

Addressing COVID-19 Outliers in BVARs with Stochastic Volatility

Andrea Carriero¹ Todd E. Clark²
Massimiliano Marcellino³ Elmar Mertens⁴

¹Queen Mary University of London, ²Federal Reserve Bank of Cleveland,
³Bocconi University, IGIER and CEPR, ⁴Deutsche Bundesbank

NBER Summer Institute 2021

Forecasting & Empirical Methods Seminar

14 July 2021

The results presented here do not necessarily represent the views of the Federal Reserve Bank of Cleveland, the Federal Reserve System, the Deutsche Bundesbank, the Eurosystem, or their respective staffs.

How to make VARs work in turbulent times?

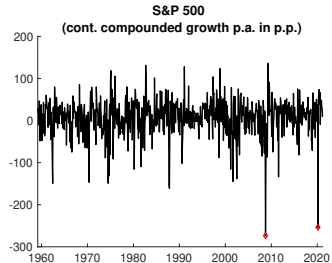
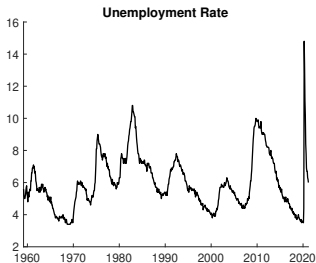
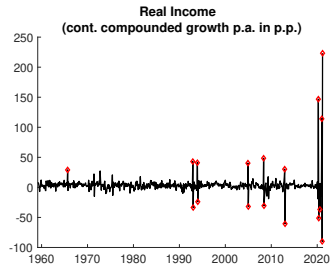
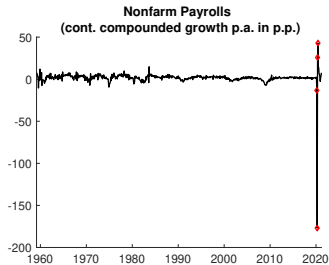
Extreme realizations since March 2020 lead to ...

- strong effects on parameter estimates
- implausible predictions in constant-variance VARs
- in terms of point and density forecasts

EXTREME DATA SINCE MARCH 2020

U.S.

Monthly data 1959:03 – 2021:03

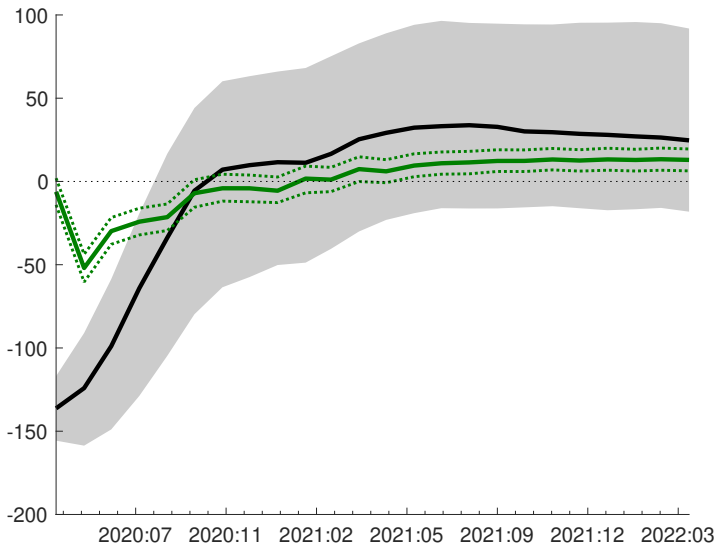


Red diamonds: outliers more than five times the IQR away from median

BVAR FORECASTS FOR PAYROLL GROWTH

APRIL 2020

parameters from data through Feb (green) or Apr 2020 (black)



Medians and 68% bands, homoskedastic BVAR, data since 1959:03

COVID-19 OUTLIERS AS HIGH-VARIANCE EVENTS

- **Some suggest to omit** COVID-19 obs from VAR estimation (Schorfheide & Song, 2020)
- **...or to place less weight on COVID-19 data** in parameter estimation (Lenza & Primiceri, 2020)

COVID-19 OUTLIERS AS HIGH-VARIANCE EVENTS

- Some suggest to omit COVID-19 obs from VAR estimation (Schorfheide & Song, 2020)
- ...or to place less weight on COVID-19 data in parameter estimation (Lenza & Primiceri, 2020)
- **Indeed, this is what VARs with SV would do:
down-weight obs with larger variance of residuals**

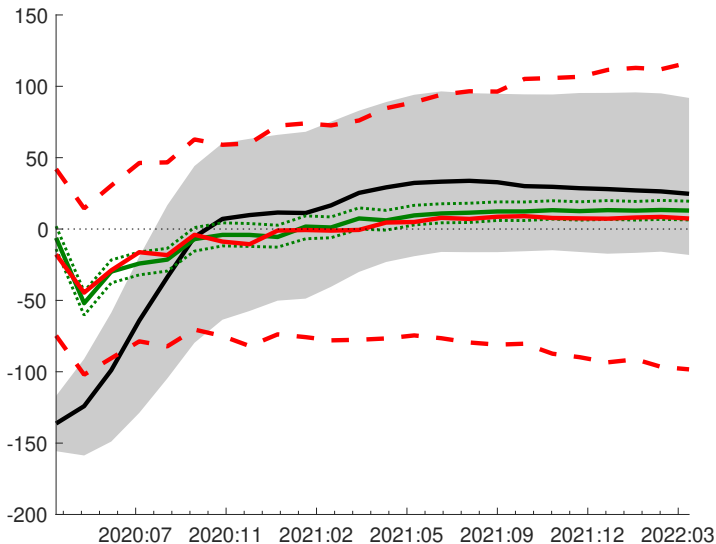
COVID-19 OUTLIERS AS HIGH-VARIANCE EVENTS

- Some suggest to omit COVID-19 obs from VAR estimation (Schorfheide & Song, 2020)
- ...or to place less weight on COVID-19 data in parameter estimation (Lenza & Primiceri, 2020)
- Indeed, this is what VARs with SV would do:
down-weight obs with larger variance of residuals
- **But, conventional VAR-SV models assume changes in volatility to be highly persistent**
- **...with strong effects on projected uncertainty**

BVAR FORECASTS FOR PAYROLL GROWTH

APRIL 2020

parameters from data through Feb (green) or Apr 2020 (black), SV (red)



Medians and 68% bands, VARs with constant (green/black) or time-varying (red) variance

RESEARCH AGENDA AND CONTRIBUTIONS

How to make VARs work in turbulent times?

