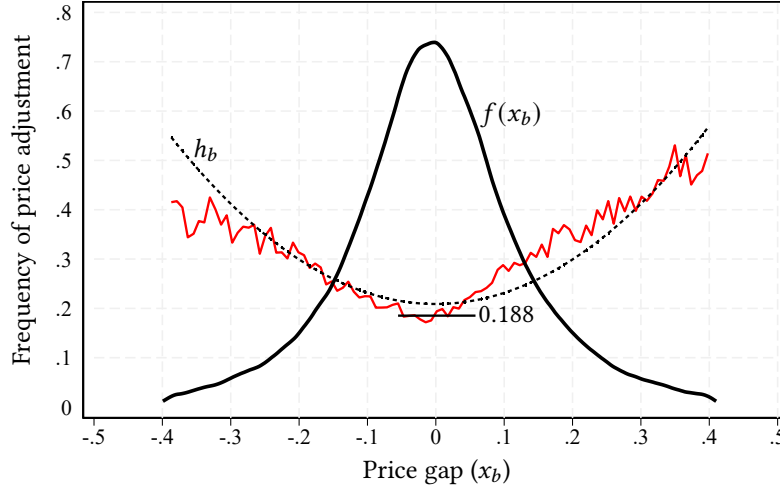
Notes. This figure presents the empirical probability density function of price gaps, $f(x_{f,t-1})$, for the pre-pandemic period (2000–2019).

distribution of price gaps. This distribution, which is typically unobserved, is of great interest, as it reflects the history of shocks faced by firms and the inefficiencies arising from nominal rigidities. The histogram in Figure 5 plots the probability density function of the price gaps, $f(x_{t-1})$, for the pre-pandemic period. Consistent with our theory, the empirical distribution of price gaps is unimodal, bell-shaped, and symmetric around the mean. Table 1 reports that the average price gap rose by approximately 1 percentage point in the post-pandemic period relative to its long-term trend. In line with model predictions, this increase corresponds closely to the average price change observed over the same period.

5 Micro evidence of state dependent pricing

Guided by the theoretical framework presented in Section 2, we design empirical tests of key model predictions that nonparametrically link micro-level pricing behavior to the underlying distribution of price gaps. These exercises provide direct evidence of the state-dependent nature of firms' pricing decisions—especially in the presence of large aggregate cost shocks—and yield novel identification results that inform the calibration of structural parameters.

Figure 6: Empirical GHF and distribution of price gaps



Notes. This figure plots the empirical probability density function of price gaps, $f(x_b)$ (black line), alongside the empirical GHF, h_b (red line). The black dotted line shows the fitted values from a cross-sectional regression of the adjustment frequency in each bin (b) on a constant and the squared average price gap in the same bin, as specified by Equation (8). Each bin is weighted by its number of observations.

5.1 The empirical generalized hazard function

We begin by analyzing the mapping between price gaps and the frequency of price adjustment—the *extensive margin*. As discussed above, in time-dependent models, the two variables are independent, yielding a flat generalized hazard function (GHF). By contrast, state-dependent models predict that the frequency of price adjustment increases monotonically with the absolute value of the price gap. In our framework, the GHF can be approximated by a convex function, specifically a second-order polynomial in the price gap—as formalized in Lemma 1. Proposition 1 provides the sample analog of this relationship, linking the average frequency of price adjustment at different points in the gap distribution to the average squared gaps.

We take these predictions to the microdata by analyzing the relationship between the frequency of price adjustment and price gaps. In Figure 6, the black line depicts the kernel estimate of the empirical probability density function of price gaps. The red line plots the empirical GHF—defined as the fraction of firms adjusting prices within each quantile (bin) of the price gap distribution. The black dotted line shows the fitted values from a cross-sectional regression of bin-level adjustment frequencies on the square of the average price gap, $\hat{h}_b = \hat{a}_0 + \hat{a}_1 \cdot x_b^2$.

The data reveal a strong, convex relationship between the size of price gaps and the frequency of price adjustment. In striking resemblance to the theoretical GHF implied by state-dependent pricing models, wider gaps (i.e., greater deviations from $x_{f,t-1} = 0$) are associated with a higher likelihood of adjustment. Moreover, consistent with our model’s prediction, a simple quadratic polynomial in price gaps fits the frequency data remarkably well. We also note that the empirical GHF exhibits a steeper slope for positive gaps, suggesting asymmetry in nominal rigidity: firms are more likely to adjust prices when they are too low—that is, when the realized markup is below the desired level—than when they are too high.

We then leverage Proposition 1 to estimate the probability of free price adjustment directly from the empirical GHF. Specifically, fitting the quadratic polynomial over an interval centered around the vertex of the parabola ($x_b \in (-0.04, 0.04)$) yields an estimate of $\hat{a}_0 = 0.188$, implying a Calvo-type parameter of $\hat{\theta}^o = 0.812$. We use this estimate in our model calibration, as detailed in Section 7.1.

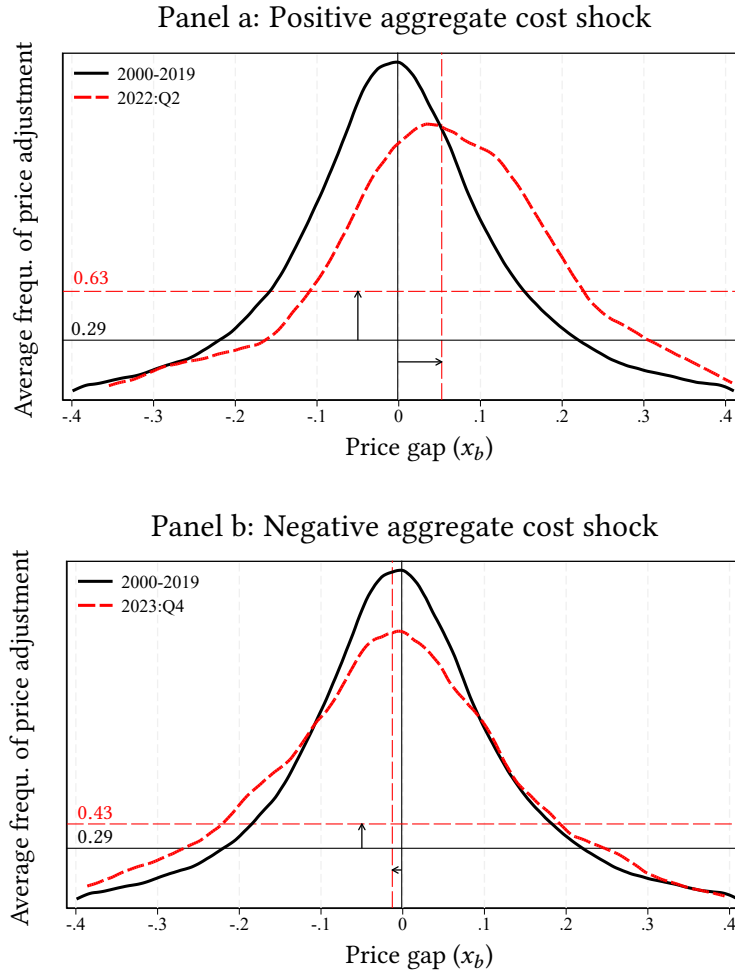
5.2 The impact of large aggregate shocks

In Section 2, we discussed how small idiosyncratic shocks generate dispersion in the price gap distribution, while large aggregate shocks shift the entire distribution, significantly increasing the fraction of firms with incentives to adjust prices (see Figure 3). The pronounced increase and subsequent normalization of production costs in the post-pandemic period offer a compelling empirical setting to test this prediction.

In Figure 7, the solid black line shows the distribution of price gaps in the pre-pandemic period. In panel (a), we overlay the distribution in 2022:Q2 (red dashed line), a quarter in which firms’ marginal costs *increased* by an average of 6.2 percent relative to the previous quarter. As predicted by the model, a shock of this magnitude shifts the entire distribution to the right, displacing many firms from their optimal price levels. The resulting compression in markups raises the cost of inaction, pushing a greater share of firms into regions where the GHF is steep. As a consequence, the average frequency of price adjustment nearly doubles within a single quarter relative to its long-run average.

Panel (b) repeats the analysis for 2023:Q3, when firms’ marginal costs *declined* by an average of 3.8 percent, driven by falling energy prices and easing supply chain pressures. Consistent with model predictions, the distribution of price gaps shifts to the left. The

Figure 7: Impact of aggregate cost shocks on the price gap distribution and average frequency of price adjustment



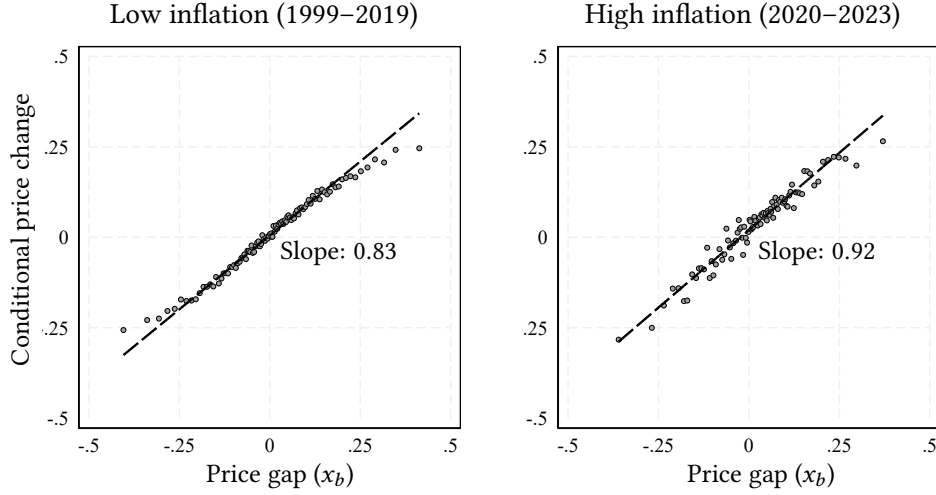
Notes. This figure shows the empirical probability density function of price gaps during the pre-pandemic period (1999–2019, black solid line) and two post-pandemic snapshots: 2022:Q2 and 2023:Q4 (red dashed lines). The solid and dashed vertical lines mark the average price gap of the different distributions. The solid and dashed horizontal lines report the average frequency of price adjustment in the pre-pandemic period (black solid line) and in 2022:Q2 and 2023:Q4 (red dashed lines).

adjustment frequency responds to this shift, as more firms reduce than raise their prices.

