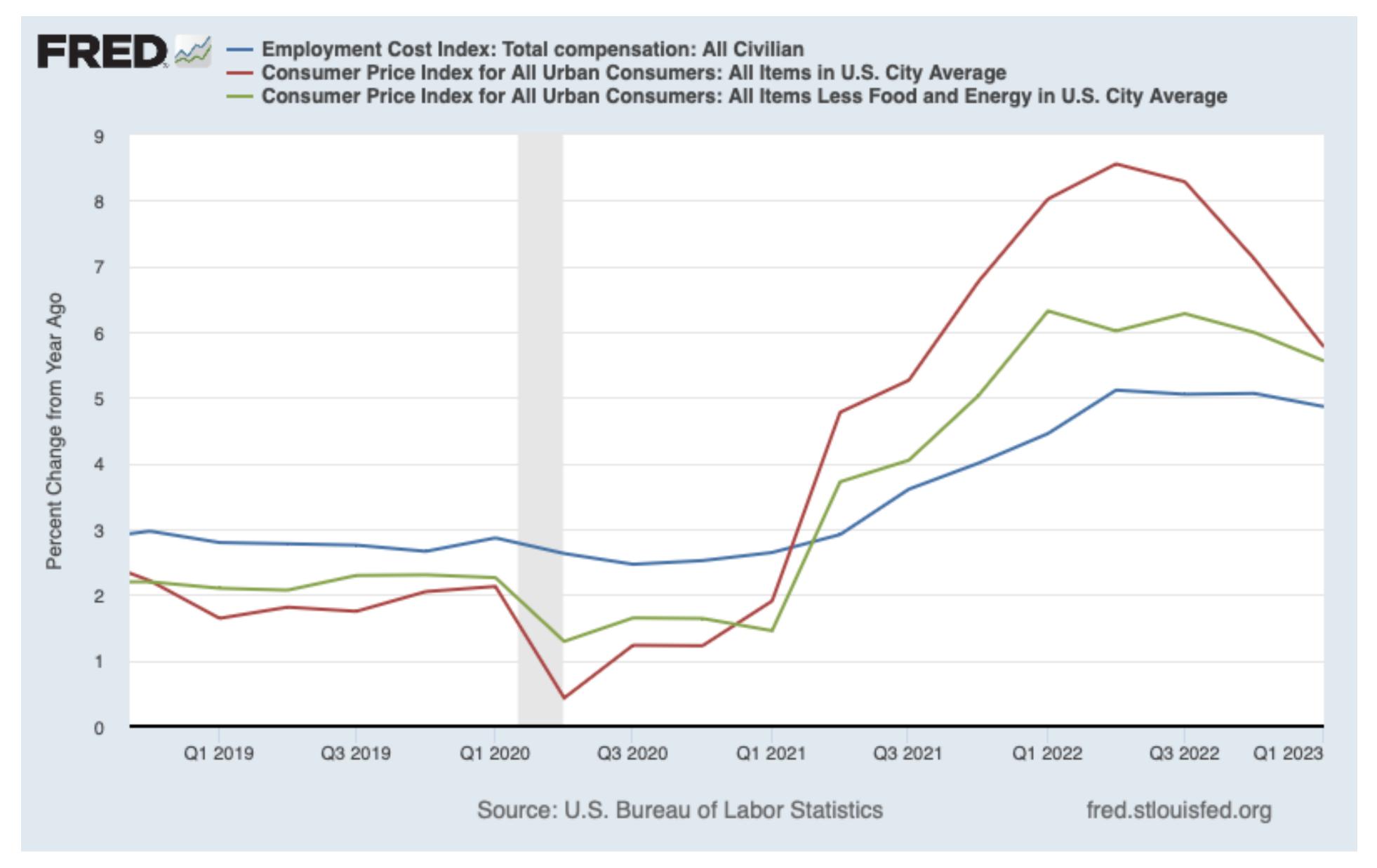
Wage Price Spirals

Guido Lorenzoni and Iván Werning

Wage inflation and price inflation



• What is a wage price spiral? An alternative shock, an alternative model?

• What is a wage price spiral? An alternative shock, an alternative model?

A mechanism, at work also in standard models

- What is a wage price spiral? An alternative shock, an alternative model? A *mechanism*, at work also in standard models
- Can we gauge power of mechanism by looking at whether W/P goes up or down?

- What is a wage price spiral? An alternative shock, an alternative model? A *mechanism*, at work also in standard models
- Can we gauge power of mechanism by looking at whether W/P goes up or down?

No: total power of mechanism \neq relative power on w and p

- What is a wage price spiral? An alternative shock, an alternative model? A *mechanism*, at work also in standard models
- Can we gauge power of mechanism by looking at whether W/P goes up or down? No: total power of mechanism \neq relative power on w and p
- Does direction of *w/p* adjustment tell us about underlying shocks?

- What is a wage price spiral? An alternative shock, an alternative model? A *mechanism*, at work also in standard models
- Can we gauge power of mechanism by looking at whether W/P goes up or down?
 - No: total power of mechanism \neq relative power on w and p
- Does direction of *w/p* adjustment tell us about underlying shocks?
 - Not necessarily: both demand and supply shocks can create inflation and push w/p down

- What is a wage price spiral? An alternative shock, an alternative model? A *mechanism*, at work also in standard models
- Can we gauge power of mechanism by looking at whether W/P goes up or down? No: total power of mechanism \neq relative power on w and p
- Does direction of *w/p* adjustment tell us about underlying shocks?

 Not necessarily: both demand and supply shocks can create inflation *and* push *w/p* down
- An optimistic perspective on current situation: shock with 3 phases:

- What is a wage price spiral? An alternative shock, an alternative model? A *mechanism*, at work also in standard models
- Can we gauge power of mechanism by looking at whether W/P goes up or down? No: total power of mechanism \neq relative power on w and p
- Does direction of *w/p* adjustment tell us about underlying shocks?

 Not necessarily: both demand and supply shocks can create inflation *and* push *w/p* down
- An optimistic perspective on current situation: shock with 3 phases:
 - scarcity pops up in some places, feeds into inflation...

- What is a wage price spiral? An alternative shock, an alternative model? A *mechanism*, at work also in standard models
- Can we gauge power of mechanism by looking at whether W/P goes up or down? No: total power of mechanism \neq relative power on w and p
- Does direction of *w/p* adjustment tell us about underlying shocks?

 Not necessarily: both demand and supply shocks can create inflation *and* push *w/p* down
- An optimistic perspective on current situation: shock with 3 phases:
 - scarcity pops up in some places, feeds into inflation...
 - ... feeds back in wage inflation

- What is a wage price spiral? An alternative shock, an alternative model? A *mechanism*, at work also in standard models
- Can we gauge power of mechanism by looking at whether W/P goes up or down? No: total power of mechanism \neq relative power on w and p
- Does direction of *w/p* adjustment tell us about underlying shocks?

 Not necessarily: both demand and supply shocks can create inflation *and* push *w/p* down
- An optimistic perspective on current situation: shock with 3 phases:
 - scarcity pops up in some places, feeds into inflation...
 - ... feeds back in wage inflation
 - ... but dies out

- What is a wage price spiral? An alternative shock, an alternative model? A *mechanism*, at work also in standard models
- Can we gauge power of mechanism by looking at whether W/P goes up or down?
 - No: total power of mechanism \neq relative power on w and p
- Does direction of *w/p* adjustment tell us about underlying shocks?
 - Not necessarily: both demand and supply shocks can create inflation and push w/p down
- An optimistic perspective on current situation: shock with 3 phases:
 - scarcity pops up in some places, feeds into inflation...
 - ... feeds back in wage inflation
 - ... but dies out
- Optimal policy

• Blanchard, Summers: predicted inflation from stimulus, but anticipated hot labor market and wage increases

- Blanchard, Summers: predicted inflation from stimulus, but anticipated hot labor market and wage increases
- This is not how it played out.

- Blanchard, Summers: predicted inflation from stimulus, but anticipated hot labor market and wage increases
- This is not how it played out.
- Blanchard-Bernanke...

- Blanchard, Summers: predicted inflation from stimulus, but anticipated hot labor market and wage increases
- This is not how it played out.
- Blanchard-Bernanke...
 - most inflation driven by commodity prices and sector price spikes in supply chains

- Blanchard, Summers: predicted inflation from stimulus, but anticipated hot labor market and wage increases
- This is not how it played out.
- Blanchard-Bernanke...
 - most inflation driven by commodity prices and sector price spikes in supply chains
 - stimulus added to this, but inflation due to good market not labor market

- Blanchard, Summers: predicted inflation from stimulus, but anticipated hot labor market and wage increases
- This is not how it played out.
- Blanchard-Bernanke...
 - most inflation driven by commodity prices and sector price spikes in supply chains
 - stimulus added to this, but inflation due to good market not labor market
- Weber-Wasner "Seller's Inflation" (often misnamed "greedflation")

- Blanchard, Summers: predicted inflation from stimulus, but anticipated hot labor market and wage increases
- This is not how it played out.
- Blanchard-Bernanke...
 - most inflation driven by commodity prices and sector price spikes in supply chains
 - stimulus added to this, but inflation due to good market not labor market
- Weber-Wasner "Seller's Inflation" (often misnamed "greedflation")
 - inflation from increase in inputs

1. Wage and Price Setting

Model

- Standard NK model with sticky nominal wages (Erceg-Henderson-Levin, 2000)
- Include non-labor input X in inelastic supply
- Preferences

$$\int_{0}^{\infty} e^{-\rho t} \left(\frac{1}{1 - \sigma} C_{t}^{1 - \sigma} - \frac{\Phi_{t}}{1 + \eta} \int_{0}^{1} N_{jt}^{1 + \eta} dj \right) dt,$$