Extreme realizations since March 2020 lead to ...

- strong effects on parameter estimates
- implausible predictions in constant-variance VARs
- in terms of point and density forecasts

We develop approaches with random outliers in SV

- Outliers seen as fast, but transitory changes in SV
- Random outliers are part of the DGP and its predictions

RESEARCH AGENDA AND CONTRIBUTIONS

How to make VARs work in turbulent times?

Extreme realizations since March 2020 lead to ...

- strong effects on parameter estimates
- implausible predictions in constant-variance VARs
- in terms of point and density forecasts

We develop approaches with random outliers in SV

- Outliers seen as fast, but transitory changes in SV
- Random outliers are part of the DGP and its predictions

We also consider simple options for known outliers

- Exogenously “known” outliers
- Not modeled, not part of the DGP
- Treated as missing data (or with dummies)

RELATED LITERATURE

BVARs with stochastic volatility

- Cogley & Sargent (2005), Primiceri (2005)
- Carriero, Clark, & Marcellino (2019)
Carriero, Chan, Clark, & Marcellino (2021)

Extreme data, outliers, and fat tails

- Lenza & Primiceri (2020), Schorfheide & Song (2020),
Bobeica & Hartwig (2021)
- Antolin-Diaz, Drechsel, & Petrella (2021),
Huber, Koop, Onorante, Pfarrhofer, & Schreiner (2020)
- Guerrón-Quintana & Zhong (2020), Mitchell & Weale (2021)
- Jacquier, Polson, & Rossi (2004), Karlsson & Mazur (2020),
Cúrdia, Del Negro & Greenwald (2014),
Clark & Ravazzolo (2015)
- Stock & Watson (2002, 2016), Breitung & Eickmeier (2011)
Artis, Banerjee, & Marcellino (2005)

RELATED LITERATURE

BVARs with stochastic volatility

- Cogley & Sargent (2005), Primiceri (2005)
- Carriero, Clark, & Marcellino (2019)
Carriero, Chan, Clark, & Marcellino (2021)

Extreme data, outliers, and fat tails

- Lenza & Primiceri (2020), Schorfheide & Song (2020),
Bobeica & Hartwig (2021)
- Antolin-Diaz, Drechsel, & Petrella (2021),
Huber, Koop, Onorante, Pfarrhofer, & Schreiner (2020)
- Guerrón-Quintana & Zhong (2020), Mitchell & Weale (2021)
- Jacquier, Polson, & Rossi (2004), Karlsson & Mazur (2020),
Cúrdia, Del Negro & Greenwald (2014),
Clark & Ravazzolo (2015)
- Stock & Watson (2002, 2016), Breitung & Eickmeier (2011)
Artis, Banerjee, & Marcellino (2005)

AGENDA

- 1 BVAR models and extreme observations
- 2 Forecast performance
- 3 Model fit
- 4 Robustness
- 5 Conclusion
- 6 (Appendix)

BVAR MODELS AND OUTLIER-ADJUSTED VOLATILITY

Dynamic model for the vector y_t

$$y_t = \Pi_0 + \Pi(L)y_{t-1} + v_t, \quad E_{t-1}v_t = 0$$

We consider the following variants:

CONST: $v_t = \Sigma^{0.5}\varepsilon_t, \quad \varepsilon_t \sim N(0, I)$

BVAR MODELS AND OUTLIER-ADJUSTED VOLATILITY

Dynamic model for the vector y_t

$$y_t = \Pi_0 + \Pi(L)y_{t-1} + v_t, \quad E_{t-1}v_t = 0$$

We consider the following variants:

CONST: $v_t = \Sigma^{0.5} \varepsilon_t, \quad \varepsilon_t \sim N(0, I)$

SV: $v_t = A^{-1} \Lambda_t^{0.5} \varepsilon_t, \quad \log \lambda_{j,t} \sim RW$

A^{-1} lower unit-triangular, Λ_t diagonal

Stylized setup: scalar, one observation, known variance etc.

Inference about slope coefficients π in stylized setup:

$$y_t = \pi y_{t-1} + v_t$$

- Given y_{t-1} , $v_t \sim N(0, \sigma_t^2)$, σ_t^2 known
- Prior: $\pi | y_{t-1} \sim N(\underline{\pi}, \underline{\omega}^2)$

Observed value y_t is noisy signal about π

Stylized setup: scalar, one observation, known variance etc.

