

# A Lost Decade of Fiscal Misallocation

Kosuke Aoki<sup>1</sup> Ippei Fujiwara<sup>2</sup> Zhenhe Lin<sup>3</sup>

Zheng (Michael) Song<sup>3</sup> Chendong Wang<sup>3</sup>

<sup>1</sup>University of Tokyo

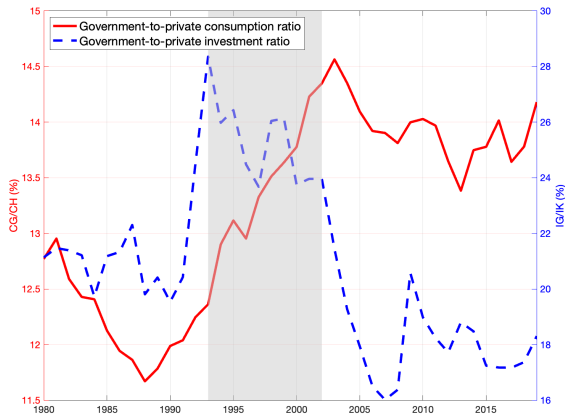
<sup>2</sup>Keio University

<sup>3</sup>The Chinese University of Hong Kong

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# Government-Private Allocation of Consumption and Investment

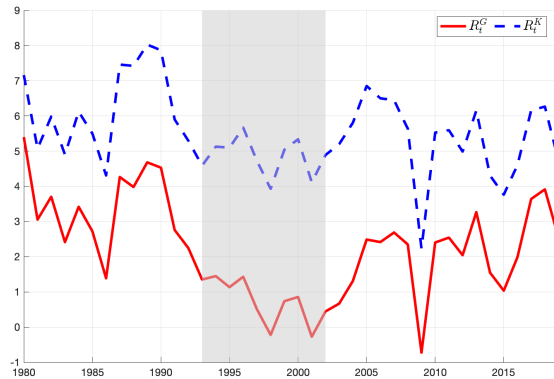
Figure 1: Government-to-Private Consumption and Investment Ratios (%)



- Government consumption: government actual final consumption (excluding social transfers in kind) Expenditure GDP Ratio

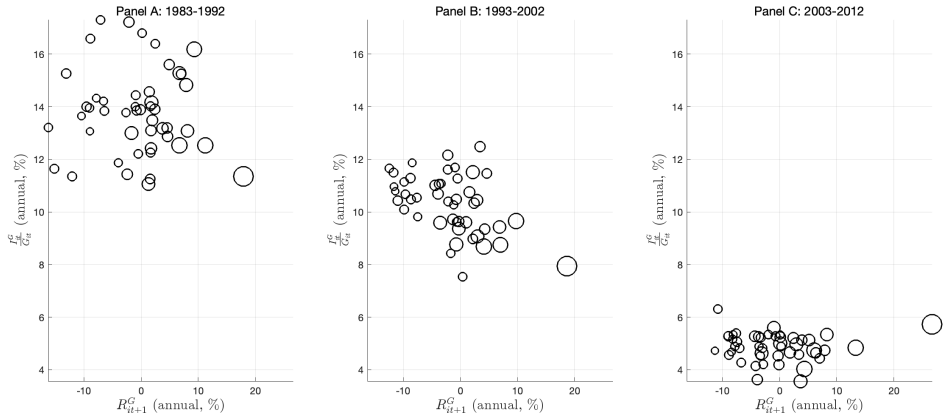
# Misallocation of Government and Private Capital

Figure 2: Aggregate Returns to Government and Private Capital (%)



# Spatial Misallocation of Government Investment

Figure 3:  $\frac{I_{it}^G}{G_{it}} \sim R_{it+1}^G$



► Capital Return:  $R_{it}^G \equiv \alpha_G \frac{\partial Y_t}{\partial G_{it}} + \frac{q_t}{q_{t-1}} (1 - \delta) - 1$ ,  $\frac{\partial Y_t}{\partial G_{it}}$  follows equation (16)

