

# Bank Runs, Fragility, and Regulation

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NBER Summer Institute

The views expressed herein are those of the authors and not necessarily those of the Federal Reserve Bank of Minneapolis or the Federal Reserve System.

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**Today:** risk of bank runs induce banks to over-leverage even absent bailouts

# A Theory of Banking Regulation

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**Mechanism:**

- ▶ Higher equity buffers induce higher asset prices  
⇒ banks more “liquid” ⇒ less prone to (inefficient) runs

# Environment

- ▶ Three periods  $t = 0, 1, 2$ 
  - ▶ Idiosyncratic risk only – realized at  $t = 1$
- ▶ Technology
  - ▶ Production linear in capital
  - ▶ Capital in fixed supply  $K$

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- ▶ Technology
  - ▶ Production linear in capital
  - ▶ Capital in fixed supply  $K$
- ▶ Continuum of banks with concave utility
  - ▶ Identical initial deposits and capital  $b_0 = B_0, k_0 = K$
  - ▶ Constant productivity  $z$  under repayment
  - ▶ Can default at  $t = 1, 2$  – outside option shock at  $t = 1$
- ▶ Creditors: linear utility and discount rate  $R$

# Individual Bank Problem

# Preferences and budget constraints

► Preferences

$$u(c_0) + \beta \mathbb{E}u(c_1) + \beta^2 \mathbb{E}u(c_2),$$

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$$c_0 = (z + p_0)k_0 - Rb_0 + q_0(b_1, k_1)b_1 - p_0k_1,$$

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## Banks Outside Options: Default Values

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- ▶ Default triggers
  - ▶ Loss in productivity or capital
  - ▶ Exclusion from borrowing and capital markets

## Banks Outside Options: Default Values

- ▶ Period 2 value

$$V_2^D(k_2) = u(z_2^D k_2)$$

- ▶  $z_2^D$  is predetermined and common across banks.

- ▶ Period 1 value

$$V_1^D(k_1, z_1^D) = u(z_1^D k_1) + \beta u(z_2^D k_1)$$

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$V^D$  independent of prices (and increasing in  $k$ )

- ▶ Generates a standard endogenous borrowing limit

## Period 2: Bank Problem

$$V_2(b_2, k_2) = \max_{d_2 \in \{0,1\}} \left\{ (1 - d_2)u(zk_2 - Rb_2) + d_2u(z_2^D k_2) \right\}$$

Default choice:

$$d_2(b_2, k_2) = \begin{cases} 1 & \text{if } Rb_2 > \phi k_2, \text{ where } \phi \equiv z - z_2^D \\ 0 & \text{otherwise,} \end{cases}$$

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$$\text{s.t. } c_1 = n_1 + b_2 - p_1 k_2$$

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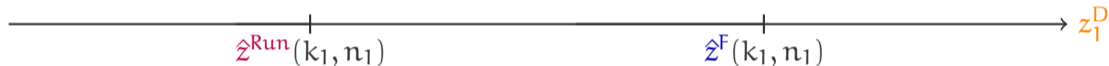
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Vulnerable to self-fulfilling runs when  $V_1^{\text{Run}}(n_1) < V_1^D(k_1, z_1^D) \leq V_1^R(n_1)$