Inference about slope coefficients π in stylized setup:

$$y_t = \pi y_{t-1} + v_t$$

- Given y_{t-1} , $v_t \sim N(0, \sigma_t^2)$, σ_t^2 known
- Prior: $\pi | y_{t-1} \sim N(\underline{\pi}, \underline{\omega}^2)$

Observed value y_t is noisy signal about π

Inference about π is a signal extraction problem

$$E(\pi | y_t, y_{t-1}) = (1 - \kappa) \underline{\pi} + \kappa \frac{y_t y_{t-1}}{y_{t-1}^2}$$

$$\text{with } \kappa = \frac{\underline{\omega}^2}{\sigma_t^2 / y_{t-1}^2 + \underline{\omega}^2}$$

Less weight on time- t data point,
the noisier the signal (the larger σ_t^2)

BVAR MODELS AND OUTLIER-ADJUSTED VOLATILITY

Dynamic model for the vector y_t

$$y_t = \Pi_0 + \Pi(L)y_{t-1} + v_t, \quad E_{t-1}v_t = 0$$

We consider the following variants:

CONST: $v_t = \Sigma^{0.5} \varepsilon_t, \quad \varepsilon_t \sim N(0, I)$

SV: $v_t = A^{-1} \Lambda_t^{0.5} \varepsilon_t, \quad \log \lambda_{j,t} \sim RW$

$v_t = A^{-1} \Lambda_t^{0.5} O_t \varepsilon_t, \quad o_{j,t} \sim iid$

A^{-1} lower unit-triangular, Λ_t, O_t diagonal

BVAR MODELS AND OUTLIER-ADJUSTED VOLATILITY

Dynamic model for the vector y_t

$$y_t = \Pi_0 + \Pi(L)y_{t-1} + v_t, \quad E_{t-1}v_t = 0$$

We consider the following variants:

CONST: $v_t = \Sigma^{0.5} \varepsilon_t, \quad \varepsilon_t \sim N(0, I)$

SV: $v_t = A^{-1} \Lambda_t^{0.5} \varepsilon_t, \quad \log \lambda_{j,t} \sim RW$

SVO: $v_t = A^{-1} \Lambda_t^{0.5} O_t \varepsilon_t, \quad o_{j,t} \sim iid$

$$o_{j,t} \sim \begin{cases} 1 & \text{with prob. } 1 - p_j \\ U(2, 20) & \text{with prob. } p_j \end{cases}$$

A^{-1} lower unit-triangular, Λ_t, O_t diagonal

BVAR MODELS AND OUTLIER-ADJUSTED VOLATILITY

Dynamic model for the vector y_t

$$y_t = \Pi_0 + \Pi(L)y_{t-1} + v_t, \quad E_{t-1}v_t = 0$$

We consider the following variants:

CONST: $v_t = \Sigma^{0.5} \varepsilon_t$, $\varepsilon_t \sim N(0, I)$

SV: $v_t = A^{-1} \Lambda_t^{0.5} \varepsilon_t$, $\log \lambda_{j,t} \sim RW$

SVO-t: $v_t = A^{-1} \Lambda_t^{0.5} O_t Q_t \varepsilon_t$, $o_{j,t}, q_{j,t} \sim iid$

$$q_{j,t} \sim \sqrt{IG\left(\frac{\nu_j}{2}, \frac{\nu_j}{2}\right)}$$

$$o_{j,t} \sim \begin{cases} 1 & \text{with prob. } 1 - p_j \\ U(2, 20) & \text{with prob. } p_j \end{cases}$$

A^{-1} lower unit-triangular, Λ_t , O_t , and Q_t diagonal

BVAR MODELS AND OUTLIER-ADJUSTED VOLATILITY

Dynamic model for the vector y_t

$$y_t = \Pi_0 + \Pi(L)y_{t-1} + v_t, \quad E_{t-1}v_t = 0$$

We consider the following variants:

CONST: $v_t = \Sigma^{0.5} \varepsilon_t$, $\varepsilon_t \sim N(0, I)$

SV: $v_t = A^{-1} \Lambda_t^{0.5} \varepsilon_t$, $\log \lambda_{j,t} \sim RW$

SVO-t: $v_t = A^{-1} \Lambda_t^{0.5} O_t Q_t \varepsilon_t$, $o_{j,t}, q_{j,t} \sim iid$

$$q_{j,t} \sim \sqrt{IG\left(\frac{\nu_j}{2}, \frac{\nu_j}{2}\right)}$$

$$o_{j,t} \sim \begin{cases} 1 & \text{with prob. } 1 - p_j \\ U(2, 20) & \text{with prob. } p_j \end{cases}$$

O_t can have more mass on large outliers than Q_t

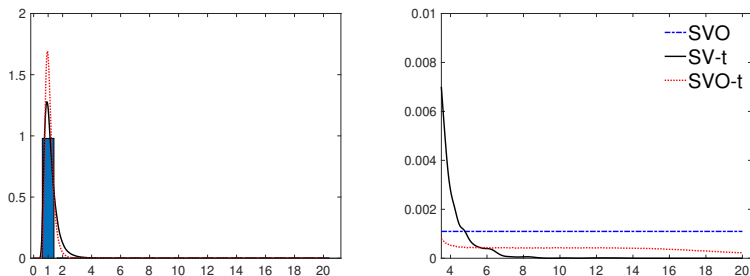
A^{-1} lower unit-triangular, Λ_t , O_t , and Q_t diagonal

SVO VS. SV-t

Densities for $o_{j,t}$ (SVO), $q_{j,t}$ (SV-t), and $o_{j,t} \cdot q_{j,t}$ (SVO-t)

$o_{j,t}$ can place more mass on large outliers than $q_{j,t}$

(Right panel zooms in on right tail of left panel.)



