

# Non-Linear Inflation Dynamics In Menu Cost Economies

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# Motivation

- Menu costs often invoked as source of price rigidities
  - firms more likely to respond to large aggregate shocks
  - so Phillips curves non-linear
- We show standard menu cost models predict linear Phillips curves
  - when consistent with the distribution of micro price changes
  - for moderate inflation rates observed in advanced economies
- Need implausibly large menu costs, esp with strategic complementarities
  - counterfactually, no comovement btw inflation and frequency of adjustment
  - and very large losses from misallocation from price dispersion

# Our Resolution

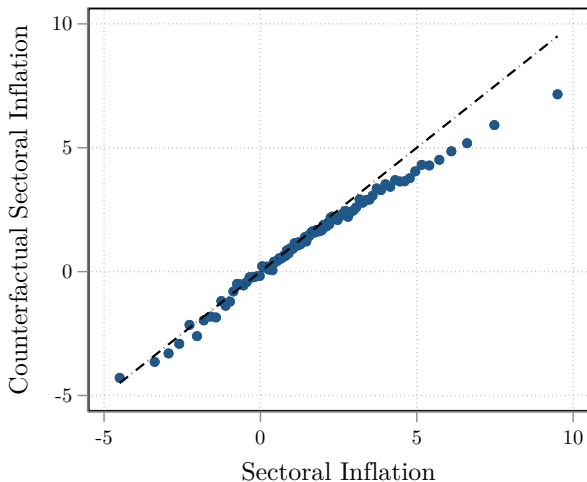
- Extend multi-product menu cost model
  - strategic complementarities at firm, not product, level
  - low elasticity of substitution between products of a firm
- Model implies less within-firm misallocation from price dispersion
  - require smaller menu costs to reproduce distribution of price changes
- Our model predicts non-linear output responses to monetary shocks
  - in contrast to standard models
  - due to strong response in the frequency of adjustment

# Motivating Fact

# Inflation and the Frequency of Adjustment

- UK micro-price data underlying the CPI, organized in 71 sectors
  - focus on regular price changes: exclude V-shaped sales < 3 months figure
- Decompose  $\pi_t(s)$  extensive and intensive margin (Klenow-Kryvtsov, 2005)
- $\pi_t(s) = \Delta_t(s)f_t(s)$ 
  - $\Delta_t(s)$  : average price change conditional on adjustment
  - $f_t(s)$  : fraction of price changes
- Isolate role of intensive margin by computing  $\pi_t^c(s) = \Delta_t(s)\bar{f}(s)$ 
  - $\bar{f}(s)$ : average frequency in sector  $s$

## Evidence From All Sectors



Extensive margin of price adjustment important at high rates of inflation

# Single-Product Model

# Model Overview

- Consumers: log-linear preferences + cash in advance constraint

- so  $W_t = P_t c_t = M_t$

- Continuum of sectors: Cobb-Douglas aggregator

- Sectoral output:  $y_t(s) = \left( \int \left( \frac{y_t(f,s)}{u_t(f,s)} \right)^{\frac{\sigma-1}{\sigma}} df \right)^{\frac{\sigma}{\sigma-1}}$

- Firm output:  $y_t(f,s) = e_t(s) u_t(f,s) l_t(f,s)^\eta$

- $e_t(s)$  and  $u_t(f,s)$  independent random walks with Gaussian innovations

- Menu costs  $\xi$  drawn from  $U[0, \bar{\xi}]$

- with probability  $1 - \lambda$  free price change



# Parameterization

- Assigned
  - period 1 month
  - $\sigma = 6$  so flexible price markup 1.20,  $\eta = 2/3$ ,  $\beta = 0.96$
- Choose menu cost and s.d. firm shocks to match UK micro data

	Data	Model
frequency $\Delta p$	0.12	0.12
<i>distribution of <math>\Delta p</math></i>		
mean	0.02	0.02
std. dev.	0.19	0.20
kurtosis	3.61	3.65
10 <sup>th</sup> percentile	-0.23	-0.23
25 <sup>th</sup> percentile	-0.08	-0.10
50 <sup>th</sup> percentile	0.03	0.02
75 <sup>th</sup> percentile	0.12	0.14
90 <sup>th</sup> percentile	0.25	0.27

