Expectations and the Rate of Inflation Iván Werning MIT

NBER Summer Institute - Impulse and Propagation Meeting - July 2022

Expectations \rightarrow **Inflation?**

Q: Passthrough in standard models



Expectations → **Inflation?**

- Widespread belief ... YES!
 - managing expectations is key...
 - ... expectations cause inflation...
 - ... near one-for-one



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- Recent events...

2021: expectations anchored, inflation will be small & transitory 2022: tighten monetary policy to lower expectations





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2021: expectations anchored, inflation will be small & transitory 2022: tighten monetary policy to lower expectations

- What do we know?...
 - Evidence: difficult, but some promising recent work
 - Theories: Calvo gives 1-to-1? others?...

Passthrough in standard models Q:

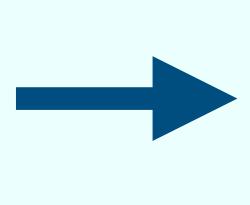




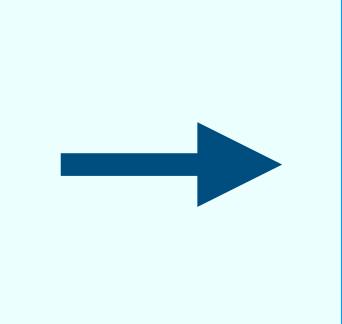
This Paper

- Standard pricing models...
 - time-dependent: Calvo, Taylor, general
 - state-dependent "menu costs"
- Solve: Optimal Pricing + Aggregation
- Important...
 - allow for arbitrary expectations π^e
 - "temporary equilibrium" (learning literature)
- Passthrough: $\pi = \phi \pi^e + \text{other stuff}$
- Full Phillips Curve $\pi_t = \sum \phi_s \pi_{t+s}^e + \sum \phi_s \pi_{t+s} + \cdots$

expectations of inflation

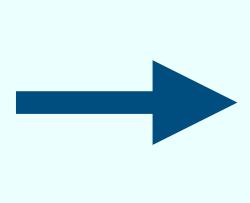


price/wage setters

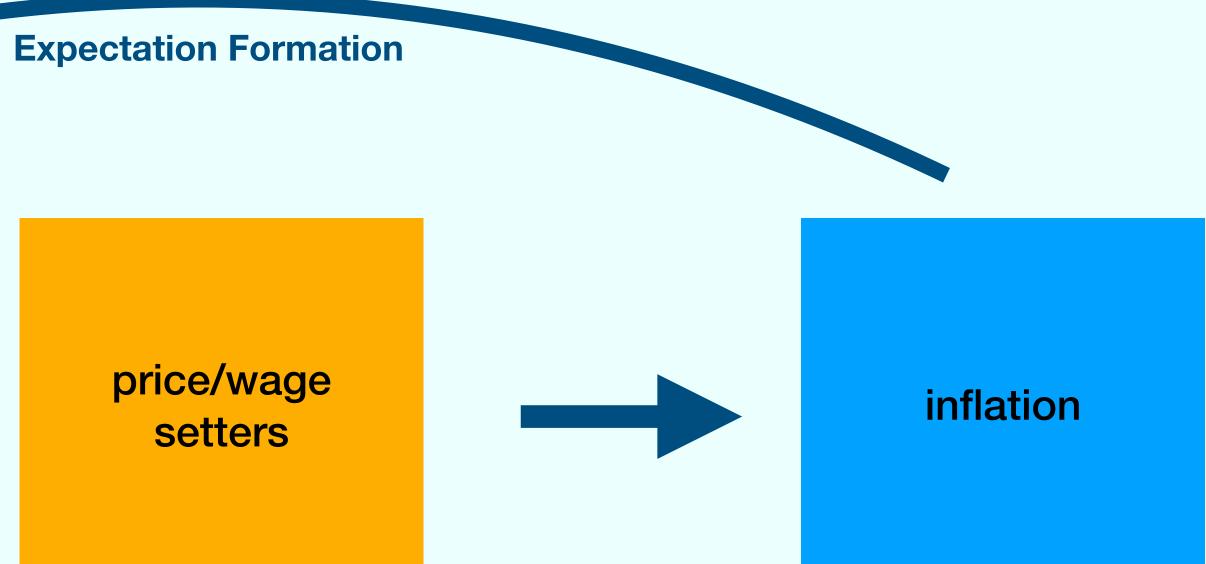


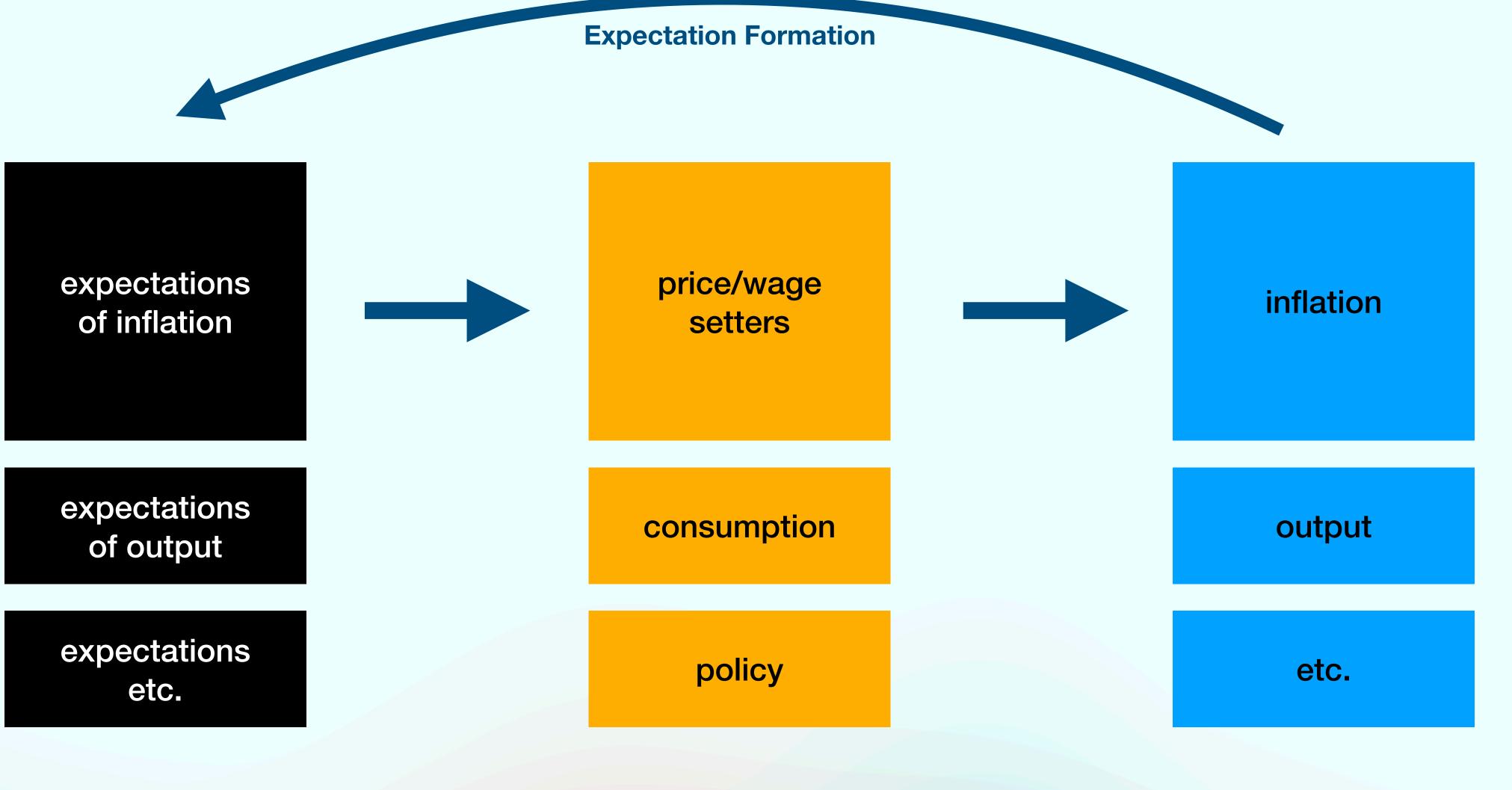
inflation

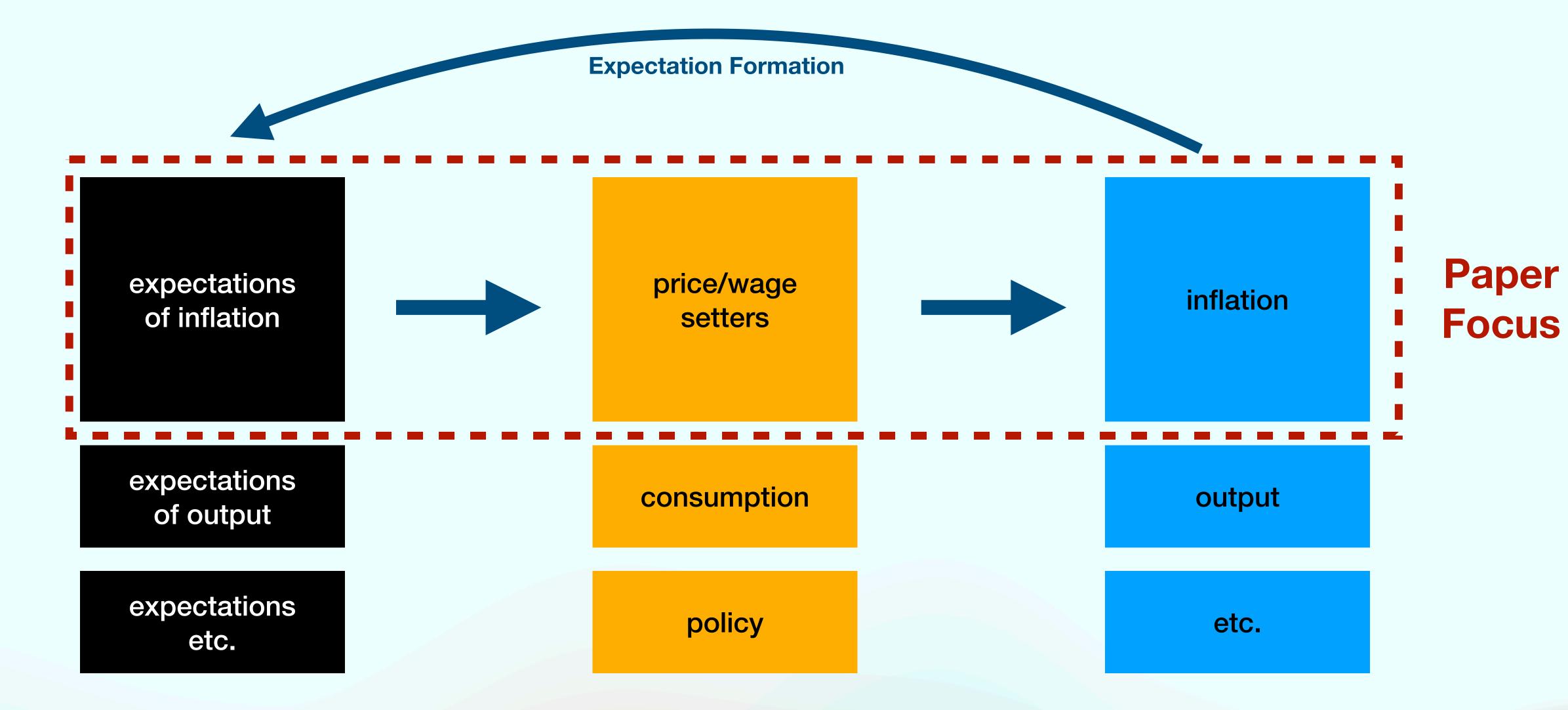
expectations of inflation



setters

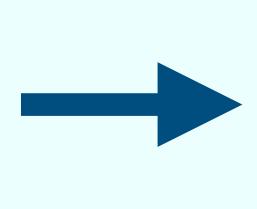




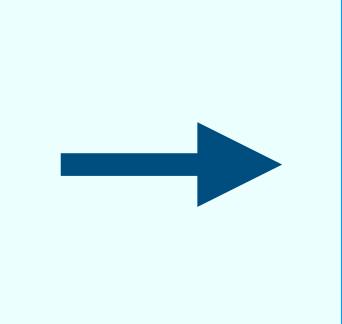




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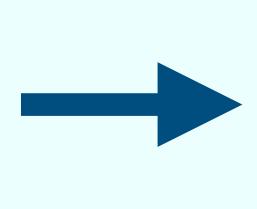


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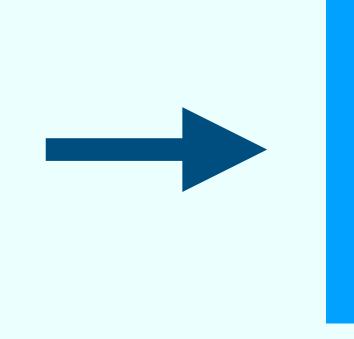


inflation

expectations of inflation



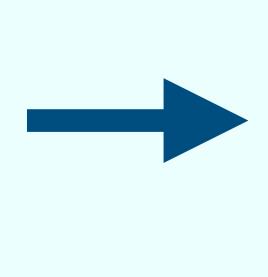
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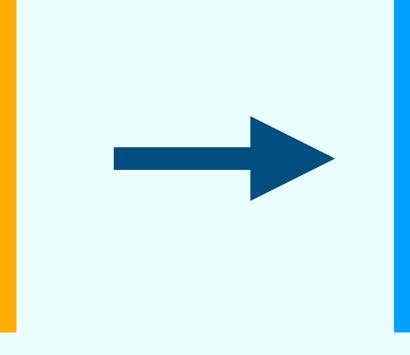
Simple Passthrough **Metric**

expectations of inflation



price/wage setters

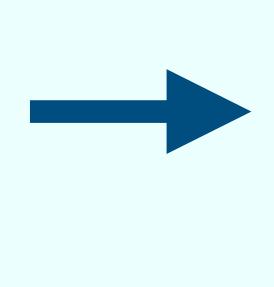
Explore Wide Range of Pricing Model



inflation

Simple Passthrough **Metric**

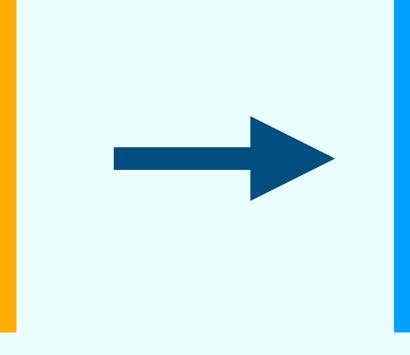
expectations of inflation



price/wage setters

Short vs Long Run **Expectations?**

Explore Wide Range of Pricing Model



inflation

Simple Passthrough **Metric**

- Passthrough: wide range...
 - dependent on pricing model
 - not ~1, potentially low
- Calvo: in theory $\phi \to 0$ if prices very sticky... ... in practice $\phi \approx 1$
- Taylor: $\phi = \frac{1}{2}$
- Sufficient statistics for general time-dependent...

duration of ongoing duration of completed

- Q: How low can we go? A: $\phi^* = \frac{1}{2}$ Taylor!
- Q: How high?

