COUNTRIES FOR OLD MEN: AN ANALYSIS OF THE AGE WAGE GAP

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- Can a larger supply of older workers be compatible with age wage gap increase?
 - Obviously, classic imperfect substitutability + supply story cannot explain this trend
- This paper: more older workers generate negative spillovers on younger cohorts
 - provide conceptual framework, show consistent evidence, and test for alternatives

Negative career spillovers in firms: success of older might come at cost for younger

This paper

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 - cannot fully renegotiate wages and job allocation of older workers
 - · firms have limited resources: cannot promote everyone who deserves it

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 - firms have limited resources: cannot promote everyone who deserves it
 - more spillovers if: more older workers, and/or retirement delays, and/or growth slowdown
- **•** Derive following predictions from increased supply of older workers:
 - 1. deterioration in wages of younger: crowd out from top jobs, not change in wage premia
 - 2. deterioration from both lower entry position and lower growth over lifecycle
 - 3. crowd-out within firm, especially in top paying ones where older workers retire later
 - 4. crowd-out between firms: younger workers pushed out of top-paying firms
 - 5. larger spillovers in more constrained firms

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 - e.g. low-growth, older, larger firms: less room for creating new positions at the top

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- 6. Complement with additional evidence to rule out alternative stories
 - among others: workforce composition, inequality trend, education and returns to experience

Literature review

- 1. Wage gap between older and younger employees
 - Relatively small literature on age wage gap (Rosolia & Torrini (2007); Naticchioni et al. (2014))
 - Our contribution:
 - Conceptual framework
 - Administrative and survey data from multiple countries
 - More tests and improved external validity
 - Implications of our results on pay and employment gap for income: Guaitoli and Pancrazi (2022)
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2. Spillovers across workers of different age groups

- Bertoni & Brunello (2020), Boeri et al. (2021), Bianchi et al. (2022), and Mohnen (2022) find that increase in retirement age worsens labor-market outcomes of younger workers
- Widening of age wage gap compatible with main takeaway of these papers

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- 3. Link age wage gap with other strands of the labor literature
 - Wage inequality (Autor et al. (2008); Card et al. (2013); Song et al. (2019)), increases in returns to experience (Jones (2009); Azoulay et al. (2020); Jeong et al. (2015)); SBTC (Acemoglu et al. (2011); Autor et al. (2006)); domestic outsourcing (Goldschmidt & Schmieder (2017)); demand for skills (Deming (2021)); selection

Conceptual framework

Data

Deterioration in Younger Workers Careers, Improvement for Older Workers Shifts along the wage distribution and firms' hierarchies

Importance of Changes in Relative Rank in Wage Distribution Entry Rank Vs. Rank Growth

The Role of Firms

Rank Increase Between Vs. Within Firms Age Gap Trend Heterogeneity Across Types of Firms

Alternative Mechanisms

Conclusions

Conceptual framework

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 - e.g. "promise keeping", adjustment costs
- 2. limited resources: cannot promote all who deserve a promotion
 - generates bottleneck at the top of firms' hierarchies, "conflict" between opportunities

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Constraint on resources: firm must pay (κ) to maintain top job and cover adjustment

$$c\left(x_{0}\right)+\kappa\cdot\left(l_{t,o}^{-1}-x_{0}+l_{t,y}\right)\leq K$$

- ► Top jobs pay some premium/wedge $\mu_{t,a}$ over bottom jobs
 - can easily microfund with efficiency wage considerations
- Workers would like to take top jobs, but they are rationed
 - firms will still be on labor demand (Acemoglu and Restrepo, 2023)
 - will demand labor until wage equal MPL

Crowding out and career spillovers

Result 1: If constraint binds, larger older cohort (lo) causes the following average wage change

$$\frac{\partial \bar{\mathbf{w}}_{\mathbf{y}}}{\partial \mathbf{l}_{\mathbf{o}}} = \underbrace{\frac{1}{\mathbf{l}_{\mathbf{y}}} \frac{\partial \mathbf{l}_{\mathbf{t},\mathbf{y}}}{\partial \mathbf{l}_{\mathbf{o}}} \left(\mu_{\mathbf{t},\mathbf{y}} - 1 \right) \mathbf{w}_{\mathbf{b},\mathbf{y}}}_{\text{Crowding out (CO)}} + \underbrace{\frac{\mathrm{RS}\left(\mathbf{F}_{\mathrm{L}_{\mathbf{y}}} \mathbf{L}_{\mathbf{o}}, \mathbf{F}_{\mathrm{L}_{\mathbf{y}}} \mathbf{L}_{\mathbf{y}} \right)}_{\mathrm{Relative labor supply (RS)}}$$

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- Extend to heterogeneous firms to get additional results

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- Use ITA as main setting, replicate for others when possible

The Careers of Young and Old Workers

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How does likelihood of being at the top changes for the two age groups?