# Menu Costs and Misallocation

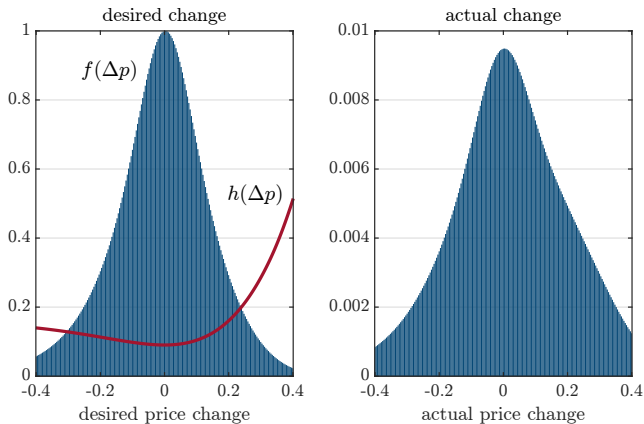
- Calibrated parameters

s.d. idios. shocks	$\sigma_u$	0.067
prob. free price change	$1 - \lambda$	0.091
menu cost rel to avg sales		0.088

- Menu costs much larger than existing estimates ( $\approx 1\%$ )
- Productivity losses from price dispersion are 21.63%
  - as large as De Loecker–Eeckhout–Unger, Baqaee–Farhi estimates
  - but they capture all distortions, not just menu costs

table

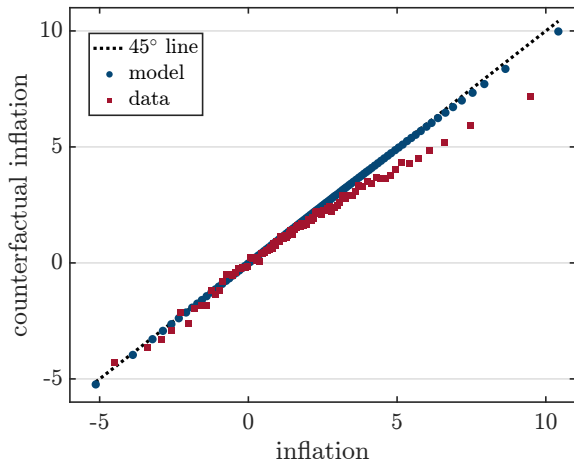
# Why Menu Costs So Large?



- Need large probability free  $\Delta p$  to match small  $|\Delta p|$
- Need relatively flat hazard to match large  $|\Delta p|$

formula

# Extensive Margin of Adjustment



Weak extensive margin even at high rates of inflation

# Multi-Product Model

# Overview

- Build on Midrigan (2011) and Alvarez–Lippi (2014) multi-product model
  - firms sell continuum of products
  - product quality shocks  $z_{it}(f, s)$ , in addition to firm-specific  $u_t(f, s)$
  - economies of scope in price adjustment: menu cost  $\bar{\xi}$  to change all prices
  
- Add two ingredients
  - specific factor (e.g. managerial input) mobile across products within firm
  - low elasticity of substitution between products of a given firm

# Technology

- Composite good of firm  $f$

$$y_t(f, s) = \left( \int_0^1 \left( \frac{y_{it}(f, s)}{z_{it}(f, s)} \right)^{\frac{\gamma-1}{\gamma}} di \right)^{\frac{\gamma}{\gamma-1}}$$

- Individual varieties produced using labor and specific factor  $m_{it}$

$$y_{it}(f, s) = e_t(s) u_t(f, s) z_{it}(f, s) m_{it}(f, s)^{1-\eta} l_{it}(f, s)^\eta$$

- specific factor mobile across products, fixed at firm level

$$\int m_{it}(f, s) di = 1 \quad \text{vs.} \quad m_{it}(f, s) = 1$$

- Firm production function

$$y_t(f, s) = e_t(s) u_t(f, s) \phi_t(f, s) l_t(f, s)^\eta$$

# Parameterization

- Two economies
  - our model:  $\gamma = 1$ ,  $\sigma = 6$ , mobile specific factor
  - standard multi-product model:  $\gamma = \sigma = 6$ , fixed specific factor