• Full Phillips Curve... • coefficients ϕ_{s} fall and zero outside rigidity

long-run Phillips curve versionen

A: any $\phi > 1!$

$\pi_t = \sum_{t=1}^{\infty} \phi_s \pi_{t+s}^e + \sum_{t=1}^{-\infty} \phi_s \pi_{t+s} + \cdots$ s=0 s=-1

ertical:
$$\sum_{s=-\infty}^{\infty} \phi_s = 1$$

- Q: How low can we go? A: $\phi^* = \frac{1}{2}$ Taylor!
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• Full Phillips Curve... • coefficients ϕ_{s} fall and zero outside rigidity

• long-run Phillips curve vertical: $\sum \phi_s = 1$

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Short-run NOT Long-Run **Expectations!**

 ∞ $s = -\infty$



- Basic state dependent "menu cost"...
 - passthrough extreme, very sensitive to specification...
 - Sheshinksi-Weiss: $\phi < 0$
 - Golosov-Lucas: $\phi > 1$
- Extensions...
 - Short run: fixed frequency $\phi < 1/2$
 - Menu costs for changing bands: $\phi = 0$

Related Literature

 Empirical Expectations: Colbion-Gorodnichenko-Ropele, Colbion-Gorodnichenko-Kumar, Rosolia

Non-Rational Expectations: Preston, Garcia-Woodford, Farhi-Werning

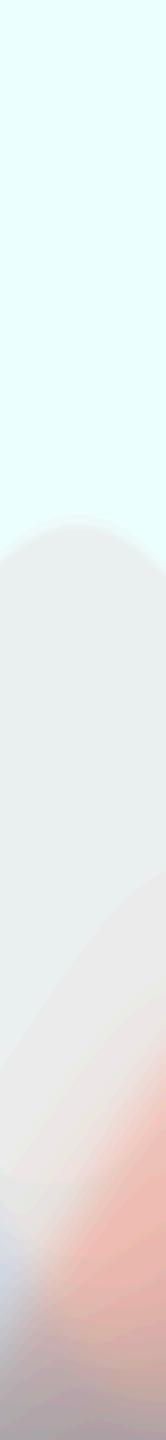
Straub

Menu Costs: Sheshinski-Weiss, Alvarez-Beraja-Gonzalez-Neumeyer

Phillips Curve: Whelan, Sheedy, Wang-Werning, Auclert-Rigato — Rognlie-



- **1.** Calvo $\phi = 1$
- 2. Taylor $\phi = \frac{1}{2}$
- 3. General Time-Dependent $\phi = \text{ongoing/completed}$
- 4. Basic State Dependent
- 5. Extension to State Dependent



- Goal...
 - passthrough from inflation expectation to inflation
 - interest rates, etc.
- Wrong answer: use NK Phillips curve $\phi = \beta \approx 1$

$$\pi_t = \kappa x_t + \beta \mathbb{E}_t \pi$$

holding everything else fixed, real marginal costs, demand,

 τ_{t+1}

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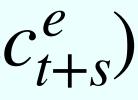


holding everything else fixed, real marginal costs, demand,

Rational Expectation inflation & real marginal costs tied up **Need to separate them!**



∞ $p_t^* = \mu + (1 - \beta \lambda) \sum_{t=1}^{\infty} (\beta \lambda)^s (P_{t+s}^e + mc_{t+s}^e)$ s=0



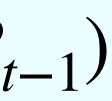


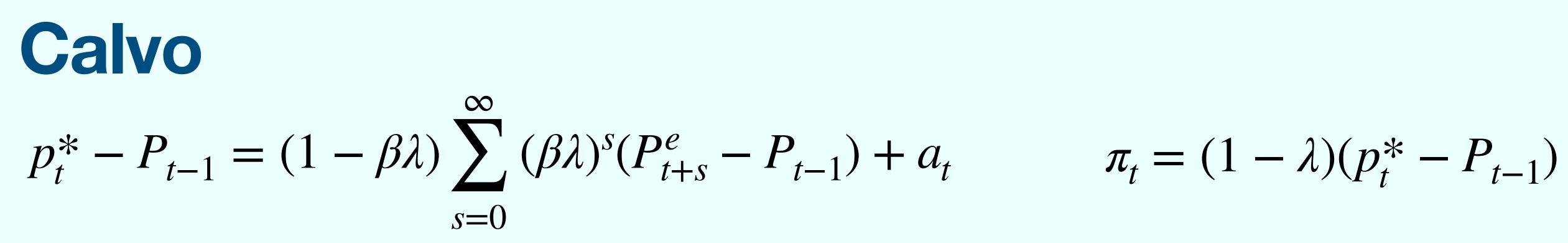
∞ $p_t^* - P_{t-1} = (1 - \beta \lambda) \sum (\beta \lambda)^s (P_{t+s}^e - P_{t-1}) + a_t$ s=0



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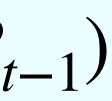
$\pi_t = (1 - \lambda)(p_t^* - P_{t-1})$

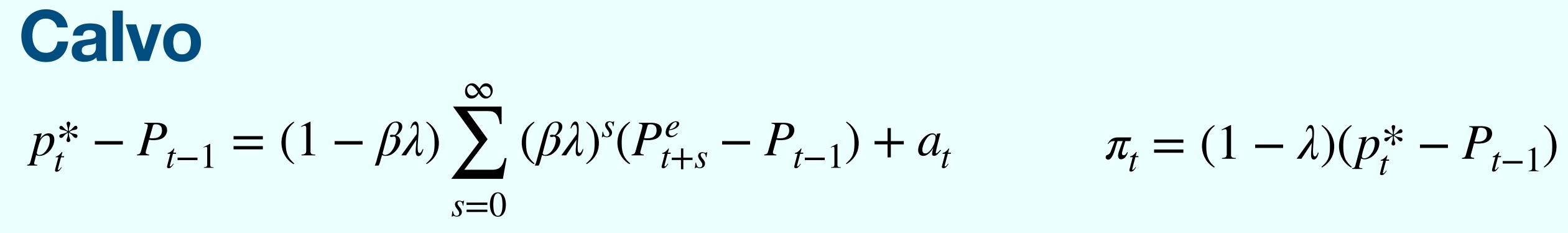




$$P_{t+s} - P_{t-1} = \pi^e (1+s)$$

Simple Inflation Expectation

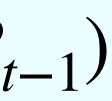


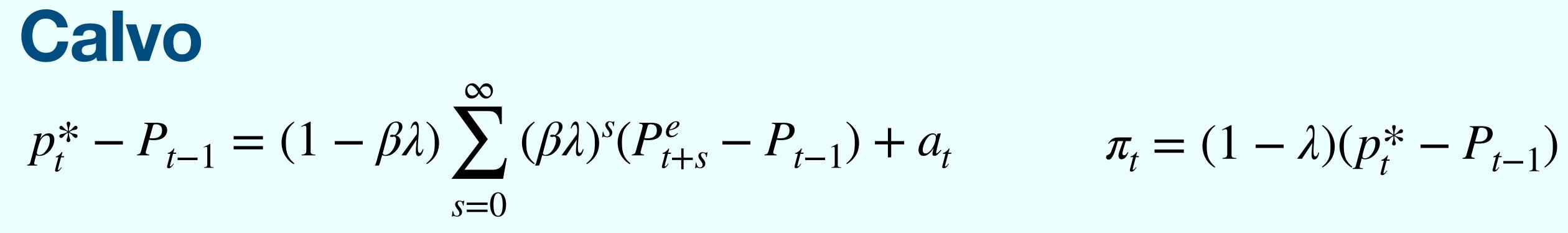


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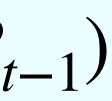


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Simple Inflation Expectation

$$\pi_t = \phi \pi^e + (1 - \lambda)a_t$$
$$\phi = \frac{1 - \lambda}{1 - \beta \lambda}$$





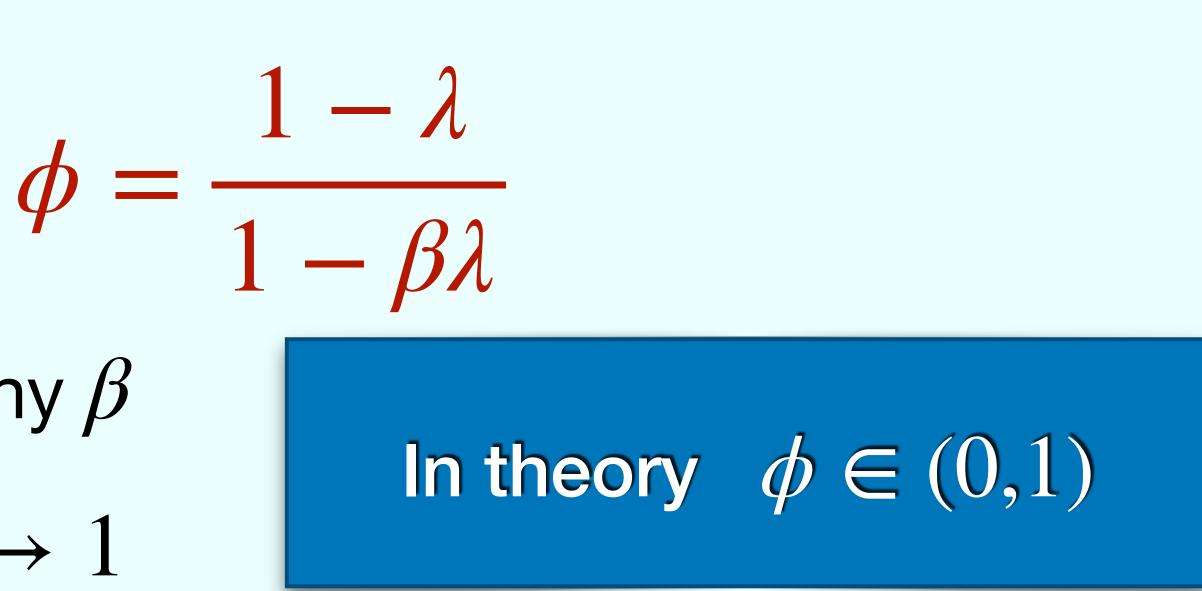


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- Continuous-time $\longrightarrow \phi = \frac{1}{\rho/\delta + 1}$ $\rho \le 0.05 \quad \delta \ge 1$ (one year stickiness)

1	— λ	
1	$-\beta\lambda$	
	In theory	$\phi \in (0,1)$

Calvo

- $\phi \to 0$ as $\lambda \to 1$ for any β
- $\phi \to 1 \text{ as } \lambda \to 0 \text{ or } \beta \to 1$
- Continuous-time $\rightarrow \phi = \frac{1}{\rho/\delta + 1}$ $\rho \le 0.05 \quad \delta \ge 1$ (one year stickiness) $\rightarrow \phi \ge 0.95$

$\phi = -\frac{1}{1}$	$1 - \lambda$
$\varphi = 1 - \beta \lambda$	
by β	In theory $\phi \in (0,1)$
→ 1	$\varphi \in (0,1)$

Calvo

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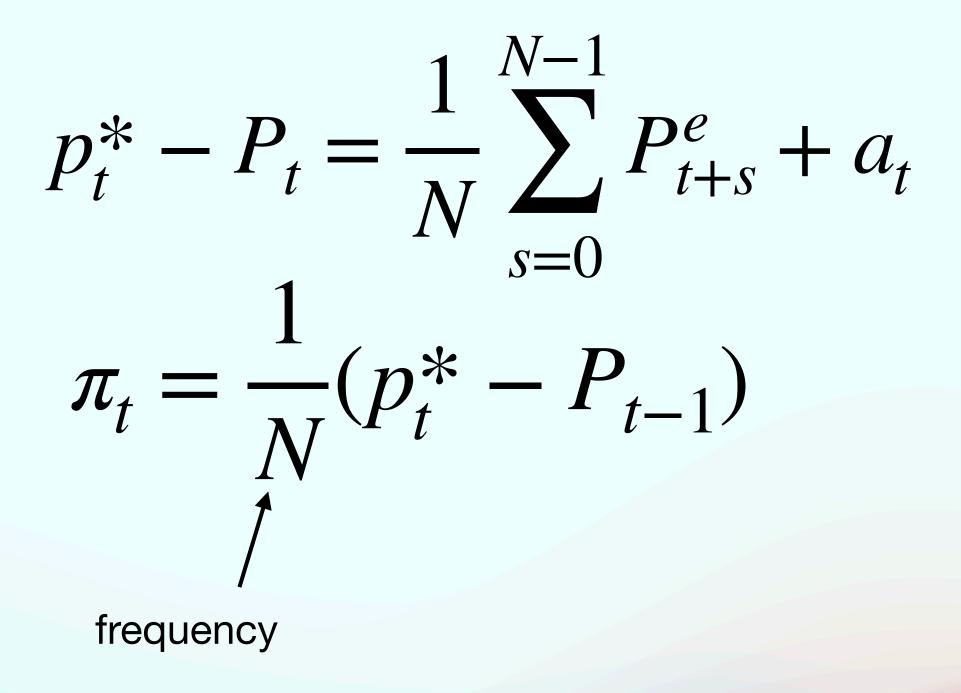
h = -	$-\lambda$ $-\beta\lambda$
$ \rightarrow 1 $	In theory $\phi \in (0,1)$
$b = \frac{1}{\rho/\delta}$	+1

