

Supply Chain Disruptions, the Structure of Production Networks, and the Impact of Globalization

Matthew Elliott
Cambridge

Matthew O. Jackson
Stanford

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BUSINESS

Tesla to Halt Production in Germany as Red Sea Conflict Hits Supply Chains

Disruption related to attacks on ships by Houthi rebels raise risk of supply-chain crisis in Europe

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Updated Jan. 12, 2024 1:45 pm ET

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Yemen-based, Iran-backed Houthi fighters have launched successive attacks on commercial ships navigating the crucial trade route in recent months,

This paper: tractable model of (global, complex) supply chains to:

- characterize short-run impact of a shock,
- contrast with long-run impact,
- investigate how impact depends on complexity,
- examine impact of globalization on fragility.

Some Related Literature

- **Foundational work:** Leontief (1936), Long Jr and Plosser (1983), Acemoglu et al. (2012)
- **Surveys:** Bernard (2018), Carvalho and Tahbaz-Salehi (2019), Baqaee and Rubbo (2022), Antràs and Chor (2022), Elliott and Golub (2022), Baldwin and Freeman (2022).
- **Production networks:** e.g., Brummitt et al. (2017), Baqaee (2018), Oberfield (2018), Acemoglu and Tahbaz-Salehi (2020), Acemoglu and Azar (2020), Baqaee and Farhi (2021), Kopytov et al. (2021), Elliott et al. (2022), Bui et al. (2022), König et al. (2022), Pellet and Tahbaz-Salehi (2023), Grossman et al. (forthcoming), Grossman et al. (2023a), Grossman et al. (2023b)
- **Trade networks:** e.g., Chaney (2014), Bernard et al. (2019)
- **Micro network structure:** e.g., Bimpikis et al. (2018), Bimpikis et al. (2019), Amelkin and Vohra (2020)

Outline

1 Introduction

2 Model

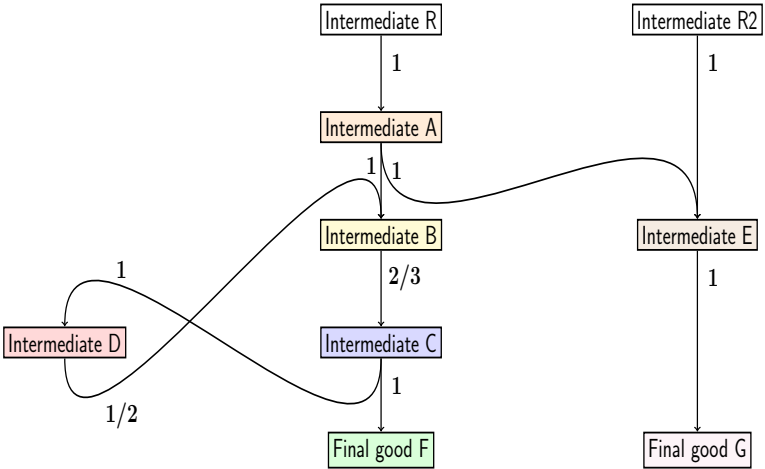
Arrow-Debreu (1954) Technologies

Constant returns to scale technologies τ

$$\left(\text{labor}, \underbrace{m_1, \dots, m_M}_{\text{intermediate}}, \underbrace{f_1, \dots, f_F}_{\text{final goods}} \right)$$

e.g., $(-2, 0, -3, 0, 1)$: 2 units labor & 3 units m_2 make 1 unit f_2 .

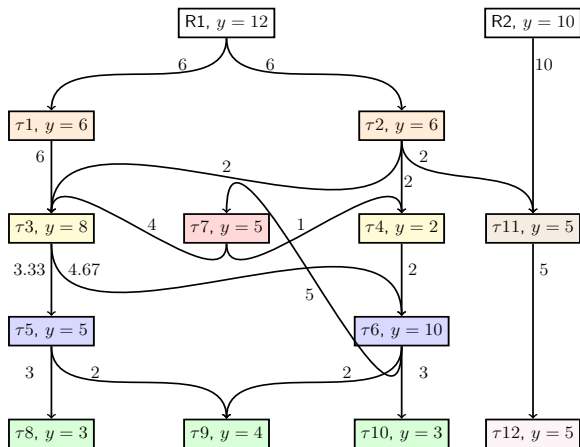
Example: Technologies



Equilibrium (in Paper)

- Laborers
 - ▶ supply labor inelastically
 - ▶ have homothetic preferences for final goods
- Producers maximize profits (price takers)
- Markets clear - Standard Arrow Debreu equilibrium

Example: Equilibrium Flows (Can Include Cycles)



Shock Impact

For τ , with output k , normalized $\tau_k = 1$.