	Data	Our model	Standard
frequency $\Delta p$	0.12	0.12	0.12
<i>distribution of <math>\Delta p</math></i>			
mean	0.02	0.02	0.03
std. dev.	0.19	0.20	0.20
kurtosis	3.61	3.57	3.51
10 <sup>th</sup> percentile	-0.23	-0.23	-0.23
25 <sup>th</sup> percentile	-0.08	-0.11	-0.09
50 <sup>th</sup> percentile	0.03	0.02	0.04
75 <sup>th</sup> percentile	0.12	0.14	0.16
90 <sup>th</sup> percentile	0.25	0.26	0.26



# Menu Costs and Misallocation

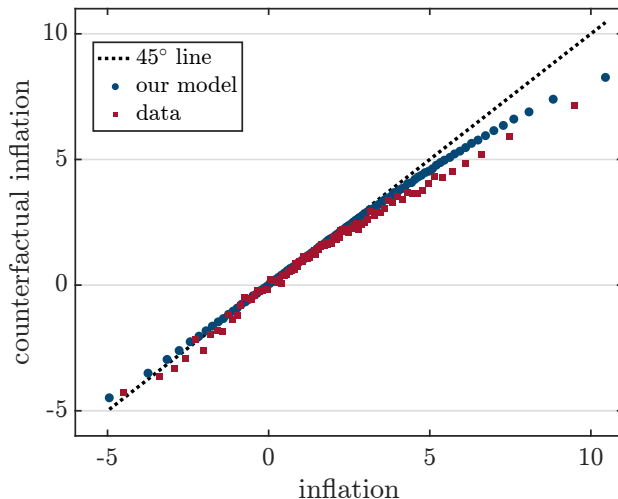
- Calibrated parameters

		Our model	Standard
s.d. product shocks	$\sigma_z$	0.062	0.058
s.d. firm shocks	$\sigma_u$	0.025	0.037
menu cost rel to avg sales		0.024	0.258

- Menu costs in our model closer to the 1% estimates
- Smaller losses from price dispersion: 1.97% (21.24%)

table

# Importance of Extensive Margin



Stronger extensive margin at high inflation, 1/2 of data

standard

table

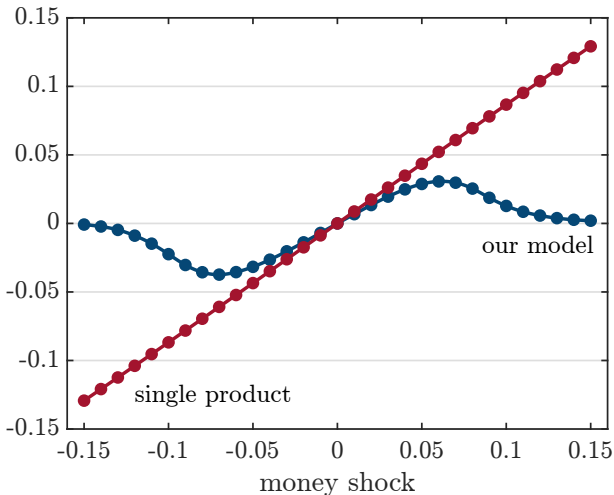
robustness

# Real Effects of Monetary Shocks

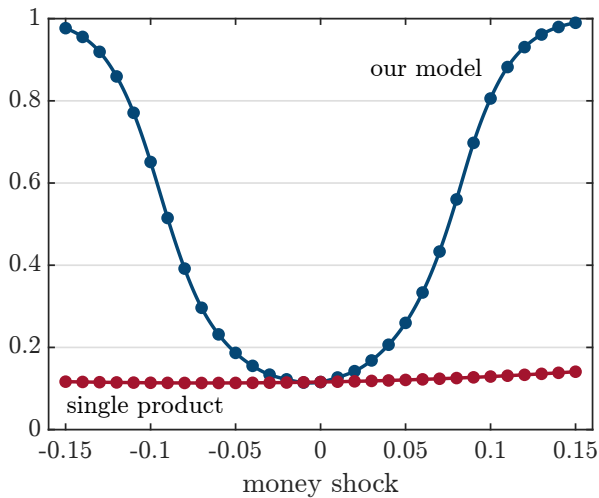
# Impulse Responses to One-Time Shocks

- Response of  $y_t$  to one-time, unanticipated, permanent changes in  $M_t$ 
  - for shocks of different sizes to gauge non-linearity
  - contrast our model to single product model
- Since  $P_t y_t = M_t$ , larger response of  $y_t$  due to slower  $P_t$  response