5.3 Price gaps and price changes conditional on adjustment

We now study the mapping from price gaps to price changes, focusing on firms that adjust their prices—the *intensive margin*. Under our assumptions, p_{ft}^o provides a close approximation of p_{ft}^* , so that $\Delta p_{ft-1} \approx x_{ft-1}$ if $\Delta p_{ft-1} \neq 0$, as formalized in Equation (12).

Figure 8: Price changes and price gaps, conditional on adjusting



Notes. This figure presents a binned scatterplot of log price changes for adjusters (i.e., firms with $p_{ft} \neq p_{ft-1}$) against their price gaps. Each dot marks the average price gap of a given percentile of the price gap distribution (x-axis) and the corresponding average percentage change in prices of firms in the same percentile (y-axis). The black dashed line depicts a linear fit of price changes on price gaps across the percentiles of the distribution of price gaps. The regression sample excludes the bottom and top 5 percentiles of the price gap distribution, to minimize the impact of outliers.

Accordingly, our model predicts that the elasticity of price changes with respect to price gaps should be approximately one. We test this prediction in Figure 8.

The figure presents binned scatterplots of average price gaps (x-axis) on average price change (y-axis) gaps on average changes for each percentile of the price-gap distribution, focusing on the subset of firms that adjust prices. The left panel focuses on the pre-pandemic period, and the right panel covers the pandemic and post-pandemic period. In both panels, the black dashed line shows a linear fit of price changes on price gaps across percentiles. The data reveal that the gradient between price changes and price gaps is not only positive but also close to one—ranging from 0.8 to 0.9 depending on the subsample—as predicted by the theory. This finding suggests that, on average, the assumptions underlying our theoretical framework—particularly that firm-level nominal marginal costs follow random-walk dynamics—are empirically plausible.

That said, theory predicts a passthrough of exactly one. Three factors may explain the observed deviation from this benchmark. First, classical measurement error in price gaps likely attenuates the estimated elasticity. Second, the approximation of $p_t^*(f)$ with $p_t^0(f)$ is an additional source of measurement error. Notably, the elasticity is closer to one

in the high-inflation period (panel b), suggesting that the approximation performs better in such environments. As discussed in Section 3, this finding is consistent with the model’s prediction: large aggregate shocks trigger a state-dependent response along the extensive margin, leading firms to discount future conditions more heavily. This behavior makes the static approximation more accurate even if marginal cost deviates from the random walk dynamics. Third, the model assumes that firms have complete information. In practice, firms may underreact to fundamentals due to inattention or incomplete information, as shown in Morales-Jiménez and Stevens (2024) and Gagliardone and Tielens (2024). Importantly, the frictions in these models are themselves state-dependent, implying that passthrough becomes stronger when shocks are large—consistent with what we observe in the data.

5.4 The empirical mapping from price gaps to price changes

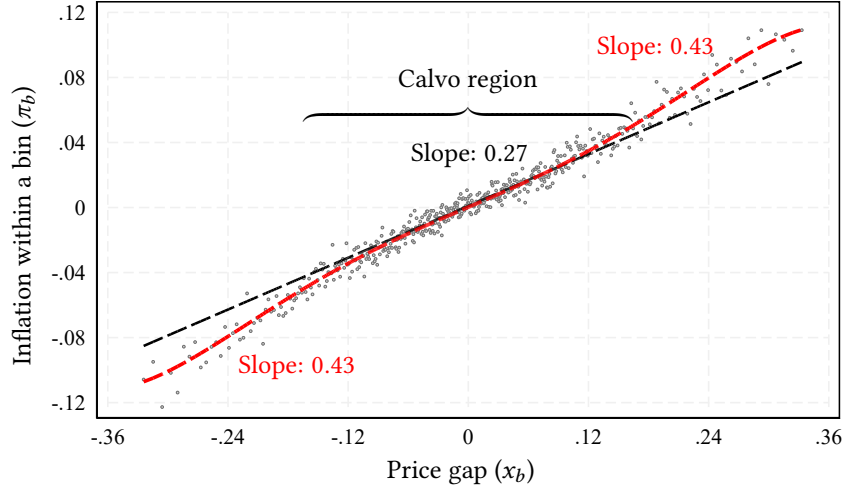
In our final analysis, we examine the joint effect of the extensive and intensive margins of price adjustment and characterize the nonlinear passthrough as a function of shocks’ magnitudes. According to Proposition 2, the mapping between price gaps and inflation (i.e., expected price changes) can be approximated by a cubic polynomial function of price gaps. This expression captures both the linear passthrough observed in response to small shocks as well as the nonlinearities introduced by state dependence when shocks are large.

The data provide strong support for the predictions summarized by Proposition 2. Figure 9 takes this prediction to the data. As before, we sort observations into quantiles (bins) spanning the price gap distribution. We then plot the average price change within the same bin (π_b , y-axis) against the corresponding average price gap (x_b , x-axis). The red dashed line in Figure 9 represents the fitted values from a cross-sectional regression estimated over the full support of the price gap distribution:

$$\pi_b = b_1 \cdot x_b + b_2 \cdot x_b^3 + \eta_b.$$

The relationship between price gaps and average price changes is S-shaped, indicating that the cross-section of firm-quarter observations can be partitioned into two distinct regions. The first comprises observations in the central part of the price gap distribution (25th to 75th percentiles), where deviations from optimal prices are relatively small. We refer to this range as the “*Calvo region*.” In this range, the mapping

Figure 9: Nonlinear price dynamics



Notes. This figure presents a scatterplot of the average price gap in each bin of the price gap distribution, x_b , against the corresponding average inflation (log price change), π_b . Bins are constructed using 500 quantiles. The black dashed line represents a linear fit of price changes on price gaps, $\hat{\pi}_b = \hat{a}_1 \cdot x_b$, estimated on the subsample of bins covering firms between the 25th and 75th percentiles of the price gap distribution, with the estimated slope (\hat{a}_1) reported in black. The red dashed line represents the fit of a third-order (odd) polynomial in price gaps, $\hat{\pi}_b = \hat{b}_1 \cdot x_b + \hat{b}_2 \cdot x_b^3$, estimated using bins across the entire price gap distribution. The average slope of the third-order polynomial fit in the tails of the distribution (below the 25th and above the 75th percentiles) is reported in red.

between price gaps and expected price changes is approximately linear, consistent with the predictions of the Calvo model (Equation 14) and characteristic of “normal times,” when shocks are modest and inflation remains low and stable. This result corroborates the theoretical results in Gertler and Leahy (2008), Alvarez et al. (2017), and Auclert et al. (2024), which show that with small shocks the price dynamics in state-dependent models resemble those of time-dependent models. Notably, the estimated gradient in this region is 0.27—nearly identical to the average frequency in the pre-pandemic period.

The second region comprises observations in the tails of the price gap distribution, where large shocks displace firms substantially from their optimal prices (by 20 percent or more). As shown above, in this part of the distribution, the frequency of price adjustment increases more than proportionally with the size of the gap. Consequently, the sensitivity of price changes to price gaps rises sharply: the gradient steepens by nearly 60 percent, from 0.27 in the Calvo region to 0.43 in the tails. The cubic term in Proposition 2 captures these nonlinearities, which arise from the joint effect of adjustments along both the extensive and intensive margins in response to large shocks.

6 Aggregate cost-price dynamics

In this section, we shift focus from micro-level dynamics to aggregate cost-price dynamics. We show that state-dependent pricing at the firm level gives rise to nonlinear inflation dynamics in the aggregate, with the passthrough of cost shocks depending systematically on their magnitude.

6.1 Aggregate inflation and aggregate costs

We use our microdata to compute domestic producer price inflation and an index of nominal marginal costs for the Belgian manufacturing sector. Following the standard approach used by national statistical agencies, we calculate domestic PPI inflation as a Törnqvist price index, averaging firms' quarterly price changes weighted by smoothed sales shares:

$$\pi_t = \sum_{f \in \mathcal{F}} \bar{s}_{ft} \cdot \Delta p_{ft} \quad \bar{s}_{ft} \equiv \frac{s_{ft} + s_{ft-1}}{2}.$$

Similarly, we construct an aggregate nominal cost index, mc_t^n , by aggregating and concatenating average changes in firm-level nominal marginal costs across producers (Δmc_t^n):

$$mc_t^n = \sum_{t=1999:Q2}^{2023:Q4} \Delta mc_t^n$$

$$\Delta mc_t^n = \sum_{f \in \mathcal{F}} \bar{s}_{ft} \cdot \Delta mc_{ft}^n,$$

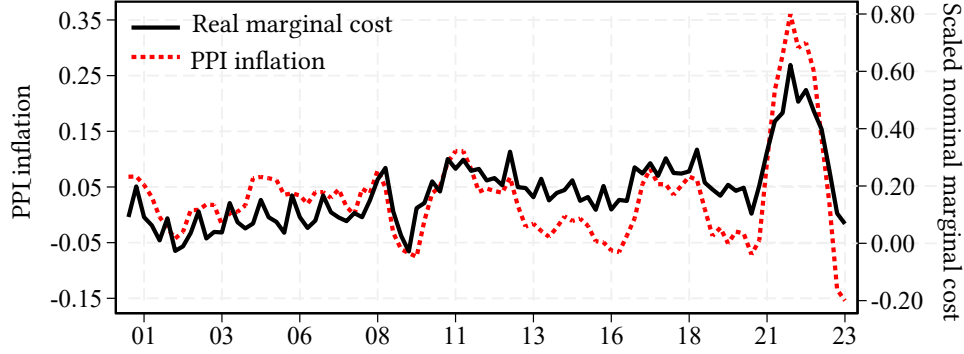
where the value of the index in the first quarter of our sample is normalized to zero.