# Correlations

Table 1:  $\frac{I_{it}^G}{G_{it}} \sim R_{it+1}^G$

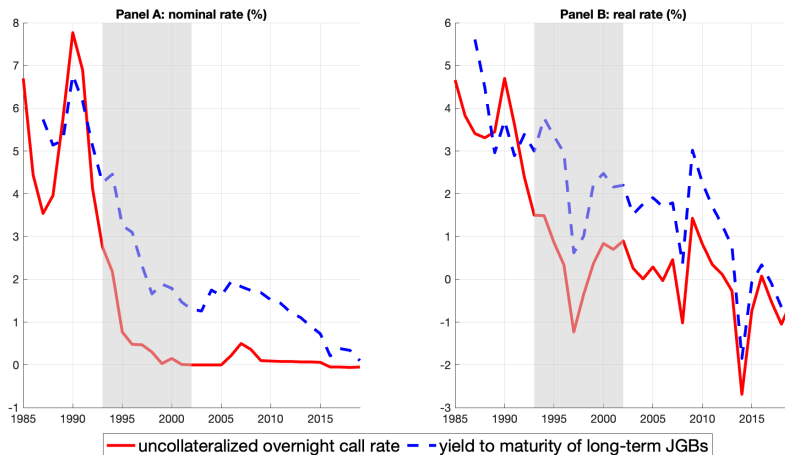
| $\frac{I_{it}^G}{G_{it}}$ | 1983-1992         | 1993-2002                   | 2003-2012         |
|---------------------------|-------------------|-----------------------------|-------------------|
| $R_{it+1}^G$              | -0.008<br>(0.033) | <b>-0.084***</b><br>(0.023) | -0.002<br>(0.011) |
| Observations              | 47                | 47                          | 47                |
| R <sup>2</sup>            | 0.001             | 0.223                       | 0.001             |

# Spatial Allocation of Government Consumption

- ▶ Spatial allocation of government consumption is highly persistent.
  - ▶ Growth of  $C_{it}^G$ : strong correlation across periods
  - ▶ Growth of  $I_{it}^G$ : zero correlation
- ▶ Abstract away from  $C_{it}^G$

# Interest Rate Cuts

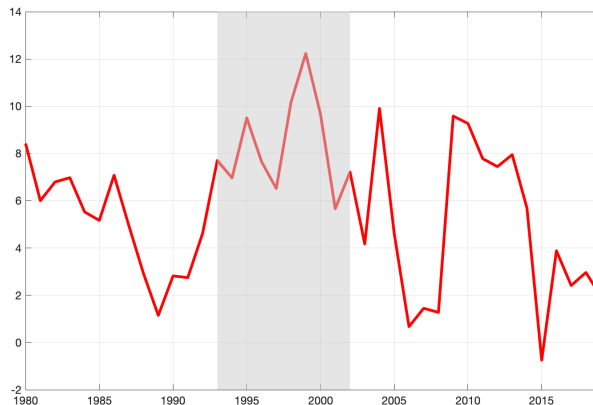
Figure 4: Interest Rate



► Real rate = Nominal rate - inflation.

# More Government Borrowing

Figure 5: Government Borrowing (in percent of GDP)



- Central and local government borrowing (excluding Fiscal Investment and Loan Program (FILP) bonds)



# Fiscal Windfalls from “Constrained” Government’s Perspective (to fix ideas)

- ▶ Government budget constraint and fiscal windfalls

$$C_t^G + I_t^G = NB_t + B_t - r_t^D D_t, \quad (1)$$

$$\text{Windfall}_t = \Delta \mathbb{E}_t [NB_t] + \Delta \mathbb{E}_t [B_t] - \Delta \mathbb{E}_t [r_t^D D_t]. \quad (2)$$

- ▶  $\mathbb{E}_t [X_{t+j}]$ : expectation of  $X_{t+j}$  in period  $t$ .
  - ▶  $\Delta \mathbb{E}_t [X_{t+j}] \equiv \mathbb{E}_t [X_{t+j}] - \mathbb{E}_{t-1} [X_{t+j}]$
- ▶  $B_t \equiv D_{t+1} - D_t$ : government borrowing.
- ▶  $NB_t$ : government non-borrowing income

## In this paper

- ▶ Much lower government borrowing cost relaxes government budget constraint through lower interest payment and more borrowing.
- ▶ A simple model to show "Government Resource Curse": More resource, more misallocation.
- ▶ Quantitative results:
  - ▶ "Fiscal windfalls" largely explain the deterioration in fiscal allocation during the Lost Decade;
  - ▶ Transferring fiscal windfalls to households could increase aggregate TFP by 0.23% and welfare by 0.87% during the Lost Decade.