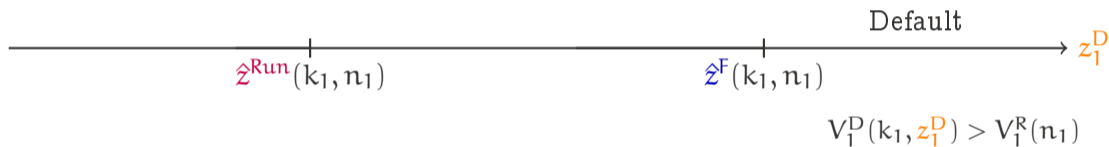
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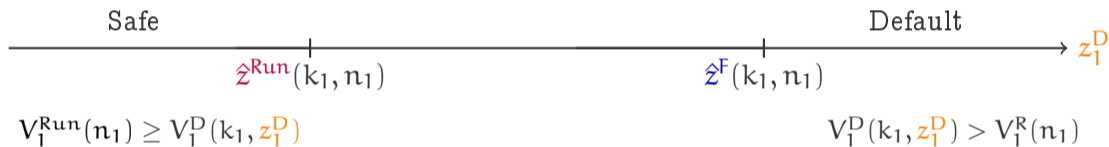
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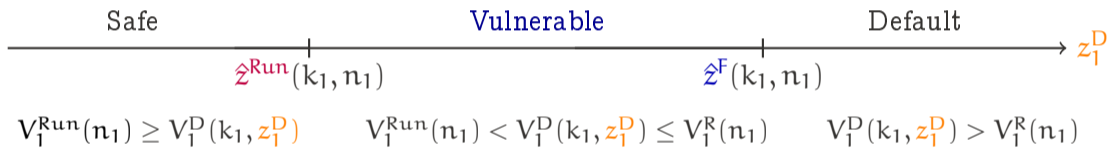
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Runs occur despite assets being liquid (Amador-Bianchi 2024)

- ▶ When  $R^K > R$ , leverage raises expected profits
  - A run prevents bank from leveraging  $\Rightarrow$  reduces profits and value of repayment  $\Rightarrow$  run may become self-fulfilling,  $\hat{z}^{Run} < \hat{z}^F$

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- ▶ Instead, if  $R^{\text{K}} = R$ , defaults only occur due to fundamentals  $\hat{z}^{\text{Run}} = \hat{z}^{\text{F}}$ .

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- ▶ Sunspot: If **vulnerable**, we assume a bank faces run with probability  $\lambda$ .



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⇒ Default probability for individual bank

$$d_1(n_1, k_1, z_1^{\text{D}}) = \begin{cases} 0 & \text{if } z_1^{\text{D}} \leq \hat{z}^{\text{Run}}(n_1, k_1) \\ \lambda & \text{if } \hat{z}^{\text{Run}}(n_1, k_1) < z_1^{\text{D}} \leq \hat{z}^{\text{F}}(n_1, k_1) \\ 1 & \text{if } z_1^{\text{D}} > \hat{z}^{\text{F}}(n_1, k_1) \end{cases}$$

## Period 0: Value and Leverage Choice

$$V_0(\mathbf{n}_0) = \max_{c_0 \geq 0, k_1 \geq 0, b_1} u(c_0) + \beta \int_{\underline{z}}^{\bar{z}} \left[ d_1(\mathbf{n}_1, k_1, \tilde{z}) V_1^D(k_1, \tilde{z}) + (1 - d_1(\mathbf{n}_1, k_1, \tilde{z})) V_1^R(\mathbf{n}_1) \right] dF(\tilde{z})$$

subject to

$$c_0 = \mathbf{n}_0 + q_0(\mathbf{n}_1, k_1) b_1 - p_0 k_1,$$

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where the bond price is given by

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Deposits allow for higher portfolio returns and  $c_0$ , but raises exposure to default

# Competitive Equilibrium

## Definition

Given  $B_0$ , and a run probability,  $\lambda$ , a *symmetric competitive equilibrium* consists of  $\{p_0, p_1, q_0, \hat{z}^F, \hat{z}^{\text{Run}}, d_1, d_2, V_1^R, V_1^D, b_1, k_1, b_2, k_2\}$  such that:

- (a) Banks optimize
- (b) Investors break even

$$q_0(n_1, k_1) = (1 - \lambda)F(\hat{z}^F(n_1, k_1)) + \lambda F(\hat{z}^{\text{Run}}(n_1, k_1))$$

- (d) The market for capital clears
  - ▶ Aggregate demand for capital equals  $K$  at  $t = 0, 1$ .