- C_t is CES composite of continuum of varieties
- Technology

$$Y_{jt} = \left(a_L L_{jt}^{\frac{\epsilon - 1}{\epsilon}} + a_X X_{jt}^{\frac{\epsilon - 1}{\epsilon}}\right)^{\frac{\epsilon}{\epsilon - 1}}$$

Labor and non-labor input

Multiple labor types

$$L_t = \left(\int_0^1 N_{jt}^{1-1/\zeta} dj\right)^{\frac{1}{1-1/\zeta}}$$

• Each supplied by monopolist wage setter (union)

- Input X supplied inelastically by representative household
- Flexible price P_{Xt}

Firms' Optimality

• All firms use same mix of labor and *X*

From now all log deviations from ss

Nominal marginal cost

$$w_t - mpl_t$$

• MPL depends on aggregate input to labor ratio and on the steady state share of the input

$$mpl_t = \frac{s_X}{\epsilon} \left(x_t - l_t \right)$$

Price of the input

$$p_{Xt} = w_t - \frac{1}{\epsilon} \left(x_t - l_t \right)$$

"Marginal Cost" of Labor

• Rate at which workers willing to supply one more unit of labor

$$mrs_{\tau,t} + p_t$$

- MRS depends on when worker's reset wages
- But on average is simply

$$mrs_t = \phi_t + \sigma y_t + \eta n_t$$

Price and Wage Setting

- Firms get to reset price: Poisson with rate λ_p
- Optimal price setting

$$p_t^* = \left(\rho + \lambda_p\right) \int_t^\infty e^{-\left(\rho + \lambda_p\right)(\tau - t)} \left(w_\tau - mpl_\tau\right) d\tau$$

For workers

$$w_t^* = \left(\rho + \lambda_w\right) \int_t^\infty e^{-\left(\rho + \lambda_w\right)(\tau - t)} \left(p_\tau + mrs_{\tau,t}\right) d\tau$$

Price and Wage Setting

- Firms get to reset price: Poisson with rate λ_p
- Optimal price setting

$$p_t^* = \left(\rho + \lambda_p\right) \int_t^\infty e^{-\left(\rho + \lambda_p\right)(\tau - t)} \left(w_\tau - mpl_\tau\right) d\tau$$

For workers

$$w_t^* = \left(\rho + \lambda_w\right) \int_t^\infty e^{-(\rho + \lambda_w)(\tau - t)} \left(p_\tau + mrs_{\tau,t}\right) d\tau$$

Price and Wage Setting

- Firms get to reset price: Poisson with rate λ_p
- Optimal price setting

$$p_t^* = \left(\rho + \lambda_p\right) \int_t^\infty e^{-\left(\rho + \lambda_p\right)(\tau - t)} \left(w_\tau - mpl_\tau\right) d\tau$$

For workers

$$w_t^* = \left(\rho + \lambda_w\right) \int_t^\infty e^{-(\rho + \lambda_w)(\tau - t)} \left(p_\tau + mrs_{\tau,t}\right) d\tau$$

Flexible Prices and Wages

Two equations above become

$$p_t = w_t - mpl_t$$

And

$$w_t = p_t + mrs_t$$

- So we need $mpl_t = mrs_t!$
- Sticky prices models capture the tension that comes from quantities not compatible with $mpl_t = mrs_t$

Price and Wage Dynamics

• Given paths for mpl_t and mrs_t + initial condition for ω_t dynamics of prices and wages fully characterized by

$$\rho \pi_{t} = \Lambda_{p} \left(\omega_{t} - mpl_{t} \right) + \dot{\pi}_{t}$$

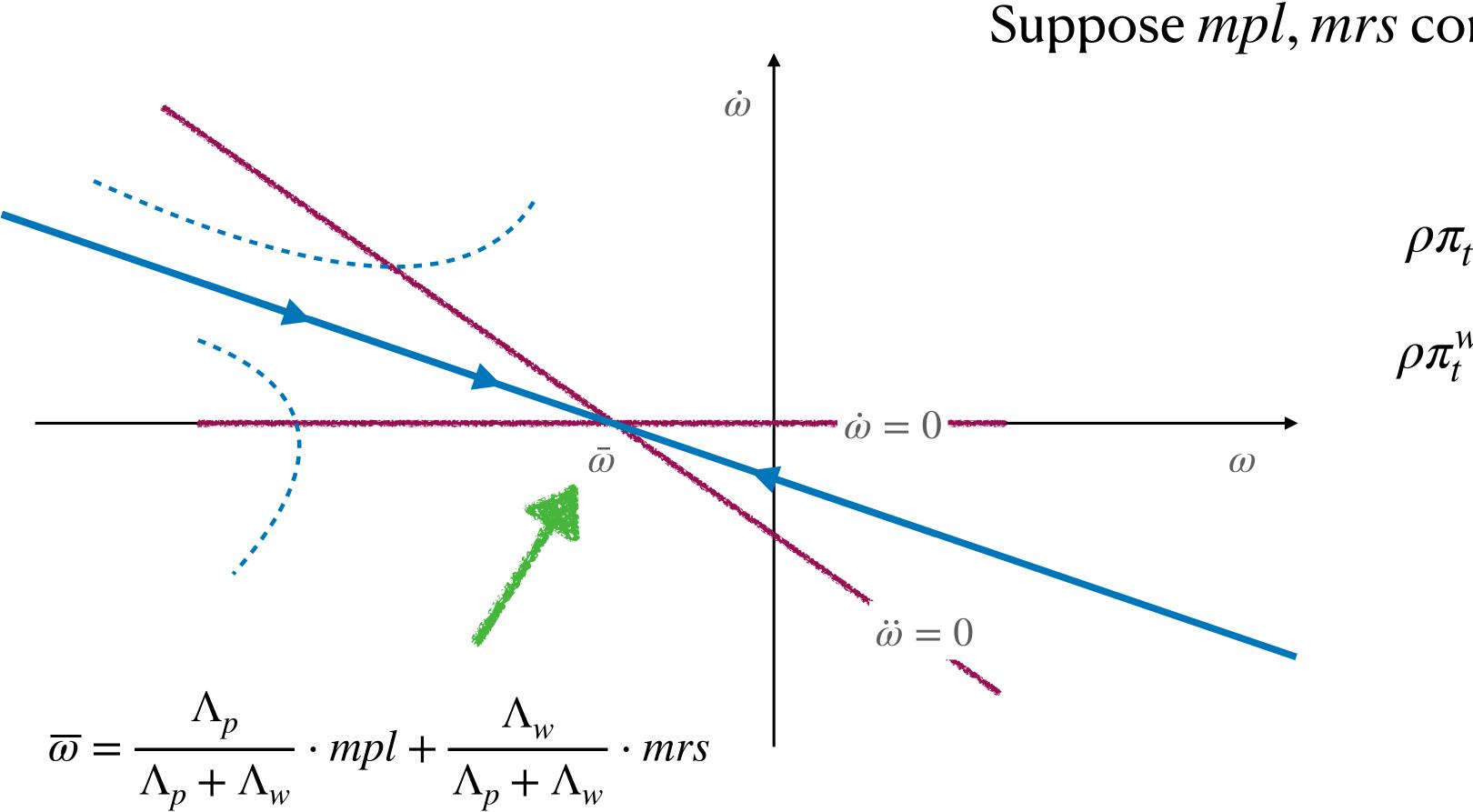
$$\rho \pi_{t}^{w} = \Lambda_{w} \left(mrs_{t} - \omega_{t} \right) + \dot{\pi}_{t}^{w}$$

$$\dot{\omega}_{t} = \pi_{t}^{w} - \pi_{t}$$

Where
$$\Lambda_p = \lambda_p \left(\rho + \lambda_p \right)$$
 and $\Lambda_w = \lambda_w \frac{\rho + \lambda_w}{1 + \eta \zeta}$

2. Real Wage Dynamics

Phase Diagram



Suppose mpl, mrs constant and $mpl \neq mrs$

$$\rho \pi_{t} = \Lambda_{p} \left(\omega_{t} - mpl \right) + \dot{\pi}_{t}$$

$$\rho \pi_{t}^{w} = \Lambda_{w} \left(mrs - \omega_{t} \right) + \dot{\pi}_{t}^{w}$$