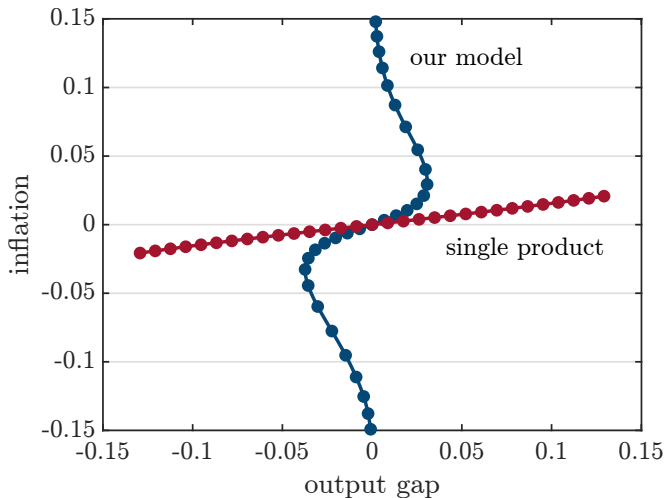
# Output Response on Impact



# Frequency of Price Changes on Impact



# Non-Linear Phillips Curve



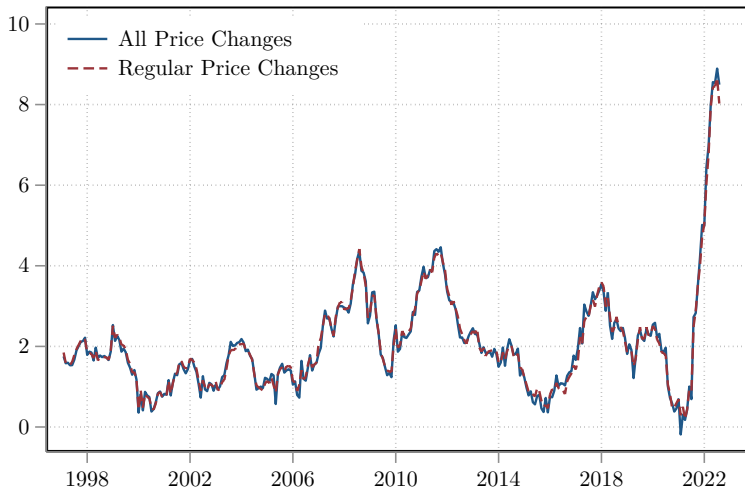
decomposition

# Conclusions

- Standard menu cost models predict linear inflation dynamics due to
  - implausibly large menu costs and misallocation from price dispersion
  - counterfactually low of comovement btw inflation and freq of adjustment
- Proposed simple extension to remedy these shortcomings
  - less misallocation from price dispersion inside the firm
- Model reproduces micro price statistics with much smaller menu costs
- Predicts non-linear output responses to monetary shocks



# Inflation in UK



# Importance of Extensive Margin

## Inflation Volatility

s.d. $\pi_t(s)$	2.87
s.d. $\pi_t^c(s)$	2.51
ratio	0.87

## Slope of $\pi_t^c(s)$ to $\pi_t(s)$

all observations	0.80
$\pi_t(s) > 75^{th}$ pct.	0.48
$\pi_t(s) > 90^{th}$ pct.	0.39

All statistics weighted using sectoral expenditure weights.

# Evidence from Other Countries

- Karadi-Reiff (2019)
  - study response of prices to 5% value added tax increase in Hungary
  - frequency price changes up from 13% to 62%
  - show menu cost model with fat-tailed shocks reproduces evidence
- Mexico: Gagnon (2009)
- Argentina: Alvarez-Beraja-Gonzalez-Rozada-Neumayer (2018)
- US: Nakamura-Steinsson (2018)

# Real Marginal Cost Index

- Define real marginal cost index

$$a_t(s) = \frac{W_t}{P_t(s) y_t(s)} \left( \frac{y_t(s)}{e_t(s)} \right)^{\frac{1}{\eta}}$$