Let's vary τ_k to capture shocks/disruptions

Analyze/contrast:

- **Long run:** new equilibrium using shocked technologies,
- **Short run:** work with existing supplies/shortages.

Long-Run: Hulten's Theorem

Proposition (Hulten's Theorem)

Consider a (generic) equilibrium and technology τ , with $O(\tau) = k$, used in positive amounts in equilibrium. Then

$$\frac{\partial \log(U)}{\partial \log(\tau_k)} = \frac{\partial \log(GDP)}{\partial \log(\tau_k)} = \frac{p_\tau y_\tau}{GDP}.$$

Long-Run: Hulten's Theorem

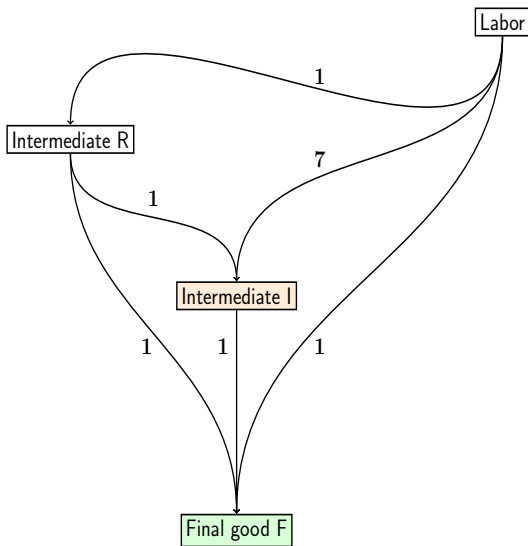
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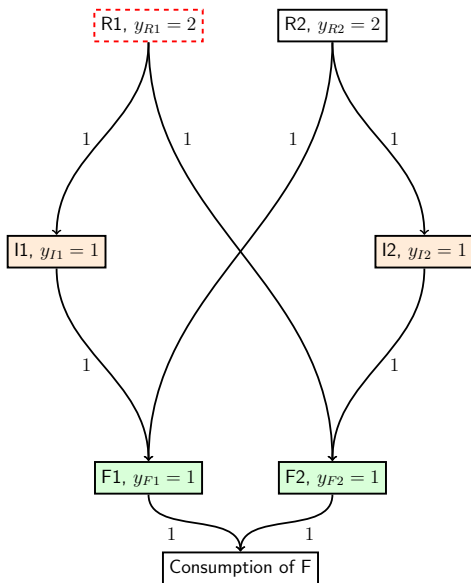
- Sufficient statistic: spending on shocked technology.
- Intuition—adjust by sourcing more inputs at the margin.
- Network matters in background as it determines equilibrium
 - ▶ but don't need to see network to estimate long-run impact.

Figure: Technologies



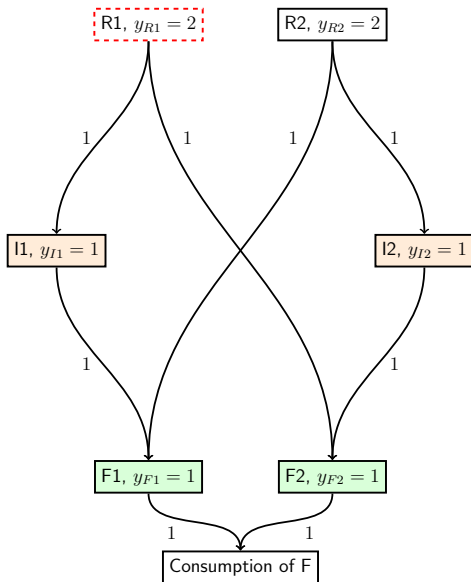
Labor endowment: 20

Figure: Equilibrium flow network



$$p = \left(\underbrace{\frac{1}{10}}_{\text{labor}}, \underbrace{\frac{1}{10}}_R, \underbrace{\frac{4}{5}}_I, \underbrace{1}_F \right)$$