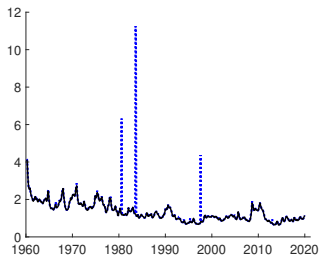
- SVO prior: 1 outlier every 4 years
- For SVO-t: prior mean lowered to 1 outlier every 10 years
- Here: all calibrated to generate same 2nd moment as SVO (will be estimated in our empirical application)

FORECAST ERROR VOL DECOMPOSITION PAYROLL GROWTH

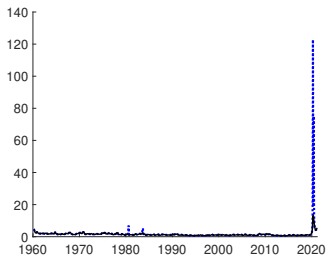
total Σ_t incl. outliers (colored), pure SV component $\tilde{\Sigma}_t$ (black)

SVO

pre COVID-19

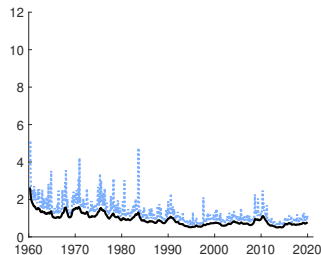


full sample

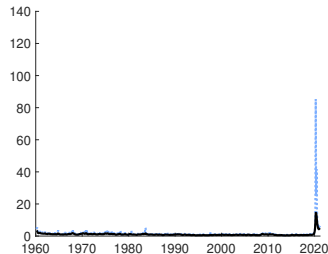


SV-t

pre COVID-19



full sample



Note: Medians. Total: $\Sigma_t = A^{-1}O_tQ_t\Lambda_tQ_tO_tA^{-T}$, pure SV: $\tilde{\Sigma}_t = A^{-1}\Lambda_tA^{-T}$

MISSING-DATA APPROACH FOR KNOWN OUTLIERS

VAR-SV with missing data: “SV-OutMiss”

- **Pre-screen data for outliers**, based on historical norms (e.g. distance from median; similar to DFM literature)
- **If outlier, treat data point z_t^j as missing data**

MISSING-DATA APPROACH FOR KNOWN OUTLIERS

VAR-SV with missing data: “SV-OutMiss”

- **Pre-screen data for outliers**, based on historical norms (e.g. distance from median; similar to DFM literature)
- **If outlier, treat data point z_t^j as missing data**
- **Special case of additive measurement errors e_t :**

$$z_t^j = y_t^j + \phi_t^j \cdot e_t^j$$

with $\phi_t^j \rightarrow \infty$ if outlier, $\phi_t^j = 0$ if otherwise

MISSING-DATA APPROACH FOR KNOWN OUTLIERS

VAR-SV with missing data: "SV-OutMiss"

- **Pre-screen data for outliers**, based on historical norms (e.g. distance from median; similar to DFM literature)
- **If outlier, treat data point z_t^j as missing data**
- **Special case of additive measurement errors e_t :**

$$z_t^j = y_t^j + \phi_t^j \cdot e_t^j$$

with $\phi_t^j \rightarrow \infty$ if outlier, $\phi_t^j = 0$ if otherwise

- **Prunes outlier effects from forecast jump off:**

$$E_t(y_{t+h}) = \Pi^h E(y_t | z^t)$$

MISSING-DATA APPROACH FOR KNOWN OUTLIERS

VAR-SV with missing data: "SV-OutMiss"

- **Pre-screen data for outliers**, based on historical norms (e.g. distance from median; similar to DFM literature)
- **If outlier, treat data point z_t^j as missing data**
- **Special case of additive measurement errors e_t :**

$$z_t^j = y_t^j + \phi_t^j \cdot e_t^j$$

with $\phi_t^j \rightarrow \infty$ if outlier, $\phi_t^j = 0$ if otherwise

- **Prunes outlier effects from forecast jump off:**

$$E_t(y_{t+h}) = \Pi^h E(y_t | z^t)$$

**Past outliers taken as given,
none anticipated in future**

AGENDA

- 1 BVAR models and extreme observations
- 2 Forecast performance**
 - before COVID-19
 - since COVID-19
- 3 Model fit
- 4 Robustness
- 5 Conclusion
- 6 (Appendix)

DATA SET

Monthly obs from 1959:03 to 2021:03; FRED-MD vintage 2021:04

Variable	FRED-MD code	Transformation	RW Prior
Real Income	RPI	$\Delta \log(x_t) \cdot 1200$	
Real Consumption Exp. IP	DPCERA3M086SBEA INDPRO	$\Delta \log(x_t) \cdot 1200$ $\Delta \log(x_t) \cdot 1200$	
Capacity Utilization	CUMFNS		yes
Unemployment Rate	UNRATE		yes
Nonfarm payrolls Hours	PAYEMS CES0600000007	$\Delta \log(x_t) \cdot 1200$	
Hourly Earnings	CES0600000008	$\Delta \log(x_t) \cdot 1200$	
PPI: Finished Goods	WPSFD49207	$\Delta \log(x_t) \cdot 1200$	yes
PCE prices	PCEPI	$\Delta \log(x_t) \cdot 1200$	yes
Housing Starts	HOUST	$\log(x_t)$	yes
SP500	SP500	$\Delta \log(x_t) \cdot 1200$	
U.S. / U.K. Forex	EXUSUKx	$\Delta \log(x_t) \cdot 1200$	
5-Year yield	GS5		yes
10-Year yield	GS10		yes
Baa spread	BAAFFM		yes

Note: Interest-rate forecasts are dynamically censored at ELB

SETUP OF OUR FORECAST COMPARISONS

BVAR estimation

- Non-conjugate priors (Minnesota-style shrinkage of Π)
- Gibbs samplers

Quasi real-time setup

- Growing estimation windows (i.e., recursive scheme)
- Forecasts up to two years out ($h = 24$)

Evaluation window 1985:01 – 2017:12
to ignore 2020-21 realizations

AGENDA

- 1 BVAR models and extreme observations
- 2 Forecast performance**
 - before COVID-19
 - since COVID-19
- 3 Model fit
- 4 Robustness
- 5 Conclusion
- 6 (Appendix)