- If price flexible,  $a_t(s) = \eta$

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# Standardized Price Changes

- Data organized in 6-digit sectors and items (product categ. within sector)
- Let  $i$  be product quote,  $j$  be item,  $\Delta p_{it}(j)$  log price change if adjust
- Standardized price change (Klenow-Kryvtsov 2008)

$$\hat{\Delta} p_{it}(j) = \frac{\Delta p_{it}(j) - \mu_{\Delta}(j)}{\sigma_{\Delta}(j)} \sigma_{\Delta} + \mu_{\Delta}$$

- $\mu_{\Delta}(j), \mu_{\Delta}$ : mean non-zero log price changes
- $\sigma_{\Delta}(j), \sigma_{\Delta}$ : std. dev. non-zero log price changes

# Demand

- Demand for individual product

$$y_{it}(f, s) = z_{it}(f, s) \left( \frac{z_{it}(f, s) P_{it}(f, s)}{P_t(f, s)} \right)^{-\gamma} y_t(f, s)$$

- Composite firm price

$$P_t(f, s) \equiv \int P_{it}(f, s) \frac{y_{it}(f, s)}{y_t(f, s)} di = \left( \int (z_{it}(f, s) P_{it}(f, s))^{1-\gamma} di \right)^{\frac{1}{1-\gamma}}$$

- Labor required to produce bundle  $y_{it}(f, s)$

$$l_t(f, s) = \left( \int \frac{y_{it}(f, s)}{e_t(s) u_t(f, s) z_{it}(f, s)} di \right)^{\frac{1}{\eta}}$$

# Markup Dispersion

- Model generates large dispersion in markups, misallocation

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cost-weighted average	1.195
sales-weighted average	1.592

*cost-weighted distribution*

10 <sup>th</sup> percentile	0.496
25 <sup>th</sup> percentile	0.691
50 <sup>th</sup> percentile	1.043
75 <sup>th</sup> percentile	1.585
90 <sup>th</sup> percentile	1.940
misallocation losses, %	21.63

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- As dispersed as De Loecker–Eeckhout–Unger, Baqaee–Farhi estimates
  - but they capture all distortions, not just menu costs

# Why Menu Costs So Large?

- Continuous time, quadratic approximation,  $\pi = 0$ ,  $\rho \downarrow 0$
- Cost of price rigidity for firm value

$$C^V = - \underbrace{\frac{\sigma(\sigma-1)}{12\eta}}_{=\frac{6 \times 5}{12 \times 2/3}} \underbrace{\mathbb{E}[\Delta p^2]}_{=0.195^2} \underbrace{(\mathbb{K}[\Delta p] + \Psi([\mathbb{K}[\Delta p]]))}_{=3.649+1.25} \times 100; \quad \Psi(1) = 1, \Psi(6) = 0$$

- Three components
  - strategic complementarities:  $\frac{\sigma(\sigma-1)}{12\eta}$
  - misallocation:  $\mathbb{E}[\Delta p^2]\mathbb{K}[\Delta p]$
  - size of menu cost:  $\mathbb{E}[\Delta p^2]\Psi([\mathbb{K}[\Delta p])$



# Importance of Extensive Margin

## Inflation Volatility

	Data	Model
s.d. $\pi_t(s)$	2.87	2.87
s.d. $\pi_t^c(s)$	2.51	2.83
ratio	0.87	0.99

## Slope of $\pi_t^c(s)$ on $\pi_t(s)$

	Data	Model
all observations	0.80	0.99
$\pi_t(s) > 75^{th}$ pct.	0.48	0.94
$\pi_t(s) > 90^{th}$ pct.	0.39	0.92

# Importance of Extensive Margin

## Inflation Volatility

	Data	Our model
s.d. $\pi_t(s)$	2.87	2.87
s.d. $\pi_t^c(s)$	2.51	2.55
ratio	0.87	0.89

## Slope of $\pi_t^c(s)$ on $\pi_t(s)$

	Data	Model
all observations	0.80	0.89
$\pi_t(s) > 75^{th}$ pct.	0.48	0.72
$\pi_t(s) > 90^{th}$ pct.	0.39	0.64