In practice $\phi \approx 1$



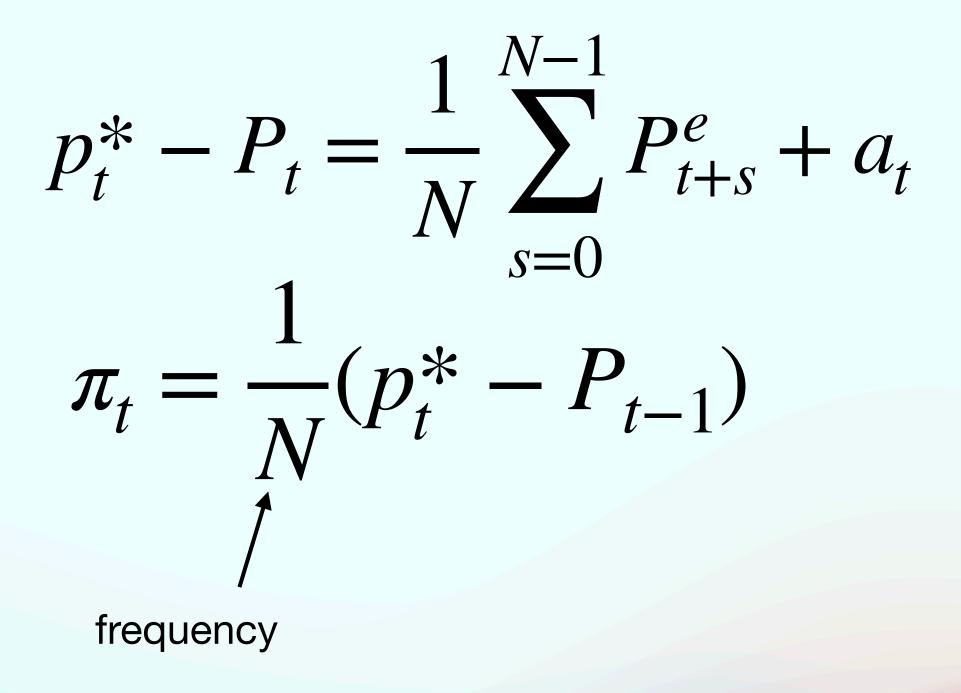
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- Fixed prices for N periods...
- ... staggered across goods



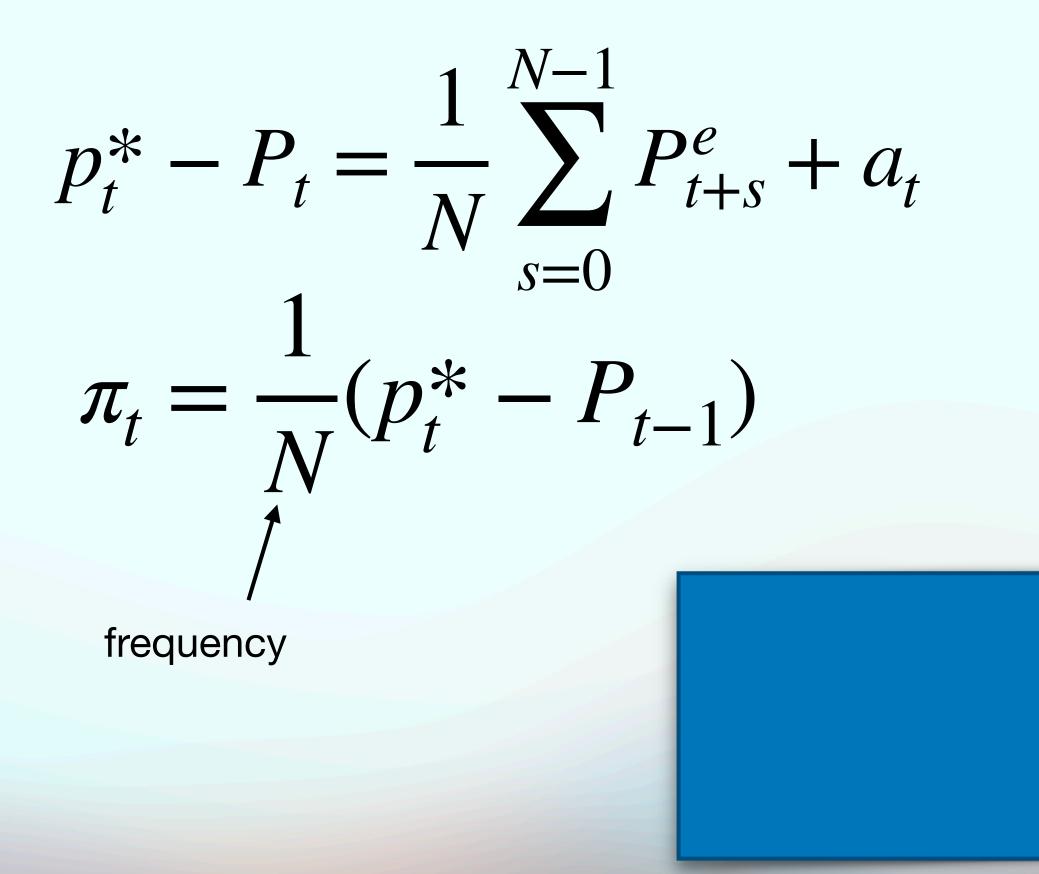


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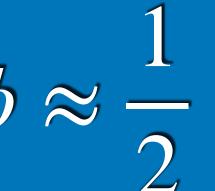


 $\pi_t = \phi \pi^e + \frac{1}{N} a_t$ $\phi = \frac{1}{2} + \frac{1}{N}$

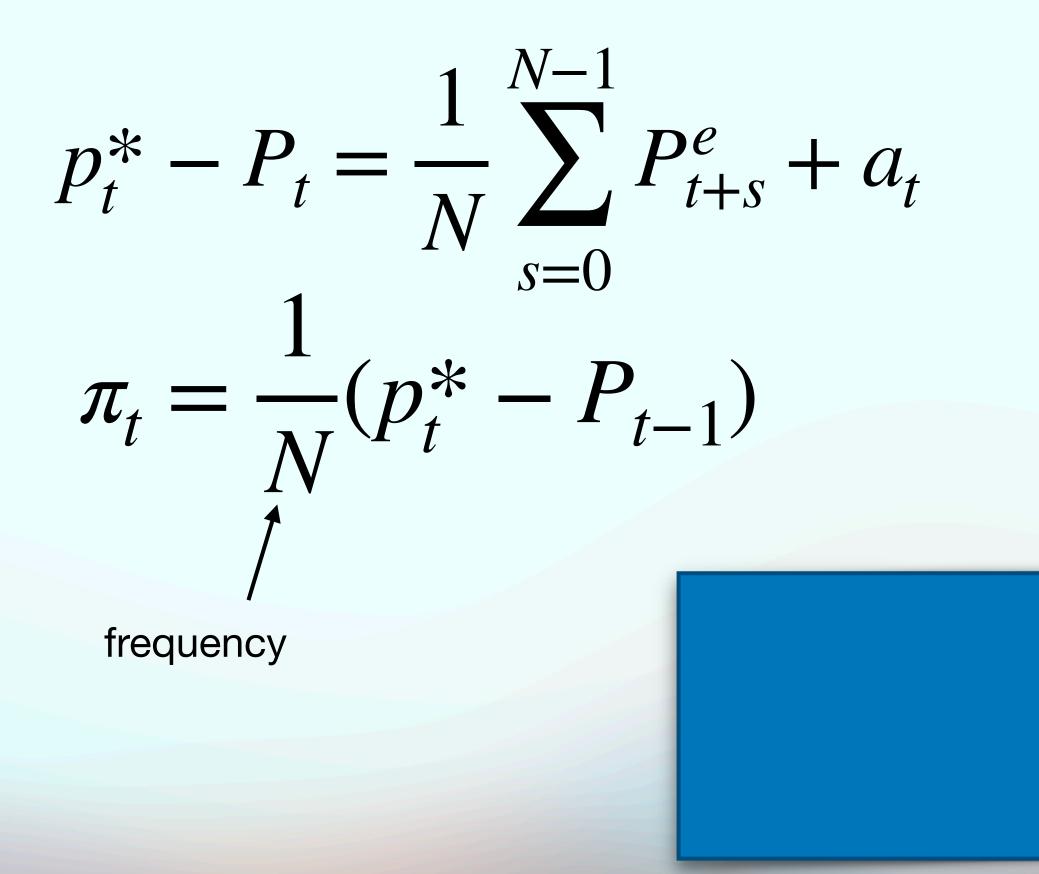
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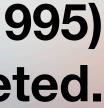


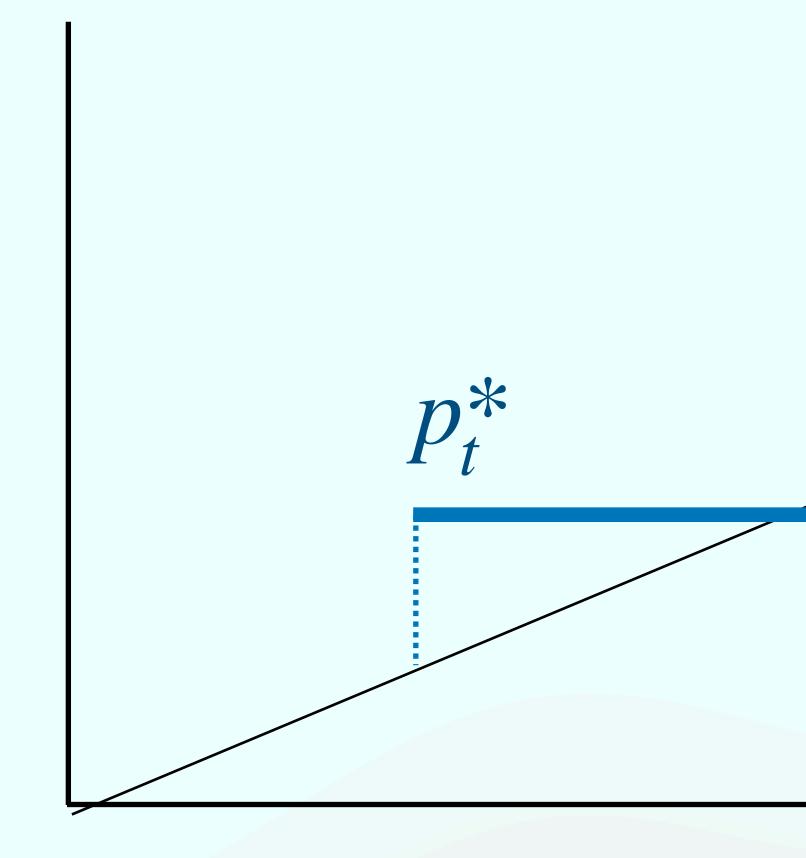
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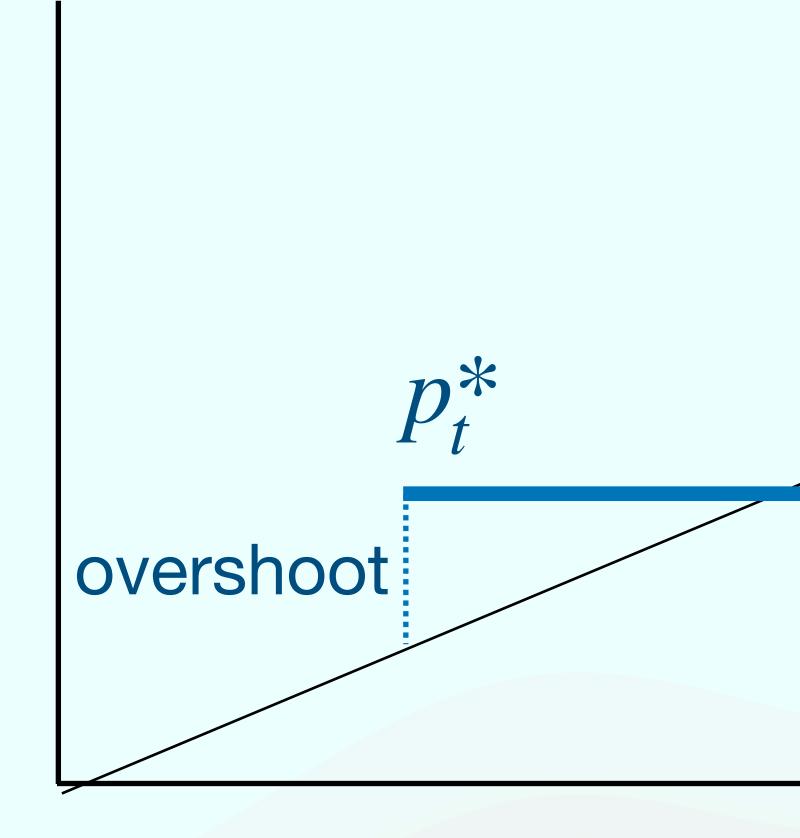
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Sidenote: Roberts (1995) equation misinterpreted.