Figure: Equilibrium flow network



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$$p = \left(\underbrace{\frac{1}{10}}_{\text{labor}}, \underbrace{\frac{1}{10}}_R, \underbrace{\frac{4}{5}}_I, \underbrace{1}_F \right)$$

$$GDP = \sum_f p_f c_f = 2.$$

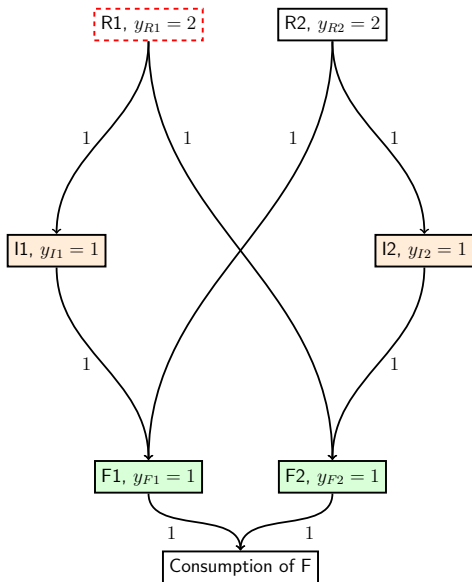
$$p_{R1} = 1/10$$

$$y_{R1} = 2$$

Marginal impact:

$$\frac{p_{R1} y_{R1}}{GDP} = \frac{1}{10}$$

Figure: Equilibrium flow network



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Extrapolating for a 50% shock,

Total impact: 1/20th of GDP

Larry Summers 2013

“There would be a set of economists who would sit around explaining that electricity was only 4% of the economy, and so if you lost 80% of electricity, you couldn't possibly have lost more than 3% of the economy...[However,] we would understand that [...] when there wasn't any electricity, there wasn't really going to be much economy.”

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Limitations:

- Result at the *margin* (relies on Envelope Theorem)
 - ▶ Baqaee and Farhi (2019)—second order effects can matter
- *Long-Run* re-optimization of production
 - ▶ Takes time—different impact in the short run.

Short-Run Impact of a Shock

Hulten: Production is perfectly flexible and fully adjusts.
(Marginal result.)

Now: Opposite benchmark with no adjustments.
(Our result holds away from the margin.)

- Cannot adjust the technologies being used.
- Cannot source additional units from alternative suppliers.
- Prices cannot adjust—rationing of disrupted goods is proportional