According to our model, firms set prices based on current and anticipated movements in marginal costs. Accordingly, year-over-year inflation ($p_t - p_{t-4}$) should depend on nominal marginal cost at t , relative to the price level at $t - 4$. The logarithmic difference between these variables, $mc_t^n - p_{t-4}$ provides a measure of real marginal cost. Panel a of Figure 10 plots the evolution of manufacturing PPI inflation (red dashed line, left axis) against the time series of real marginal costs (black line, right axis) throughout our sample period. Note that the scales of the two axes differ for the variables.

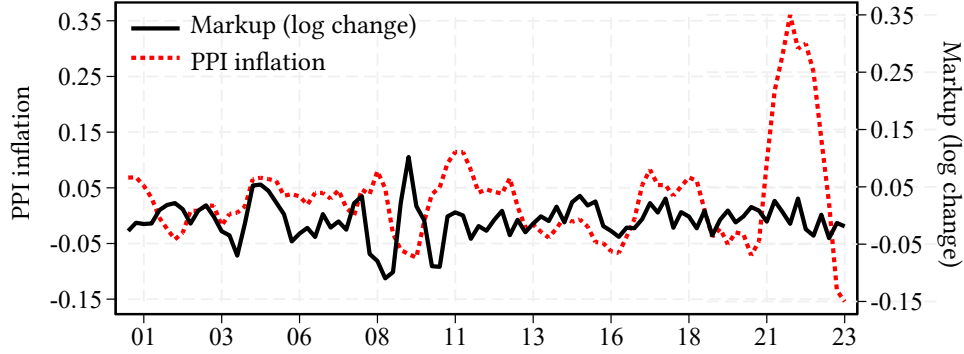
Two patterns emerge. First, consistent with the theory, inflation closely tracks fluctuations in real marginal cost throughout the sample, albeit with incomplete

Figure 10: Inflation, cost, and markup dynamics

Panel a: Aggregate inflation and real marginal cost



Panel b: Aggregate inflation and markup



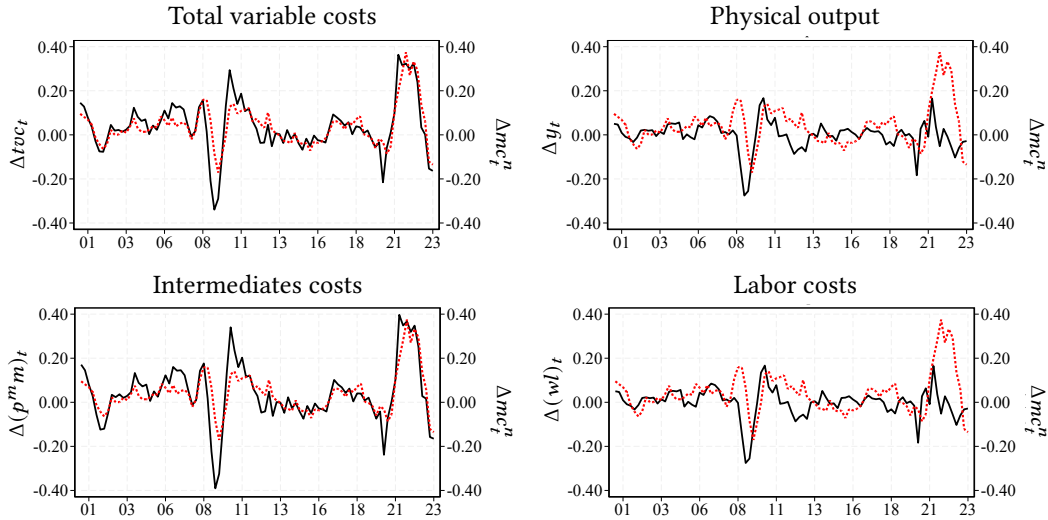
Notes. This figure shows the time series of year-over-year PPI inflation ($p_t - p_{t-4}$), plotted alongside the time series of the real marginal cost index ($mc_t^n - p_{t-4}$, Panel a) and the log change in average realized markups ($\Delta \ln(\text{Markup}_t)$, Panel b) for the Belgian manufacturing sector.

passthrough: price changes respond less than one-for-one to cost movements. Second, the sharp rise and subsequent fall in inflation during the pandemic period mirrors the large swings in real marginal costs.

To further stress the contribution of cost passthrough to movements in inflation, panel b of Figure 10 contrasts inflation with changes in average realized markups. We compute the latter using the identity $\Delta \ln(\text{Markup}_t) \equiv \pi_t - \Delta mc_t^n$. This exercise illustrates that, at least in our sample, the hypothesis that rising markups explain the recent inflation surge finds little support in the data. This finding echoes findings in Alvarez et al. (2024), who use firm-level data from a large multinational manufacturer.

Finally, to get a sense of what drove the fluctuations in nominal costs, Figure

Figure 11: Decomposition of aggregate nominal marginal cost index



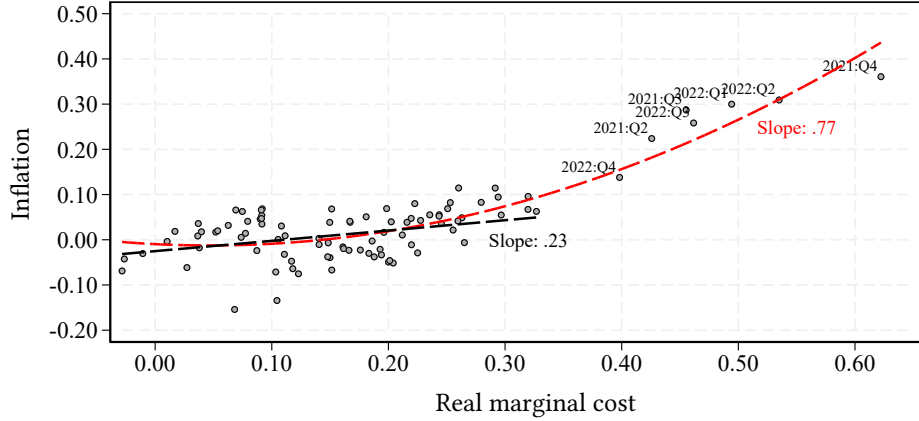
Notes. This figure decomposes the log change in our nominal aggregate marginal cost index (Δmc_t^n) into the log change in total variable costs (Δtvc_t , top left panel), real output (Δy_t , top right panel), intermediates costs ($\Delta(p^m m)_t$, bottom left panel), and labor costs ($\Delta(wl)_t$, bottom left panel).

11 presents a decomposition of our aggregate cost index into its different components (Equation (17)). The top left panel plots the growth rates of total variable costs and real output (black lines), alongside the growth rate of the nominal marginal cost index (red dashed line). The two panels make clear that throughout the sample, and in particular during the recent inflation surge, fluctuations in total variable costs are the main drivers of the time series evolution of nominal marginal cost.

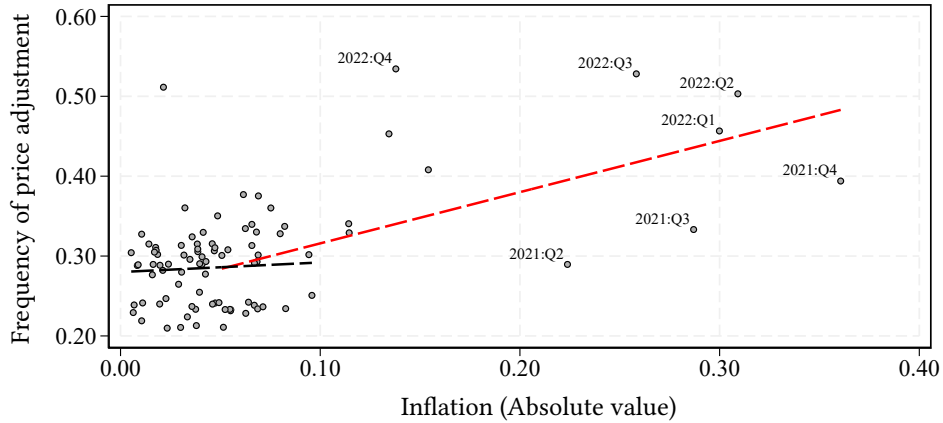
The two bottom panels of Figure 11 further decompose total variable costs into intermediate input costs (purchases of materials, services, and energy) and labor costs. As we can see, both cost components rose during the post-pandemic period. However, the increase in intermediate input costs was roughly four times larger. On average, this component alone accounts for approximately 70 percent of manufacturing firms' revenues. Moreover, over 80 percent of intermediate input costs are paid to foreign suppliers. These figures underscore that the surge in the cost of foreign-supplied intermediates—rather than labor costs—was the main driver of inflation between 2021 and 2023, at least in our sample.

Figure 12: Passthrough of costs into inflation

Panel a: Nonlinear passthrough of costs into inflation



Panel b: Frequency of price adjustment and inflation



Notes. This figures displays the intertwined the dynamics of real marginal costs, aggregate inflation, and the average frequency of price adjustment. Panel a plots year-over-year manufacturing PPI inflation against our aggregate real marginal cost index, with quarters sorted by the latter. Panel b plots the average frequency of price adjustment against inflation, with quarters sorted by the latter. The average frequency of price adjustment is a rolling average of the quarterly frequency of price adjustment over the previous four quarters. In both panels, the black dashed line represents the linear fit of the variable on the y-axis based on the values of the variables on the x-axis during periods of low inflation (below 10 percent year-over-year); the red dashed line represents a fit across both high- and low-inflation periods.

6.2 Nonlinear aggregate passthrough

Panel a of Figure 12 plots PPI inflation against the real marginal cost index, with quarters sorted by the latter. The black dashed line shows a linear fit estimated over low-inflation periods (below 10 percent year-over-year), while the red dashed line shows a quadratic

fit estimated over the full sample. The slopes of these curves provide descriptive evidence on how aggregate cost passthrough varies with the magnitude of shocks to marginal cost.