## One-Period Model: The Economy

- ▶ There are  $N$  regions. For each region  $i$ , the production function is given by:

$$Y_i = A_i G_i^\alpha \quad (3)$$

- ▶ The representative household's utility function follows:

$$U^H = u(C), \quad C = \left(C^H\right)^\rho \left(C^G\right)^{1-\rho} \quad (4)$$

- ▶  $u' > 0, u'' < 0$

- ▶ Resource constraint:

$$C^G + C^H + G = W^G + W^H + Y, \quad (5)$$

- ▶ Aggregation:  $G \equiv \sum_i G_i$  and  $Y \equiv \sum_i Y_i$

## First-Best Allocation

- ▶ A benevolent planner maximizes  $U^H$  by choosing  $\{G_i\}_i, C^G, C^H$ , subject to (5).
- ▶ FOC w.r.t.  $G_i$  yields:

$$R_i^G \equiv \frac{\partial Y}{\partial G_i} = \alpha \frac{Y_i}{G_i} = 1. \quad (6)$$

- ▶ Aggregate TFP  $A \equiv \frac{Y}{G^\alpha}$  maximized by equalizing  $R_i^G$ :  $\bar{A} \equiv \left( \sum_i A_i^{\frac{1}{1-\alpha}} \right)^{1-\alpha}$ .
- ▶ FOC w.r.t.  $C^G$  and  $C^H$  yields:

$$\frac{C^G}{C^H} = \frac{1-\rho}{\rho}. \quad (7)$$

# Political Economy

- ▶ Government objective function:

$$U^G = u(C) + \sum_i \kappa_i v(G_i) \quad (8)$$

- ▶  $v' > 0, v'' < 0$

- ▶  $\kappa_i > 0$ : local lobbying capacity (e.g., Sato (2002); Ihori et al. (2009))

- ▶ Budget constraint:

$$C^G + \sum_i G_i + T = W^G + \tau Y, \quad (9)$$

where  $T$  and  $\tau$ : lump-sum transfers and output tax rate.

- ▶ Government chooses  $C^G$  and  $\{G_i\}$ .  $T$  and  $\tau$  are exogenous.

## Wedges

- ▶ Consumption wedge

$$\text{Consumption Wedge} = \frac{\rho}{1 - \rho} \frac{C^G}{C^H} - 1 \quad (10)$$

- ▶ Positive consumption wedge: distorted consumption allocation favoring  $C^G$
- ▶ FOC w.r.t.  $C^G$  and  $\{G_i\}$ :

$$\left[ 1 + \underbrace{\frac{\kappa_i C^G}{(1 - \rho) \alpha Y_i} \frac{v'(G_i) G_i}{u'(C) C}}_{\text{Government Capital Wedge}} + (1 - \tau) \times \text{Consumption Wedge} \right] R_i^G = 1 \quad (11)$$

- ▶  $\tau \rightarrow 1$  or consumption wedge = 0: overinvestment of  $\{G_i\}$  relative to the first-best allocation

## "Government Resource Curse"

- ▶ Assumption:  $u(\cdot) = v(\cdot) = \log(\cdot)$ , sufficiently high  $\tau$
- ▶ Oversupply of Government Capital: The discrepancy between  $G_i$  and its first-best level increases monotonically with government wealth  $W^G$ .
- ▶ Spatial Misallocation of Government Capital: Aggregate TFP  $A$  decreases monotonically with government wealth  $W^G$ .
  - ▶ As  $W^G \rightarrow \underline{W}^G$ ,  $\{G_i\}$  converges to  $G_i \propto A_i^{\frac{1}{1-\alpha}}$ : **efficiency-driven allocation rule.**
  - ▶ As  $W^G \rightarrow \infty$ ,  $\{G_i\}$  converges to ,  $\{G_i\}$  converges to  $v'(G_i) \propto \frac{1}{K_i}$ : **purely politically-driven allocation.**

## Sketch of Full-Blown Model

- ▶ The central government at period  $t$ , subject to an exogenous exit rate, allocates  $C_{t+j}^G$ ,  $B_{t+j}$ , and  $\{I_{it+j}^G\}$  for  $j \geq 0$ ;
- ▶ Overlapping generations of households;
- ▶ Small open economy with mobile labor and private capital across regions; evidence
- ▶ Region-specific and time-varying parameters  $\kappa_{it}$ ,  $\tau_{it}^K$ ,  $\tau_{it}^L$  calibrated to match  $I_{it}^G$ ,  $K_{it}$ , and  $L_{it}$ ;
- ▶ MIT shocks.



## Household

- The representative household solves

$$\max_{C_{t,t}^H, C_{t,t+1}^H, W_{t+1}^H} U_t^H = \log \left( (C_{t,t}^H)^\rho (C_t^G)^{1-\rho} \right) + \beta \log \left( (C_{t,t+1}^H)^\rho (C_{t+1}^G)^{1-\rho} \right)$$

subject to the budget constraint  $C_{t,t}^H + W_{t+1}^H = Y_t^H + T_t$  and  $C_{t,t+1}^H = (1 + r_{t+1})W_{t+1}^H$ .