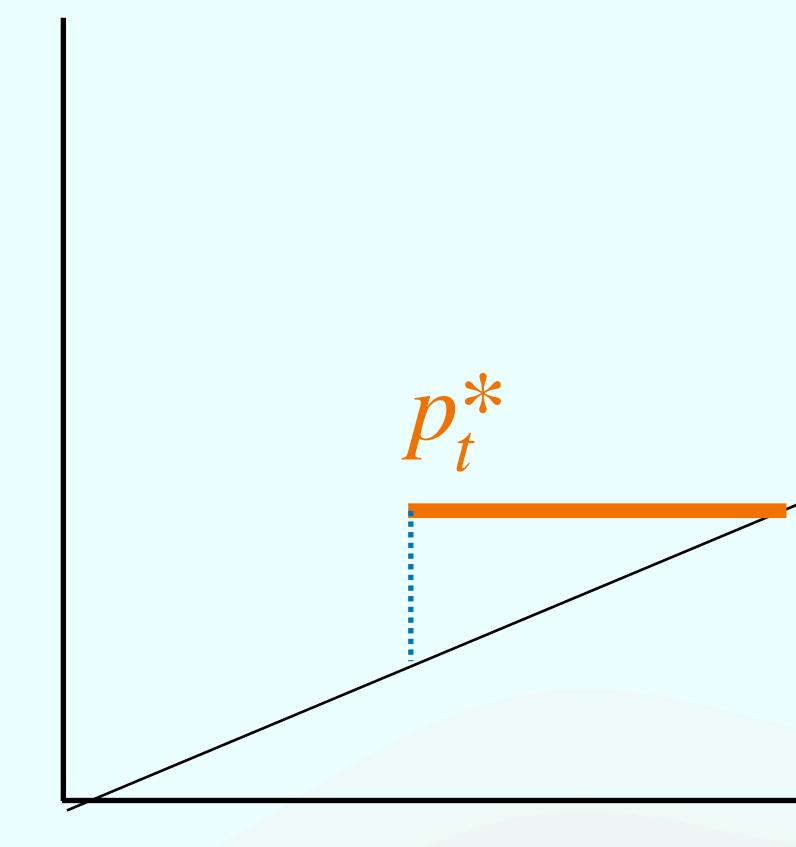




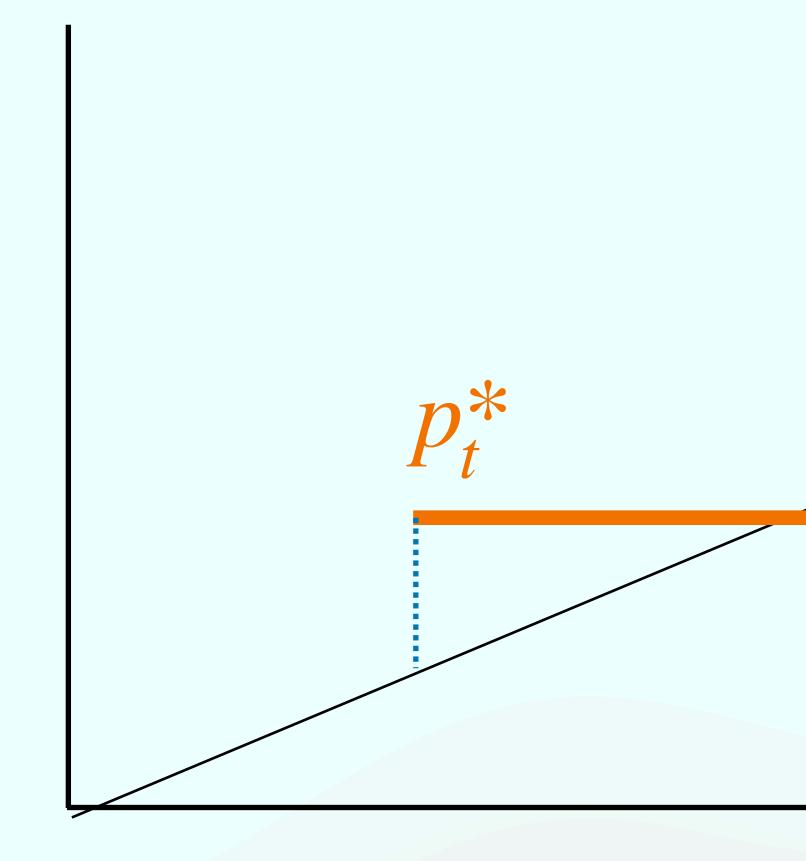




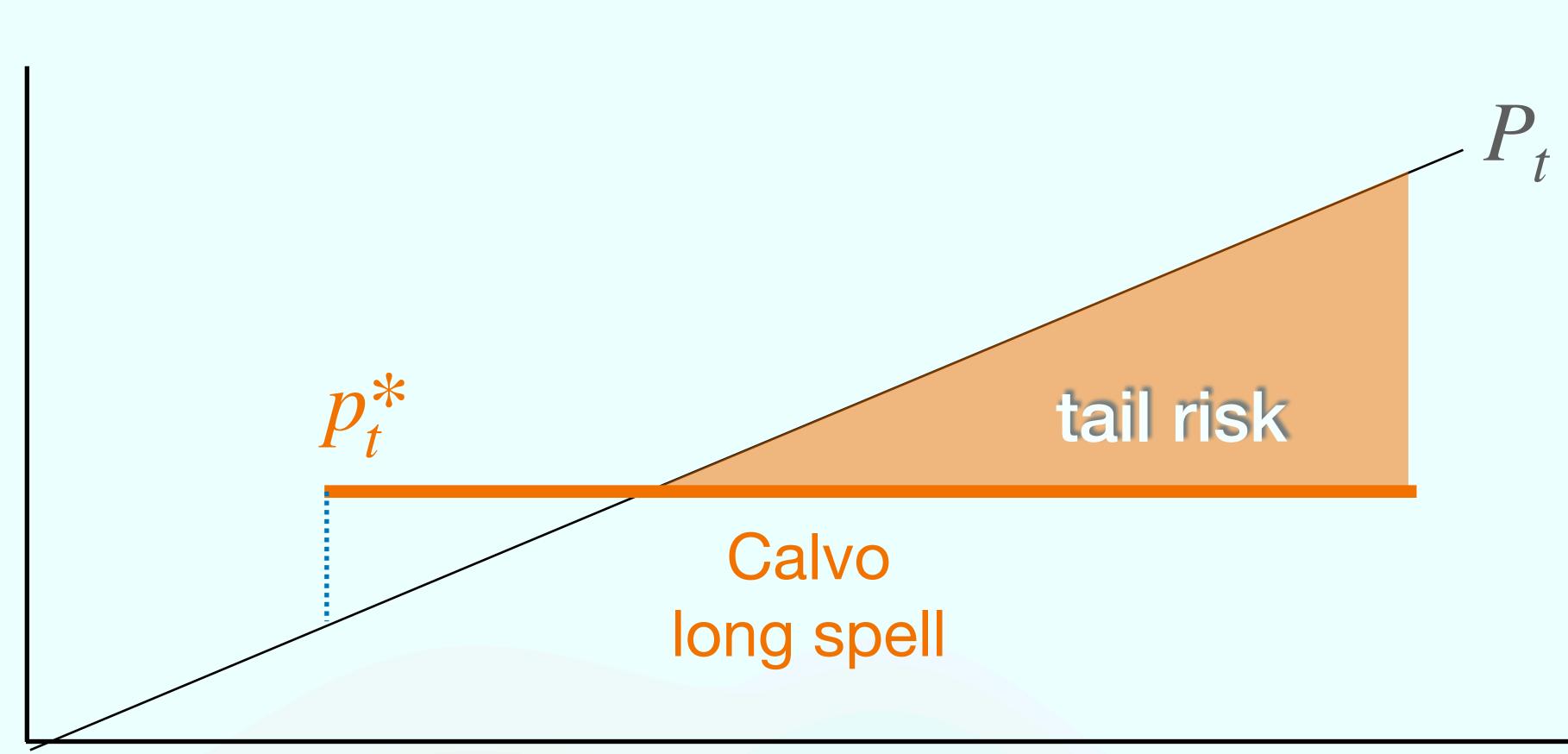




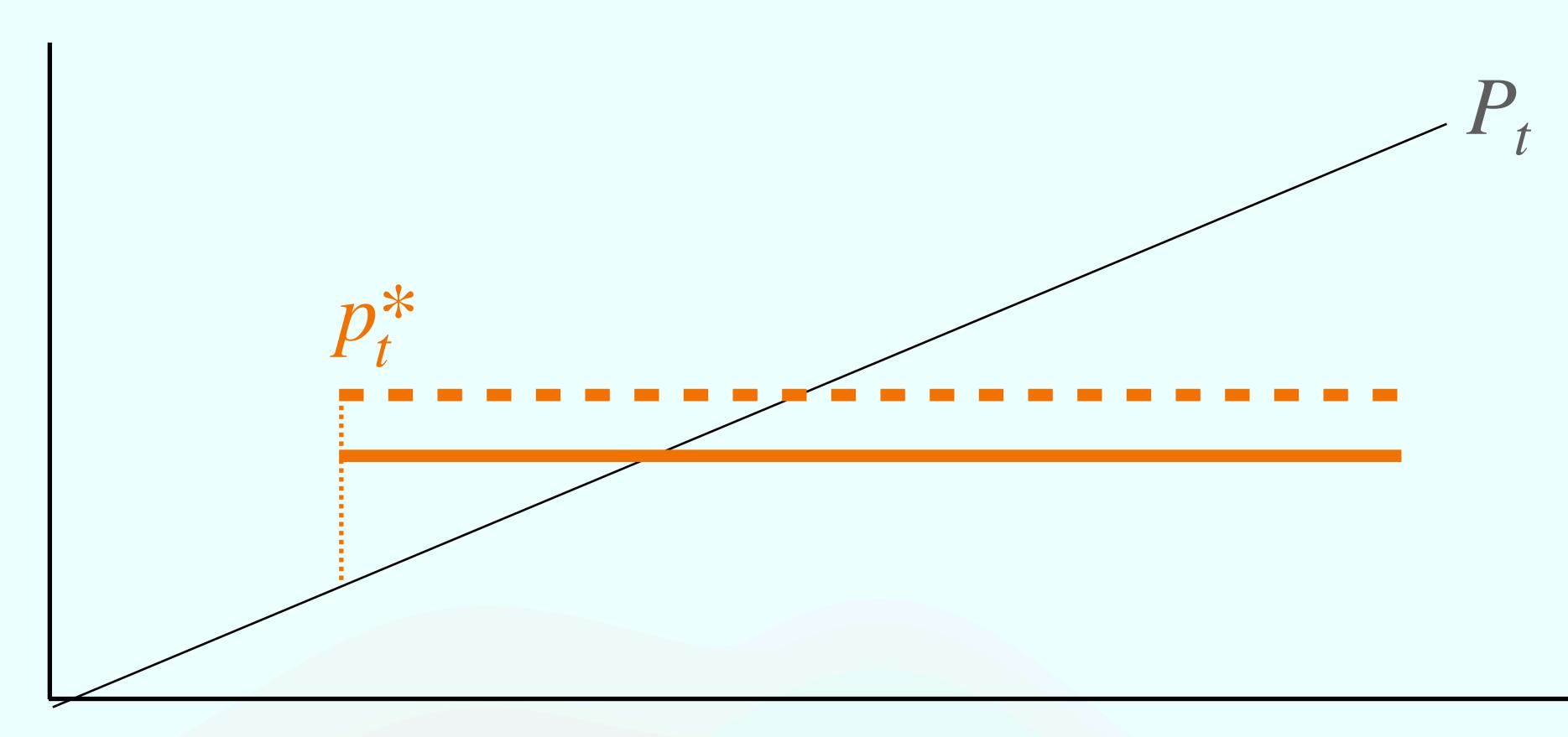
Calvo short spell



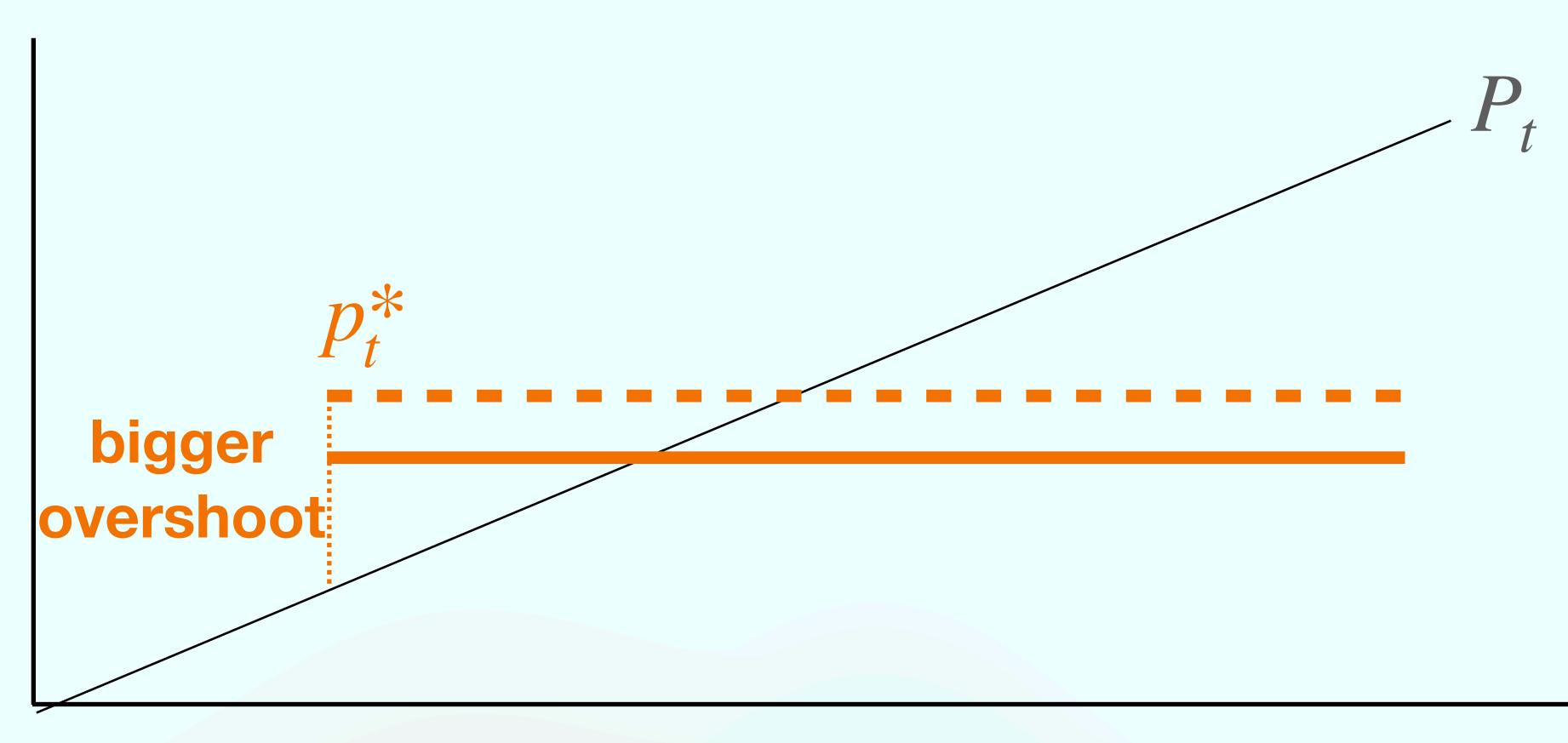








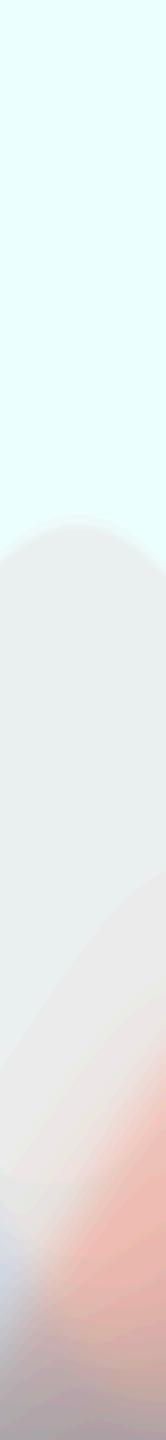
long spell



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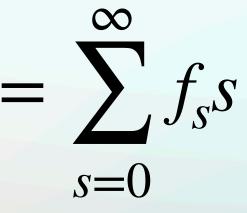
General Time Dependent Model

- General profit function: complementarities, markups, real marginal costs etc.
- General hazard rate $\{h_s\}$ for s = 0, 1, ...
- Two probability densities...
 - completed spells f_s (fraction of spells ending at s)
 - ongoing spells ω_{c} (fraction time spent at s)
- Accounting...