U35 workers move towards bottom vigintiles



055 workers move towards top vigintiles



Opposite shifts over the distribution of wages, consistent with changes in careers Job title movements

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Can we quantify contribution of each force?

Decomposition: rank gap and distributional gap

The change in mean wages for age group a between periods t and t' can be written as follows:

$$\Delta w_{a}^{t,t'} = \underbrace{\sum_{v} s_{a,v,t} \left(\bar{w}_{v,t'} - \bar{w}_{v,t} \right)}_{\text{Distributional gap}} +$$

- ▶ $s_{a,v,t}$ = share of workers in age group $a \in \{U35, 055\}$, vigintile v of the distribution of wages, and year t
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- $\bar{w}_{v,t}$ = mean log wage in vigintile v and year t
- ▶ Difference between age groups a \in {U35, O55} to decompose change in age wage gap



Most of the increase in age wage gap from larger rank gap



Rank gap more important in most countries



Entry Rank Vs. Rank Growth

Result 2: lower entry position and lower growth over lifecycle

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 - Intercept: change in rank at labor-market entry between t and t'
 - Slope: change in post-entry rank growth between t and t'

Details of the decomposition

U35: loss from both entry and post-entry growth



The Importance of Within and Between Firm Dynamics

Sorting of workers

- Younger people lose and older gain
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- In every year, divide workers into 50,000 firm-worker groups (Machado & Mata (2005)):
 - 100 firm groups (f) depending on average firm wage
 - 500 worker groups (e) within each firm group

Decomposition within vs between firms

U35 lose rank within any level of firm pay, 055 gain almost everywhere



055 concentrate in high-paying firms and generate competition



Firm Heterogeneity

Result 5: career spillovers are larger in more constrained firms

- Key: crowd-out depends on constraints in adding higher-ranked jobs
- Constrained firms: do not grow, are in mature stage of their life cycle
- Consistent with prior findings (Bennett & Levinthal (2017); Bianchi et al. (2022)
- These firms are becoming more common:

Larger effects within older, larger, slow-growing firms



Alternative Mechanisms

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- Changes in workforce composition Evidence
 - residual (education, gender, type of contract) age gap shows similar increase
 - look at subpopulations: e.g. men, women, domestic, permanent contract
 - focus on 55-60 males to avoid changes in composition b/c of pension reforms

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- These results point to the importance of negative career spillovers
- Implications for gender pay gap: Arellano-Bover, Bianchi, Lattanzio, Paradisi (soon!)
 - younger men's opportunities deteriorate more than women: started from higher positions
 - compression of younger opportunities is important driver of gender pay gap decrease

THANK YOU

Appendix

Wage gap between older and younger workers increased



ITA: Increase of Age Wage Gap at Mean and Median



Steeper Wage Curve Over Life Cycle



U35 workers from top to bottom quartile





055 workers from bottom to top quartile



U-35 move to apprenticeship, O-55 to managerial jobs



Shares of Managerial Positions





Shares in Age Group with Managerial Job





Two types of increases in the age wage gap

► Wage distribution at baseline:



Age wage gap can increase through a change in wage rank:



Two types of increases in the age wage gap

► Wage distribution at baseline:



Age wage gap can increase through a change in mean wages at different percentiles:



Decomposition by age group: U35 lose, while 055 gain



Rank Gap with Yearly Labor Earnings



Rank Gap in Germany - Daily Wages



Entry rank Vs. rank growth

Decomposition of wage-rank loss for U35 workers between period t and t'

Entry rank Vs. rank growth

- Decomposition of wage-rank loss for U35 workers between period t and t'
- Change in rank at labor-market entry between t and t' (e is years from entry)

$$\underbrace{\sum_{e \in [0,18]} s_{e,t} \cdot \sum_{v} \left[\left(s_{e,t',v}^{\mathsf{E}} - s_{e,t,v}^{\mathsf{E}} \right) \cdot \bar{w}_{v,t} \right]}_{\text{Change in entry rank}}$$

- s^E_{e,t,v} = the share of workers who are e years from entry in year t in vigintile v at the time of entry in the labor market (E)
- s_{e,t} = the share of workers who are e years from entry in year t out of all U-35