- $T_t$  : lump-sum government transfer or tax
- Household takes  $\{C_t^G, C_{t+1}^G\}$  as given

Closed-form solutions:

$$C_{t,t}^H = \frac{1}{1+\beta} (Y_t^H + T_t), \quad C_{t,t+1}^H = \frac{\beta(1+r_{t+1})}{1+\beta} (Y_t^H + T_t). \quad (12)$$

## Firm

- ▶ Local output by the production of a representative firm:

$$Y_{it} = A_{it} G_{it}^{\alpha_G} K_{it}^{\alpha_K} L_{it}^{\alpha_L} \quad (13)$$

- ▶ Land's share in production is  $1 - \alpha_G - \alpha_K - \alpha_L$ .
- ▶ The firm faces a proportional tax rate  $\tau_t$ , labor and private capital wedges  $\tau_{it}^L$  and  $\tau_{it}^K$ :

$$\max_{K_{it}, L_{it}} (1 - \tau_t) Y_{it} - \left(1 + \tau_{it}^K\right) (1 + r_t^K) K_{it} - \left(1 + \tau_{it}^L\right) w_t L_{it} \quad (14)$$

## Local and Aggregate Output

- ▶ Exogenous rental rate of capital  $r_t^K$  and exogenous aggregate labor supply  $L_t \equiv \sum_i L_{it}$ .
- ▶ Firm's first-order conditions imply

$$Y_{it} \propto \left( \frac{A_{it}}{(1 + \tau_{it}^K)^{\alpha_K} (1 + \tau_{it}^L)^{\alpha_L}} \right)^{\frac{1}{1 - \alpha_K - \alpha_L}} G_{it}^{\frac{\alpha_G}{1 - \alpha_K - \alpha_L}}. \quad (15)$$

- ▶  $Y_t \equiv \sum_{i=1}^N Y_{it}$ . The marginal product of  $G_{it}$  at the aggregate level is

$$\frac{\partial Y_t}{\partial G_{it}} = \frac{\alpha_G}{1 - \alpha_K - \alpha_L} \frac{Y_{it}}{G_{it}} - \frac{\alpha_G \alpha_L}{(1 - \alpha_K - \alpha_L)(1 - \alpha_K)} \frac{L_{it}}{L_t} \frac{Y_t}{G_{it}}, \quad (16)$$

- ▶ Central government objective function:

$$U_t^C = \omega \log \left( \left( C_{t-1,t}^H \right)^\rho \left( C_t^G \right)^{1-\rho} \right) + \sum_{j=0}^{\infty} \beta_C^j \left( U_{t+j}^H + \sum_{i=1}^N \kappa_{it+j} \log G_{it+j+1} \right) \quad (17)$$

- ▶  $\beta_C = \beta p$ ,  $p \in (0, 1)$  is the probability of staying in office next period.
- ▶  $\kappa_{it}$ : Institutional parameter for local governor's lobbying capacity.
- ▶  $\omega$ : The weight on the current old generation. We assume  $\omega = \frac{\beta}{\beta_C}$  such that the central government's preference is time-consistent.

# Budget

- ▶ Central government budget constraint:

$$C_t^G + \sum_{i=1}^N q_t^G I_{it}^G + T_t + \Phi_t = \tau_t Y_t + D_{t+1} - (1 + r_t^D) D_t + D_{t+1} - (1 + r_t^D) D_t - \frac{\psi_t^D}{2} \left( r_{t+1}^D D_{t+1} - \overline{rD} \right)^2, \quad (18)$$

- ▶ Quadratic adjustment cost parameter:  $\psi_t^D$ ;  $D$  v.s.  $r^D D$
- ▶  $\Phi_t$ : Residual component.

# Government Optimization

- FOCs imply:

$$\frac{C_{t+j+1}^G}{C_{t+j}^G} = \beta_C \frac{1 + r_{t+j+1}^D}{1 - \psi_{t+j}^D r_{t+j+1}^D (r_{t+j+1}^D D_{t+j+1} - \bar{rD})}, \quad (19)$$

$$\begin{aligned} \frac{C_{t+j+1}^G}{C_{t+j}^G} = & \beta_C \left( \tau_{t+j+1} \frac{\partial Y_{t+j+1}}{\partial G_{it+j+1}} + q_{t+j+1}^G (1 - \delta) \right) \\ & + \frac{1}{(1 - \rho)(1 + \omega) q_{t+j}^G} \left( \beta_C \rho \frac{C_{t+j+1}^G}{C_{t+j+1,t+j+1}^H} \frac{\partial Y_{t+j+1}^H}{\partial G_{it+j+1}} + \kappa_{it+j} \frac{C_{t+j+1}^G}{G_{it+j+1}} \right). \end{aligned} \quad (20)$$

- RHS of equation (20): Economic returns; spillover effects through household consumption; political gains.