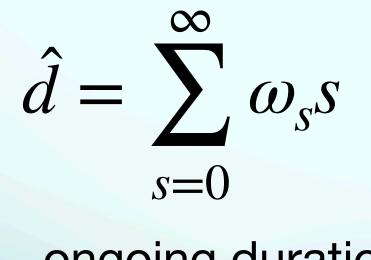
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$$\bar{h} = \sum_{s=0}^{\infty} \omega_s h_s = \frac{1}{\bar{d}} \qquad \bar{d} =$$
frequency comp



pleted duration



ongoing duration

$$\phi = \bar{h} \sum_{s=0}^{\infty} \omega_s (1+s) = \frac{\sum_{s=0}^{\infty} \omega_s (1+s)}{\sum_{s=0}^{\infty} f_s (1+s)} = \frac{\hat{d}}{\bar{d}}$$

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- Frequency of price adjustments irrelevant! ↑frequency ↓overshoot



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- Heterogeneity

$$\phi = \int \frac{\hat{d}(i)}{\bar{d}(i)} di$$



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$$\phi = \int \frac{\hat{d}(i)}{\bar{d}(i)} \, di \neq \int \frac{1}{\bar{d}(i)} \, di \cdot \int \hat{d}(i) \, di$$

Ongoing Completed



$$\phi = \bar{h} \sum_{s=0}^{\infty} \omega_s (1+s) = \frac{\sum_{s=0}^{\infty} \omega_s (1+s)}{\sum_{s=0}^{\infty} f_s (1+s)} = \frac{\hat{d}}{\bar{d}}$$

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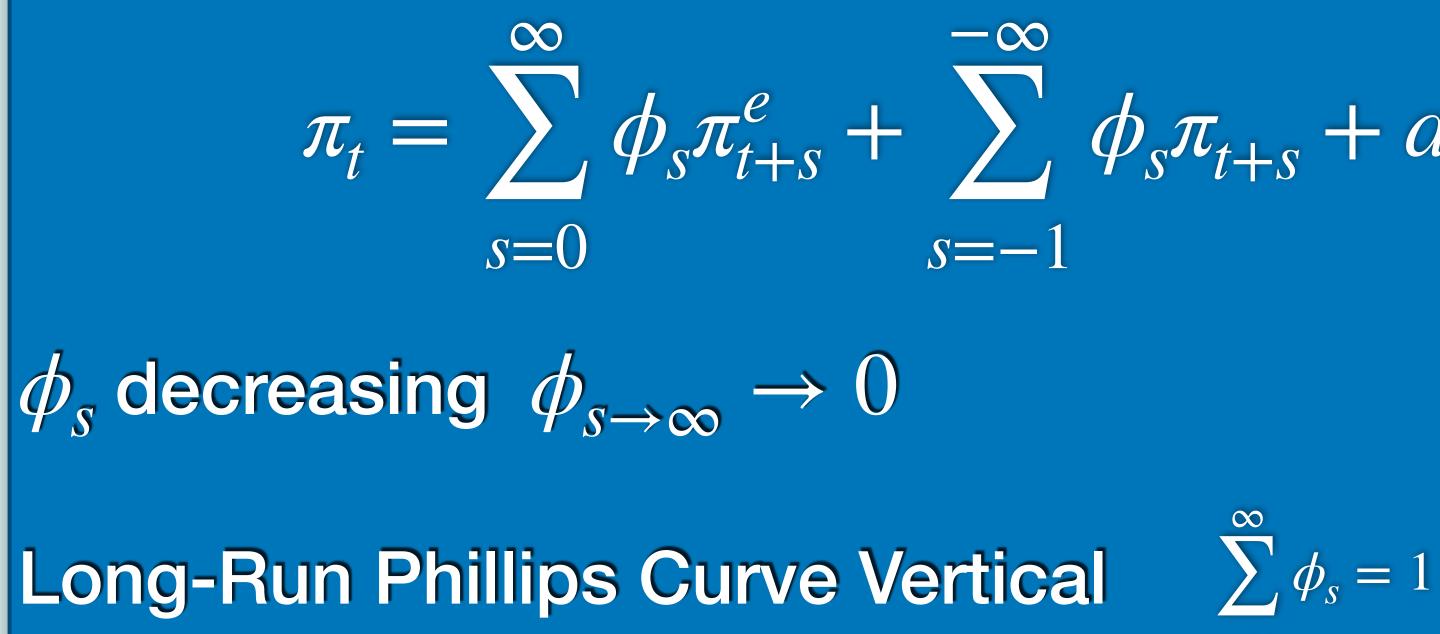
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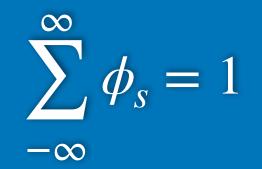
 $\frac{di}{di} \cdot \hat{d}(i) di \neq \frac{\int \hat{d}(i) di}{di}$ $\int \bar{d}(i) di$

Phillips Curve

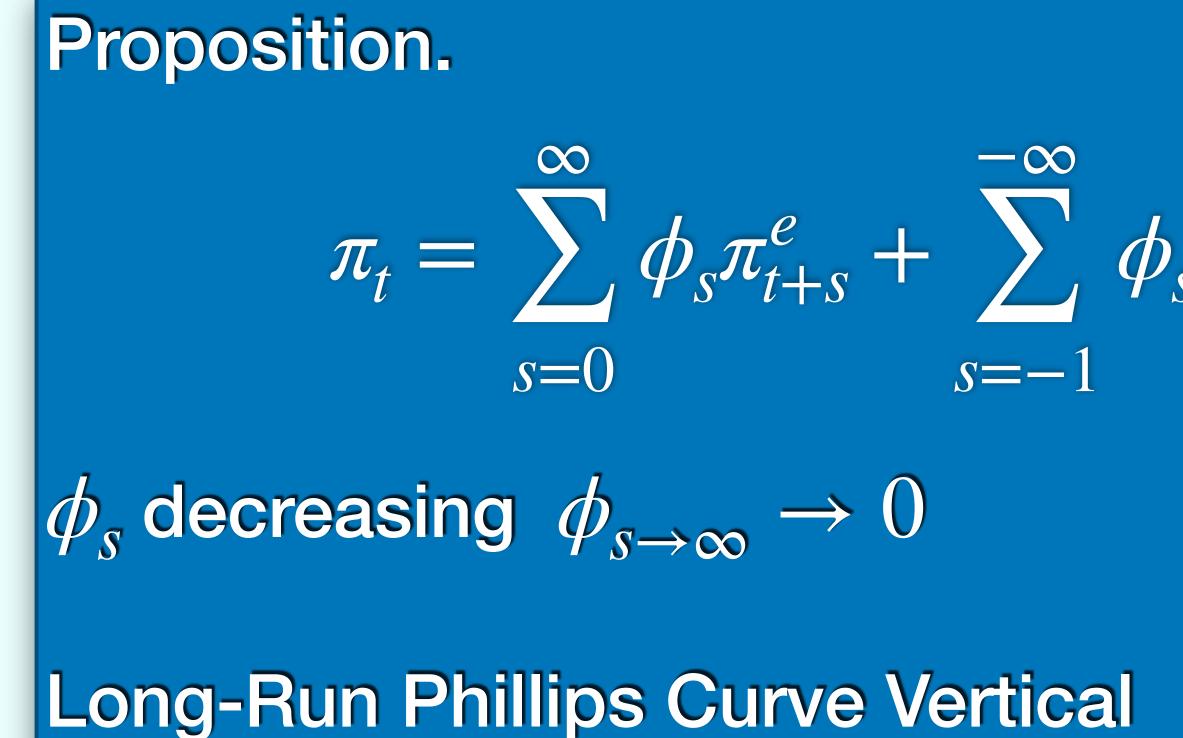
Proposition.



 $\pi_t = \sum_{s=0}^{\infty} \phi_s \pi_{t+s}^e + \sum_{s=0}^{-\infty} \phi_s \pi_{t+s} + a_t$



Phillips Curve

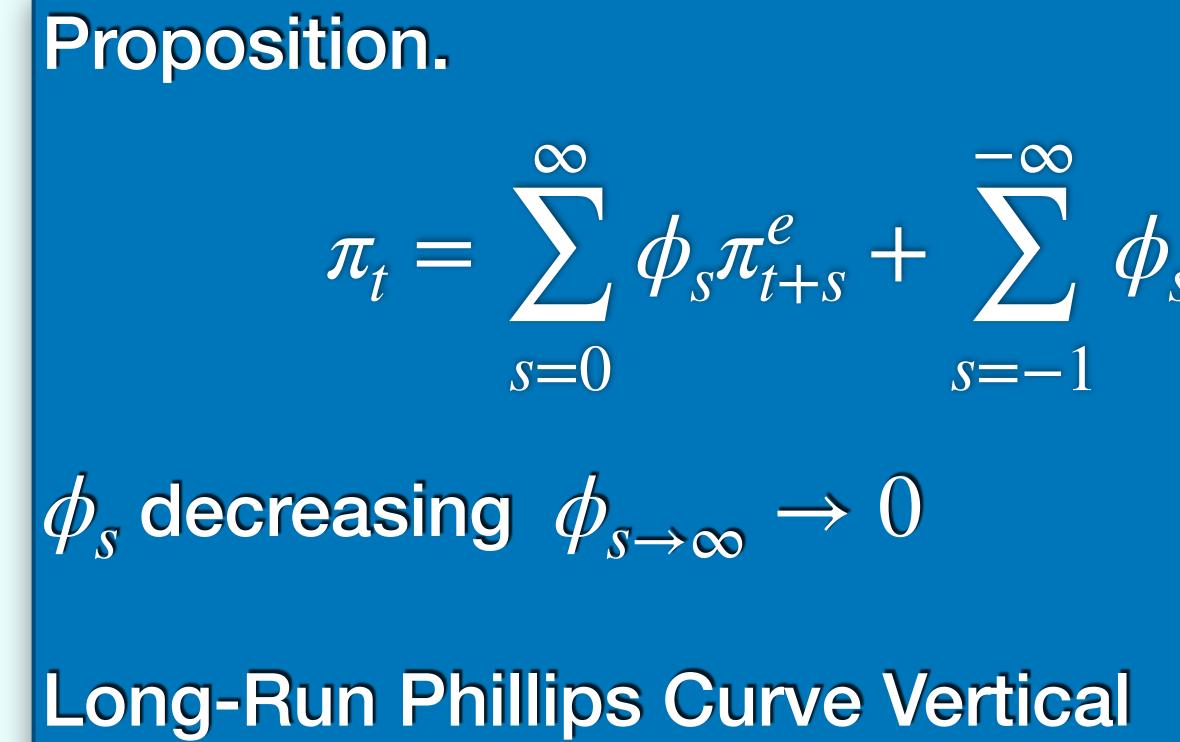


effects zero outside rigidity!

 $\pi_t = \sum_{s=0}^{\infty} \phi_s \pi_{t+s}^e + \sum_{s=0}^{\infty} \phi_s \pi_{t+s} + a_t$ $\sum \phi_s = 1$ $-\infty$

Intuition: early inflation affects current and future periods

Phillips Curve



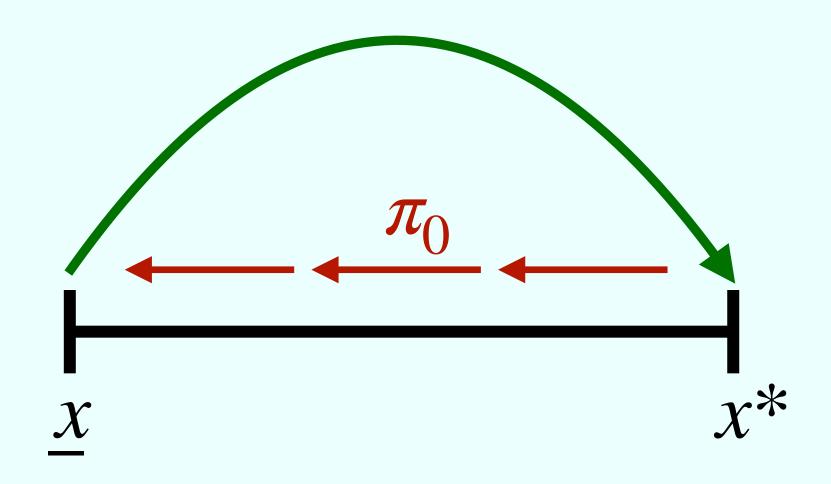
 Intuition: early inflation affects current and future periods effects zero outside rigidity!