Consistent with the micro-level dynamics documented in Section 5, we find a linear relationship between aggregate inflation and nominal costs during periods of low inflation. As discussed, a linear passthrough is consistent with the predictions of both the Calvo and menu-cost models when aggregate shocks are small. The estimated reduced-form slope is 0.23, closely matching the aggregate passthrough coefficient estimated by Gagliardone et al. (Forthcoming) for a low inflation environment.

However, this linear relationship breaks down when the economy experiences large aggregate shocks. During the recent inflation surge, the passthrough coefficient more than tripled, revealing pronounced nonlinear cost-price dynamics. At the core of this nonlinearity is the endogenous nature of the frequency of price adjustment. Panel b sorts quarters by their annual inflation rates and plots aggregate inflation against the average frequency of price adjustment. As before, the black dashed line shows the fit for low-inflation periods, while the red dashed line includes high-inflation quarters as well. As in the Calvo model, the average frequency of price adjustment is essentially stable during low-inflation periods. This finding reinforces the view that time-dependent models are well suited to capturing nominal rigidities under low inflation. In contrast, inflation and the frequency of price adjustment are strongly correlated during high-inflation periods, consistent with evidence from Argentina in Alvarez et al. (2019) from Europe and the US reported by Cavallo et al. (2023) and Blanco et al. (2024a).

7 Quantitative implications

Having established the close connection between theory and data, we now calibrate the menu-cost model presented in Section 2 and conduct two types of quantitative exercises. First, we simulate cost shocks of varying magnitudes and compare the dynamics under our state-dependent specification with those under a standard time-dependent Calvo model. Second, we feed the model a sequence of aggregate marginal cost shocks extracted from the data and evaluate how well the resulting inflation series matches observed inflation.

7.1 Calibration

The calibration involves seven parameters. Four are set to standard values from the literature. We calibrate the elasticity of substitution between goods σ , to 6, implying a 20 percent markup in the symmetric steady-state equilibrium. The firm’s risk-neutral discount factor, β , is set to 0.99. As in our empirical analysis, we calibrate $\Omega = 0.5$ to properly account for the strength of strategic complementarities in the microdata (Amiti et al. 2019; Gagliardone et al. Forthcoming). To align model and data, we allow for a drift in the aggregate component of nominal marginal cost, $\mu_g = 0.005$, consistent with 1.6 percent annual trend inflation.

We develop a new approach to calibrate the parameters θ^o , σ_ϵ^2 , and $\bar{\chi}$, which govern the degree of nominal rigidity and the state dependence of price adjustment. In the absence of data on price gaps, the standard calibration strategy relies on model inversion to recover structural parameters that match moments from the observed distribution of price changes—typically, the standard deviation of price changes, the average frequency of price adjustments, and the kurtosis of price changes.¹⁸ In theory, this approach identifies the parameters of interest through the lens of a specific model. In practice, obtaining a reliable measure of the kurtosis of price adjustments is challenging due to measurement error and the inability to control for unobserved heterogeneity (Alvarez et al. 2016; Cavallo and Rigobon 2016; Berger and Vavra 2018). These issues are particularly relevant in our setting due to reliance on unit values. We therefore avoid targeting kurtosis directly and proceed as follows:

Step 1. As discussed in Section 5.1, we use the empirical GHF to calibrate the free price adjustment probability $(1 - \theta^o)$. Specifically, we match the frequency of price adjustment in a neighborhood around the vertex of the empirical GHF, near $x_{ft-1} \approx 0$. Averaging across observations near zero makes the calibration robust to small measurement errors from spurious unit value changes.¹⁹ As discussed in Section 5, this yields $(1 - \hat{\theta}^o) = 0.188$.

Step 2. With low trend inflation and i.i.d. Gaussian idiosyncratic shocks, Alvarez et al. (2016) show that the following identity links the steady-state variance of shocks, σ_ϵ^2 , to

¹⁸See, e.g., Alvarez et al. (2022) and Blanco et al. (2024a).

¹⁹See Appendix A.4, for a formal discussion on the consistency of this estimator.

Table 2: Calibration: Data vs. model

	Price change ($p_{ft} - p_{ft-1}$)				Price gap (x_{ft-1})			Share MC
	Mean	Std.	Freq. Adj.	Kurt.	Mean	Std.	Kurt.	Mean (%)
Data	0.00	0.12	0.29	3.26	-0.00	0.13	2.86	1.22
Menu cost	0.00	0.12	0.29	2.62	0.00	0.09	3.30	1.70
Calvo	0.00	0.12	0.29	5.21	0.00	0.12	5.21	

Notes. This table reports moments of the distribution of price changes and price gaps computed during the period 2000–2019 and the corresponding moments for the menu-cost model and Calvo model, in steady-state, under our baseline calibration. The last column shows the average share of menu costs as a fraction of firms’ revenues, with the data estimate sourced from Zbaracki et al. (2004)

the average frequency and variance of price changes:

$$\sigma_\epsilon^2 = h \cdot \text{Var}_{ss}(p_t(f) - p_{t-1}(f)).$$

Using this identity, we calibrate σ_ϵ^2 to 0.0036 to match the product of the average frequency and the variance of price changes reported in panel a of Table 1.

Step 3. Given σ_ϵ^2 and θ^0 , we calibrate $\bar{\chi}$ —the upper bound of the uniform distribution of menu costs—to 0.61 so that the model matches the frequency of price changes in the pre-pandemic period.

Table 2 compares empirical moments of the price change distribution (panel a) and the price gap distribution (panel b) to those generated by the menu-cost model, in steady state, under our baseline calibration. The model fits the data closely. Notably, the calibrated model implies menu costs equal to 1.7 percent of firm revenues in steady state. Although not directly targeted, the implied value is reasonable and broadly consistent with empirical estimates from Levy et al. (1997) and Zbaracki et al. (2004), which find that menu costs in the data are reasonably small. The model also reproduces a kurtosis of price changes broadly in line with the data, despite potential measurement issues discussed earlier.²⁰

²⁰To this point, Blanco et al. (2024a) shows that in a standard menu-cost model with single-product firms, calibrating to match the kurtosis of price changes may require implausibly high menu costs to generate sufficient volatility in the frequency of price adjustment. We confirm this result: targeting the observed kurtosis in our data yields sufficient variation in adjustment frequency only at the cost of implausibly high—more than double—menu costs.

Calibration of the Calvo model. In our quantitative exercises, we also consider a standard time-dependent Calvo model. As discussed in Section 2, our menu-cost model nests the Calvo model as a special case. We calibrate the Calvo model by setting the maximum menu cost, $\bar{\chi}$, to an arbitrarily large number and adjusting the free adjustment probability to match the steady-state frequency, $(1 - \theta^c = h)$. The theoretical moments derived from the calibrated Calvo model are reported in the third row of Table 2. As is well known, the Calvo model exhibits substantial leptokurtosis, a feature that contrasts sharply with the empirical distribution of price changes.

7.2 Impulse-responses to small and large aggregate shocks

We use our calibrated menu-cost and Calvo models to study price dynamics in response to both small and large shocks under state- and time-dependent pricing. Starting from an economy in steady state, we shock the system with permanent and unanticipated aggregate cost shocks of different magnitudes, $g_t = 2, 10$, and 20 percent.

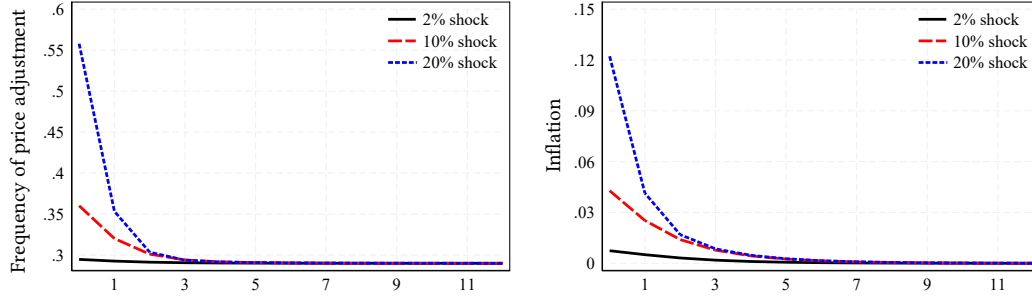
Figure 13 plots the impulse response functions (IRFs) of the frequency of price adjustment (left panels) and aggregate inflation (right panels) for both models. In all cases, the shocks raise the optimal reset price, shifting the distribution of price gaps to the right and triggering an inflation response. However, as discussed in Section 2 and shown empirically in Section 5, large shocks in the menu-cost model displace firms into regions of the price gap distribution where the GHF is steep. This leads to a spike in the adjustment frequency and, in turn, a sharper and faster rise in inflation relative to the Calvo benchmark.

Comparing IRFs across shocks of varying magnitudes highlights the nonlinearities inherent in state-dependent pricing, which become increasingly pronounced as shock size grows. On impact, a large shock generates an inflation response and adjustment frequency nearly three times greater than that of a medium shock, even though its magnitude is only twice as large (10 vs. 20 percent). In contrast, under the Calvo model, both the frequency of price adjustment and inflation rise proportionally with the size of the shock.

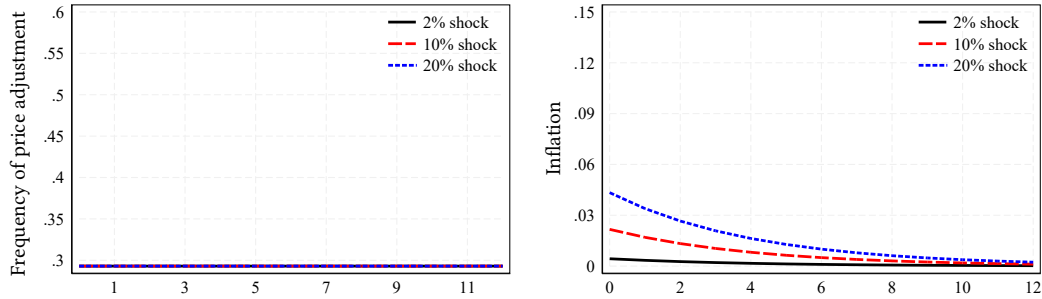
A second key difference concerns the speed at which permanent cost shocks are absorbed into prices. Figure 14 overlays inflation IRFs from both models in response to small and large shocks. While passthrough dynamics are nearly identical for small shocks, the menu-cost model exhibits significantly faster passthrough in response to large shocks.