Figure: Shock Propagation

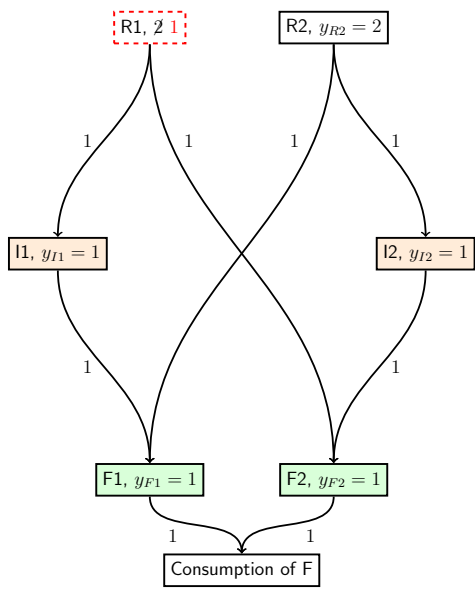


Figure: Shock Propagation

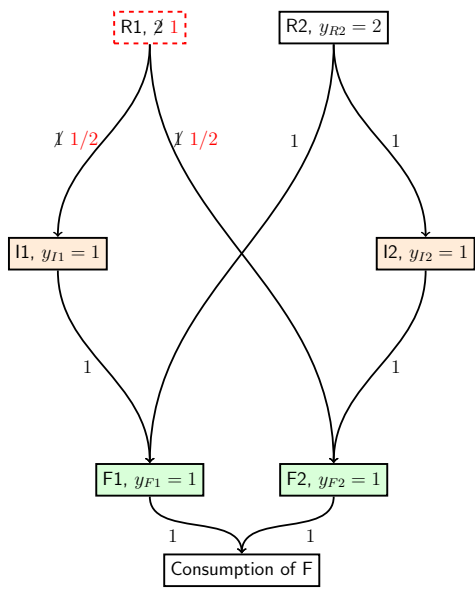


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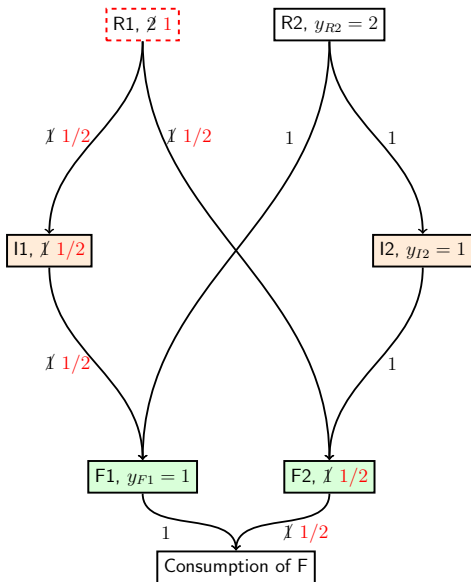
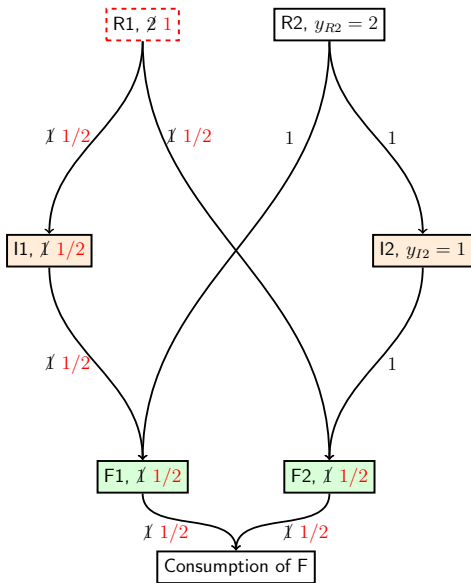


Figure: Shock Propagation



Total impact: $1/2$ of GDP

(versus $1/20$ th in long run)

Shock Propagation Algorithm

Define an algorithm that traces shock (like example): it converges to the unique solution of a minimum disruption problem (in paper).

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Let $F(\Psi)$ be the final goods that can be affected by shocks

Proposition (Upper Bound)

Consider a shock that reduces the output of technologies $\tau \in \Psi$ to $\lambda < 1$ of their original levels. The proportion of lost GDP is bounded above by

$$(1 - \lambda) \left(\frac{\sum_{f \in F(\Psi)} p_f c_f}{GDP} \right).$$

Hulten's Theorem Comparison

Long Run, Hulten's Theorem,

$$\frac{\partial \log(U)}{\partial \log(\tau_k)} = \frac{\partial \log(GDP)}{\partial \log(\tau_k)} = \frac{p_\tau y_\tau}{GDP}.$$

Short Run, when bound binds

$$\frac{\Delta \log(U)}{\Delta \log(\lambda)} = \frac{\Delta \log(GDP)}{\Delta \log(\lambda)} = \frac{(1 - \lambda) \sum_{f \in F(\tau)} p_f c_f}{GDP}.$$

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- Long Run: shocking more expensive technologies has a larger impact.
 - ▶ Might expect these to be more *downstream*.
- Short Run: shocking technologies that are used in more final goods has a larger impact.
 - ▶ Might expect these to be more *upstream*.

Sufficient Conditions for Bound to Bite

- All producers of given good and any “substitute” for it in a supply chain are shocked.
- Globalization: for low iceberg costs generically get unique technologies used.
- Other sufficient conditions in paper.

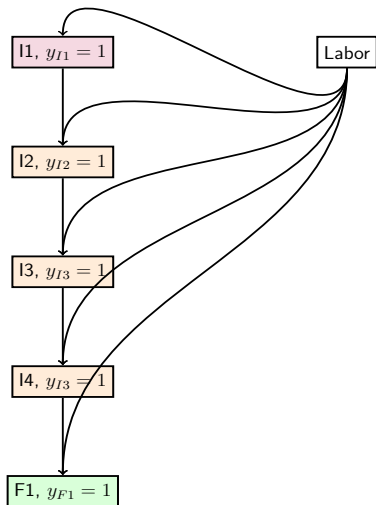
Supply Chain Complexity and Disruption

Under the bound, randomly disrupt technology to $\lambda < 1$:

- Probability π disrupt any given technology, independent.
- S = average # technologies used produce a final good.
- $q = E[(\text{cost of random input})/(\text{final good cost})]$.