## Equilibrium at $t = 1$

- ▶ Characterization in terms of **leverage**  $l_1 = b_1/k_1$ 
  - ▶ Redefine thresholds as  $\hat{z}^F(l_1|p_1)$ ,  $\hat{z}^{\text{Run}}(l_1|p_1)$
  - ▶ In the aggregate  $L_1 = b_1/K$
- ▶ Share of banks defaulting is increasing in  $L_1$ :

$$\underbrace{[1 - F(\hat{z}^F(L_1|p_1))]}_{\text{Fundamentals}} + \lambda \underbrace{[F(\hat{z}^F(L_1|p_1)) - F(\hat{z}^{\text{Run}}(L_1|p_1))]}_{\text{Runs}}$$

- ▶ Price for capital  $p_1$  decreasing in  $L_1$  when banks are constrained

$$p_1(L_1) \equiv \begin{cases} \frac{z}{R} & \text{if } L_1 \leq \hat{L}, \\ \beta z + (1 + \beta) \frac{\phi}{R} - \beta R L_1 & \text{if } L_1 \in (\hat{L}, \bar{L}). \end{cases}$$

# Roadmap for Normative Analysis

- ▶ Constrained-efficient planner problem
- ▶ Evaluate competitive equilibrium vs. constrained-efficient
  - ▶ Without runs  $\lambda = 0$
  - ▶ With runs  $\lambda > 0$

## Constrained-Efficient Leverage

- ▶ Planner chooses  $L_1$  and banks retain all other decisions
  - ▶ Market for capital clears competitively in period 1
  - ▶ Banks choose default decisions at  $t = 1, 2$

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and where:

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Creditors remain indifferent

# Analysis without Runs

## Proposition (Constrained-efficiency)

*Suppose  $\lambda = 0$ . Any competitive equilibrium is constrained efficient.*

## Prelude for the Proof

Lemma: Consider any aggregate leverage  $L_1$  and its associated price  $p_1 = \mathcal{P}_1(L_1)$

$$(i) V_1^R((z+)K - RKL_1|p_1) \leq V_1^R((z + \hat{p}_1)K - RKL_1|\hat{p}_1);$$

$$(ii) q_0(L_1|p_1) \leq q_0(L_1|\hat{p}_1),$$

with the first inequality is strict if  $\hat{p}_1 \neq p_1$ .

Key idea:

- ▶ In equilibrium, banks are neither net buyers nor net sellers
  - ▶ If price deviates from eqm. one, value of repayment goes up (for same leverage).

## Proof of Constrained-Efficiency with $\lambda = 0$

Let  $L^E$  and  $L^P$  be the competitive eqm. and planner's leverage

Associated prices:  $p_1^E = \mathcal{P}(L^E)$  and  $p_1^P = \mathcal{P}(L^P)$

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- In the competitive eqm., banks prefer  $(L^E, K)$  rather than  $(L^P, K)$  when facing  $p_1^E$ :

$$\begin{aligned} & u(zK - RB_0 + q_0(L^E|p_1^E)L^EK) + \beta \mathbb{E}V_1(L^E, K|p_1^E) \\ & \geq u(zK - RB_0 + q_0(L^P|p_1^E)L^PK) + \beta \mathbb{E}V_1(L^P, K|p_1^E). \end{aligned}$$

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By prev. lemma:  $\mathbb{E}V_1(L^P, K|p_1^E) \geq \mathbb{E}V_1(L^P, K|p_1^P)$

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$\Rightarrow$  Banks can achieve weakly higher utility than planner.

But planner can also choose  $L^E$ .