POINT FORECAST COMPARISON

RELATIVE RMSE

Values below one indicate improvement over SV

Variable / Horizon	SVO-t			SV-OutMiss		
	3	12	24	3	12	24
Real Income	1.00	1.01**	0.93*			
Real Consumption	1.00	1.00	1.01			
IP	0.99	1.00	0.96***			
Capacity Utilization	0.99	1.00	0.97			
Unemployment Rate	0.99	0.99	0.99			
Nonfarm Payrolls	1.00	1.01	0.98			
Hours	1.00	0.99	1.00			
Hourly Earnings	1.00	1.01**	1.03*			
PPI (Fin. Goods)	0.99	1.00	1.00			
PCE Prices	1.00	1.01	1.03*			
Housing Starts	0.99	0.99	1.03***			
S&P 500	1.00	1.00	1.01**			
USD / GBP FX Rate	1.00	1.00	0.86			
5-Year yield	1.00	1.01	0.97			
10-Year yield	1.00	1.01	0.98			
Baa Spread	0.99	0.99	0.97			

Note: Eval from 1985:01 through 2017:12. Stars denote DMW significance

POINT FORECAST COMPARISON

RELATIVE RMSE

Values below one indicate improvement over SV

Variable / Horizon	SVO-t			SV-OutMiss		
	3	12	24	3	12	24
Real Income	1.00	1.01**	0.93*	1.00	1.01	0.94
Real Consumption	1.00	1.00	1.01	0.99	1.00	1.00
IP	0.99	1.00	0.96***	1.00	0.99	0.98*
Capacity Utilization	0.99	1.00	0.97	1.02	0.98	0.97
Unemployment Rate	0.99	0.99	0.99	1.00	0.99*	1.00
Nonfarm Payrolls	1.00	1.01	0.98	1.00	0.99	0.98
Hours	1.00	0.99	1.00	1.01	1.00	1.01
Hourly Earnings	1.00	1.01**	1.03*	1.00	1.00	1.00
PPI (Fin. Goods)	0.99	1.00	1.00	1.00	1.00	1.00
PCE Prices	1.00	1.01	1.03*	0.99	1.02**	1.02
Housing Starts	0.99	0.99	1.03***	1.00	0.99	1.00
S&P 500	1.00	1.00	1.01**	1.00	1.00	1.01
USD / GBP FX Rate	1.00	1.00	0.86	0.99*	1.00	0.84
5-Year yield	1.00	1.01	0.97	0.99*	1.00	0.96
10-Year yield	1.00	1.01	0.98	0.99	1.00	0.98
Baa Spread	0.99	0.99	0.97	0.99	0.99*	1.01

Note: Eval from 1985:01 through 2017:12. Stars denote DMW significance

DENSITY FORECAST COMPARISON

RELATIVE CRPS

Values below one indicate improvement over SV

Variable / Horizon	SVO-t			SV-OutMiss		
	3	12	24	3	12	24
Real Income	0.96***	0.94***	0.86***	0.94***	0.94***	0.87***
Real Consumption	0.99	0.97***	0.91***	0.98*	0.98***	0.94***
IP	0.99*	0.96***	0.90***	1.01	0.98***	0.96***
Capacity Utilization	0.99	1.00	0.96	1.01	0.99	0.96**
Unemployment Rate	1.00	1.01	1.00	0.99	0.99	0.99
Nonfarm Payrolls	1.00	0.98*	0.93***	0.99	0.98**	0.96***
Hours	0.99	0.98*	0.92***	1.01	0.99	0.97***
Hourly Earnings	0.99**	0.98***	0.93***	1.00	0.99**	0.97***
PPI (Fin. Goods)	0.99*	0.98***	0.95***	0.99	0.99**	0.97***
PCE Prices	1.00	1.00	0.98***	0.99**	0.99	0.97***
Housing Starts	1.00	1.01	1.01*	1.00	0.99	0.99
S&P 500	0.99**	0.97***	0.92***	0.99	0.98***	0.96***
USD / GBP FX Rate	0.99*	0.97***	0.92***	0.99**	0.97**	0.93***
5-Year yield	1.00	1.01*	1.01	0.99	1.00	0.99*
10-Year yield	1.01	1.01	1.01*	1.00	1.00	0.99
Baa Spread	0.99	0.99	0.97**	0.98*	0.98**	0.98*

Note: Eval from 1985:01 through 2017:12. Stars denote DMW significance

TAKE AWAYS: FORECAST PERFORMANCE PRIOR 2020

Evaluating the out-of-sample forecast with origins from 1985–2017 ...

Across variables and forecast horizons, we typically find:

- **SV outperformed the CONST benchmark**
(see paper)
- **SVO-t did as well as, if not better, than SV**
- **SV-OutMiss performed similarly to SVO-t**

**Outlier-adjusted SV helpful for outlier-prone variables
while not hurting otherwise,
and similarly so for missing-data treatment**

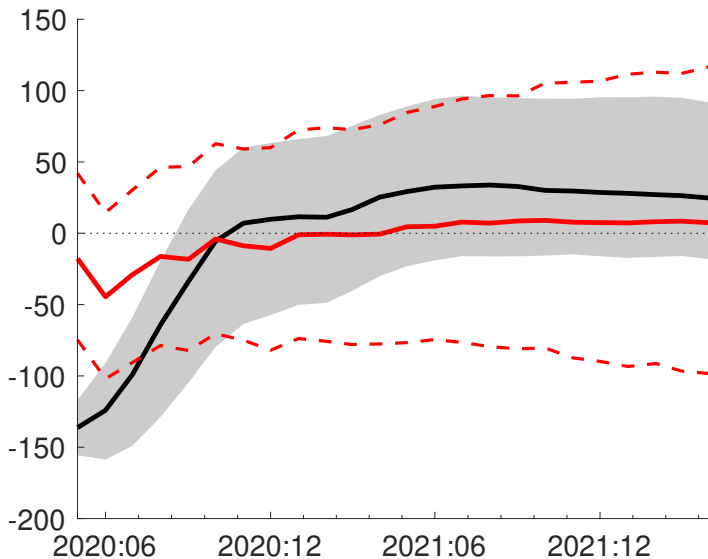
AGENDA

- 1 BVAR models and extreme observations
- 2 Forecast performance**
 - before COVID-19
 - since COVID-19
- 3 Model fit
- 4 Robustness
- 5 Conclusion
- 6 (Appendix)