# External Calibration: Time-Invariant Parameters

Table 2: Externally Calibrated Time-Invariant Parameters

| Parameters           | Value | Target   |
|----------------------|-------|--|
| $\alpha_K$           | 0.312 | $\alpha_G + \alpha_K = \alpha = 0.362$ (Hayashi and Prescott (2002)) |
| $\alpha_G$           | 0.050 | Song and Xiong (2024)  |
| $\alpha_L$           | 0.538 | land share = 0.1   |
| annualized $\delta$  | 0.089 | capital depreciate rate in Hayashi and Prescott (2002)               |
| annualized $\beta$   | 0.980 |  |
| annualized $\beta_C$ | 0.850 | 25% probability of staying in office in a full decade                |
| $\rho$               | 0.965 | government to household consumption ratio in 1983-1992               |
| annualized $g_A$     | 0.005 | 0.5% annual TFP growth   |

# External Calibration: Time-Varying Parameters

Table 3: Externally Calibrated Time-Varying Parameters

| Parameters              | $t = 0$ (83-92) | $t = 1$ (93-02) | $t = 2$ (03-12) | Target                                    |
|-------------------------|-----------------|-----------------|-----------------|---|
| $q_t$                   | 1.40            | 1.41            | 1.45            | relative price of fixed capital formation |
| $\tau_t$ (%)            | 23.26           | 21.26           | 21.17           | total government revenue to GDP ratio     |
| $r_t^K$ (annualized, %) | 3.56            | 1.77            | 0.61            | rental rate of private capital            |

Table 4: Calibration of Regional Parameters

| Parameters    | Target   |
|---------------|--|
| $A_{it}$      | $\log A_{it} = \log Y_{it} - \alpha_G \log G_{it} - \alpha_K \log K_{it} - \alpha_L \log L_{it}$ |
| $\tau_{it}^K$ | $1 + \tau_{it}^K \propto \frac{Y_{it}}{K_{it}}, \sum_{i=1}^N \tau_{it}^K K_{it} = 0$             |
| $\tau_{it}^L$ | $1 + \tau_{it}^L \propto \frac{Y_{it}}{L_{it}}, \sum_{i=1}^N \tau_{it}^L L_{it} = 0$             |



# Expectation

- ▶ Variables for  $t > 2$  ( $t = 1$  for Lost Decade):
  - ▶  $A_{it} = \hat{A}_{it}A_t$ , where  $A_t$  grows at the constant rate  $g_A$  for  $t > 2$ .
  - ▶  $X_t = X_2$  for the other time-varying parameters with  $t > 2$ .
- ▶ Expectations:
  - ▶ Perfect foresight for aggregate TFP growth.
  - ▶ MIT-shock on  $X_t = \{i_{t+1}, \pi_t, i_t(m), \psi_t^D, \tau_t, \Phi_t, T_t, \{\tau_{it}^K\}, \{\tau_{it}^L\}, \{\kappa_{it}\}, \{\hat{A}_{it}\}\}$ ,

$$\mathbb{E}_t[X_{t+j}] = X_t, \quad \forall j \geq 1. \quad (21)$$

## Expected Interest Rate

► Expected real interest rate:  $\forall j \geq 1$ ,

►  $\mathbb{E}_t[r_{t+j}^D] = \mathbb{E}_t[i_{t+j}^D - \pi_{t+j}]$

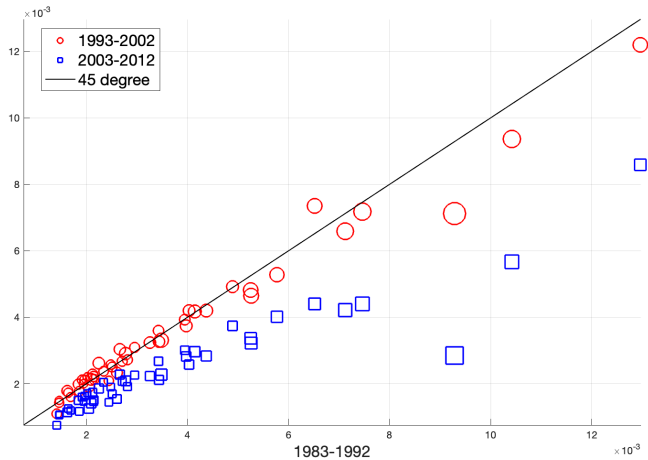
Table 5: Expected Interest Rates (%)