$\Rightarrow L^E$  must solve the planner's problem

## Uniqueness and Existence

### Proposition (Uniqueness)

*Suppose that: (i) there is a unique solution to the planner problem, or (ii) there exists a competitive equilibrium with leverage  $L_1 = B_1/K > \hat{L}$ .*

*Then, there is at most one (symmetric pure-strategy) competitive equilibrium.*

### Proposition (Existence)

*Suppose that Assumption 2 holds and*

- i)  $f$  is continuous and such that  $f(\underline{z}) = f(\bar{z}) = 0$ .*
- ii)  $\left[ \frac{1-F(z)}{1+\beta} + \frac{f(z)}{F(z)}z \right]$  is decreasing in  $z$  for any  $z \in [\underline{z}, \bar{z}]$ .*

*Then, there  $\exists$  a competitive equilibrium.*

Available theorems with default risk only in *partial equilibrium*

Economy with runs  $\lambda > 0$

## Preview: Thresholds as a Function of Aggregate Leverage

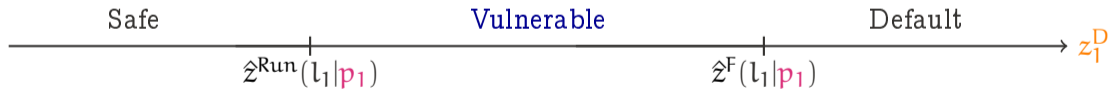
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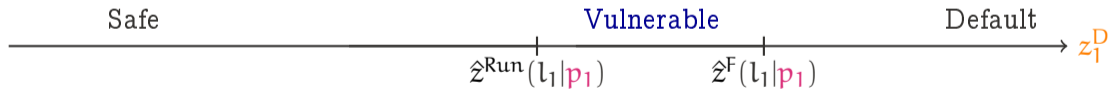
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## Preview: Thresholds as a Function of Aggregate Leverage

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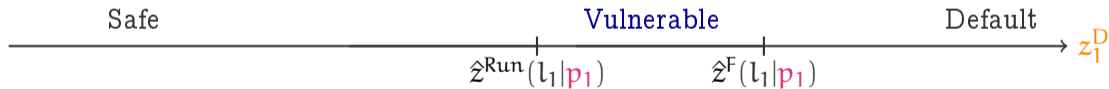
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- ▶ Zero *first-order* effects on  $\hat{z}^F$  (neither net buyer nor net seller)
- ▶ But  $\uparrow \hat{z}^{\text{Run}}$  because banks are net sellers in a run
  - ▶ Not internalized by individual banks





## Over-leverage with $\lambda > 0$

$$\begin{aligned}
 \frac{1}{c_0} - \frac{\beta R}{c_1} &= - \frac{(1 - \lambda)f(\hat{z}^F) \frac{\partial \hat{z}^F}{\partial L_1} + \lambda f(\hat{z}^{\text{Run}}) \frac{\partial \hat{z}^{\text{Run}}}{\partial L_1}}{q_0} \frac{L_1}{c_0} \\
 &- \frac{\lambda f(\hat{z}^{\text{Run}}) \frac{\partial \hat{z}^{\text{Run}}}{\partial L_1}}{q_0} \frac{\beta}{K} \left[ V_1^R(n_1|p_1) - V_1^D(K, \hat{z}^{\text{Run}}) \right] \\
 &- \frac{\lambda f(\hat{z}^{\text{Run}})}{q_0} \underbrace{\frac{\partial \hat{z}^{\text{Run}}(L_1|p_1)}{\partial p_1} \mathcal{P}'_1(L_1)}_{\text{G.E.}} \left[ \frac{L_1}{c_0} + \frac{\beta}{K} \left[ V_1^R(n_1|p_1) - V_1^D(K, \hat{z}^{\text{Run}}) \right] \right]
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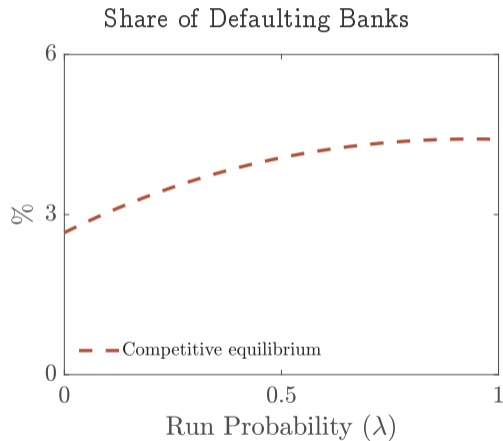
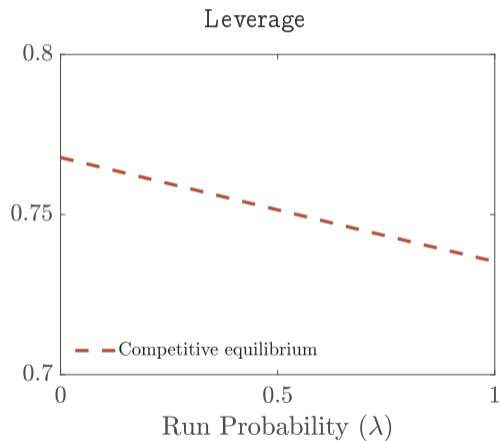
$$- \frac{\lambda f(\hat{z}^{\text{Run}}) \frac{\partial \hat{z}^{\text{Run}}}{\partial L_1}}{q_0} \frac{\beta}{K} \left[ V_1^R(n_1|p_1) - V_1^D(K, \hat{z}^{\text{Run}}) \right]$$