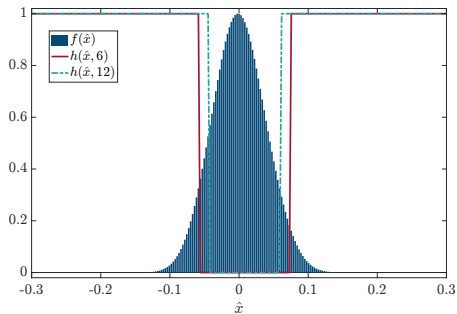
# Markup Dispersion

- Our model: much less dispersion in markups, misallocation

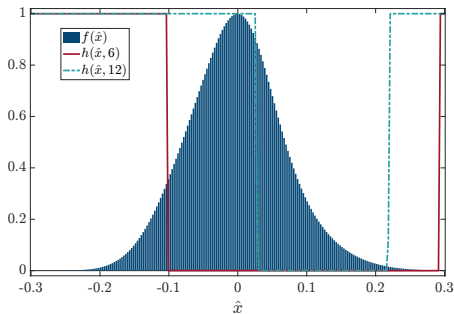
	Our model	Standard
cost-weighted average	1.194	1.191
sales-weighted average	1.210	1.285
<i>cost-weighted distribution</i>		
10 <sup>th</sup> percentile	1.019	0.827
25 <sup>th</sup> percentile	1.088	0.918
50 <sup>th</sup> percentile	1.195	1.103
75 <sup>th</sup> percentile	1.266	1.405
90 <sup>th</sup> percentile	1.382	1.793
misallocation losses, %	1.97	21.24

# Distribution of Firm Price Gaps

Our Model



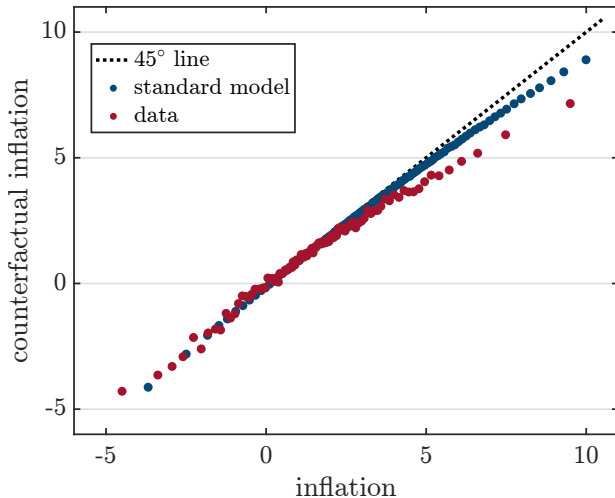
Standard



Narrower  $(s, S)$  bands, less dispersed price gap distribution in our model

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# Extensive Margin: Standard Model



# Importance of Extensive Margin

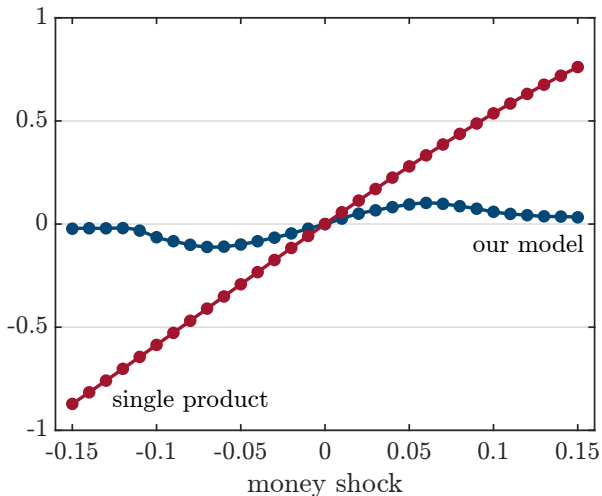
## Inflation Volatility

	Data	Our model	Standard
s.d. $\pi_t(s)$	2.87	2.87	2.86
s.d. $\pi_t^c(s)$	2.51	2.55	2.70
ratio	0.87	0.89	0.94

## Elasticity of $\pi_t^c(s)$ to $\pi_t(s)$

	Data	Our Model	Standard
all observations	0.80	0.89	0.94
$\pi_t(s) > 75^{th}$ pct.	0.48	0.72	0.82
$\pi_t(s) > 90^{th}$ pct.	0.39	0.64	0.78