Figure 13: Impact of aggregate cost shocks in state- and price-dependent models

Panel a: State-dependent pricing (Menu costs)

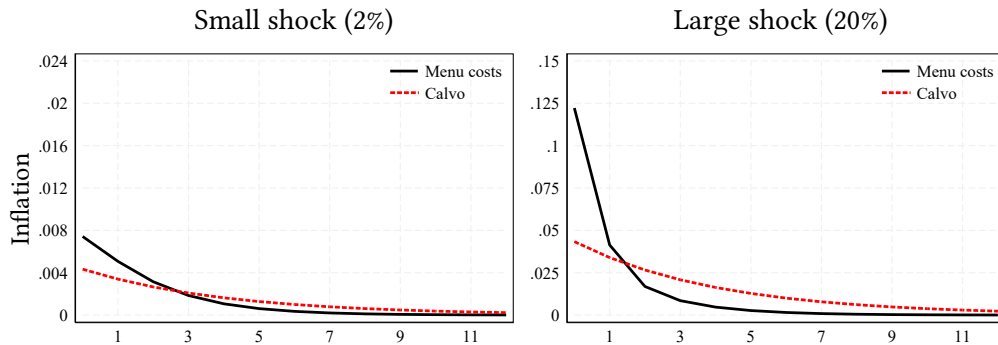


Panel b: Time-dependent pricing (Calvo)



Notes. This figure presents impulse responses of inflation and the frequency of price adjustment to aggregate cost shocks of varying magnitudes. Panel a shows results for the menu-cost model (state-dependent), and Panel b for the Calvo model (time-dependent). The x-axis reports quarters since the shock.

Figure 14: Persistence of inflation in state- and time-dependent models



Notes. This figure compares inflation impulse responses to marginal cost shocks of different magnitudes under the menu-cost and Calvo models. The x-axis shows quarters since the shock.

This differential response again reflects the endogenous increase in adjustment frequency and the selection effect unique to the state-dependent setting.

Appendix B presents two additional quantitative exercises. In the first exercise, we examine how cost shocks of different magnitudes affect both the static target price, p_{ft}^o , and the dynamic optimal price, p_{ft}^* . We show that the gap between the two prices is negligible for small cost shocks, as expected, and remains modest even when the shock is larger.

Static and dynamic reset prices are more closely aligned in the menu-cost model than in the Calvo model, consistent with the model's assumptions and in line with empirical findings from Section 5, particularly in response to large shocks. As discussed in Section 2, this reflects the fact that, in the menu-cost model, the discount factor is time-varying and state-dependent, fluctuating with the current and expected probability of price adjustment. By contrast, the Calvo model features a fixed discounting structure, with the discount factor defined as a power function of the constant adjustment probability.

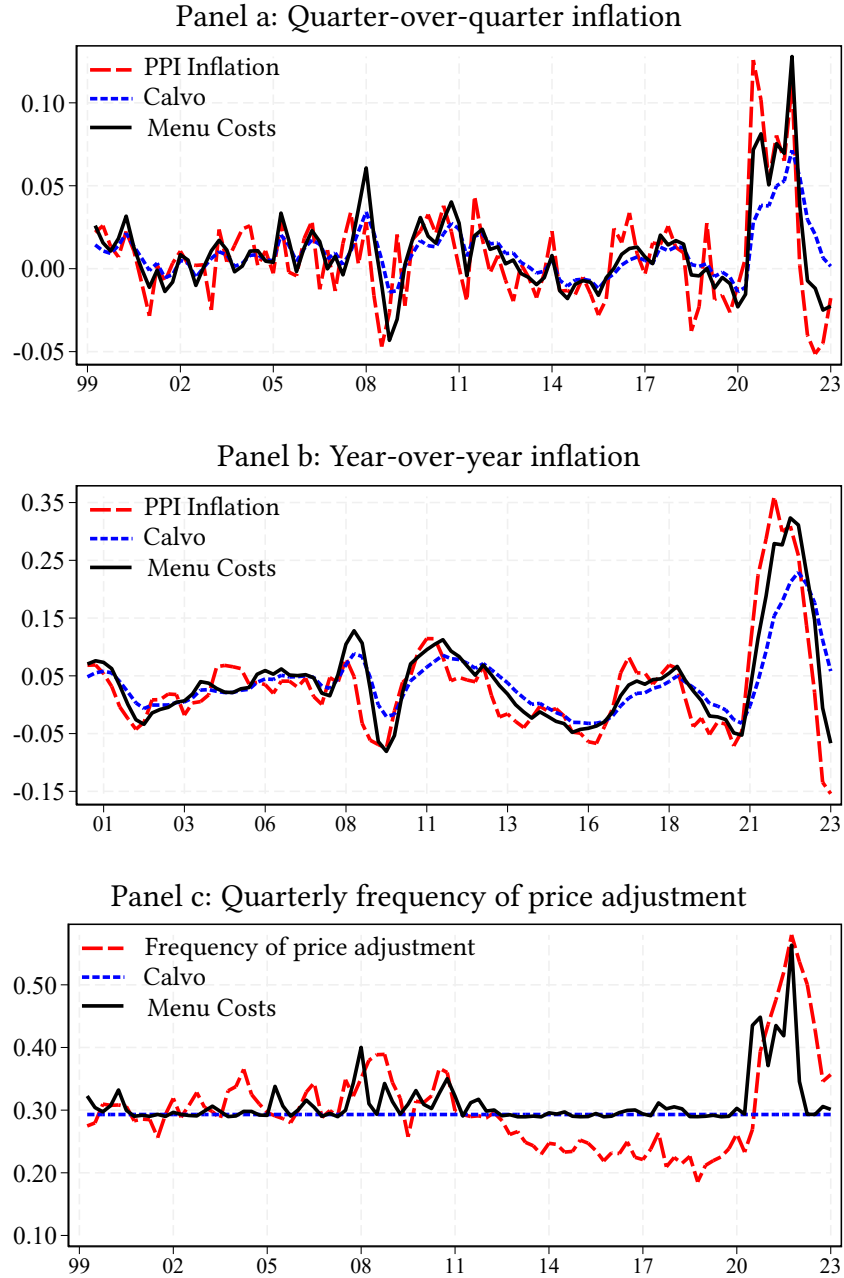
The second exercise examines the role of strategic complementarities. We compare inflation dynamics under high and low cost shocks in models with and without strategic complementarities ($\Omega = 0$ vs. $\Omega = 0.5$). As expected, strategic complementarities dampen cost passthrough in both modeling frameworks. However, due to the greater curvature of the value function under state dependence, the difference in IRFs with and without complementarities is smaller in the menu-cost model, particularly in response to large shocks.

7.3 Explaining the time series of inflation

We now evaluate the ability of time- and state-dependent pricing models to account for the observed time series of aggregate inflation. We feed the models the sequence of aggregate cost shocks extracted from the data and simulate their implications for aggregate inflation and the frequency of price adjustment.

Specifically, we perform the following quantitative exercise: We begin in 1999:Q1, assuming the economy is in steady state. We then feed the model a shock to the aggregate component of marginal cost, equal to the log change in our nominal marginal cost index, Δmc_t^n , between 1999:Q1 and 1999:Q2. In doing so, we maintain the model's assumption that the logarithm of the aggregate component of firms' marginal costs follows a random walk with drift. Given this shock, we solve the model and compute the updated distribution

Figure 15: Inflation and frequency of price adjustment: Model versus data



Notes. This figure compares the time series of PPI manufacturing inflation and the frequency of price adjustment in the data (red dashed line) with the corresponding simulated series from the Calvo model (blue dashed line) and the menu-cost model (black solid line). In both models, the simulated sequences are generated by feeding in the same time series of aggregate cost shocks recovered from the data.

of price gaps, the resulting inflation response, and the frequency of price adjustment, assuming all future aggregate shocks are unanticipated, as in a standard impulse-response exercise. Using the updated price gap distribution as the new equilibrium, we repeat this procedure for all subsequent quarters through 2023:Q4, the final quarter in our sample.

Figure 15 compares the model simulations to the data for three series: quarterly inflation, year-over-year inflation, and the quarterly frequency of price adjustment. Panels a and b show that the menu-cost model (black line) can capture fluctuations in manufacturing inflation well, both during the low inflation regime that characterized the pre-pandemic period and during the pandemic and post-pandemic inflation surge and bust. We also see how during the pre-pandemic period, the menu-cost model is nearly indistinguishable from the Calvo model, consistent with the relatively stable frequency of price adjustment over this time. By contrast, the Calvo model captures only a modest portion of the inflation surge in the data (about two-thirds), despite being fed the same cost sequence as the menu-cost model. Equally important is the sluggish inflation response of the Calvo model, which, unlike the menu-cost model, fails to replicate the rapid decline in inflation observed by the end of 2023.

Finally, Panel c compares the quarterly frequency of price adjustment in the model to that in the data. Our calibrated menu-cost model tracks the stable adjustment frequency observed in the pre-pandemic period—though it misses the gradual downward trend between 2012 and 2019—and captures the sharp increase in frequency following the onset of the pandemic, both in timing and magnitude. We note, however, that as inflation fell in the second half of 2023, the model-implied adjustment frequency fell more rapidly than in the data. This discrepancy may reflect firms anticipating the mean reversion in nominal marginal costs more accurately than implied by our random walk assumption.

8 Concluding remarks

We develop a unified approach to studying cost-price dynamics in the cross-section of firms, aiming to capture aggregate inflation both during normal times and inflation surges. Using detailed microdata on prices and costs, we construct a direct measure of firms' price gaps and provide novel nonparametric evidence on the passthrough from costs to prices across shocks of varying magnitudes. Variation in price gaps explains both the likelihood

of a firm adjusting its price and the magnitude of adjustment, providing strong empirical support for the predictions of our state-dependent pricing framework.