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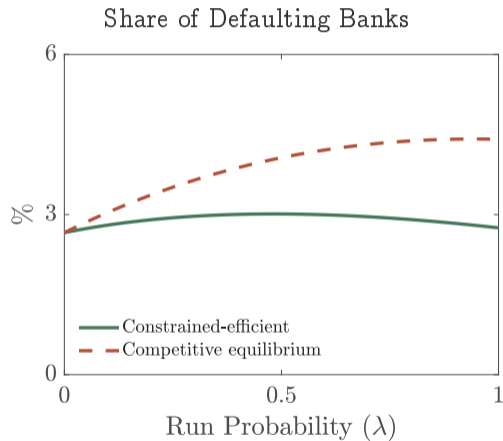
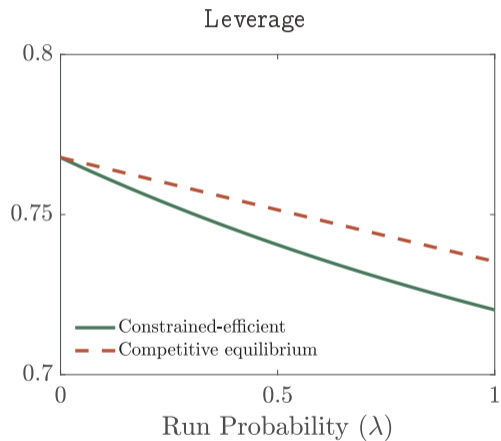
$$- \frac{\lambda f(\hat{z}^{\text{Run}})}{q_0} \underbrace{\frac{\partial \hat{z}^{\text{Run}}(L_1|p_1)}{\partial p_1} \mathcal{P}'_1(L_1)}_{\text{G.E.}} \left[ \frac{L_1}{c_0} + \frac{\beta}{K} \left[ V_1^R(n_1|p_1) - V_1^D(K, \hat{z}^{\text{Run}}) \right] \right]$$

- ▶ An increase in  $p_1$  helps  $\uparrow V^{\text{Run}}$  because banks facing a run are net sellers  
 $k_1^{\text{Run}} < K \Rightarrow$  fewer banks vulnerable
- ▶ Planner internalizes that  $\downarrow L_1$  leads to  $\uparrow p_1$  and fewer runs