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- Change in post-entry rank growth between t and t'

$$\underbrace{\sum_{e \in [0,18]} \mathbf{s}_{e,t} \cdot \sum_{v} \left[\left(\Delta \mathbf{s}_{e,t',v}^{t'-E} - \Delta \mathbf{s}_{e,t,v}^{t-E} \right) \cdot \bar{\mathbf{w}}_{v,t} \right]}_{\text{Change in rank growth}}$$

• $\Delta s_{e,t',v}^{t'-E} = s_{e,t,v} - s_{e,t,v}^{E}$ = change in share at vingtile v of those who are e years from entry in t

U30 Loss Mostly Comes from Worse Rank at Entry



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$$\underbrace{\sum_{\mathbf{v}} \left(\mathbf{s}_{\mathbf{a},\mathbf{v},t'} - \mathbf{s}_{\mathbf{a},\mathbf{v},t} \right) \bar{\mathbf{w}}_{\mathbf{v},t}}_{\text{Rank gap}} = \underbrace{\sum_{g \in (f,e)} \left(\mathbf{s}_{\mathbf{a},f,t'} - \mathbf{s}_{\mathbf{a},f,t} \right) \cdot \mathbf{s}_{\mathbf{a},(e|f),t} \cdot \bar{\mathbf{w}}_{g,t}}_{\text{Between firms}}$$



Back

The change in the rank gap for age group a \in {U35, O55} can be written as follows:

$$\underbrace{\sum_{\mathbf{v}} (\mathbf{s}_{\mathbf{a},\mathbf{v},t'} - \mathbf{s}_{\mathbf{a},\mathbf{v},t}) \, \bar{\mathbf{w}}_{\mathbf{v},t}}_{\text{Rank gap}} = \underbrace{\sum_{\mathbf{g} \in (f,e)} (\mathbf{s}_{\mathbf{a},f,t'} - \mathbf{s}_{\mathbf{a},f,t}) \cdot \mathbf{s}_{\mathbf{a},(\mathbf{e}|f),t} \cdot \bar{\mathbf{w}}_{\mathbf{g},t}}_{\text{Between firms}} + \underbrace{\sum_{\mathbf{g} \in (f,e)} \mathbf{s}_{\mathbf{a},f,t} \cdot \left(\mathbf{s}_{\mathbf{a},(\mathbf{e}|f),t'} - \mathbf{s}_{\mathbf{a},(\mathbf{e}|f),t}\right) \cdot \bar{\mathbf{w}}_{\mathbf{g},t}}_{\text{Within firms}} + \underbrace{\varepsilon_{\mathbf{a}}^{t,t'}}_{\text{Residual}}$$

 \blacktriangleright You can further differentiate between two age groups a \in {U35, O55}

Within-firm component accounts for 61% of rank-gap increase





Within firm dynamics are mostly important for U35



Between Vs. Within Firms in Germany



Between Vs. Within Firms in Germany - By Age Group



U35 lose rank within firms at entry, and for lower growth



U35 find it harder to grow within firms

Within-firm loss is the main source of U35 career deterioration

- U35 enter in lower-ranked position and progress less within their firm
- ► U35 lose rank in any firm group

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Within-firm loss is the main source of U35 career deterioration

- U35 enter in lower-ranked position and progress less within their firm
- U35 lose rank in any firm group

Older workers have small/zero gains within firms

- ► Two opposing forces:
 - longer tenure improves their relative position within firm
 - higher competion with other 055 deteriorates their relative position
- Consistently, 055 gain everywhere within firms, except at the top where they concentrate



U35 seem to have been crowded out of high-paying firms

Older workers concentrate more in top-paying firms

- Not as a consequence of late move: have high tenure (> 12 yrs in above median group)
- > Tenure change across firms follows 055 incentives (lower tenure loss in higher groups)
- O55 age increases more for top-paying firm groups (delay retirement more)
- High-paying groups have more than doubled firm age
 - 055 concentration at top might have been favored by business dynamics

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U35 became more likely to be in low-paying firms

- U35 less present in top-paying firms where 055 concentrate
- U35 seem to have been segregated more to low-paying firms