• Sheedy (2010) Rational Expectations: $\hat{\phi}_1 = 1$ (as NK) and $\hat{\phi}_s < 0$

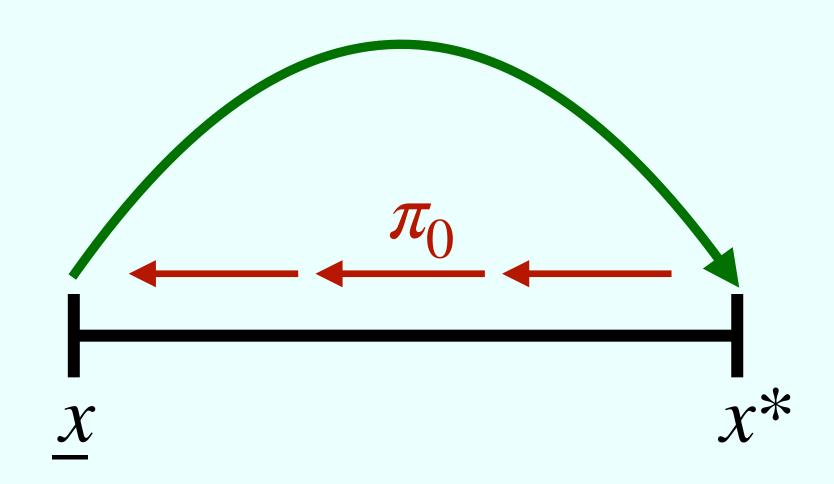
 $\pi_t = \sum_{t=1}^{\infty} \phi_s \pi_{t+s}^e + \sum_{t=1}^{-\infty} \phi_s \pi_{t+s} + a_t$ $\sum \phi_s = 1$ $-\infty$

Overview

- 1. Calvo $\phi = 1$
- 2. Taylor $\phi = \frac{1}{2}$
- 3. General Time-Dependent $\phi = \text{ongoing/completed}$
- 4. State Dependent
- 5. State Dependent with Frictions

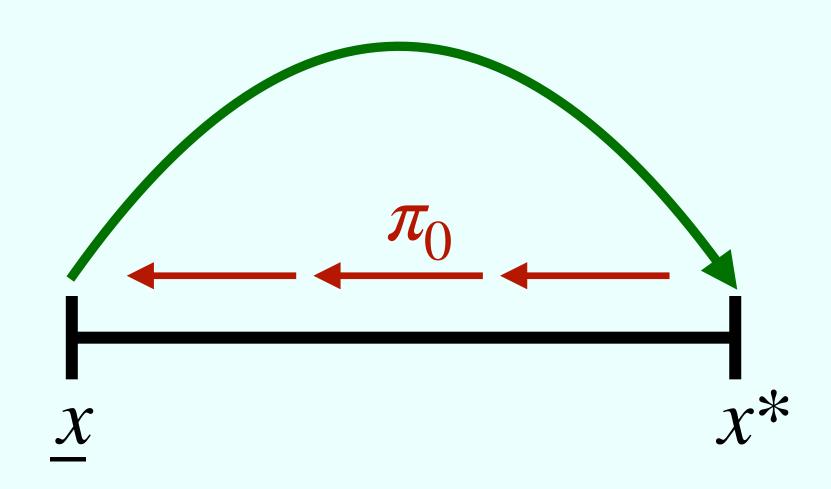


- Steady State: Sheshinski-Weiss (1977)
 - menu cost c of changing price
 - constant inflation π
 - bands for x = p P



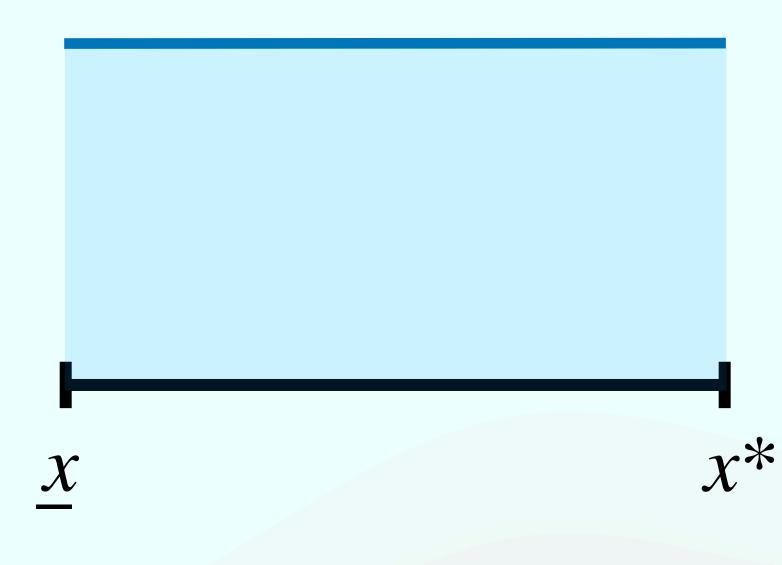
- Steady State: Sheshinski-Weiss (1977)
 - menu cost c of changing price
 - constant inflation π
 - bands for x = p P

- Out of Steady Steady...
 - start at steady state π_0
 - shock expectations: π^e rises
 - what do firms do on in short run?

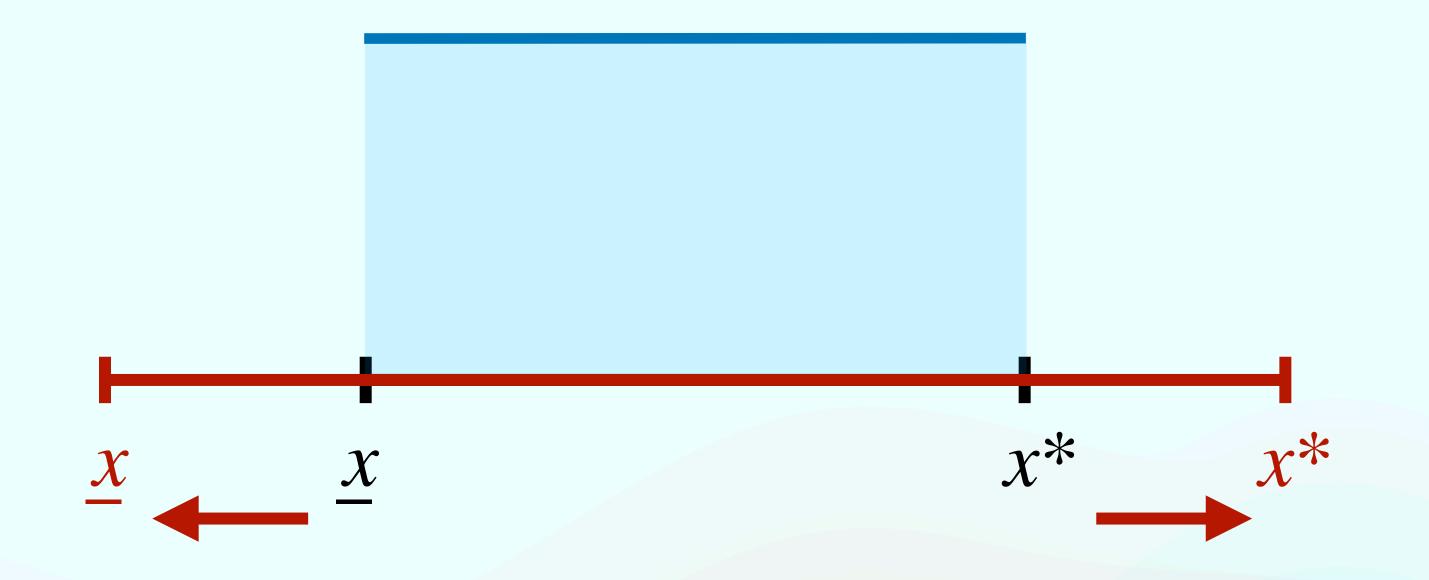




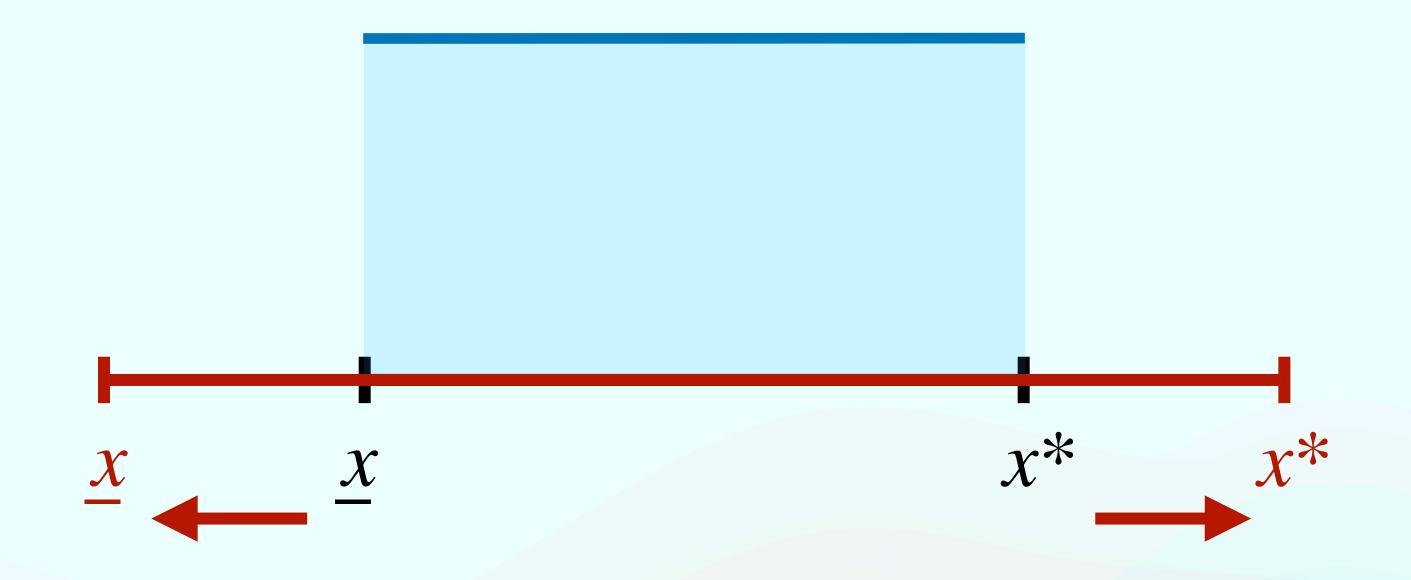
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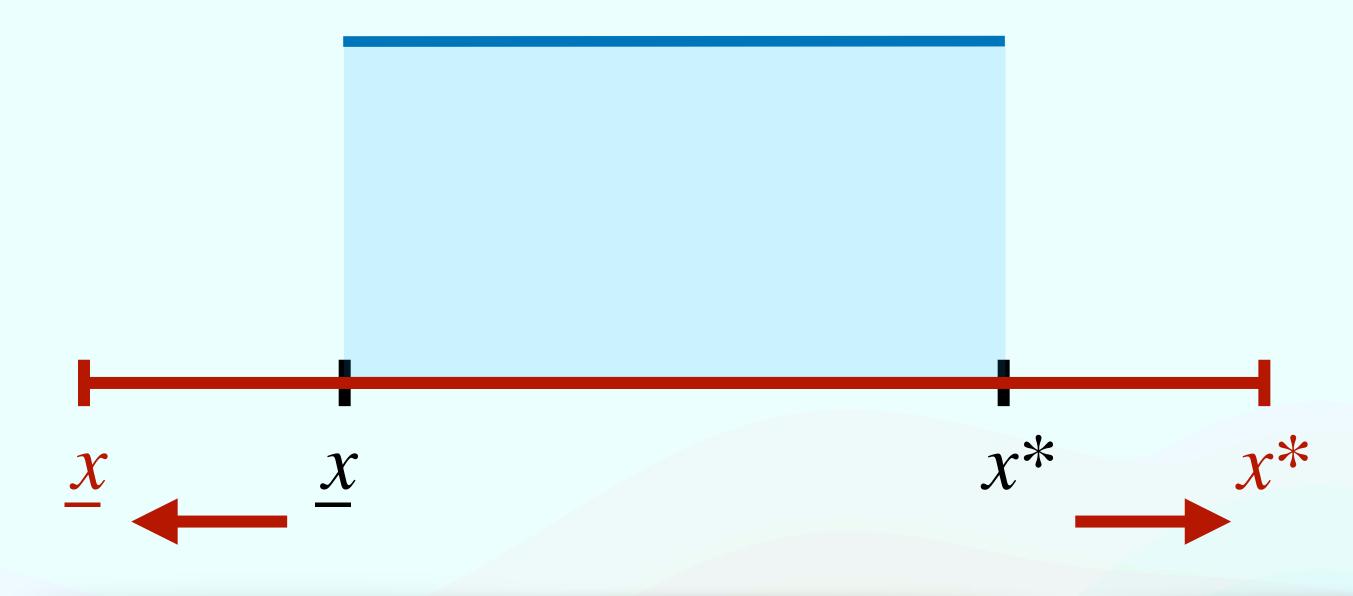


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No Price Changes! $\pi = 0$

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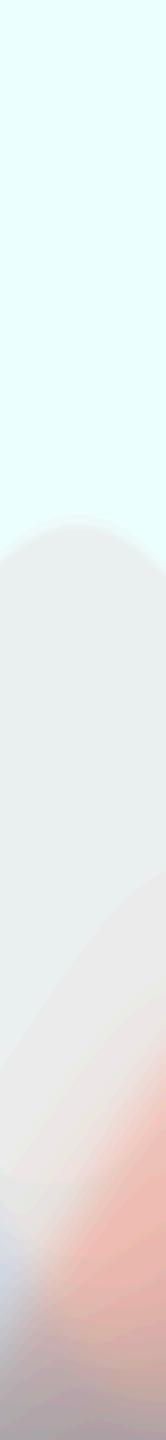
No Price Changes! $\pi = 0$





Overview

- 1. Calvo $\phi = 1$
- 2. Taylor $\phi = \frac{1}{2}$
- 3. General Time-Dependent $\phi = \text{ongoing/completed}$
- 4. Basic State Dependent
- 5. Extension to State Dependent



State Dependent

- Extreme shifts in frequency of price changes
- Realistic? Maybe not...
 - Firms *really* stop changing prices? Unlikely!
 - Two ideas...
 - short-run fixed frequency
 - fixed costs of changing bands