|                       | $t = 1$ (93-02) | $t = 2$ (03-12) | $t = 3$ (13-22) |
|-----------------------|-----------------|-----------------|-----------------|
| $i_t^D$               | 3.71            | 1.40            | 0.95            |
| $\mathbb{E}_0[i_t^D]$ | 5.03            | 4.60            | 4.60            |
| $\mathbb{E}_1[i_t^D]$ | -               | 1.12            | 0.85            |
| $\mathbb{E}_2[i_t^D]$ | -               | -               | 0.96            |
| $r_t^D$               | 3.53            | 1.53            | 0.94            |
| $\mathbb{E}_0[r_t^D]$ | 3.24            | 2.80            | 2.80            |
| $\mathbb{E}_1[r_t^D]$ | -               | 0.95            | 0.67            |
| $\mathbb{E}_2[r_t^D]$ | -               | -               | 1.09            |

# Internal Calibration

- ▶ The remaining parameters are internally calibrated to match the observed data:
  - ▶  $\{\kappa_{it}\}_{i=1}^N$  to match  $\{G_{it+1}\}_{i=1}^N$ ;
  - ▶  $\Phi_t$  to match  $C_t^G$ ;
  - ▶  $T_t$  to match  $C_t^H$ ;
  - ▶  $\psi_t^D$  to match  $D_{t+1}$ ;
  - ▶  $\overline{rD}$  to match an average adjustment cost that accounts for half of interest payments and management fees.

Figure 6: Prefecture-level  $\kappa_{it}$

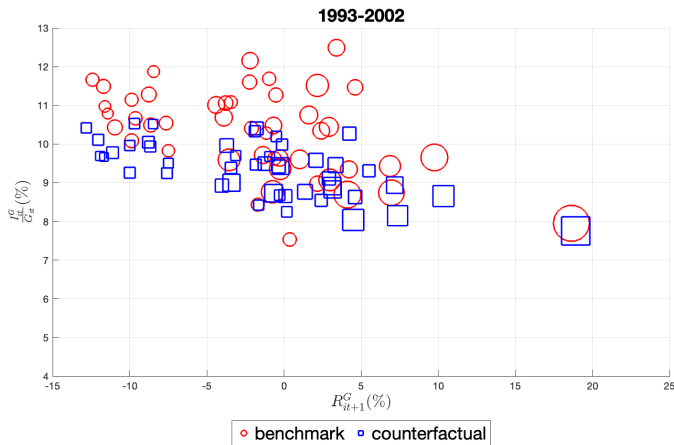


## Counterfactual: Lobby Incentives and Prefecture-level Wedges

- ▶ Set the local lobby capacity parameter in the lost decade to the average of pre- and post-Lost Decade levels:  $\kappa_{i1} = \frac{1}{2}(\kappa_{i0} + \kappa_{i2})$
- ▶ Set the local private capital or labor wedge in the lost decade to the average of pre- and post-Lost Decade levels:  $\tau_{i1}^K = \frac{1}{2}(\tau_{i0}^K + \tau_{i2}^K)$  or  $\tau_{i1}^L = \frac{1}{2}(\tau_{i0}^L + \tau_{i2}^L)$

# Counterfactual: Lobby Incentives

Figure 7:  $\kappa_{i1} = \frac{\kappa_{i0} + \kappa_{i2}}{2}$



## “Fiscal Windfalls”

- Following equation (2),  $\forall j \geq 0$ :

$$\mathbb{E}_t [\text{Windfall}_{t+j}] = -\Delta \mathbb{E}_t [r_{t+j}^D D_{t+j}] + \Delta \mathbb{E}_t [B_{t+j}] + \Delta \mathbb{E}_t [NB_{t+j}] \quad (22)$$

where  $NB_t \equiv \tau_t Y_t - \Phi_t - T_t$ .

Table 6: “Fiscal windfalls” perceived at 1993-2002 ( $t = 1$ , in percent of GDP)

|  | $t + j = 1$ (93-02) | $t + j = 2$ (03-12) | $t + j = 3$ (13-17) | steady state |
|--|---------------------|---------------------|---------------------|--------------|
| $\Delta \mathbb{E}_1 [-r_{t+j}^D D_{t+j}]$ | -0.27               | 1.40                | 1.39                | 1.47         |
| $\Delta \mathbb{E}_1 [B_{t+j}]$            | 5.55                | 7.68                | 1.38                | 1.08         |
| $\Delta \mathbb{E}_1 [NB_{t+j}]$           | -1.79               | -2.14               | -2.14               | -2.88        |
| $\mathbb{E}_1 [\text{Windfall}_{t+j}]$     | 3.49                | 6.94                | 0.63                | -0.33        |

## Counterfactual: Transferring “Fiscal Windfalls”

- ▶ Government commits to transferring “windfalls” perceived during 1993-2002 ( $\mathbb{E}_1[\text{Windfall}_{1+j}], j \geq 0$ ).
- ▶ Government prohibited from adjusting its borrowing (the same debt trajectory).
- ▶ Government can only optimize  $C_{t+j}^G$  and  $\{G_{it+j+1}\}_i$  for  $j \geq 0$  in each period  $t \geq 1$ .