At the macro level, cost-price dynamics are approximately linear in normal times, when aggregate inflation is low: aggregate inflation is well approximated by the product of a fixed frequency of price adjustment and the average price gap. In contrast, during the inflation surge, the dynamics became highly nonlinear. The sharp rise in marginal costs not only widened price gaps but also triggered a significant increase in the frequency of price adjustment. This extensive margin of adjustment—a key feature of state-dependent pricing models—is absent from time-dependent frameworks such as the canonical Calvo (1983) model. Importantly, our analysis shows that, conditional on the path of cost shocks extracted from the data, the state-dependent pricing model captures price and frequency dynamics well at both the firm and aggregate levels.

We view two promising directions for future research. First, due to data availability, our analysis focuses on producer price inflation in the manufacturing sector. We are currently working on expanding the scope of the analysis to other sectors—such as services and retail—which exhibited similar inflation dynamics both before and after the pandemic. Price adjustment in the pre-pandemic period primarily occurred along the intensive margin, while the post-pandemic period also featured pronounced movements along the extensive margin (Blanco et al. 2024b; Cavallo et al. 2024; Morales-Jiménez and Stevens 2024). As in our setting, these patterns are consistent with state-dependent pricing. To the extent that reliable cost data can be obtained for these sectors, we expect the main findings of this paper to extend more broadly.

Another promising direction is to refine the modeling of marginal cost and its connection to real activity. The conventional New Keynesian framework (e.g., Galí 2015) typically models labor as the sole variable input, implying that marginal costs are captured by the labor share. However, our analysis highlights that the sharp increase in intermediate input costs was the primary driver of marginal cost variation during the inflation surge. Extending a state-dependent New Keynesian model to incorporate intermediate inputs (e.g., primary commodities and energy) and supply chain disruptions represents a promising direction for future research.

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Micro and macro cost-price dynamics in normal times and during inflation surges

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Appendix

A Derivations and proofs

A.1 Derivation of the markup function

Assume that a perfectly competitive retailer assembles a bundle of intermediate inputs into a final product, Y_t . The bundle is a Kimball aggregator of differentiated goods produced by a continuum of producers (indexed by f):

$$\int_0^1 \Upsilon \left(\frac{Y_t(f)}{Y_t} \right) df = 1,$$

where $\Upsilon(\cdot)$ is strictly increasing, strictly concave, and satisfies $\Upsilon(1) = 1$.

Taking as given demand Y_t , each firm minimizes costs subject to the aggregate constraint:

$$\min_{Y_t(f)} \int_0^1 \tilde{P}_t(f) Y_t(f) df \quad \text{s.t.} \quad \int_0^1 \Upsilon \left(\frac{Y_t(f)}{Y_t} \right) df = 1.$$

where $\tilde{P}_t(f) \equiv \frac{P_t(f)}{e^{\varphi_t(f)}}$ is the quality-adjusted price. Denoting by ψ the Lagrange multiplier of the constraint, the first-order condition of the problem is:

$$\tilde{P}_t(f) = \psi \Upsilon' \left(\frac{Y_t(f)}{Y_t} \right) \frac{1}{Y_t}. \quad (\text{A.1})$$

Define implicitly the industry price index P_t as:

$$\int_0^1 \phi \left(\Upsilon'(1) \frac{\tilde{P}_t(f)}{P_t} \right) df = 1,$$

where $\phi \equiv \Upsilon \circ (\Upsilon')^{-1}$. Evaluating the first-order condition (A.1) at symmetric prices, $\tilde{P}_t(f) = P_t$, we get $\psi = \frac{P_t Y_t}{\Upsilon'(1)}$. Replacing for ψ , we recover the demand function:

$$\frac{\tilde{P}_t(f)}{P_t} = \frac{1}{\Upsilon'(1)} \Upsilon' \left(\frac{Y_t(f)}{Y_t} \right). \quad (\text{A.2})$$

Therefore, the demand function faced by firms when resetting prices is:

$$\mathcal{D}_t(f) = (\Upsilon')^{-1} \left(\Upsilon'(1) \frac{\tilde{P}_t^o(f)}{P_t} \right) Y_t.$$

Taking logs of Equation (A.1) and differentiating, we obtain the following expression for the residual elasticity of demand:

$$\varsigma_t(f) \equiv -\frac{\partial \ln \mathcal{D}_t(f)}{\partial \ln \tilde{P}_t^o(f)} = -\frac{\Upsilon' \left(\frac{Y_t(f)}{Y_t} \right)}{\Upsilon'' \left(\frac{Y_t(f)}{Y_t} \right) \cdot \left(\frac{Y_t(f)}{Y_t} \right)}. \quad (\text{A.3})$$

We now use this result to derive the expression for the log-linearized desired markup. As above, for ease of exposition, we focus on the symmetric steady state. Denote the steady-state residual demand elasticity by $\varsigma = -\frac{\Upsilon'(1)}{\Upsilon''(1)}$. Then the derivative of the residual demand elasticity $\varsigma_t(f)$ in (A.3) with respect to $\frac{Y_t(f)}{Y_t}$, evaluated at the steady state, is given by:

$$\varsigma' = \frac{\Upsilon'(1) (\Upsilon'''(1) + \Upsilon''(1)) - (\Upsilon''(1))^2}{(\Upsilon''(1))^2} \leq 0, \quad (\text{A.4})$$

which holds with equality if the elasticity is constant (e.g., under CES preferences).

The desired markup is given by the Lerner index. Log-linearizing the Lerner index around the steady state and using Equation (A.4), we have that, up to a first-order approximation, the log-markup (in deviation from the steady state) is equal to:

$$\mu_t(f) - \mu(f) = \frac{\varsigma'}{\varsigma(\varsigma - 1)} (y_t(f) - y_t)$$

Finally, log-linearizing the demand function (A.1) and using it to replace the log difference in output, we obtain:

$$\mu_t(f) - \mu(f) = -\Gamma (\tilde{p}_t^o(f) - p_t)$$

where, in the case of Kimball preferences, the sensitivity of the markup to the relative price is given by $\Gamma \equiv \frac{\varsigma'}{\varsigma(\varsigma - 1)} \frac{1}{\Upsilon''(1)}$. Finally, replacing the log-linearized markup into the formula for the static optimal target price (obtained from cost minimization):

$$\begin{aligned} p_t^o(f) &= \mu_t(f) + mc_t^n(f) \\ &= (1 - \Omega)(\mu(f) + mc_t^n(f)) + \Omega(p_t + \varphi_t(f)) \end{aligned}$$

where $\Omega \equiv \frac{\Gamma}{1 + \Gamma}$ is the degree of strategic complementarities.

A.2 Derivation of the optimal reset gap

Under the quadratic profits, the problem of the firm at time t is:

$$\max_x -B(x)^2 + \beta \mathbb{E}_t \{ h_{t+1}(x) \cdot V_{t+1}^a + (1 - h_{t+1}(x)) \cdot V_{t+1}(x) \},$$

where $B \equiv \frac{\sigma(\sigma-1)}{2(1-\Omega)}$. The first-order condition evaluated at the optimal reset gap x_t^* is:

$$Bx_t^* = \beta \mathbb{E}_t \left\{ (1 - h_{t+1}(x_t^*)) \frac{\partial V_{t+1}(x)}{\partial x} \Big|_{x=x_t^*} + (V_{t+1}^a - V_{t+1}(x_t^*)) \frac{\partial h_{t+1}(x)}{\partial x} \Big|_{x=x_t^*} \right\}.$$

Because the adjustment probability is minimized at x_t^* , the condition simplifies to:

$$Bx_t^* = \beta \mathbb{E}_t \left\{ (1 - h_{t+1}(x_t^*)) \frac{\partial V_{t+1}(x)}{\partial x} \Big|_{x=x_t^*} \right\}.$$

Using that $\partial x_t / \partial x_{t-1} = 1$, the envelope condition is:

$$\frac{\partial V_{t+1}(x_t)}{\partial x_{t-1}} = -Bx_t + \beta \mathbb{E}_t (1 - h_{t+1}(x_t)) \frac{\partial V_{t+1}}{\partial x_t}.$$

Denoting $h_{t+\tau}(x_t) := h_{t+\tau}$ to ease notation, we repeatedly replace the derivative above into the first-order condition to obtain:

$$\mathbb{E}_t \left\{ \sum_{i=0}^{\infty} \beta^i \prod_{\tau=0}^i (1 - h_{t+\tau}) x_{t+\tau}^* \right\} = 0, \quad h_t \equiv 0.$$

Rearranging the condition by using the random walk dynamics of $mc_t^n(f)$ and the fact that taste shocks are i.i.d., we obtain the following expression that characterizes the optimal reset price:

$$\begin{aligned} p_t^*(f) &= (1 - \Omega)(\mu(f) + mc_t^n(f)) + \Omega p_t + \Omega \frac{\mathbb{E}_t \{ \sum_{i=1}^{\infty} (p_{t+i} - p_t) \beta^i \prod_{\tau=1}^i (1 - h_{t+\tau}) \}}{\mathbb{E}_t \{ \sum_{i=0}^{\infty} \beta^i \prod_{\tau=0}^i (1 - h_{t+\tau}) \}} \\ &= p_t^0(f) + \Omega \Psi_t. \end{aligned} \tag{A.5}$$

The equation above decomposes the optimal (dynamic) reset price into two terms. The first is the static reset price, $p_{ft}^0 \equiv (1 - \Omega)(\mu(f) + mc_t^n(f)) + \Omega p_t$, which captures the effects of current cost shocks and the price index. The second term, Ψ_t , captures the expected future dynamics of aggregate prices. These influence the optimal price p_{ft}^* as the firm anticipates that the price set today may also apply to future periods due to nominal rigidities.²¹

Finally, under our assumption that costs follow a random walk and i.i.d. taste

²¹See Dotsey and King (2005) for a discussion of the properties of the dynamic reset price under general assumptions about cost and demand dynamics.

shocks, the second term in Equation (A.5) (i) does not depend on the identity of the firm, (ii) is exactly zero in the absence of strategic complementarities ($\Omega = 0$), and (iii) is approximately zero even with strategic complementarities when trend inflation is sufficiently low ($p_{t+k} - p_t \approx 0 \ \forall k$). Properties (i)–(ii) are inherited by the optimal gap.