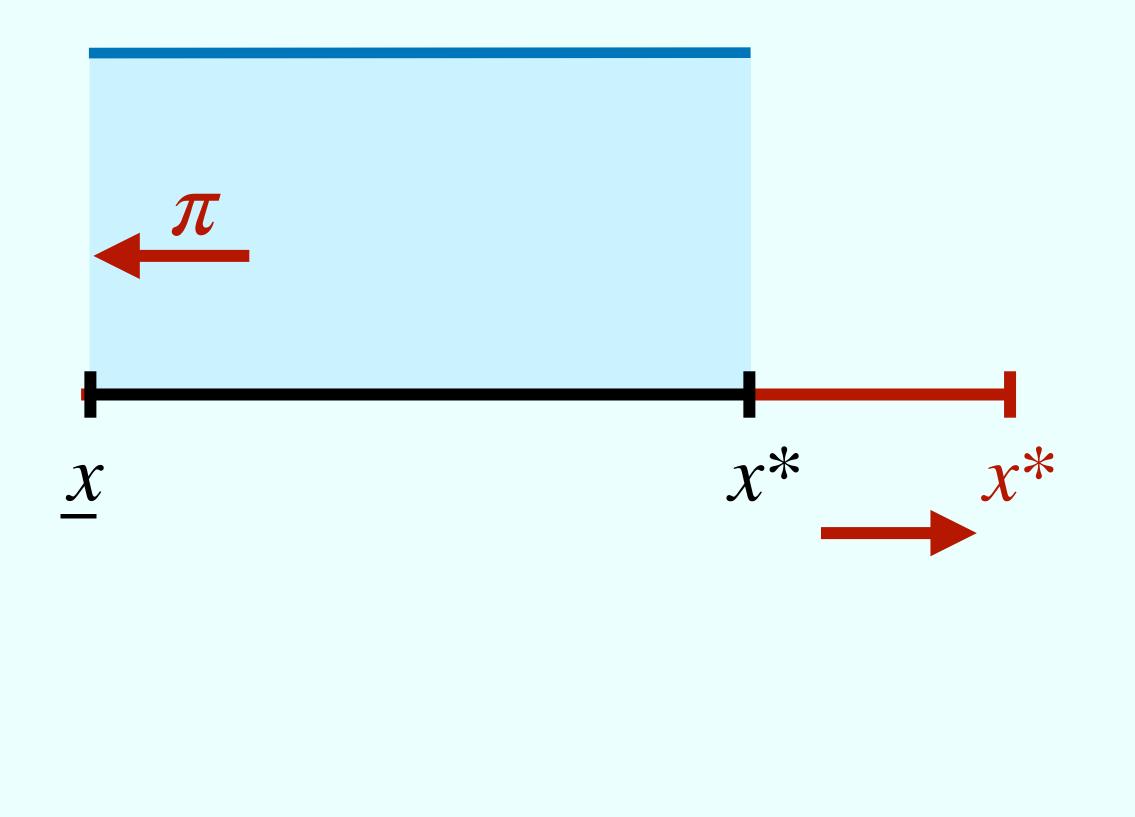
Short Run Frictions (Extension #1)

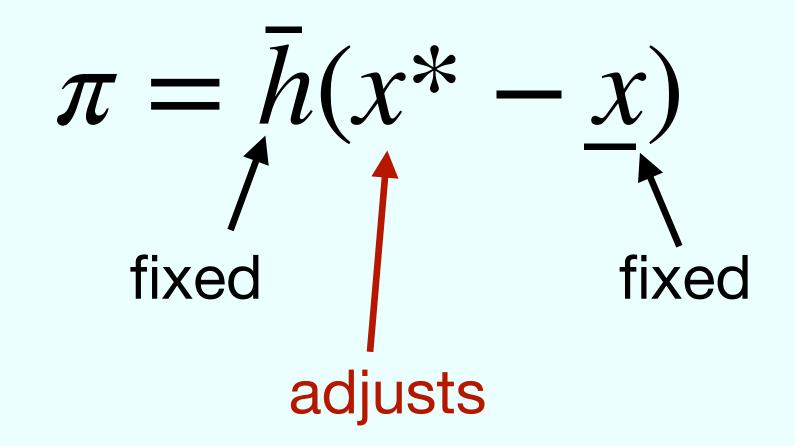
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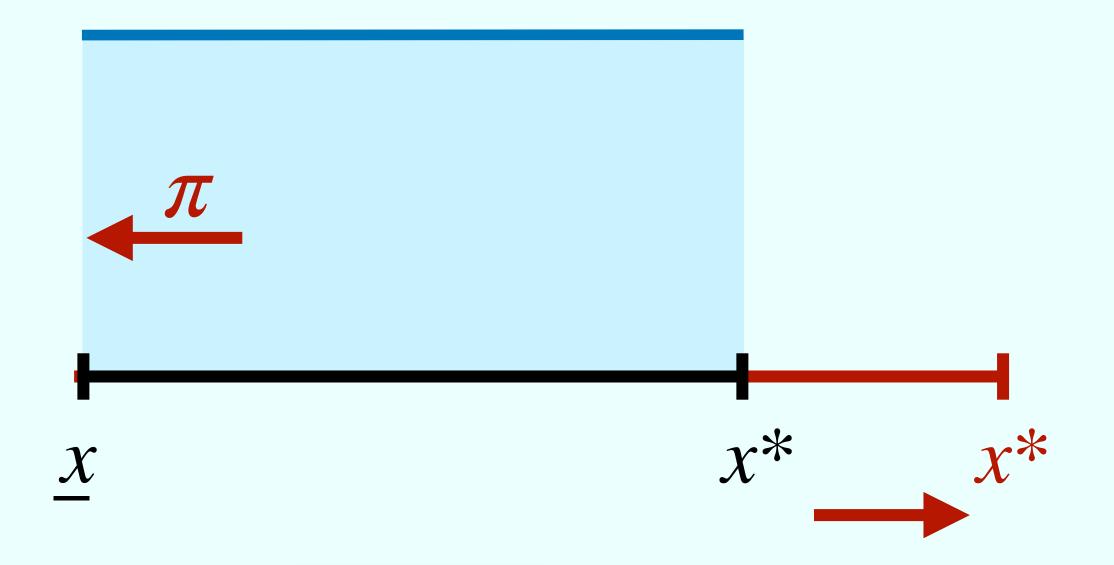
- Idea...
 - devoted resources for changing prices
 - fixed in very short run (or adjustment costs)...
 - ... but not in medium run

Short Run Frictions (Extension #1)

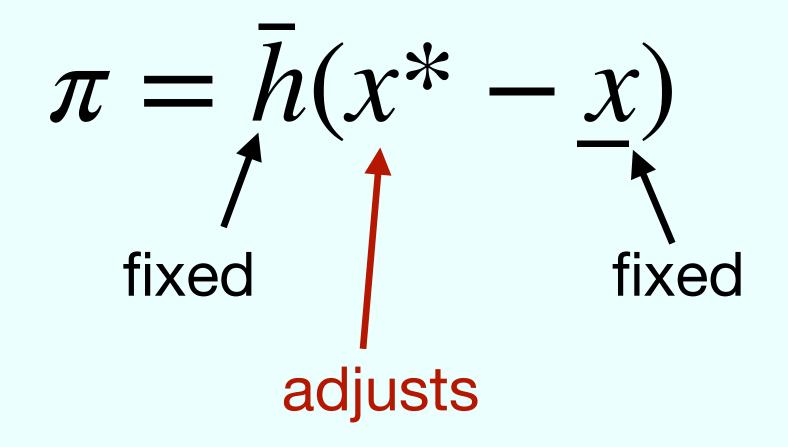
- Idea...
 - devoted resources for changing prices
 - fixed in very short run (or adjustment costs)...
 - ... but not in medium run
- Optimal...
 - firm keeps changing lowest prices
 - how much upper bound?

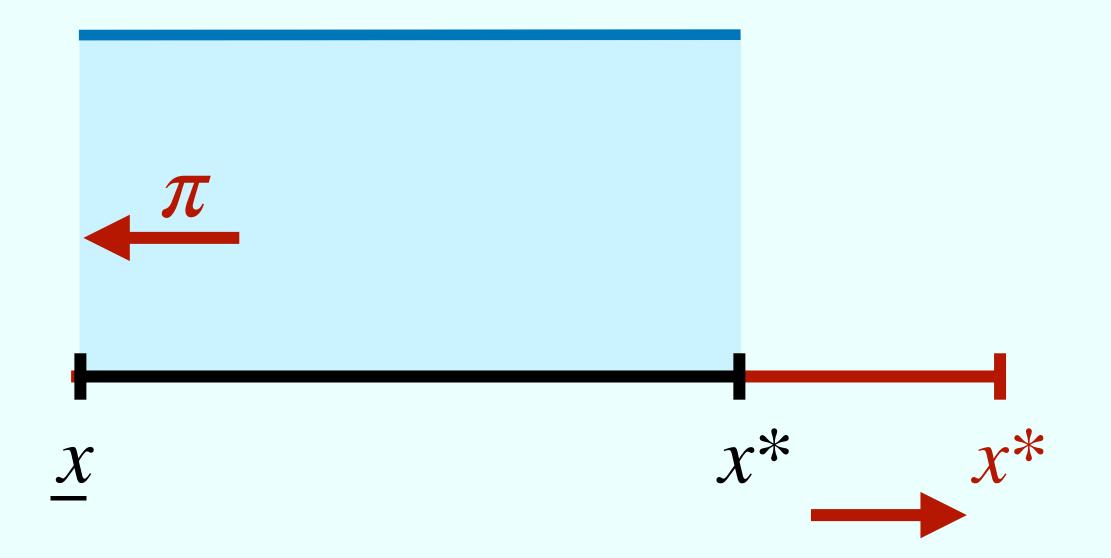






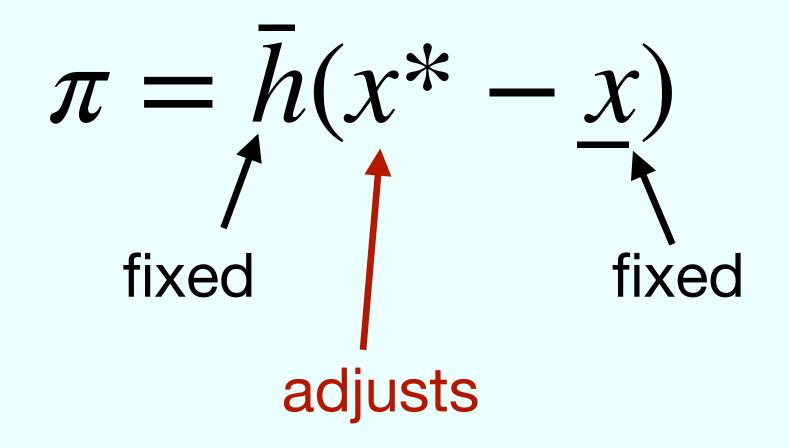
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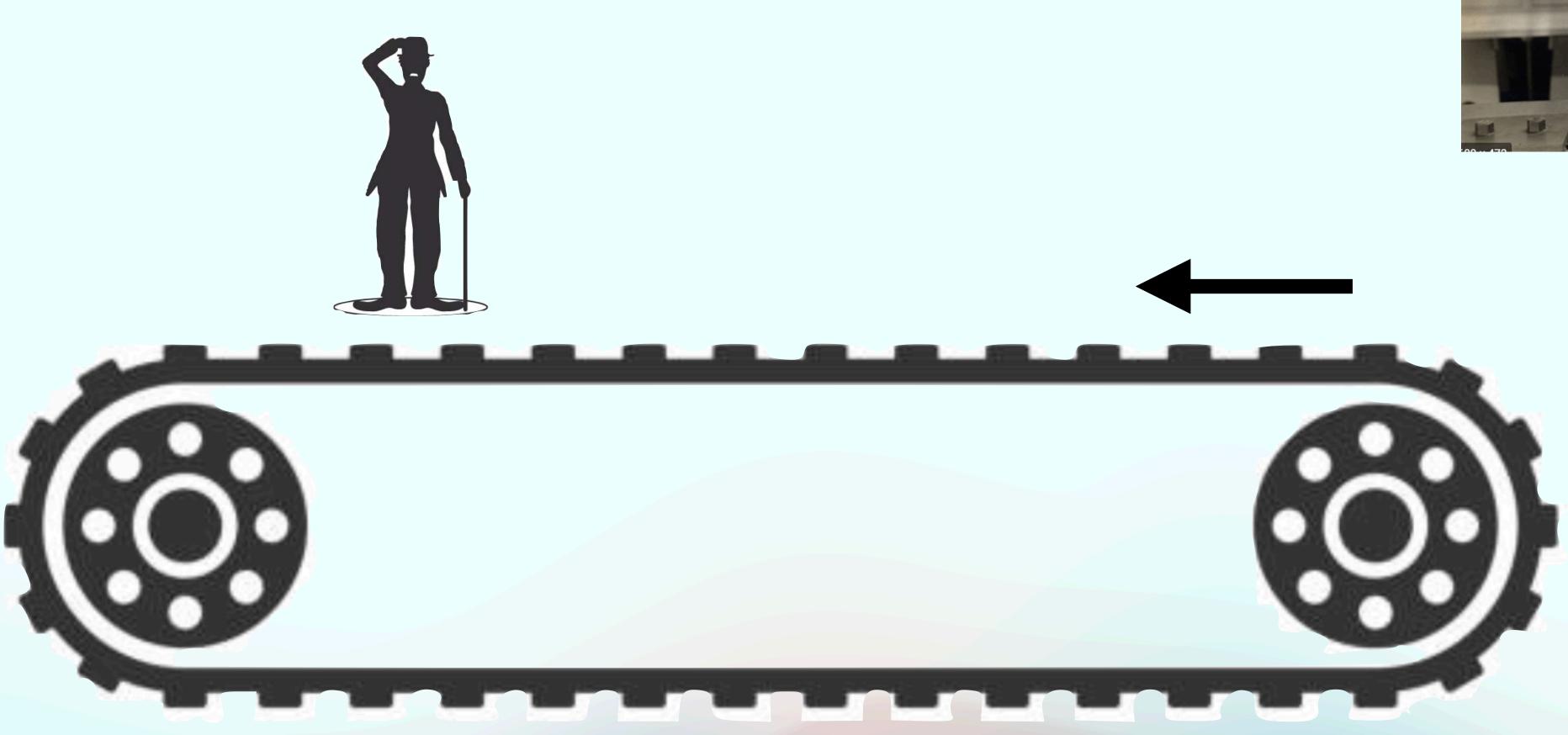