# Cumulative Impulse Response



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# Inflation Pass-through to Monetary Shock $\Delta m$

- Absent shock, inflation equal to

$$\pi = \int \omega h(\omega) df(\omega)$$

- $\omega$ : desired price change,  $h(\omega)$ : adjustment hazard,  $f(\omega)$ : distribution

- Shock changes inflation to

$$\tilde{\pi} = \int (\omega + \alpha) \tilde{h}(\omega) df(\omega)$$

- $\alpha = \tilde{x}^* - x^* + \Delta m$ : response of reset price to shock
- $\tilde{h}(\omega)$ : adjustment hazard after shock

- Caballero-Engel 2007 decomposition

$$\Delta\pi = \underbrace{\alpha \int h(\omega) df(\omega)}_{\text{Calvo}} + \underbrace{\alpha \int (\tilde{h}(\omega) - h(\omega)) df(\omega)}_{\text{frequency}} + \underbrace{\int \omega (\tilde{h}(\omega) - h(\omega)) df(\omega)}_{\text{selection}}$$



# Decompose Inflation Pass-through $\Delta\pi/\Delta m$

	Single-product			Our model		
	1%	5%	10%	1%	5%	10%
total pass-through	0.129	0.135	0.146	0.323	0.421	0.861
<i>Calvo</i>	0.094	0.096	0.098	0.095	0.099	0.111
<i>frequency</i>	0.001	0.004	0.011	0.009	0.123	0.660
<i>selection</i>	0.035	0.036	0.037	0.219	0.198	0.090

- Our model: larger, more non-linear inflation response
  - stronger selection effect for small shocks
  - stronger frequency response for large shocks

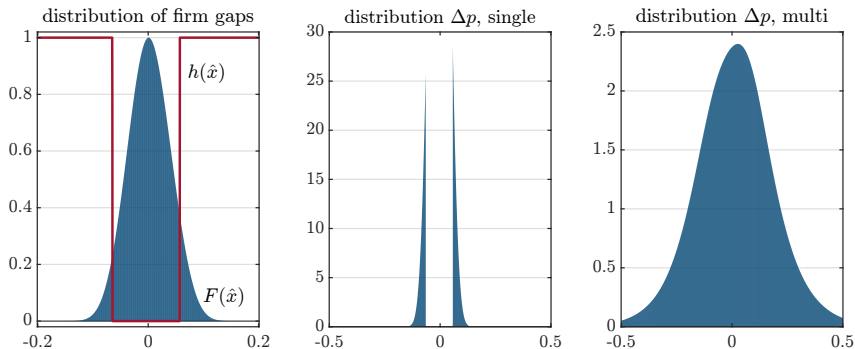
# Economy Without Within-Firm Misallocation

- Set  $\gamma = 0$  so no firm misallocation,  $\phi_t(f, s) = \exp\left(-d_t(f, s)\gamma\frac{\sigma_z^2}{2}\right) = 1$
- Problem of multi-product firm identical to single-product firm ( $\sigma_z = 0$ )
- Provided adjust trend money growth  $g_m$  so same drift in

$$\hat{x}' = \exp\left(\left(1 - \gamma\right)\frac{\sigma_z^2}{2} + \sigma_u \varepsilon_{t+1}^u(f, s) - g_m\right) \hat{x}$$

- Calibrate multi-product economy, compare to equivalent single-product

# Distribution of Price Changes



- Unlike single-product, multi-product economy matches distribution  $\Delta p$
- But output responses identical to single-product economy
- Single-product model has strong selection effect (Golosov-Lucas, 2007)

# Robustness

- Single-product model without strategic complementarities,  $\eta = 1$
- Multi-product model with  $\gamma = 0$  and  $\gamma = 3$
- Recalibrate to match same set of micro price statistics

	Single-product $\eta = 1$	Multi-product $\gamma = 0$ $\gamma = 3$	
menu costs/sales	0.021	0.014	0.047
misallocation, %	5.71	0.92	3.97
slope of $\pi_t^c$ on $\pi_t$			
all observations	0.99	0.88	0.89
$\pi_t > 90^{th}$ pct.	0.93	0.61	0.63