Figure: Vertical supply chain

(All flows equal 1)



Labor endowment: 5

$$p = \left(\underbrace{\frac{1}{5}}_{\text{labor}}, \underbrace{\frac{1}{5}}_{I1}, \underbrace{\frac{2}{5}}_{I2}, \underbrace{\frac{3}{5}}_{I3}, \underbrace{\frac{4}{5}}_{I4}, \underbrace{1}_F \right)$$

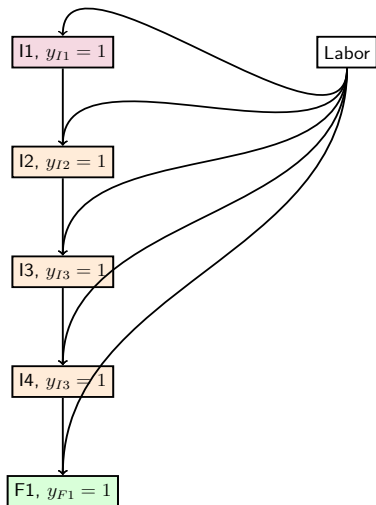
Complexity: $S = 5$.

Average input cost: $1/2$

Average input cost / final good cost: $q = 1/2$

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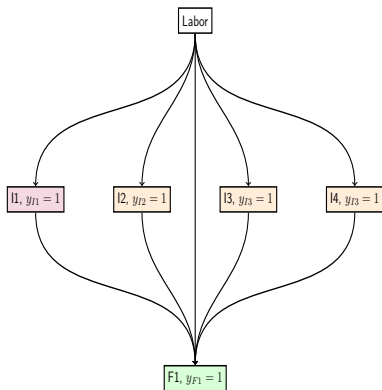
Average input cost / final good cost: $q = 1/2$

SR marginal impact of shock to inter.: 1

LR Av. marginal impact of shock to inter.: $1/2$

Figure: Horizontal supply chain

(All flows equal 1)



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$$p = \left(\underbrace{\frac{1}{5}}_{\text{labor}}, \underbrace{\frac{1}{5}}_{I1}, \underbrace{\frac{1}{5}}_{I2}, \underbrace{\frac{1}{5}}_{I3}, \underbrace{\frac{1}{5}}_{I4}, \underbrace{1}_F \right)$$

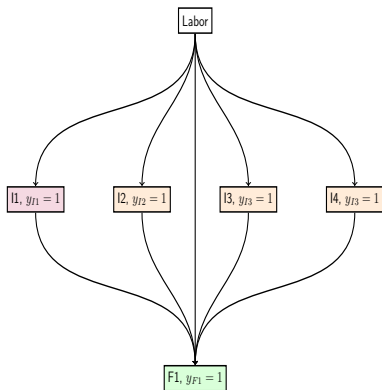
Complexity: $S = 5$.

Average input cost: $1/S = 1/5$

Average input cost / final good cost: $q = 1/5$

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Average input cost / final good cost: $q = 1/5$

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Supply Chain Complexity and Disruption

Proposition (Complexity and Fragility)

For small π

$$\text{Short-Run } \mathbb{E} \left[\frac{\Delta GDP}{GDP} \right] \approx -(1 - \lambda)\pi S,$$

$$\text{Long-Run } \mathbb{E} \left[\frac{\Delta GDP}{GDP} \right] \approx -(1 - \lambda)\pi Sq.$$

Supply Chain Complexity and Disruption

Short Run:

- Increased number of goods (S) per supply chain to disrupt,
- Each would disrupt the final good fully (by $1 - \lambda$).
- Overall effect $(1 - \lambda)\pi S$.

Long Run:

- Increased number of goods (S) per supply chain to disrupt,
- But each has a fractional value (q) relative to final good.
- Overall effect $(1 - \lambda)\pi S q$.

Supply Chain Complexity and Disruption

Short Run — *shape (breadth vs depth) of supply chain is irrelevant:*

- Increased number of goods (S) per supply chain to disrupt,
- Each would disrupt the final good fully (by $1 - \lambda$),
- Overall effect $(1 - \lambda)\pi S$.

Long Run — *shape of supply chain matters:*

- Supply chains are horizontal, $q \approx 1/S$: overall effect $(1 - \lambda)\pi$.
- Supply chains are vertical, $q \approx 1/2$: overall effect $(1 - \lambda)\pi S/2$.

Concluding remarks

- Short and long run can differ dramatically, both very tractable.
- Range of outcomes between the short and long run.
- Anticipation, inventories, buffers, not in model.
- Diversity is good (rather than globalization is bad).
- Policy implications (within model): subsidize diversity and shallow supply chains.

Discussion

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