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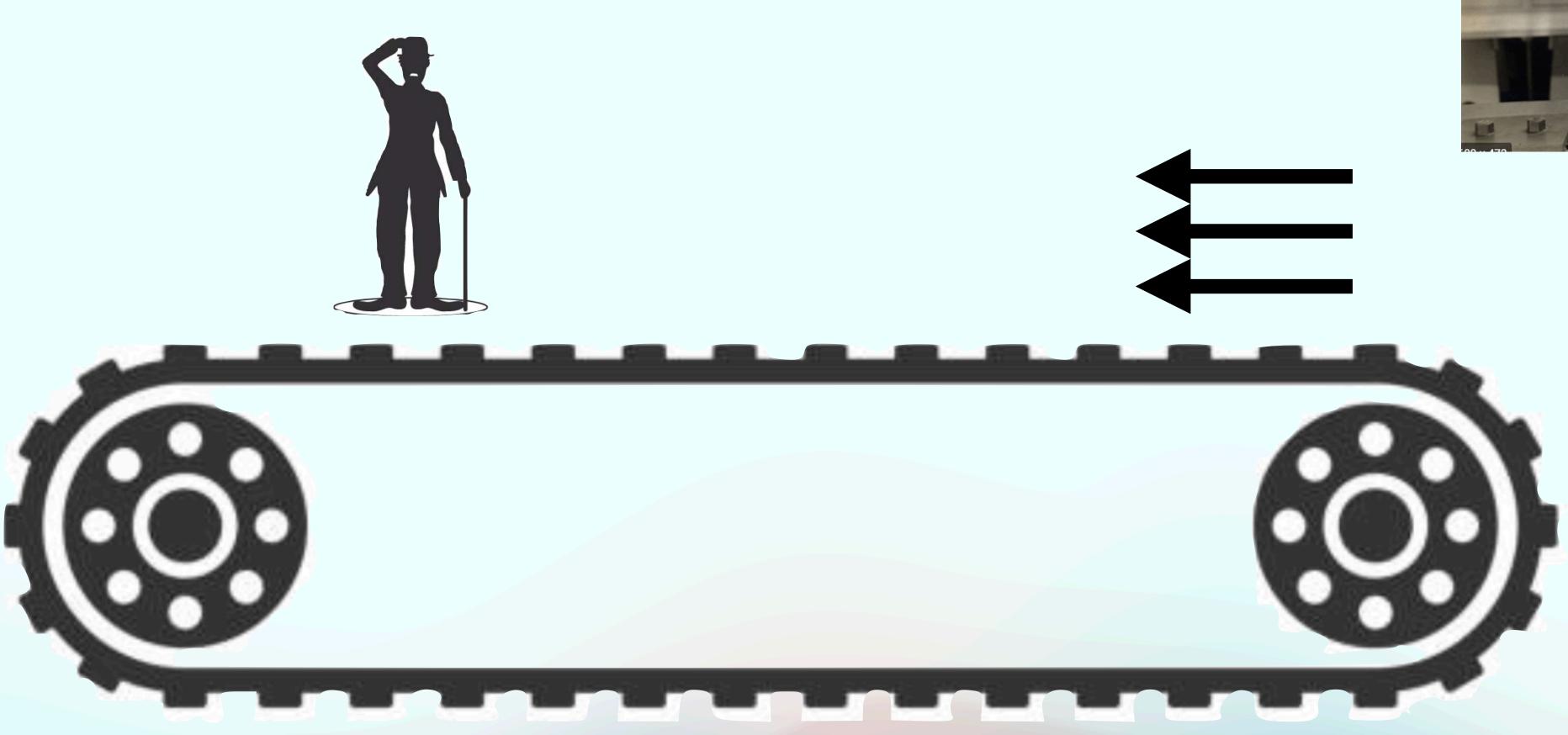
- Intuition...
 - adjust reset price up, but less than Taylor!
 - firm anticipates adjusting reset price more quickly



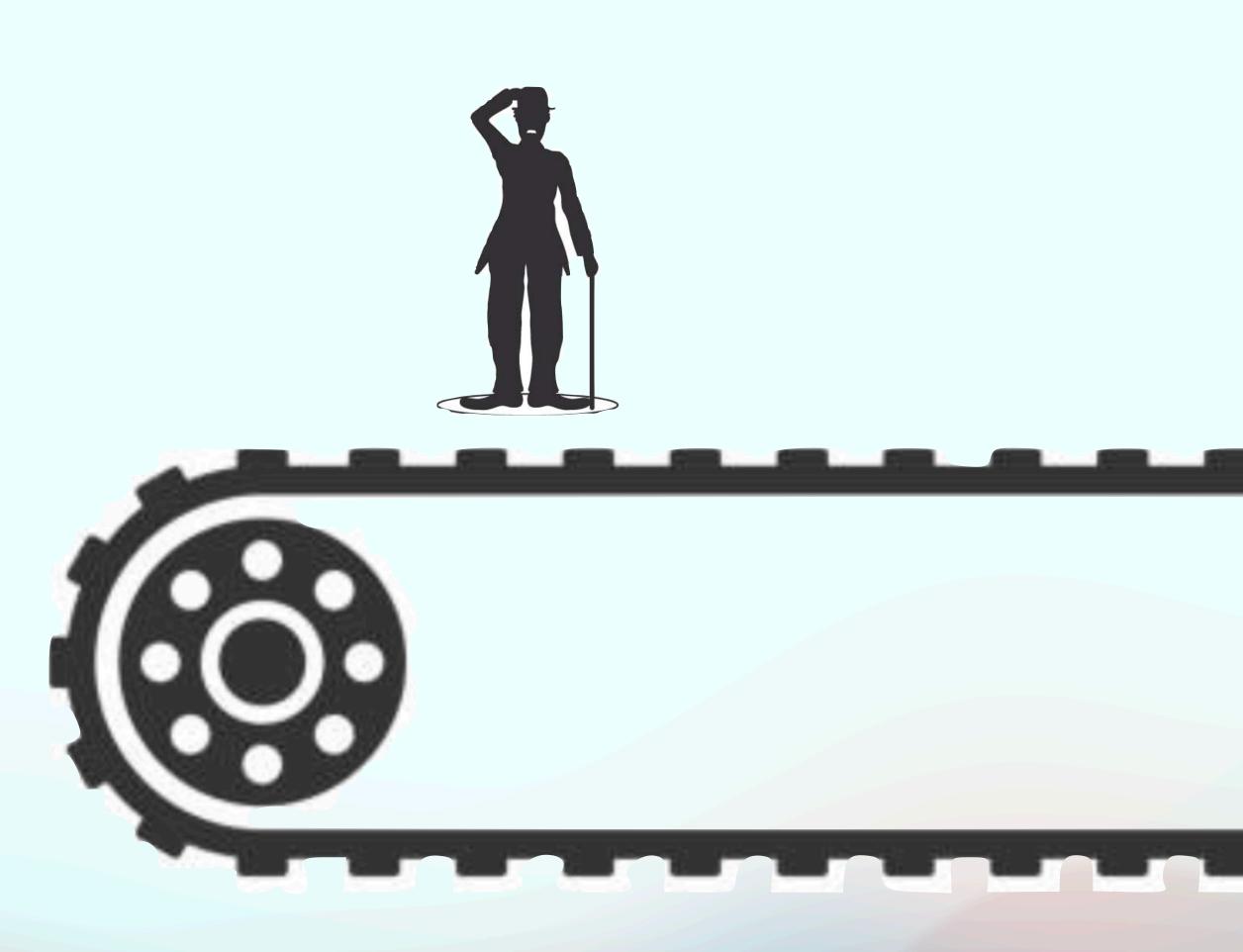




















- Menu costs?...
 - cost of menus/stickers
 - manager time
- ... but changing pricing also incurs manager time!

- Cost c_R of changing bands e.g.
- Used old policies if

$$c_B/c \in [1,10]$$



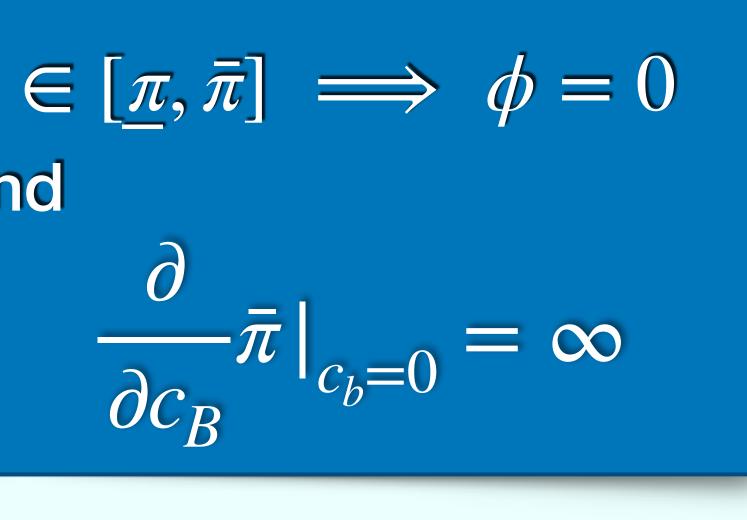
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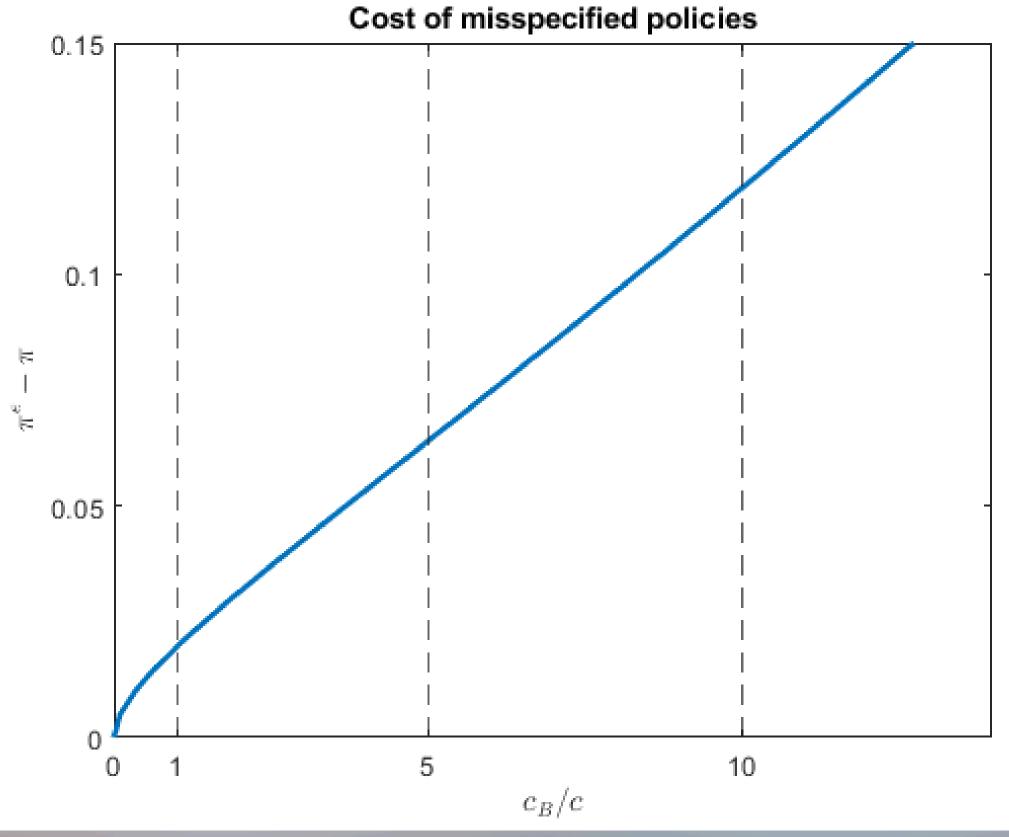
$$V(\underline{x}(\pi_0), x^*(\pi_0), \pi^e) \ge V^*(\pi^e) + c_B$$

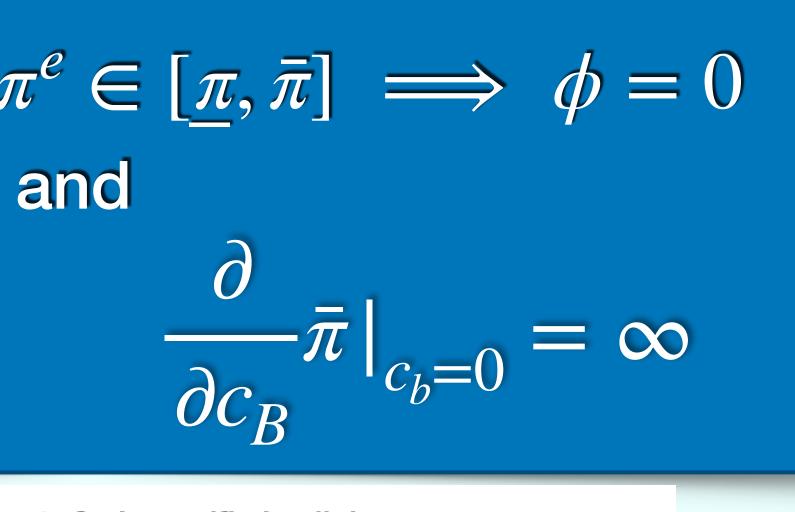
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- Generation 3.0 menu cost models? (N goods, free price changes, etc.)

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- Results...
 - expectations ...
 - state dependent: extreme, added frictions

• time dependent: lower passthrough than 1, sufficient statistics, short-run

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- Results...
 - expectations ...
 - state dependent: extreme, added frictions
- Other benefits?...
 - inspect mechanisms: economic intuition (overshoot)
 - look at other shocks in menu costs than just monetary policy
 - suggests extensions of menu cost models
 - spillovers to learning: inspect feedback (understood to be important)
 - spillover to empirics: measure overshoot, sufficient stats, ...

• time dependent: lower passthrough than 1, sufficient statistics, short-run

Inattention and Behavioral Agents

- Other options to affect response of inflation
 - agents do not revise expectations
 - or just do not act on them:
 - curve



Examples: rational inattention, imperfect information, Hybrid NK Phillips