$$\dot{\omega}_{t} = \pi_{t}^{w} - \pi_{t}$$

$$\kappa \equiv \frac{\Lambda_p}{\Lambda_p + \Lambda_w}$$

Asymptotic Inflation

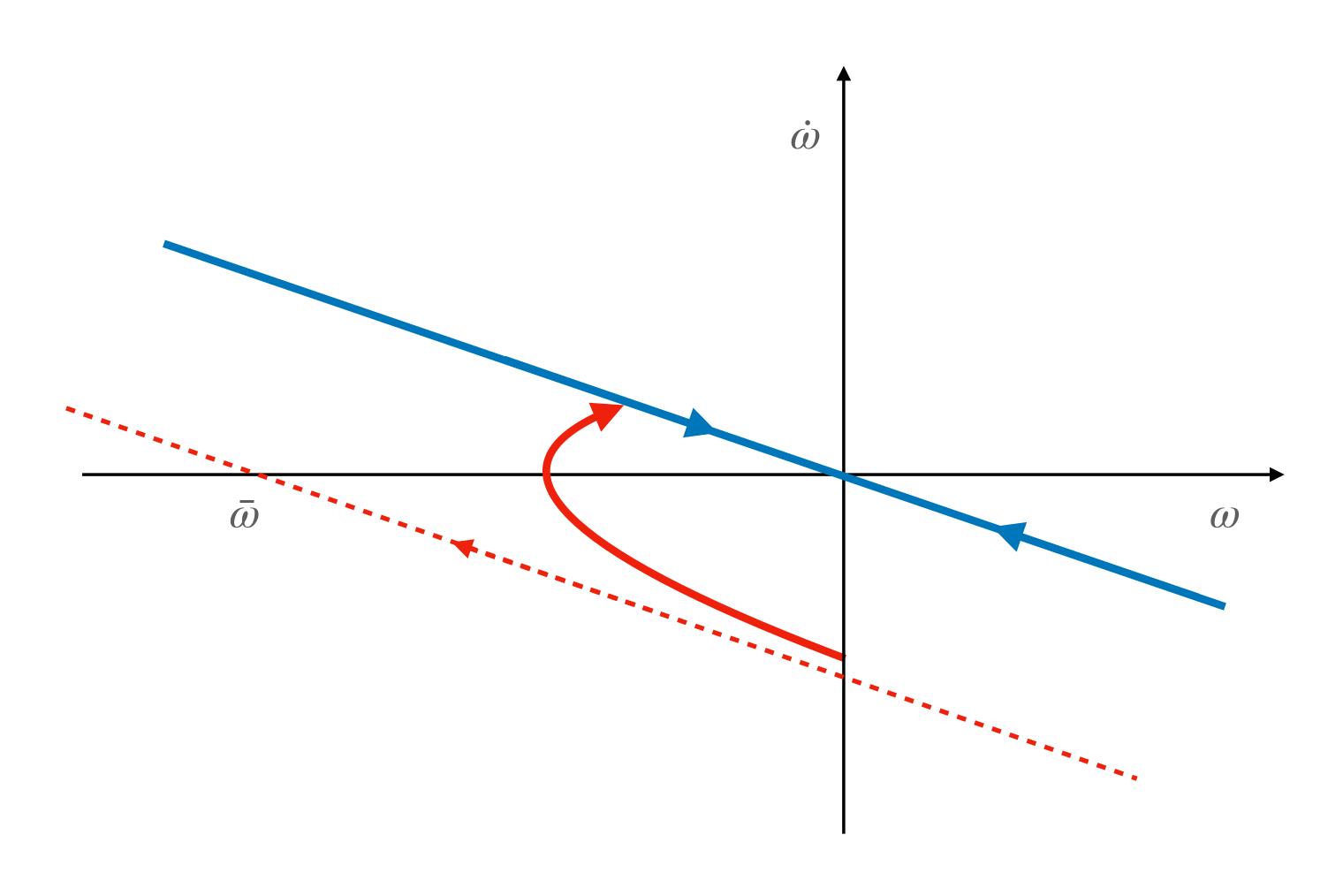
$$\rho\pi = \Lambda_{p} \left(\overline{\omega} - mpl\right)$$

$$\rho\pi^{w} = \Lambda_{w} \left(mrs - \overline{\omega}\right)$$

$$\pi = \pi^{w} = \frac{1}{\rho} \frac{\Lambda_{p} \Lambda_{w}}{\Lambda_{p} + \Lambda_{w}} (mrs - mpl)$$

- Inflation from disagreement
- Inflation does not resolve disagreement between mpl and mrs
- It just equalizes the tension on the two sides
- If $\rho \to 0$ then $\pi \to \infty$ (vertical Phillips curve)
- To bring down inflation we need to bring *mpl* = *mrs* (monetary policy)

Phase Diagram: Transitory Shock



A General Decomposition

$$\pi_t = \Pi_t^C - \kappa \cdot \Pi_t^A$$

$$\pi_t^w = \Pi_t^C + (1 - \kappa) \cdot \Pi_t^A$$

"Conflict"

$$\Pi_t^C = \frac{\Lambda_p \Lambda_w}{\Lambda_n + \Lambda_w} \int_0^\infty e^{-\rho s} (mrs_{t+s} - mpl_{t+s}) ds$$

"Adjustment"

$$\Pi_t^A = \dot{\omega}_t = (\Lambda_p + \Lambda_w) \int_0^\infty e^{-\rho s} (\tilde{\omega}_{t+s} - \omega_{t+s}) \, ds,$$
$$\tilde{\omega}_t = \kappa \cdot mpl_t + (1 - \kappa) \cdot mrs_t$$

Which Way Does W/P Go?

Q: Given paths for mpl and mrs

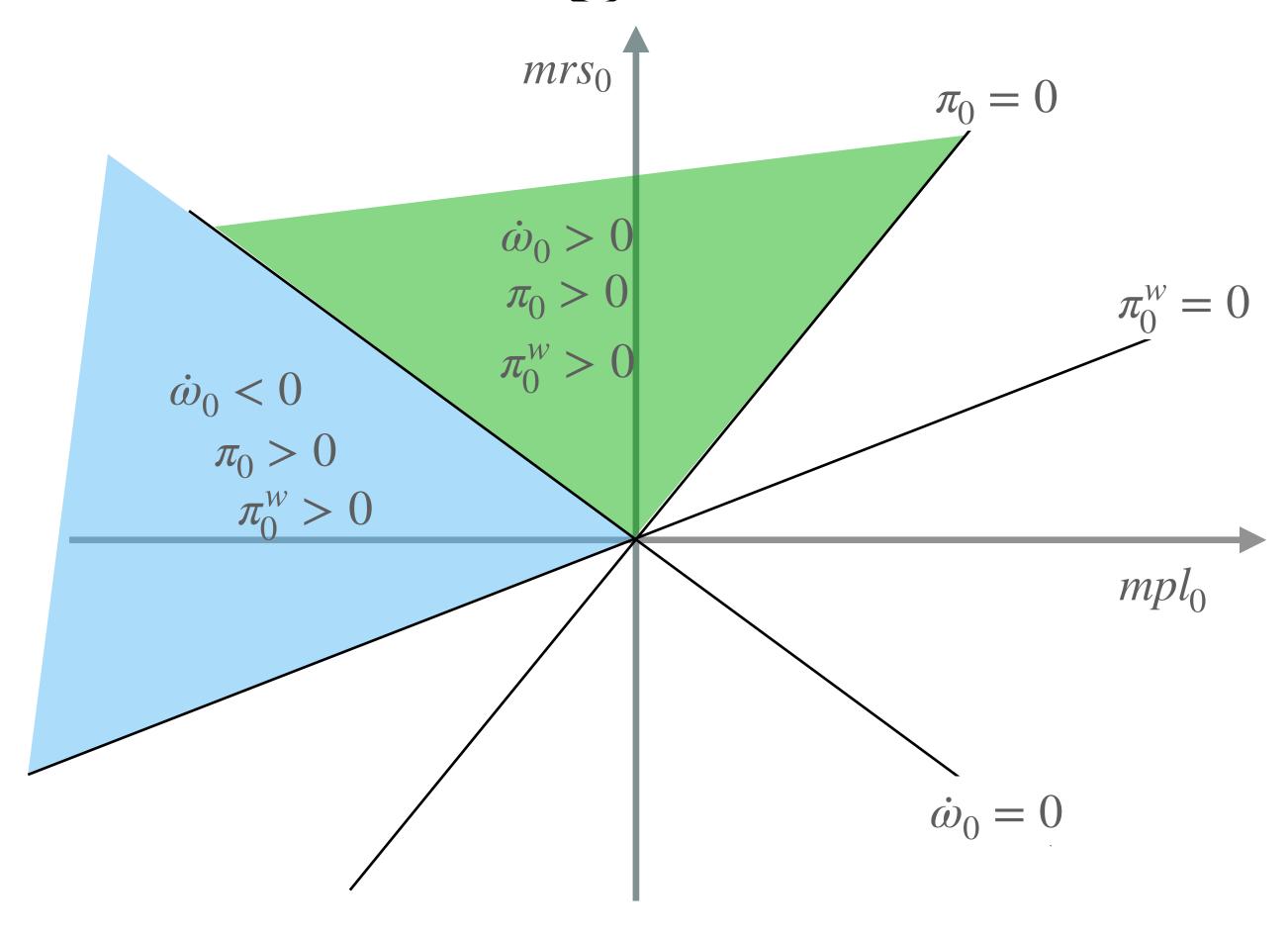
- When do we get price inflation?
- When wage inflation?
- Which one is stronger (on impact, down the line)?
- Economy starts in steady state
- For t < 0: no conflict $mpl_t = mrs_t = 0$, real wage in steady state $w_t p_t = 0$ no inflation
- Shock:

$$mrs_0 \neq 0, \qquad mpl_0 \neq 0$$

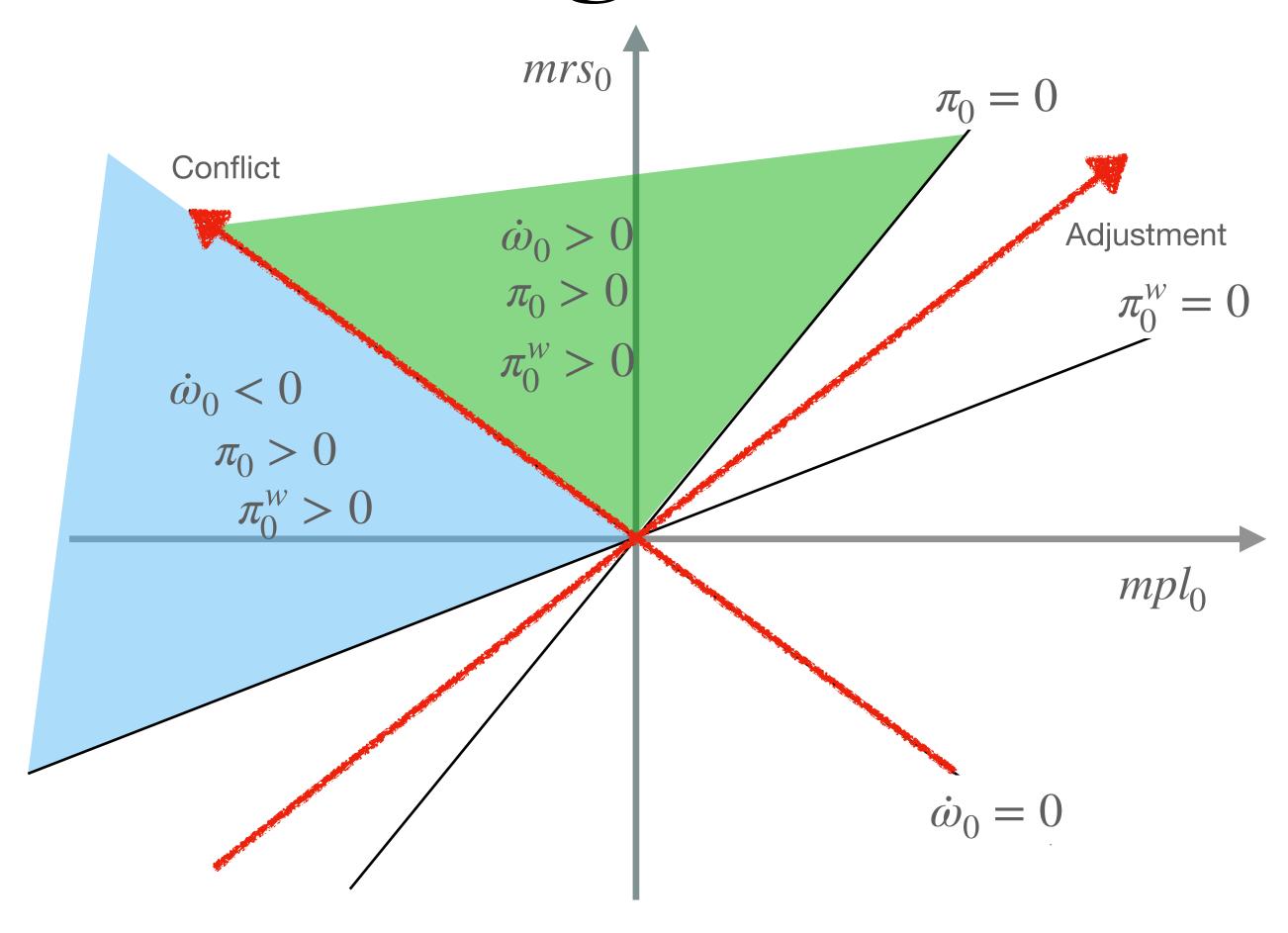
Then

$$mirs_t = -\delta \cdot mrs_t, \quad \dot{mpl}_t = -\delta \cdot mpl_t$$

Regions



Regions

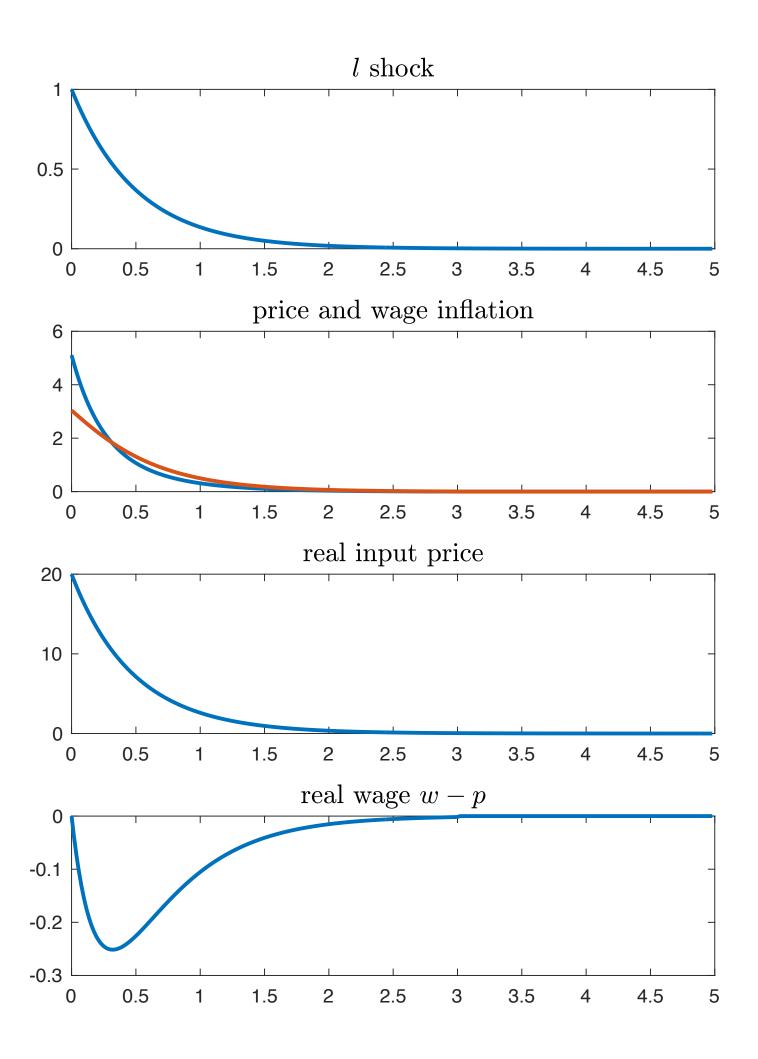


3. Demand and Supply Shocks

A Demand Shock

- A monetary policy mistake
- Economy is in steady state with $\pi = \pi^w = 0$ and y = n = 0
- Monetary stimulus causes unexpected shock $n_0 > 0$ with $n_t = e^{-\xi t} n_0$
- What happens to inflation in:
 - Input X price
 - Other goods
 - Wages

A Demand Shock

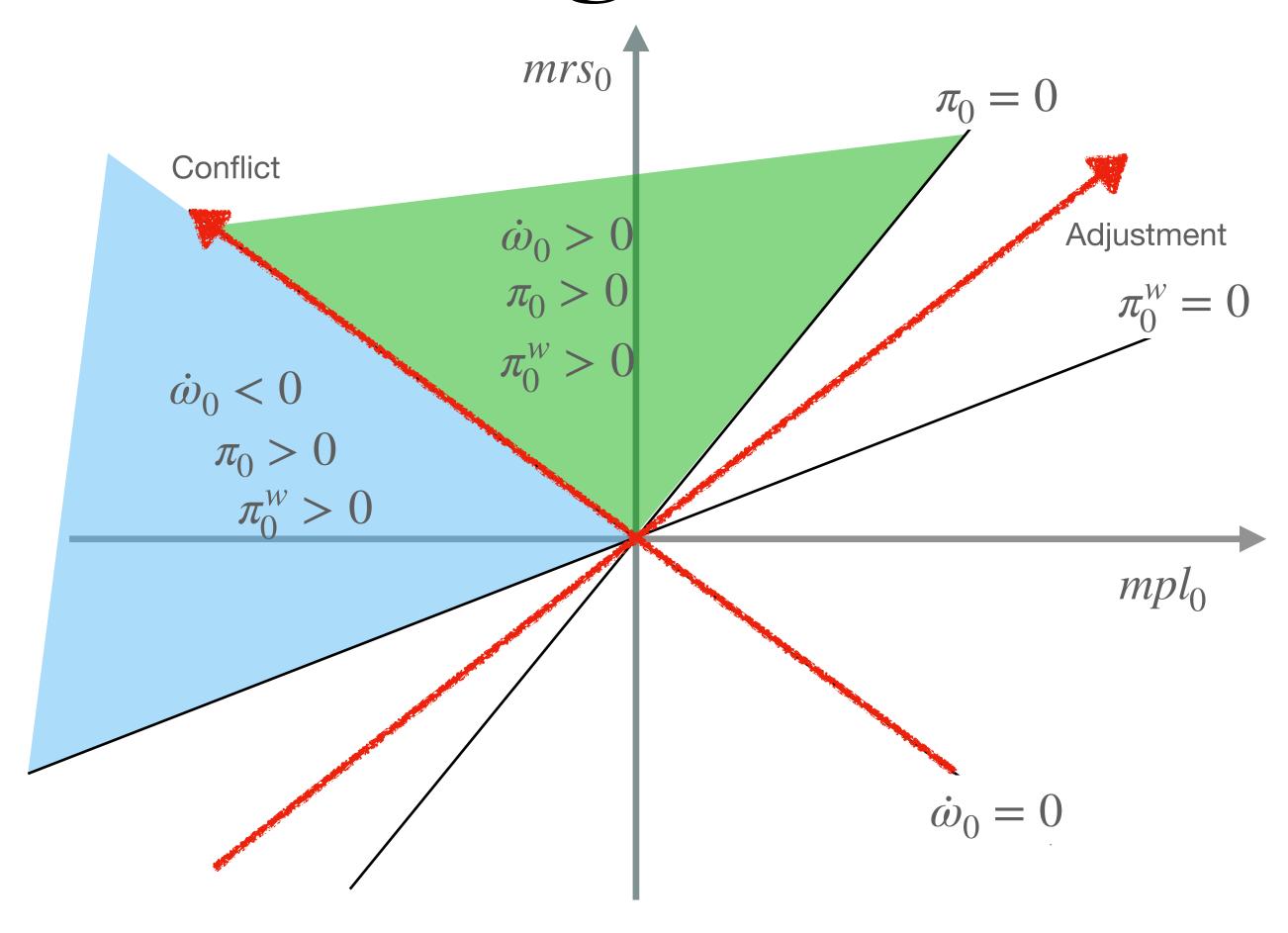


Three phases:

- Very fast response of *X* price
- Pass-through into other goods
- Reaction of wages

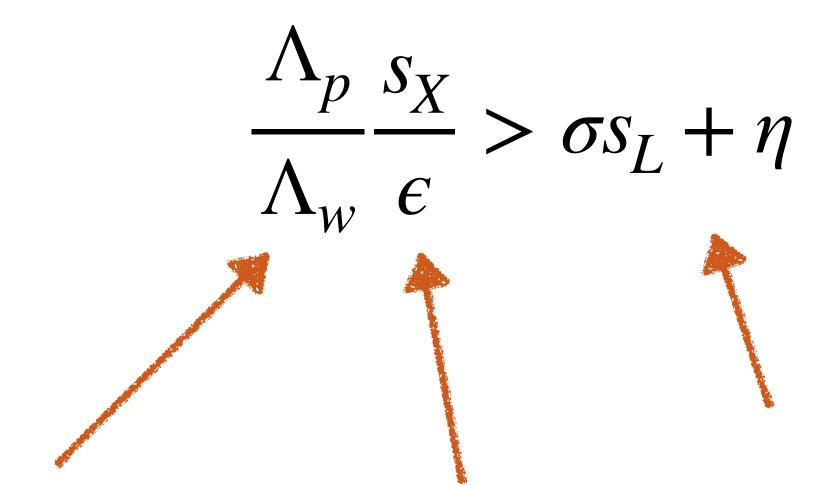
See Ball, Leigh, Mishra (2022) for importance of passthrough from non-core to core inflation

Regions



When Does a Demand Shock Produce Lower Wages?

A supply-constrained demand shock



Prices relatively less sticky than wages

Scarce input has high share and low elasticity of substitution with labor

Relatively weak response of real wage demands to hot labor market

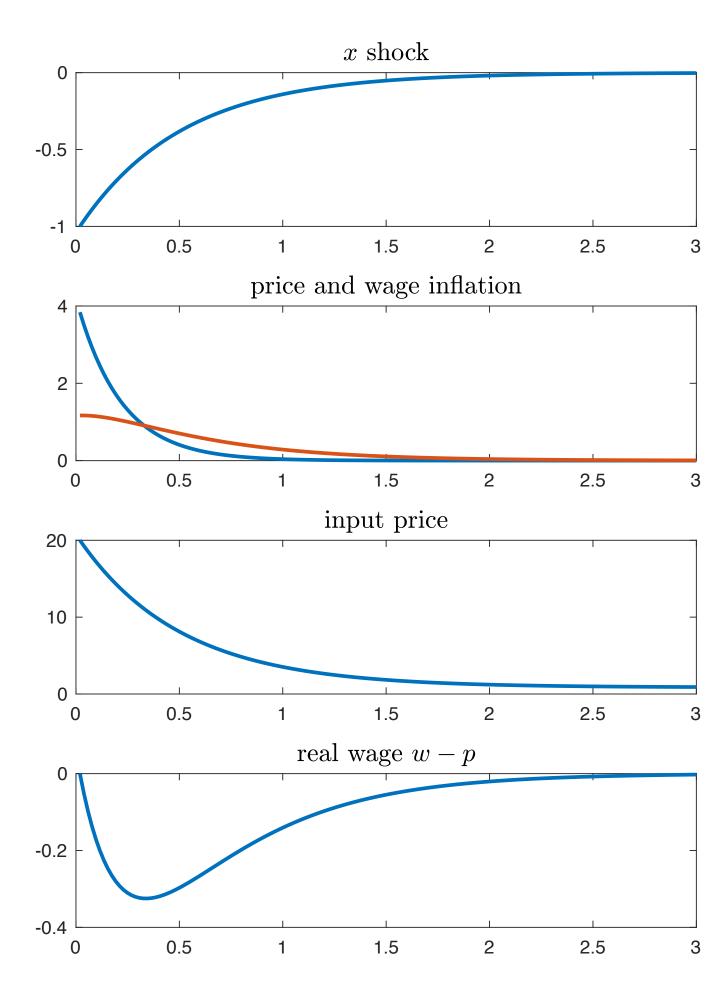
A supply shock

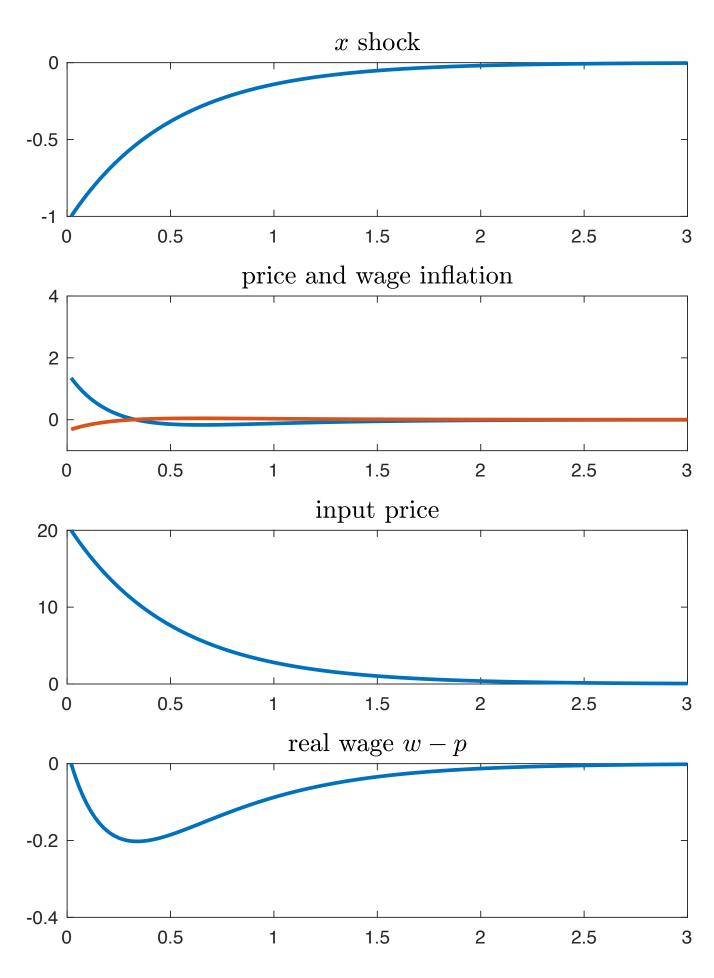
- Availability of input falls temporarily
- Two different responses of monetary policy captured by y path

- Response 1: keep y on original path (zero)
- Response 2: let y replicate flexible price benchmark y*