PAYROLL GROWTH FORECASTS

APRIL 2020

SV (red), CONST (black)

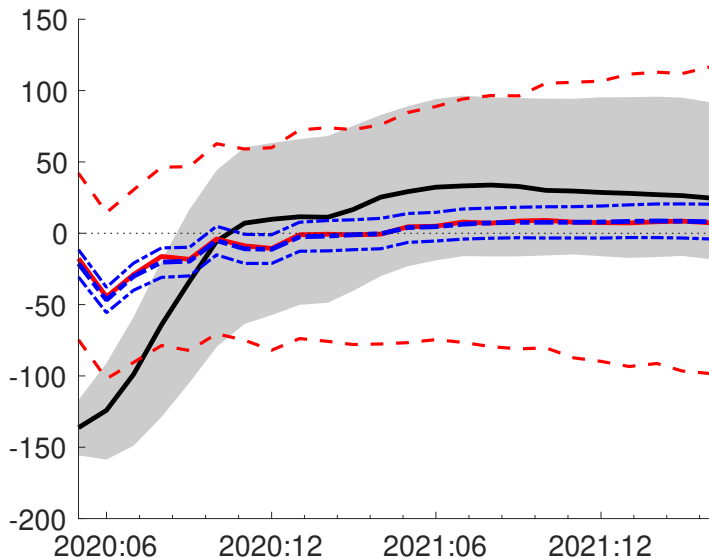


Note: Medians and 68% bands

PAYROLL GROWTH FORECASTS

APRIL 2020

SVO-t (blue), SV (red), CONST (black)

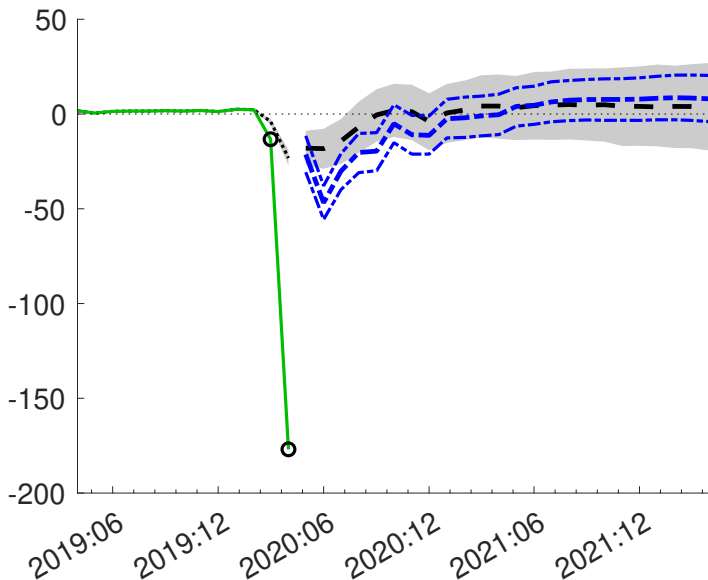


Note: Medians and 68% bands

PAYROLL FORECASTS W/KNOWN OUTLIERS

APRIL 2020

SVO-t (blue), SV-OutMiss (black)

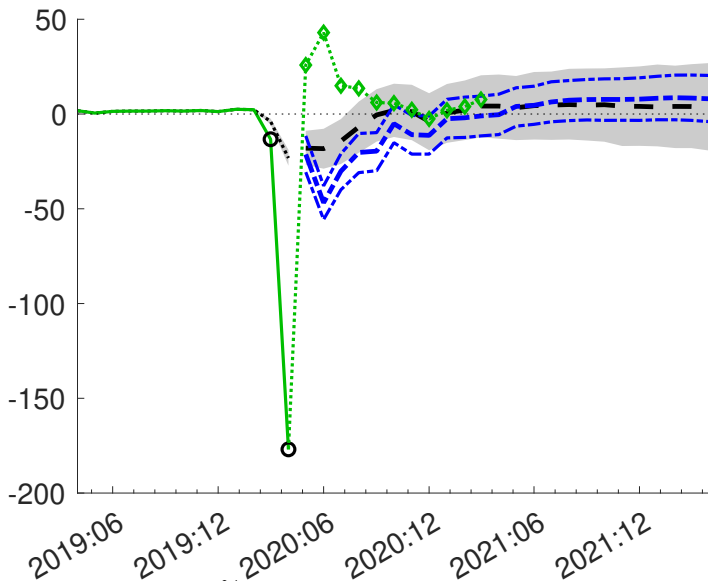


Note: Medians and 68% bands. Circles: Pre-identified outlier data

PAYROLL FORECASTS W/KNOWN OUTLIERS

APRIL 2020

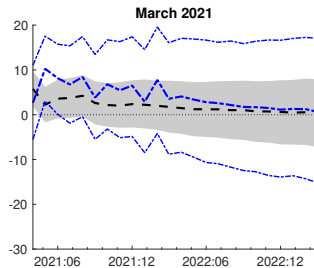
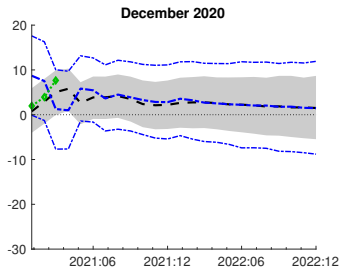
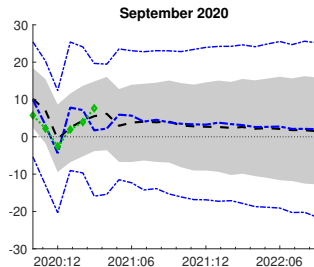
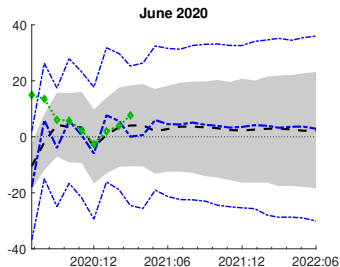
SVO-t (blue), SV-OutMiss (black), realized (green)