A.3 Quadratic approximation of generalized hazard function

We now derive the expression for the quadratic approximation of the hazard function in Equation (8) and describe how we take this equation to the data. We take a second-order approximation of the hazard function $h_t(x_{t-1})$ characterized in Equation (7) around x_t^* to obtain:

$$\begin{aligned} h_t(x_{t-1}) &= (1 - \theta^0) - \frac{\theta^0}{\bar{\chi}} \frac{\partial V_t(x)}{\partial x} \Big|_{x=x_t^*} (x_{t-1} - x_t^*) - \frac{\theta^0}{2\bar{\chi}} \frac{\partial^2 V_t(x)}{\partial x^2} \Big|_{x=x_t^*} (x_{t-1} - x_t^*)^2 + o(x_{t-1} - x_t^*)^2 \\ &= (1 - \theta^0) - \frac{\theta^0}{2\bar{\chi}} \frac{\partial^2 V_t(x)}{\partial x^2} \Big|_{x=x_t^*} (x_{t-1})^2 + o(x_{t-1})^2, \end{aligned}$$

where the second equation follows from $\frac{\partial V_t(x)}{\partial x} \Big|_{x=x_t^*} = 0$ for a firm that is resetting its price and from our assumption that $x_t^* \approx 0$. Assuming stationarity of the value function, and defining $\phi \equiv -\frac{\theta^0}{2\bar{\chi}} \frac{\partial^2 V(x)}{\partial x^2} \Big|_{x=0}$, we have that the GHF can be approximated, up to second order, by a quadratic function of the price gap as in Equation (8):

$$h(x_{t-1}(f)) = (1 - \theta^0) + \phi \cdot ((x_{t-1}(f))^2 + o((x_{t-1}(f))^2)), \quad (\text{A.6})$$

where the parameter ϕ controls the sensitivity of the GHF to changes in gaps (i.e., the “steepness” of the parabola).

A.4 Estimator of the probability of free adjustment

First, we derive the expression for the average frequency of price adjustment in a bin. The quadratic approximation (8) means that every $\epsilon/2 > 0$ there exists a $\delta_f > 0$ such that for $|x_f| \leq \delta_f$:

$$|h_f - (1 - \theta^0) - \phi x_f^2| \leq \frac{\epsilon}{2} x_f^2.$$

Taking the average of both sides of the equation between observations falling within a given bin b :

$$\begin{aligned} |h_b - (1 - \theta^o) - \phi(x_b^2 + \sigma_b^2)| &\leq \int_{f \in b} |h_f - (1 - \theta^o) - \phi x_f^2| df \\ &\leq \frac{\epsilon}{2} \int_{f \in b} x_f^2 df \\ &= \frac{\epsilon}{2} (x_b^2 + \sigma_b^2) \leq \epsilon x_b^2, \end{aligned}$$

where the last inequality uses the fact that, when bins are arbitrarily small, $\sigma_b^2 \leq x_b^2$. Figure A.1 shows that this inequality holds in the data given our choice of quantiles. It follows that, letting $\delta_b \equiv \sup_{f \in b} \delta_f$, we get that:

$$h_b = (1 - \theta^o) + \phi(x_b^2 + \sigma_b^2) + o(x_b^2).$$

Next, we show how knowledge of the empirical frequency of price adjustment within a bin allows us to recover the probability of free price adjustment, θ^o . We denote by \tilde{b} the bin such that $x_{\tilde{b}} = 0$. Label $\tilde{b} = 0$ and let $b' = -b'' \iff x_{b'} = -x_{b''}$. Let $h(b) \equiv h_b$ for all b s. As we have shown above, the frequency $h(b)$ is a convex function of the bins. Therefore, for any open interval of gaps around \tilde{b} it holds that:

$$\int_{(-b, b)} h(b) db \geq 1 - \theta^o.$$

We want to show that the integral on the LHS converges to the RHS as the interval $(-b', b')$ shrinks.

Let the bins take values on $b \in \{-\frac{1}{N}, -\frac{1}{N+1}, \dots, 0, \dots, \frac{1}{N+1}, \frac{1}{N}\}$ for some finite $N \in \mathbb{N}_+$. Consider a sequence of decreasing bounds $1/n$, for $n = K, K+1, \dots$, with $N < K \in \mathbb{N}_+$. Then the sequence:

$$1 - \int_{\{-\frac{1}{n}, \dots, 0, \dots, \frac{1}{n}\}} h(b) db$$

is non-decreasing (as h convex and integral is monotone in the support) and bounded above by θ^o . Therefore, by the monotone convergence theorem, it converges to its supremum which is given by:

$$1 - \lim_{n \rightarrow \infty} \int_{\{-\frac{1}{n}, \dots, 0, \dots, \frac{1}{n}\}} h(b) db = 1 - h(\tilde{b}) = \theta^o.$$

For a sufficiently small interval around \tilde{b} , the mean of the frequencies of price adjustment over that interval recovers the probability of free adjustment.

A.5 Cubic approximation of inflation within a bin

Starting from the expression for aggregate inflation in Equation (9), we want to derive the cubic expression for inflation within a bin in Equation (13), under the assumption that $p_t^*(f) = p_t^o(f)$ and associated cross-sectional regression model. Again we partition the distribution of price gaps into equal frequency bins (quantiles) denoted by b and adopt the same labeling convention of bins described in Appendix A.4. Denote by γ_b the skewness within a bin. Consider a bin b in the positive range ($x_f > 0$ for all $f \in b$). Then for every $\epsilon/5 > 0$, there exists a $\delta_f > 0$ such that for $x_f \leq \delta_f$:

$$\begin{aligned} \left| \int_{f \in b} (h_f - (1 - \theta^o) - \phi x_f^2) \cdot x_f df \right| &\leq \int_{f \in b} |h_f - (1 - \theta^o) - \phi x_f^2| \cdot x_f df \\ &\leq \frac{\epsilon}{5} \int_{f \in b} x_f^3 df \\ &= \frac{\epsilon}{5} (x_b^3 + 3\sigma_b^2 x_b + \gamma_b \sigma_b^3) \leq \epsilon x_b^3 \end{aligned}$$

where the last step uses that bins can be chosen arbitrarily small (and the distribution of gaps is smooth) so that $\sigma_b^2 \leq x_b^2$ and $|\gamma_b| \leq 1$ and that $\gamma_b \geq 0 \iff x_b \geq 0$ because the distribution of gaps is single-peaked at zero. We note that the same argument applies for the negative range by switching signs of x_f (x_b) and γ_b and reversing the inequalities. Setting $\delta_b \equiv \sup_{f \in b} \delta_f$, for every $\epsilon/5 > 0$ it then holds that for $|x_f| \leq \delta_b$ for all $f \in b$:

$$\left| \frac{\mathbb{E}_b(h_f \cdot x_f) - (1 - \theta^o)x_b - \phi \mathbb{E}_b(x_f^3)}{x_b^3} \right| \leq \epsilon.$$

Hence:

$$\mathbb{E}_b(h_f \cdot x_f) = (1 - \theta^o)x_b + \phi \mathbb{E}_b(x_f^3) + o(x_b^3)$$

Using this approximation, the covariance within a bin satisfies:

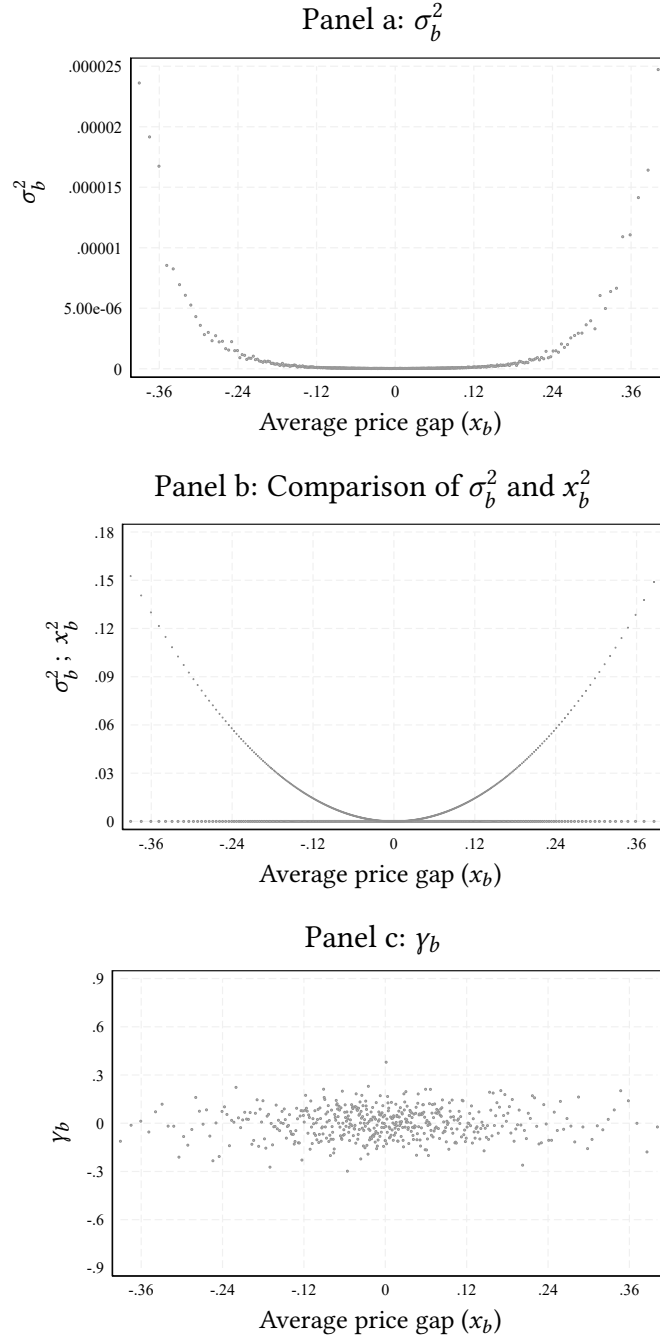
$$\begin{aligned} Cov_b(h_f, x_f) &= \phi \mathbb{E}_b(x_f^3) + o(x_b^3) - \phi \mathbb{E}_b(x_f^2)x_b - o(x_b^2)x_b \\ &= \phi(2x_b\sigma_b^2 + \gamma_b\sigma_b^3) + o(x_b^3) \end{aligned}$$