Supply shock

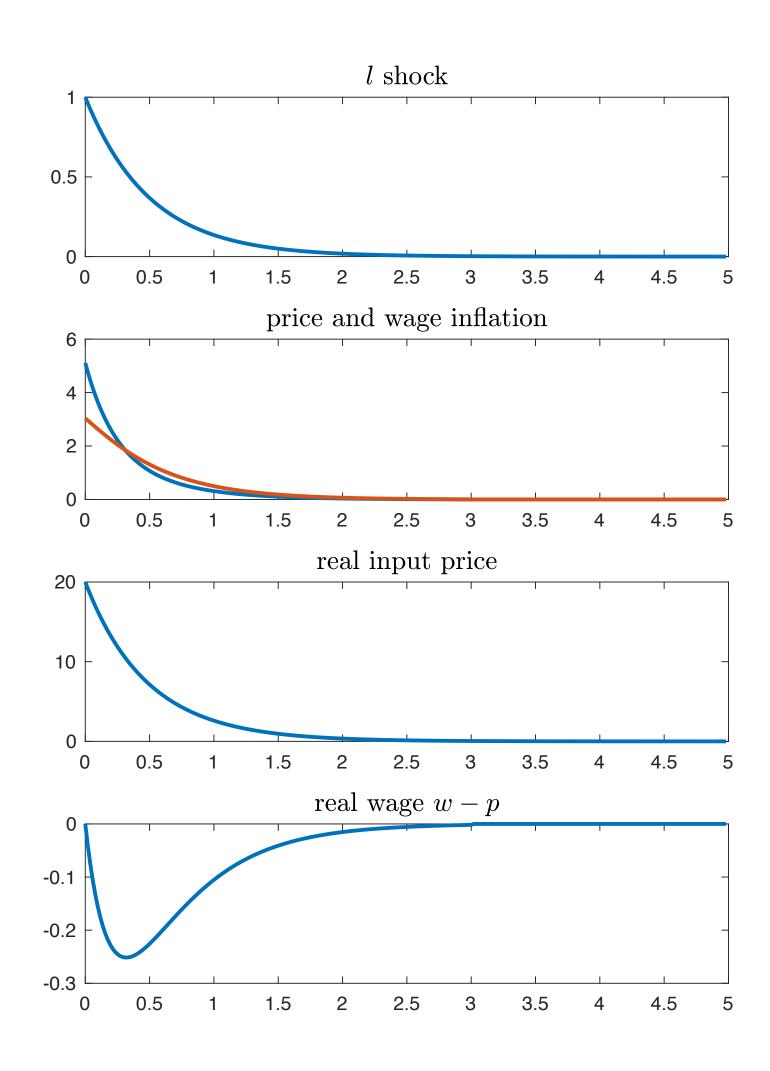
Two responses

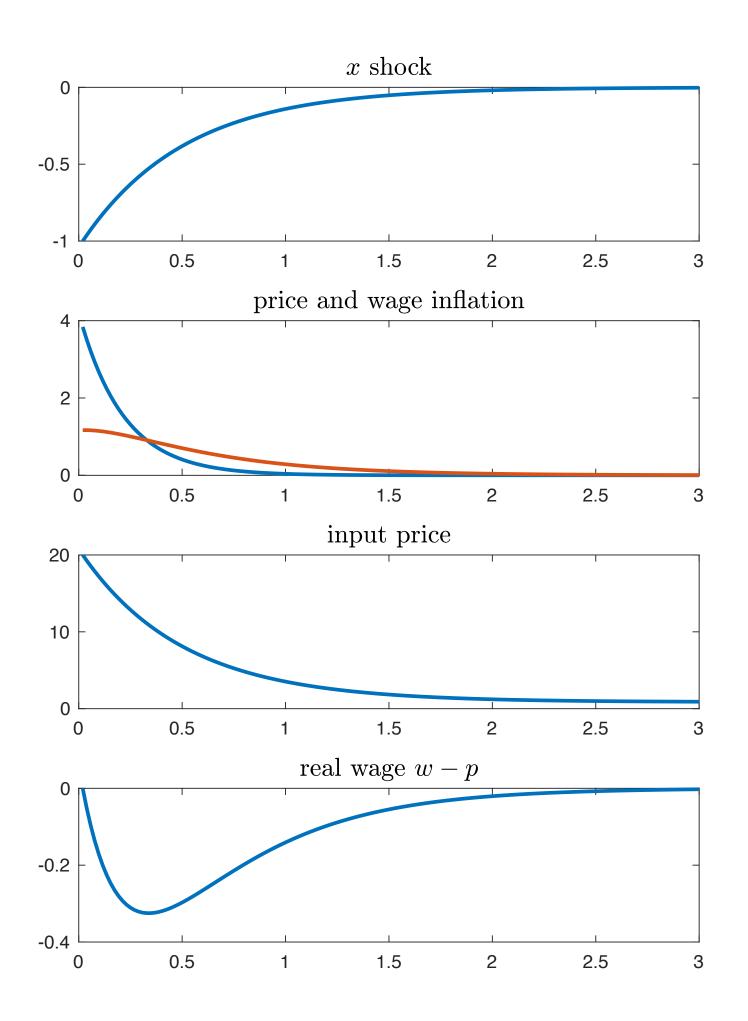




Why w/p falls less?

Demand or Supply Shocks?

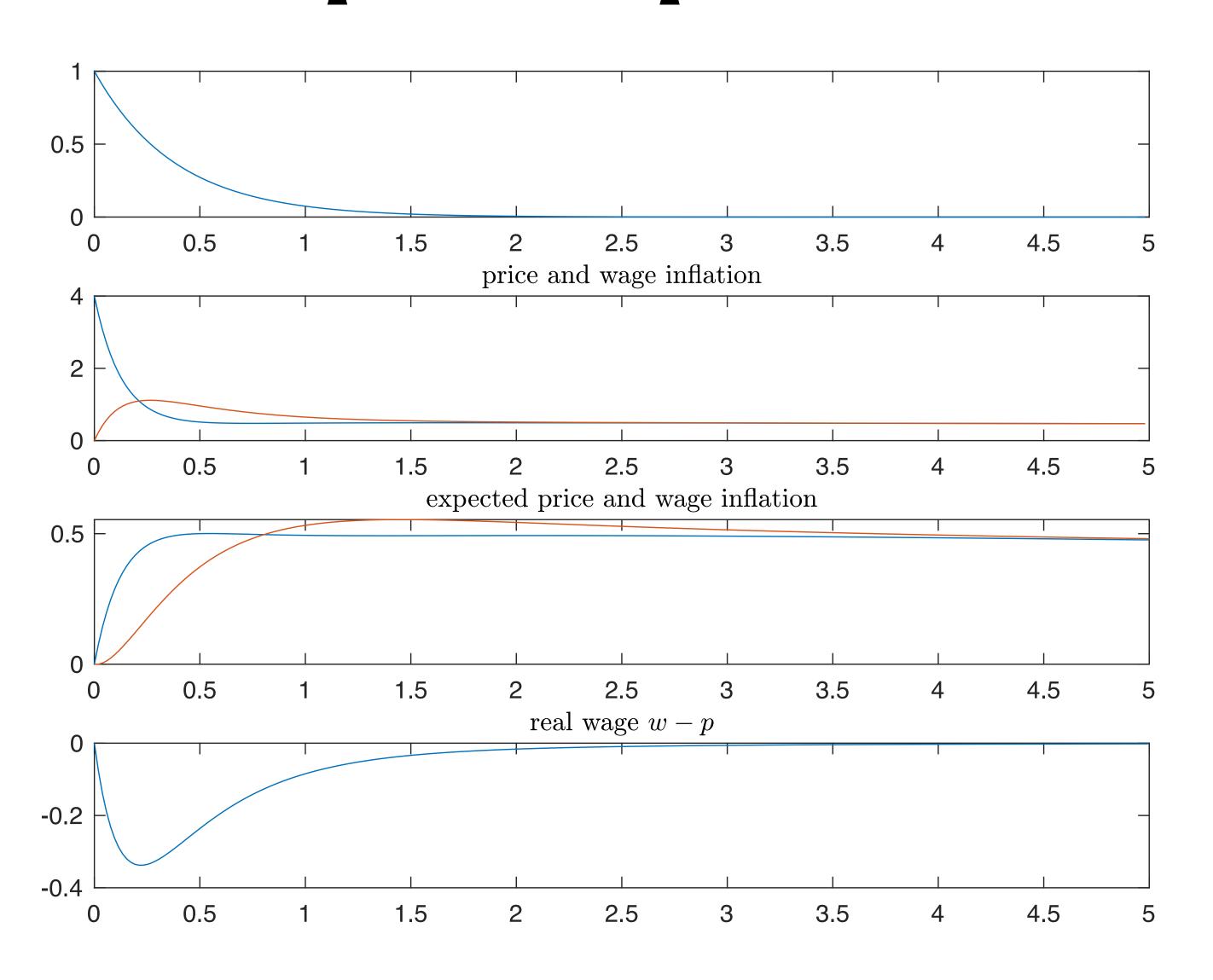




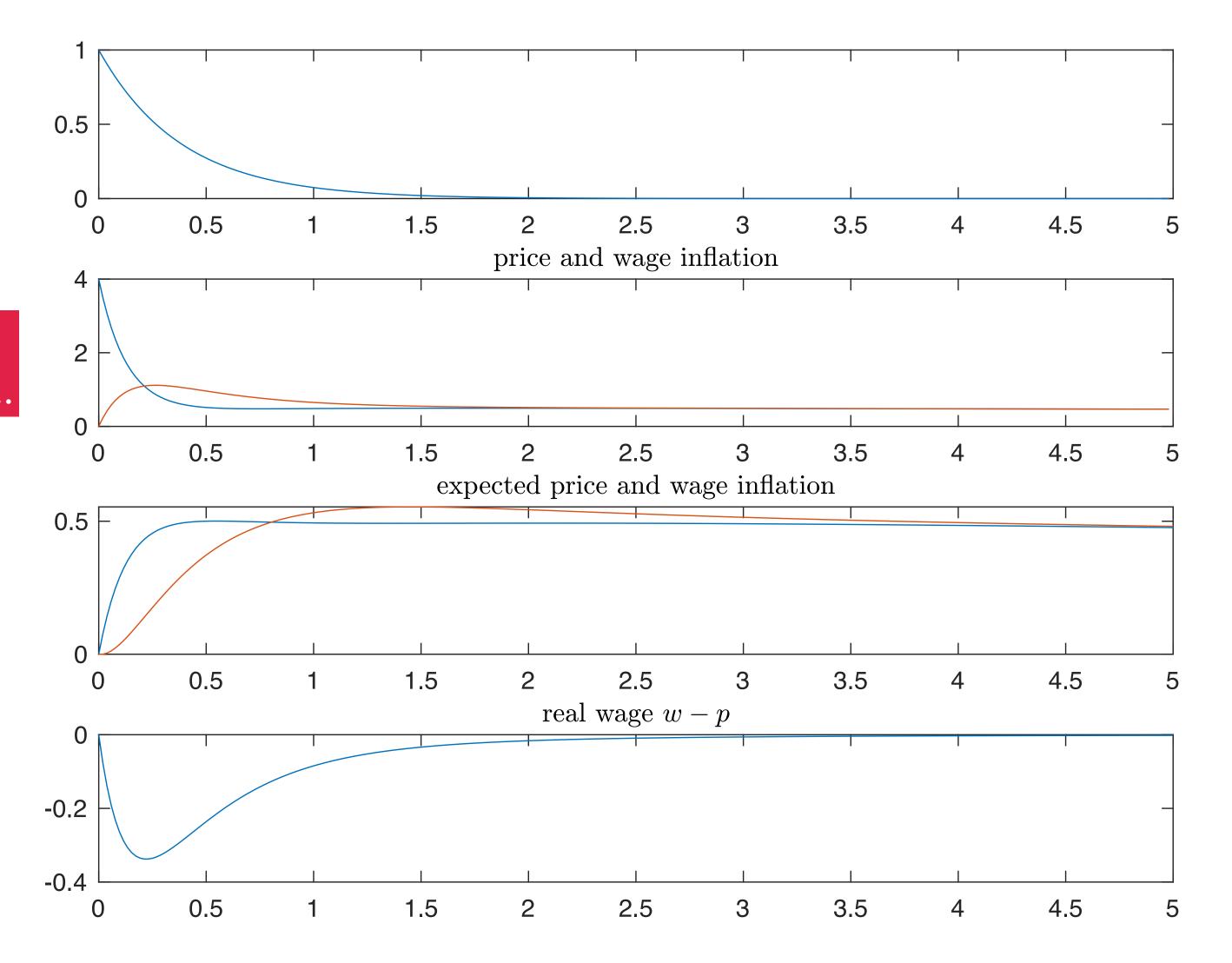
Why Does Inflation Fall?