Note: Medians and 68% bands. Circles: Pre-identified outlier data

PAYROLL GROWTH FORECASTS W/KNOWN OUTLIERS

SVO-t (blue), SV-OutMiss (black), realized (green)



Medians and 68% bands. Circles depict pre-identified past outliers

Typically, across all 16 variables ...

Point forecasts

- **Very similar: for all of our SV variants**
(SV, SVO-t, SV-Dummy)
- **Some differences compared to SV-OutMiss,**
which proved more accurate so far (RMSE, for $h \leq 6$)

Typically, across all 16 variables ...

Point forecasts

- Very similar: for all of our SV variants (SV, SVO-t, SV-Dummy)
- Some differences compared to SV-OutMiss, which proved more accurate so far (RMSE, for $h \leq 6$)

Predictive densities

- **SV: very wide**
- **When COVID-19 obs are dummied out: very tight** (see paper)
- **SVO-t and SV-OutMiss: in between**

FORECAST PERFORMANCE 2020:03 – 2021:02

Typically, across all 16 variables ...

Point forecasts

- Very similar: for all of our SV variants (SV, SVO-t, SV-Dummy)
- Some differences compared to SV-OutMiss, which proved more accurate so far (RMSE, for $h \leq 6$)

Predictive densities

- SV: very wide
- When COVID-19 obs are dummied out: very tight (see paper)
- SVO-t and SV-OutMiss: in between
- **Near-term CRPS:** Some advantage of SVO-t over SV, with SV-OutMiss at least as strong

Caveat: Only few realizations observed so far

AGENDA

- 1 BVAR models and extreme observations
- 2 Forecast performance
- 3 Model fit**
- 4 Robustness
- 5 Conclusion
- 6 (Appendix)

MODEL FIT MEASURED BY PREDICTIVE SCORES

Differences in log-scores $\sum_t \log p(y_t|y_{t-1}, M)$ of model M relative to SV

Samples	Models				
	SVO-t	SVO	SV-t	SV-OutMiss*	CONST
Full sample					
1975-2021					
G Inflation					
1975-1984					
G Moderation					
1985-2007					
GFC					
2008-2014					
COVID-19					
2020:03-2021:02					

MODEL FIT MEASURED BY PREDICTIVE SCORES

Differences in log-scores $\sum_t \log p(y_t|y_{t-1}, M)$ of model M relative to SV

Samples	Models				
	SVO-t	SVO	SV-t	SV-OutMiss*	CONST
Full sample					
1975-2021	218.92	-116.13	195.19	-800.17	-9200.01
G Inflation					
1975-1984	15.08	24.30	10.37	TBD	-250.02
G Moderation					
1985-2007	-44.93	-44.57	-52.00	-6.64	-385.43
GFC					
2008-2014	24.15	33.67	13.69	-56.28	-236.40
COVID-19					
2020:03-2021:02	191.49	-144.57	193.28	-739.52	-8167.44

MODEL FIT MEASURED BY PREDICTIVE SCORES

Differences in log-scores $\sum_t \log p(y_t|y_{t-1}, M)$ of model M relative to SV

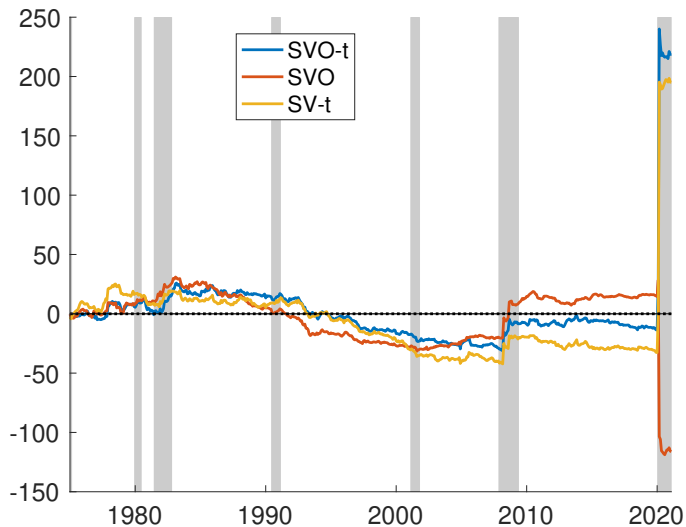
Samples	Models				
	SVO-t	SVO	SV-t	SV-OutMiss*	CONST
Full sample					
1975-2021	218.92	-116.13	195.19	-800.17	-9200.01
G Inflation					
1975-1984	15.08	24.30	10.37	TBD	-250.02
G Moderation					
1985-2007	-44.93	-44.57	-52.00	-6.64	-385.43
GFC					
2008-2014	24.15	33.67	13.69	-56.28	-236.40
COVID-19					
2020:03-2021:02	191.49	-144.57	193.28	-739.52	-8167.44

SVO-t with consistent strength in turbulent times
(Great Inflation, GFC and COVID-19)

Great Moderation: SV best, followed by SV-OutMiss

PREDICTIVE SCORES OVER TIME

Differences in log-scores $\sum_t \log p(y_t | y_{t-1}, M)$ of model M relative to SV



Outlier adjusted SV strongest in turbulent times

AGENDA

- 1 BVAR models and extreme observations
- 2 Forecast performance
- 3 Model fit
- 4 Robustness**
- 5 Conclusion
- 6 (Appendix)

ROBUSTNESS

We also consider ...