It follows that inflation within a bin simplifies to:

$$\begin{aligned} \pi_b &= \int_{f \in b} h(x(f)) df \cdot \int_{f \in b} x(f) df + Cov_b(h(f), x(f)) \\ &= ((1 - \theta^o) + 3\phi\sigma_b^2) x_b + \phi x_b^3 + \phi\gamma_b\sigma_b^3 + o(x_b^3) \end{aligned}$$

A.6 Variance and skewness across the price gap distribution

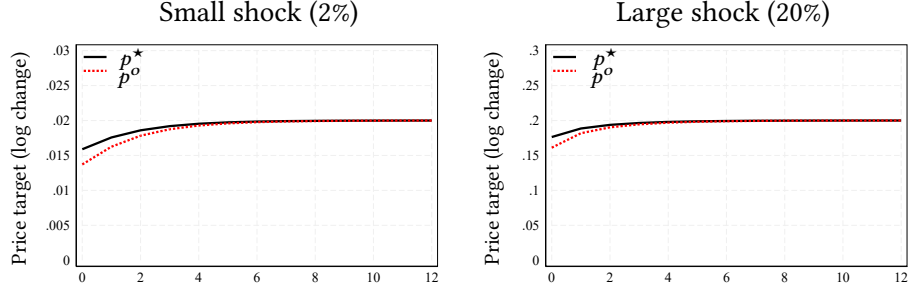
Figure A.1: Within bin variance, square of the mean, and skewness



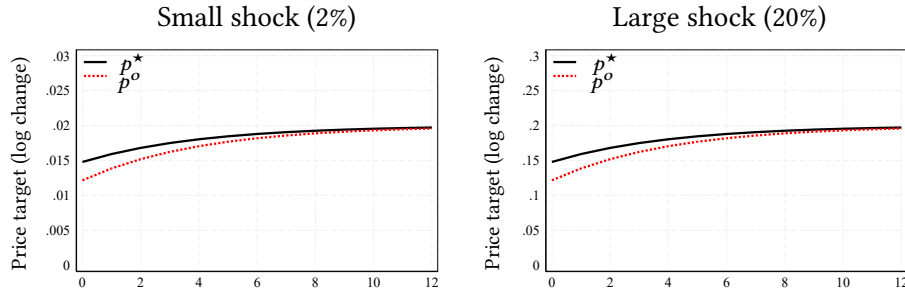
Notes. This figure plots three moments of the price gap distribution by bin (quantile): the within-bin variance of price gaps (σ_b^2 , panel a), the square of the within-bin average gap (x_b^2 , panel b), and the within-bin skewness of price gaps (γ_b , panel c). In panel b, x_b^2 (crosses) is plotted alongside σ_b^2 (circles) on the same scale to facilitate comparison.

Figure A.2: Impulse responses: Static vs. dynamic price targets

Panel a: State-dependent pricing (Menu costs)



Panel b: Time-dependent pricing (Calvo)



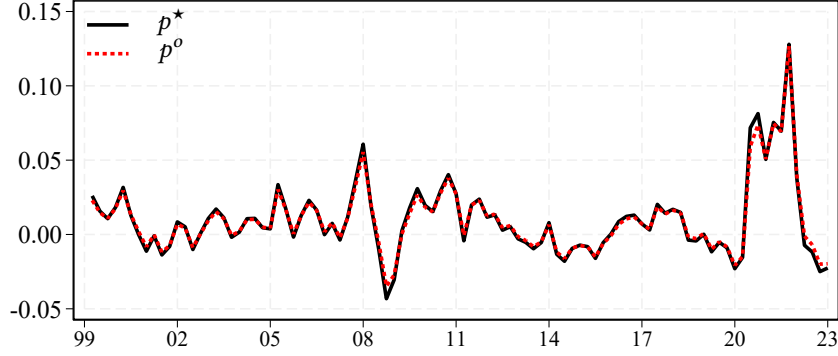
Notes. This figure compares impulse responses of the static target price (p^o) and the dynamic optimal reset price (p^*) to aggregate cost shocks of different magnitudes. The x-axis denotes quarters since the shock.

B Additional quantitative exercises

Approximation of p_{ft}^* with p_{ft}^o . As discussed in Section 2, the two prices coincide in a steady state with zero trend inflation and constant markups. We also argued that the two prices remain sufficiently close to each other as long as trend inflation is not too large, even in the presence of strategic complementarities in pricing. We therefore assumed $p_{ft}^o \approx p_{ft}^*$, which implies that $x_{ft}^* \approx 0$, and derived expressions for aggregate inflation and within-bin inflation as a function of price gaps (Equations (9) and (13), respectively). The question is how well p_{ft}^o approximates p_{ft}^* away from the steady state.

The impulse response functions shown in Figure A.2 indicate that, as expected, the dynamic reset price responds more than the static one to cost shocks, since p_{ft}^* accounts for marginal cost being a persistent process, though not a pure random walk, due to strategic pricing motives. However, this exercise also shows that the gap between the two prices is negligible if the shock is small, as expected, and remains small even when

Figure A.3: Quarter-over-quarter inflation: Static vs. dynamic price targets



Notes. This figure contrasts the inflation dynamics generated by the menu-cost model using p^* (the exact, dynamic reset price) and using p^o (the static approximation of p^*) when solving the model. As in Figure 15, we solve the model feeding it a sequence of aggregate nominal marginal cost shocks that matched the one observed in the data.

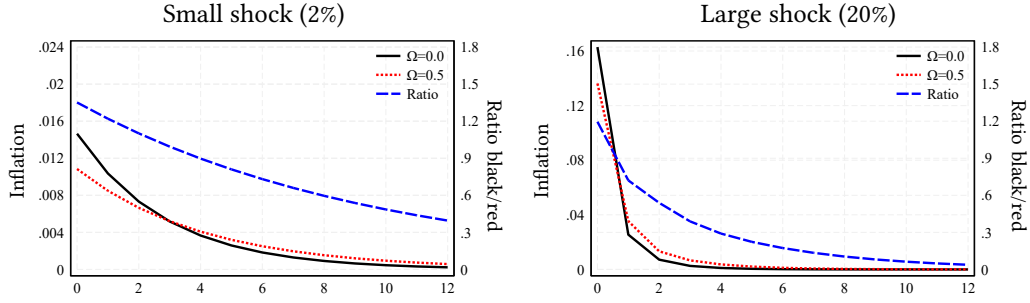
the shock is large. Thus, the assumption that $p_{ft}^o \approx p_{ft}^*$ is sensible. Additionally, this exercise demonstrates how the dynamics of the two prices are particularly close in the context of the menu-cost model relative to the Calvo model.

Next, we verify that using p_{ft}^o as an approximation for p_{ft}^* has a small impact on the aggregate inflation dynamics once we feed the model a sequence of aggregate nominal marginal cost shocks that matched the one observed in the data. Figure A.3 repeats the same quantitative exercise presented in Figure 15. The black line displays the time series of model-based quarterly inflation using p_{ft}^* as a measure of target price; the red dashed line displays the time series of model-based inflation, solving the model with p_{ft}^o as a proxy for p_{ft}^* .

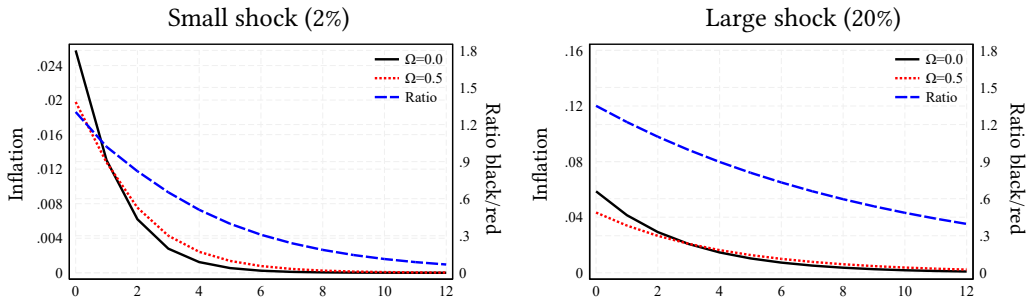
The role of strategic complementarities. Strategic complementarities in price setting help explain the differing dynamics of static and dynamic reset prices in time- and state-dependent models. Figure A.4 compares inflation dynamics after high- and low-cost shocks, without strategic complementarities ($\Omega = 0$) and with strategic complementarities ($\Omega = 0.5$). As before, Panels a and b report the impulse response functions for the menu-cost model and the Calvo model, respectively. As expected, strategic complementarities generate additional discounting, which reduces cost passthrough in both models. However, we can see how the difference between the impulse-response functions with and without complementarities is narrower in the menu-cost model,

Figure A.4: The role of strategic complementarities

Panel a: State-dependent pricing (Menu costs)



Panel b: Time-dependent pricing (Calvo)



Notes. This figure shows inflation impulse responses to aggregate cost shocks under two pricing assumptions: no strategic complementarities ($\Omega = 0$, black line) and with complementarities ($\Omega = 0.5$, red dotted line). The blue dashed line shows the ratio of the responses. Panels a and b report results for the menu-cost and Calvo models, respectively. The x-axis reports quarters since the shock.

especially in response to a large shock. This is due to the greater curvature of the value function under state-dependent pricing.