- We have shown price inflation can fall even with higher wage inflation
- Why does price inflation fall while W/P rises?
 - price of other input falls (negative inflation)...
 - ... supply constraints easing...
 - ... related: profit margin is high, room for real wages to recover;
 - wage increases partially priced in (forward looking rational expectations)
- Caveats in reality...
 - are input prices (or supply constraints) falling enough?
 - adaptive non-rational expectations?

Adaptive Expectations

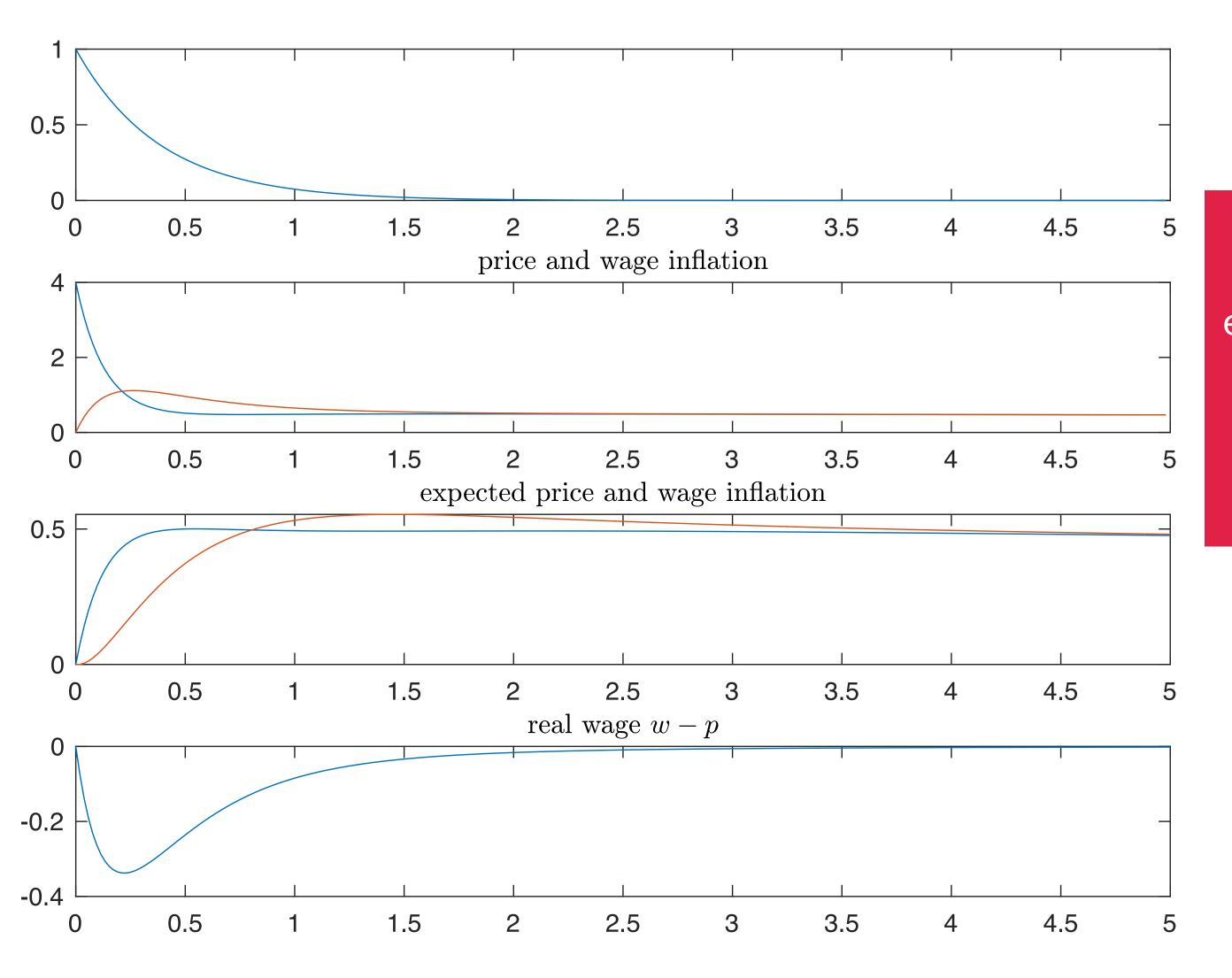


Adaptive Expectations



Wage inflation takes more time to develop....

Adaptive Expectations



Wage inflation takes

more time to develop....

Inflation stays positive for much longer! Does eventually go to zero slowly (outside figure's range)

Takes a recession to bring infaltion down?

Zero Output Gap Policy

- Result: if CB targets zero output gap, we cannot have $\pi > 0$ and $\pi^w > 0$
- Why?
- Zero output gap is equivalent to $mrs_t = mpl_t = \omega_t^*$ so

$$\pi_t = \Lambda_p \int_t^{\infty} e^{-\rho(s-t)} \left(\omega_s - \omega_s^*\right) ds$$

$$\pi_t^w = \Lambda_w \int_t^{\infty} e^{-\rho(s-t)} \left(\omega_s^* - \omega_s\right) ds$$

• Is zero output gap optimal?

4. Optimal Policy

Quadratic Approximation

- Usual approach: quadratic approximation of welfare near undistorted steady state
- Objective function

$$-\int_{0}^{\infty} e^{-\rho t} \frac{1}{2} \left[\Phi_{y} \left(y_{t} - y_{t}^{*} \right)^{2} + \Phi_{p} \pi_{t}^{2} + \Phi_{w} \left(\pi_{t}^{w} \right)^{2} \right] dt$$

- Distorted labor supply margin and distortions due to dispersion in relative prices and relative wages
- Coefficients Φ are functions of model's underlying parameters

Optimal problem

A permanent shock

- Focus on a permanent shock to x_t
- Equivalent to analyze no shock but wrong initial condition: $\omega_0 \neq 0$
- Maximize

$$-\int_{0}^{\infty} e^{-\rho t} \frac{1}{2} \left[\Phi_{y} y_{t}^{2} + \Phi_{p} \pi_{t}^{2} + \Phi_{w} \left(\pi_{t}^{w} \right)^{2} \right] dt$$
subject to
$$\rho \pi_{t} = \Lambda_{p} \left(\omega_{t} + \xi_{p} y_{t} \right) + \dot{\pi}_{t}$$

$$\rho \pi_{t}^{w} = \Lambda_{w} \left(\xi_{w} y_{t} - \omega_{t} \right) + \dot{\pi}_{t}^{w}$$

$$\dot{\omega}_{t} = \pi_{t}^{w} - \pi_{t}$$
given ω_{0}

Questions

• Well known that divine coincidence fails here, but that's just a statement on feasibility

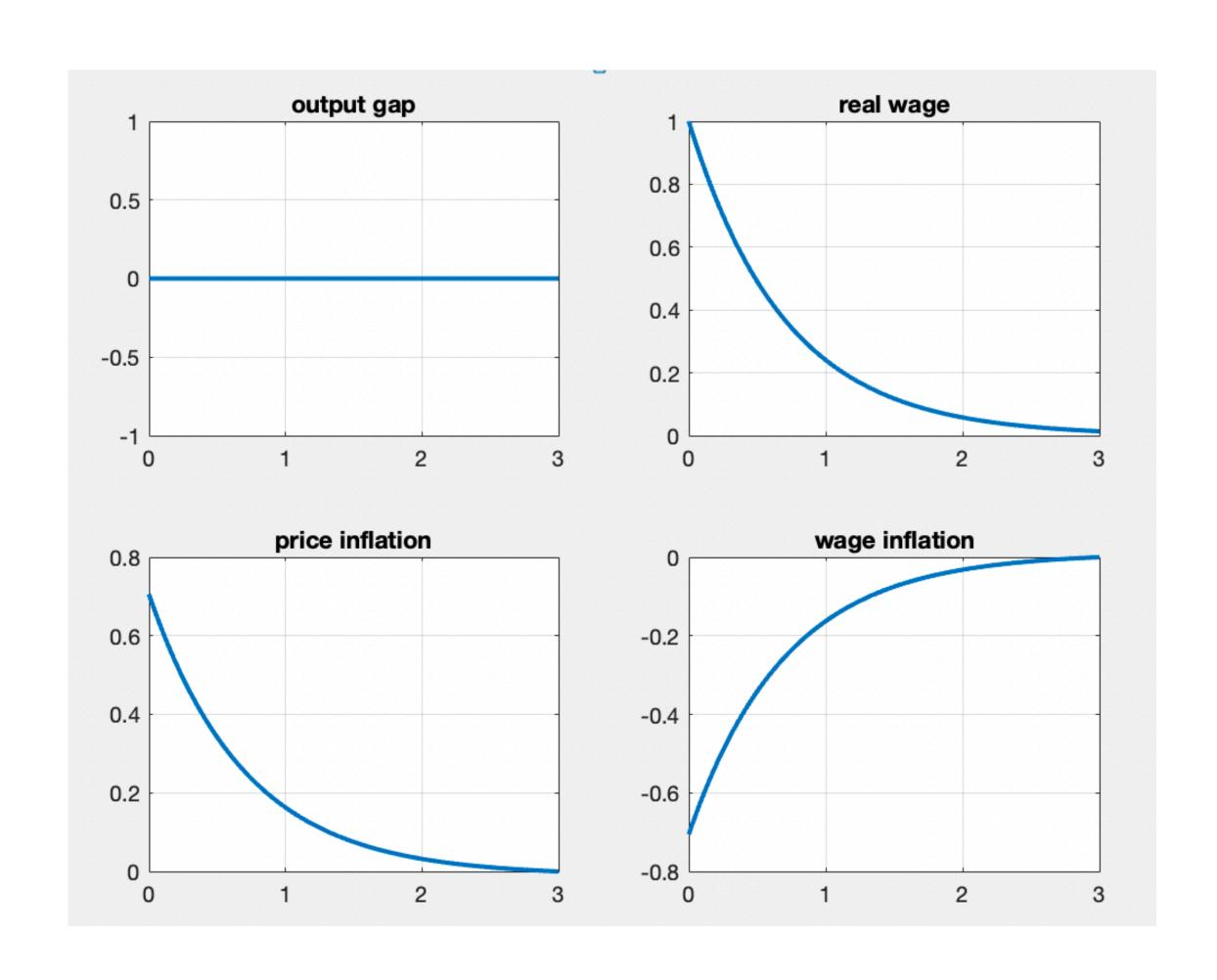
- Can it be optimal to run the economy hot? I.e., have $y_t > 0$ and $\pi_t > 0$
- Can it be optimal to have generalized inflation? I.e., have $\pi_t > 0$ and $\pi_t^w > 0$
- Can it be optimal to have a hot economy AND generalized inflation