# Competitive Eqm. vs. Constrained Efficient



# Competitive Eqm. vs. Constrained Efficient

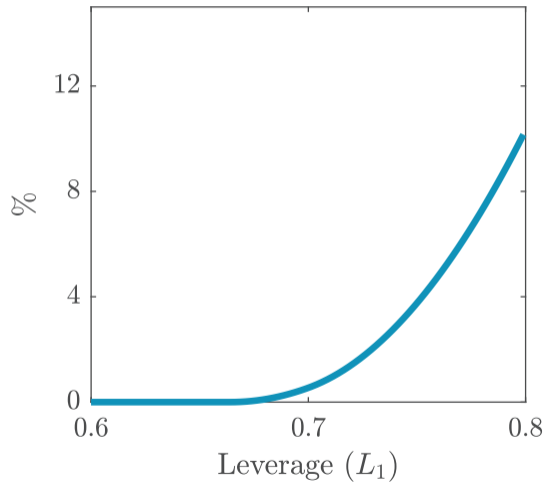


# Conclusions

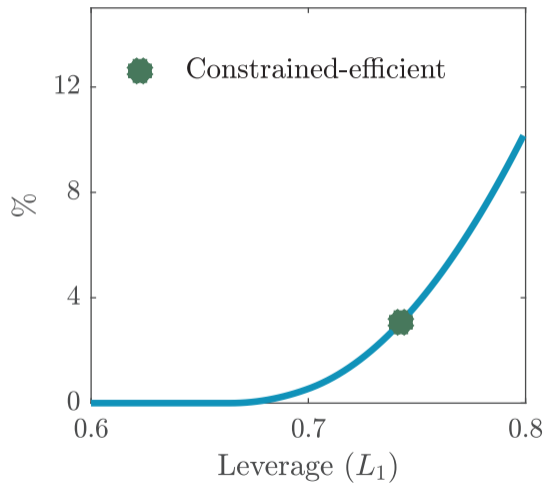
- ▶ A macroprudential theory of banking regulation under self-fulfilling runs
- ▶ Banks do not internalize that by raising leverage
  - ▶ they contribute to lower asset prices
  - ▶ making other banks more vulnerable to runs
- ▶ Higher capital requirements can implement the constrained-efficient allocation



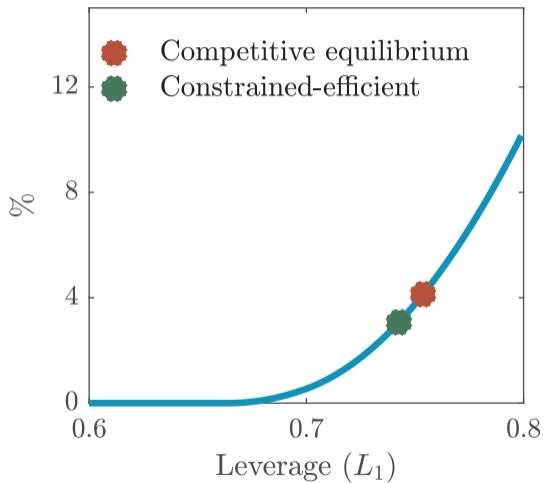
## Share of Defaulting Banks



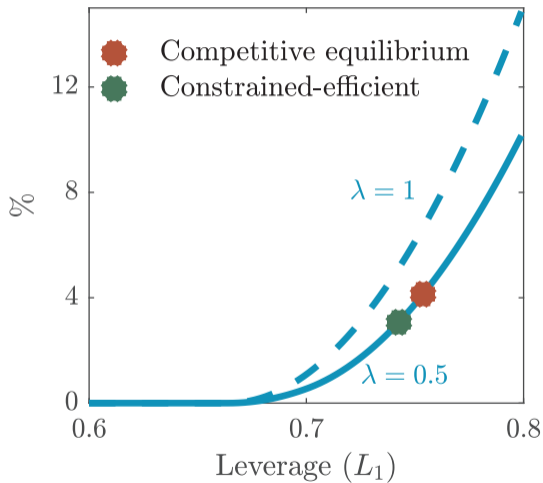
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