Shares with Turnover Events



Despite larger turnover, average rank growth in turnover declines



Despite larger turnover, average rank growth in turnover declines


Despite larger turnover, average rank growth in turnover declines



Mean Firm Age



Decreasing GDP Growth In Most High-Income Countries



Within-Occupation Component Accounts Most of Rank-Gap Increase



Numerical Framework - Mincerian Equation

Consider a simple but general wage equation:

$$\mathsf{w}_{\mathsf{i},\mathsf{a}}^\mathsf{t} = eta_\mathsf{0} + eta_\mathsf{1}^\mathsf{t} \mathsf{x}_{\mathsf{i},\mathsf{a}}^\mathsf{t}$$

- w^t_{i,a} = wage of worker i of age group a in period t
- x^t_{i,a} = quantity of wage-enhancing factor possessed by worker i in period t
- β_1^t = unitary price of factor x in period t
- Older workers posses on average a higher quantity of x
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- Age wage gap can increase because
 - Price of factor x increases
 - Gap in quantity of x between older and younger workers increases



Simulate Changes in Price

- Baseline scenario (matches data moments in Italian admin data):
 - $x_Y^t \sim N(4.6, 0.25)$ and $x_0^t \sim N(4.7, 0.49)$
 - $\beta_1^t = 1$, $\beta_0 = 1$
 - Share older workers $(\mathbf{s_0^t}) = \mathbf{0.08}$

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 - "Normal" price hike & more older workers: $\beta_1^{t'} = 2$, $s_0^{t'} = 0.2$
 - "Normal" price hike & way more older workers: $\beta_1^{t'} = 2$, $s_0^{t'} = 0.35$
 - "Large" price hike: $\beta_1^{t'} = 4$



Price Hikes Act Through Distributional Gap



Price Hikes Act Through Distributional Gap



Simulate Changes in Quantities

- Baseline scenario (matches data moments in Italian admin data):
 - * $x_Y^t \sim N(4.6, 0.25)$ and $x_0^t \sim N(4.7, 0.49)$
 - $\beta_1^t = 1$, $\beta_0 = 1$
 - Share older workers $(s_0^t) = 0.08$
- 4 simulated changes in distribution of x
 - "Normal" distribution change: $\mathbb{E}\left[\mathbf{x}_{0}^{t'}\right] = 4.8$
 - "Normal" distribution change & more older workers: $\mathbb{E}\left[x_{0}^{t'}\right] = 4.8$, $s_{0}^{t'} = 0.2$
 - "Normal" distribution change & way more older workers: $\mathbb{E}\left[x_{0}^{t'}\right] = 4.8, s_{0}^{t'} = 0.35$

• "Large" distribution change:
$$\mathbb{E}\left[\mathbf{x}_{0}^{t'}
ight]=5$$



Quantity Changes Act Mostly Through Rank Gap



Intuition About Results of Numerical Framework

- Price increase when baseline difference in xs
 - increases dispersion of young and old distribution
 - spreads out the overall earnings distribution
 - captured by distributional component

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 - spreads out the overall earnings distribution
 - captured by distributional component
- Quantity increase with overlapping distributions
 - moves young and old distributions apart
 - more overlap at baseline: more older workers overcome young
 - captured by rank component
- Similar logic in Bayer and Charles (2018) for black-white gap
 - positional: reduced discrimination, better access to schools
 - distributional: changes in returns to education, skills



Increases in price of wage-enhancing factors incompatible with increased rank gap:

- Increase in returns to experience (Jones (2009); Azoulay et al. (2020); Jeong et al. (2015))
- Skill-biased technological change (Acemoglu & Autor (2011); Autor et al. (2006))



Within-Sector Component Accounts for 90% of Rank-Gap Increase



Between Vs. Within Firms: No High-Outsourcing Sectors



Notes: Sample does not include all sectors identified by Goldschmidt and Schmieder (2017) as primary receivers of most domestically outsourced jobs: 49.2, 49.4, 50.2, 50.4, 51.2, 52.1, 52.2, 56.2, 78.1, 78.2, 78.3, 80.1, 80.2, 80.3, 81.1, 81.2, 82.1, 82.2, 82.9 (NACE Rev. 2).

Changing Composition of U-35 and 055 Workforce

- Trends in other characteristics of young and old can be confounders
- We might be referring to age the byproduct of something else
- Some contemporaneous changes in demographics
 - increased share migrants in U35
 - increased share temporary contracts in U35
 - increased share of females in U35
 - increased education for both age groups
 - health improvements for older workers over time
 - longer working lives for 0-55



Age Wage Gap After Controlling for Demographic and Labor Variables



Notes: Age wage gap with controls uses residuals from year-specific regressions of log wages on gender, nationality (race in US), temp. contracts, education, disability status.

055 Workers = 56-60 Years Old Men