$$y_t > 0, \quad \pi_t > 0, \quad \pi_t^w > 0$$

If yes, why?

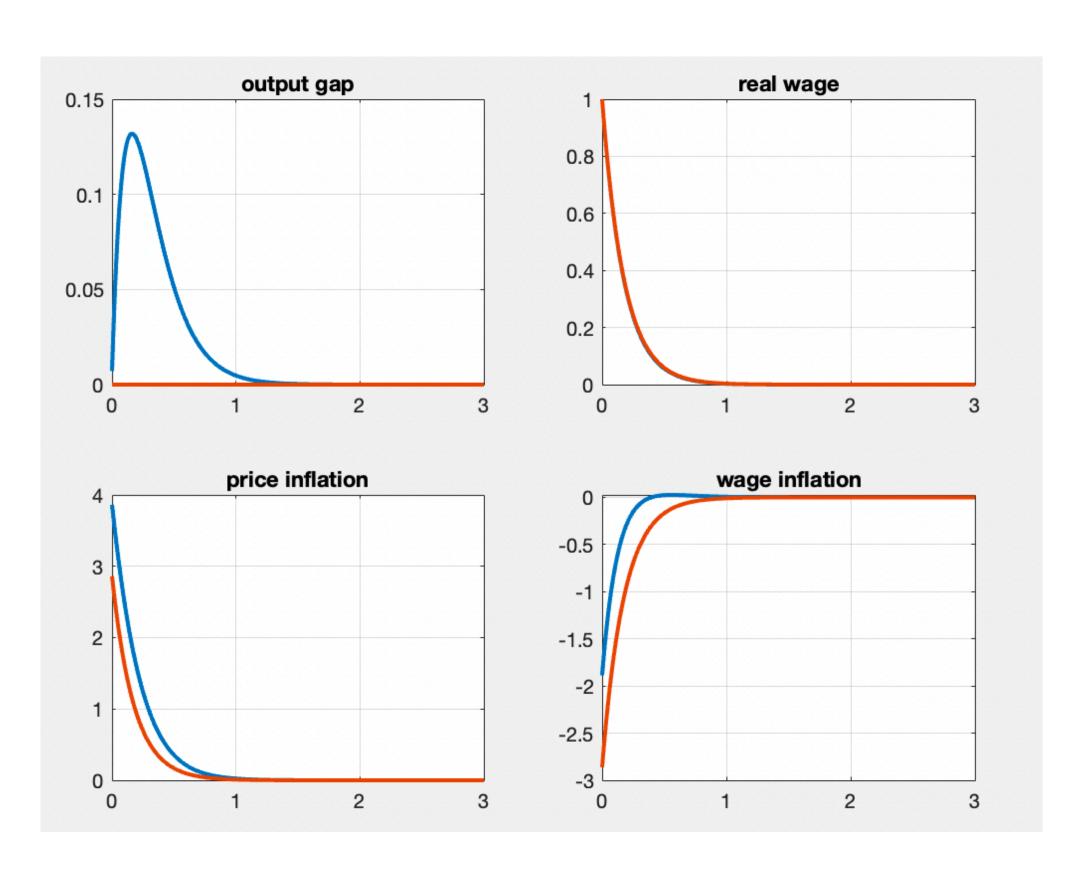
Example 1: symmetry

- A very symmetric example where parameters are such that
 - 1. $\Phi_p = \Phi_w$ same welfare weights
 - 2. $\Lambda_p = \Lambda_w$ same stickiness
 - 3. $\xi_p = \xi_w$ same responses of mpl and mrs to output gap deviations



Example 2: hot economy

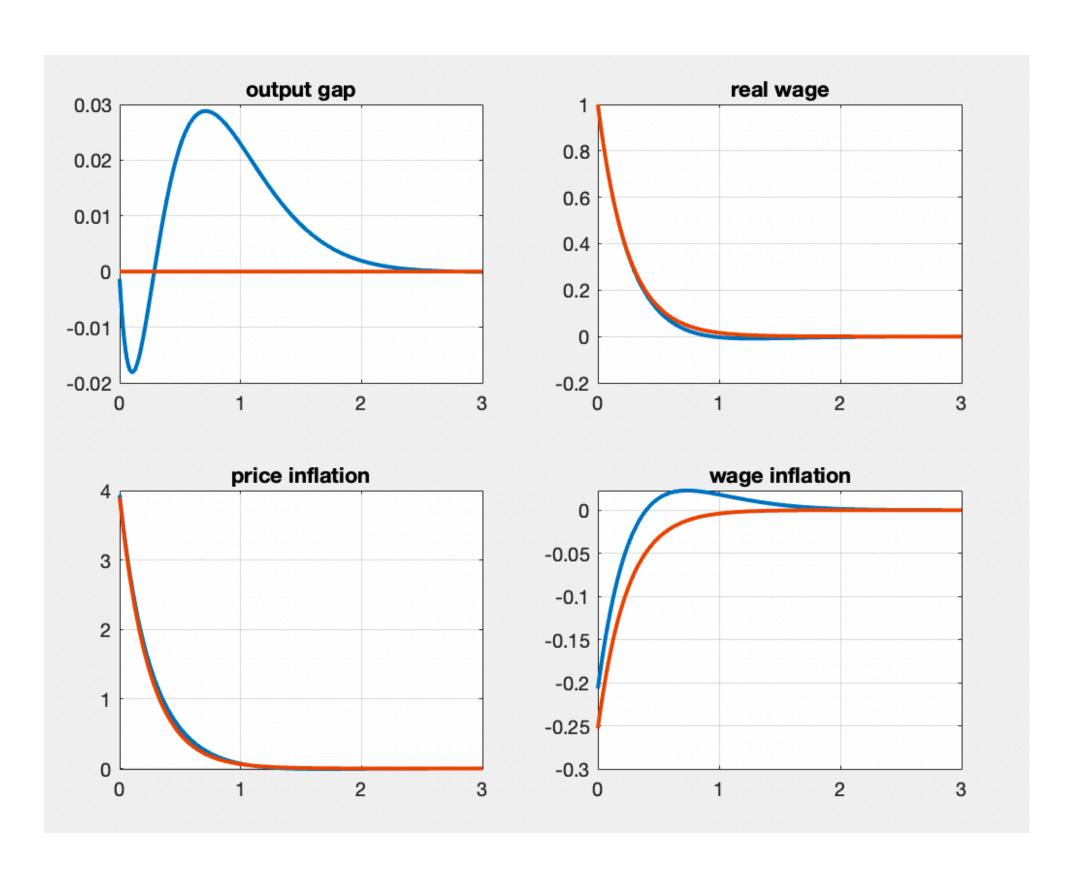
- 1. $\Phi_p < \Phi_w$ more concern with wage distortions
- 2. $\Lambda_p > \Lambda_w$ prices more flex
- 3. $\xi_p \approx \xi_w$ similar responses of mpl and mrs to output gap deviations



In blue: optimal path
In red: zero output gap

Example 4: hot+generalized

- 1. $\Phi_p < \Phi_w$ more concern with wage distortions
- 2. $\Lambda_p > \Lambda_w$ prices more flex
- 3. $\xi_p \approx \xi_w$ similar responses of mpl and mrs to output gap deviations



In blue: optimal path In red: zero output gap

Concluding

- Wage price spirals are a component of existing macro models
- Which way W/P goes during a spiral depends on relative force of disturbances
- Pure aggregate demand shock can cause a real wage contraction
- 3 phase shock (demand or supply): scarcity pops up in some places, then it feeds back in general inflation, then it feeds back in wage inflation
- Shortages and relative price jumps tend to fade earlier than general wage and price inflation
- Optimal response may involve combinations of $y > y^*$, $\pi > 0$, $\pi^w > 0$