Counterfactual:  $I_{it}^G \sim R_{it+1}^G$  at 1993-2002

Figure 8:  $\kappa_{i1} = \frac{\kappa_{i0} + \kappa_{i2}}{2}$

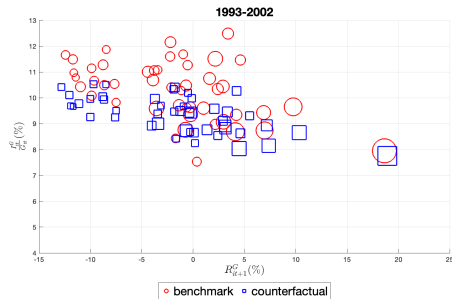
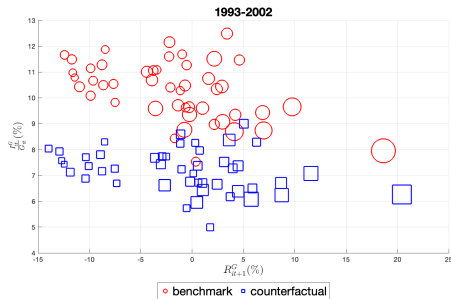


Figure 9: Transferring “Fiscal Windfalls”



## Counterfactual: Welfare Analysis

Table 7: Aggregate TFP, output and welfare changes (%)

|                                   | $\kappa_{i1} = \frac{\kappa_{i0} + \kappa_{i2}}{2}$ | $\tau_{i1}^K = \frac{\tau_{i0}^K + \tau_{i2}^K}{2}$ | $\tau_{i1}^L = \frac{\tau_{i0}^L + \tau_{i2}^L}{2}$ | transfers |
|-----------------------------------|---|---|---|-----------|
|                                   | (1)   | (2)   | (3)   | (4)       |
| Aggregate TFP change in 03-12     | 0.12  | -0.28   | -0.08   | 0.23      |
| Aggregate output change in 03-12  | -0.35   | -0.60   | -0.17   | -1.46     |
| Households income change in 93-02 | 0   | -1.18   | -0.49   | 4.41      |
| in 03-12                          | -0.26   | -0.77   | -0.28   | 8.92      |
| Welfare change ( $\varphi$ )      | -0.04   | -0.38   | -0.14   | 0.87      |

# The End of the Decade of Fiscal Misallocation

- ▶ Our story: Low interest rate regime (windfalls are gone)
- ▶ FILP Reform
- ▶ "Trinity Reforms" on central government transfers to local governments
  - ▶ Sticks: Fiscal restructuring (Yubari city)
  - ▶ Carrots: "Great Heisei Mergers"

# Conclusion

- ▶ Low-interest-induced misallocation as an understudied channel
  - ▶ Complementary to the literature on low interest rate and stagnation (zombie lending, Caballero, Hoshi and Kashyap (2008); overvalued (intangible) assets, Kiyotaki, Moore and Zhang (2021); misallocation via financial frictions, Asriyan et al. (2024))
- ▶ Implications for today's China
  - ▶  $\kappa_{it}$  as career incentives (Song and Xiong (2024))
  - ▶ Potential fiscal misallocation and welfare losses by debt swap and low interest rate

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# Forecasts Using Bond Issuance Data

Figure 10: Nominal borrowing rate

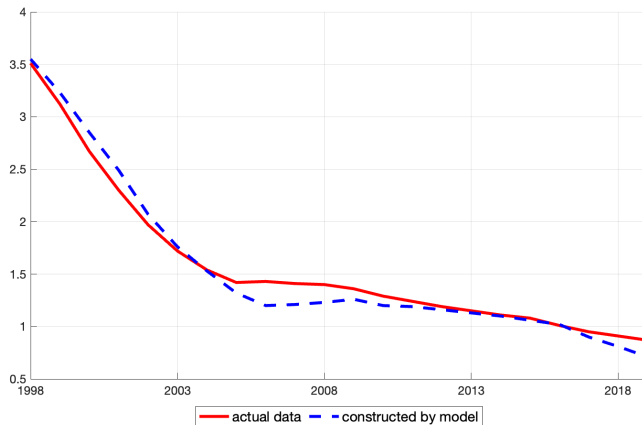
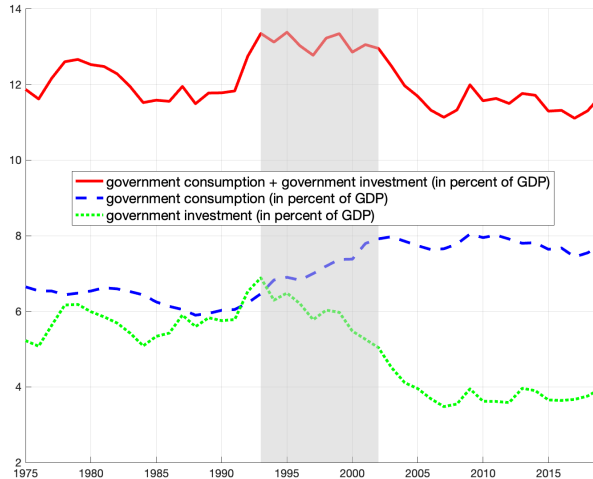


Table 8: Cross-Region Allocation

|                | 1978-82             | 1983-87             | 1988-92             | 1993-97             | 1998-02             | 2003-07             | 2008-12             | 2013-17             |
|----------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|
| $\log K_{it}$  |                     |                     |                     |                     |                     |                     |                     |                     |
| $\log G_{it}$  | 1.091***<br>(0.072) | 1.126***<br>(0.075) | 1.188***<br>(0.081) | 1.225***<br>(0.086) | 1.230***<br>(0.088) | 1.266***<br>(0.099) | 1.276***<br>(0.104) | 1.270***<br>(0.107) |
| Observations   | 47                  | 47                  | 47                  | 47                  | 47                  | 47                  | 47                  | 47                  |
| R <sup>2</sup> | 0.838               | 0.834               | 0.828               | 0.818               | 0.813               | 0.784               | 0.770               | 0.758               |
| $\log L_{it}$  |                     |                     |                     |                     |                     |                     |                     |                     |
| $\log G_{it}$  | 1.030***<br>(0.046) | 1.108***<br>(0.051) | 1.184***<br>(0.057) | 1.186***<br>(0.057) | 1.194***<br>(0.062) | 1.249***<br>(0.073) | 1.284***<br>(0.075) | 1.291***<br>(0.076) |
| Observations   | 47                  | 47                  | 47                  | 47                  | 47                  | 47                  | 47                  | 47                  |
| R <sup>2</sup> | 0.918               | 0.912               | 0.904               | 0.907               | 0.892               | 0.868               | 0.867               | 0.865               |

# Government Expenditure GDP Ratio

Figure 11: Government-to-Private Consumption and Investment Ratios (%)

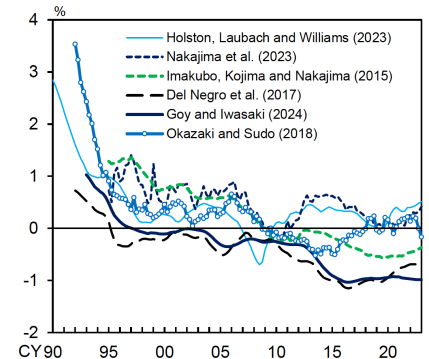




# Nature Rate of Interest and Expected Growth Rate

Figure 12: Natural Rate of Interest and Expected Growth Rate

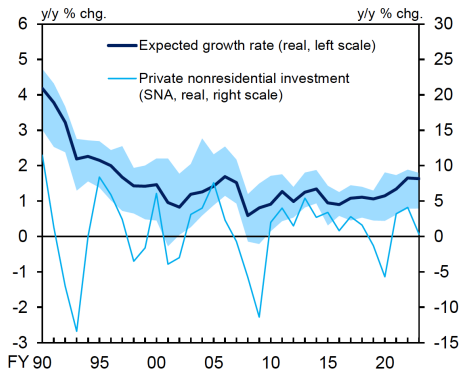
Chart 1-1-1: Natural Rate of Interest



Sources: Bank of Japan; Ministry of Finance; Ministry of Health, Labour and Welfare; Cabinet Office; Ministry of Internal Affairs and Communications; Bloomberg; Consensus Economics Inc., "Consensus Forecasts."

Note: The estimates are based on staff calculations using the models proposed in the different papers.

Chart 1-1-4: Expected Growth Rate



Source: Cabinet Office.

Note: The "expected growth rate" is the average of firms' forecasts of the real growth rate of industry demand over the next five years. The shaded area indicates the 20-80 percentile band of the expected growth rate.

Figure 13:  $D$  and  $r^D D$  (in percent of GDP)