Common vs variable-specific outliers

- Common outlier posits one scalar factor, o_t , that simultaneously scales all variables up or down

$$v_t = o_t \cdot A^{-1} \Lambda_t^{0.5} \varepsilon_t \quad \varepsilon_t \sim N(0, I)$$

- Maybe ok for tightly selected variables during COVID-19
- Less plausible for broader set of variables

Other model variants

- **VAR in levels:** ongoing work, results similar to baseline
- **SV w/AR(1):** mean-reversion in SV helps, with further room for improvement through outlier-adjusted SV
- **Ordering of variables in VAR:** Not too sensitive

AGENDA

- 1 BVAR models and extreme observations
- 2 Forecast performance
- 3 Model fit
- 4 Robustness
- 5 Conclusion**
- 6 (Appendix)

CONCLUSIONS

Benefits of outlier-adjusted SV in BVARs

- Detects outliers as random, not known, events
- Delineates transitory spikes from persistent changes in SV
- Pre-COVID-19: a little better, no worse than regular SV
- Since COVID-19: more plausible forecast densities
- Same pattern confirmed by log scores for GFC, G Inflation

Alternative: missing-data approach

- Require outliers to be known/identified ex-ante
- Outliers not modeled, densities assume standard VAR-SV
- Robust performance; but, neglect risk of future outliers

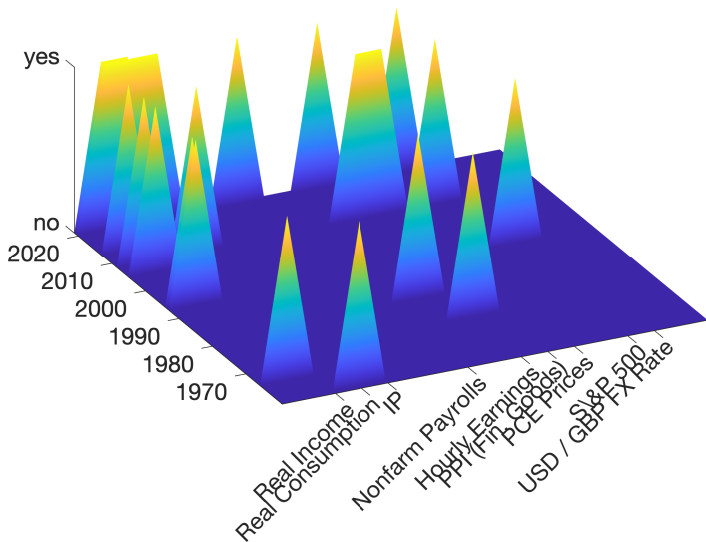
Makes BVARs work through turbulent times

APPENDIX

- **Outliers in post-war data**
- Individual vs common outliers
- Payroll forecasts in 2020/2021
- Forecast errors since COVID-19
- Ordering of Variables

OUTLIERS IN POST-WAR DATA

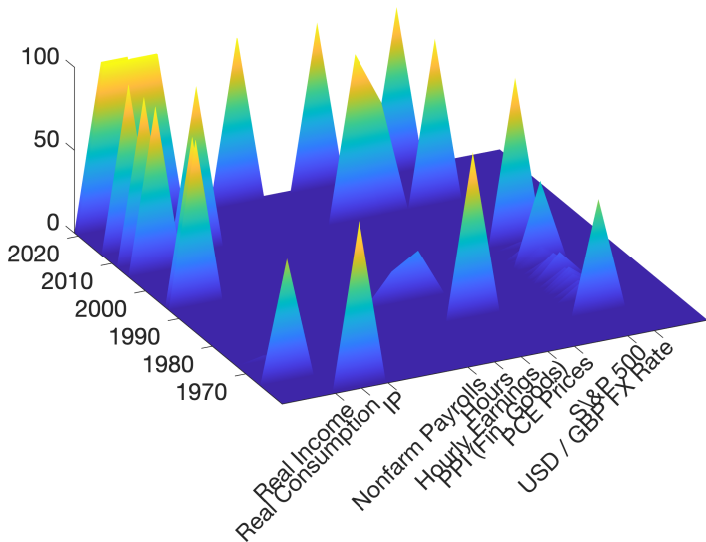
Occurrence of observations more than 5 times the IQR away from median



Measured over full sample of monthly data 1959:03–2021:03. Later we use growing samples in quasi-real time.

OUTLIERS IN POST-WAR DATA

Odds of observations counted as outlier in growing samples starting 1985



Occurrence of observations more than 5 times the IQR away from median

APPENDIX

- Outliers in post-war data
- **Individual vs common outliers**
- Payroll forecasts in 2020/2021
- Forecast errors since COVID-19
- Ordering of Variables

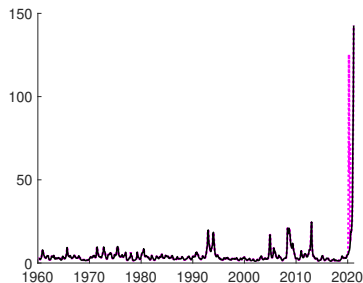
INDIVIDUAL VS COMMON OUTLIER MODEL

- Common outlier posits one scalar factor, \mathbf{o}_t , that simultaneously scales all variables up or down

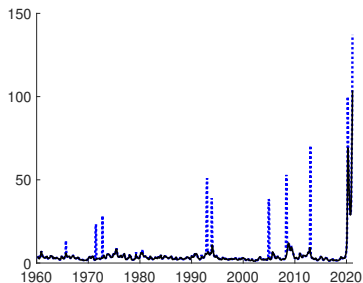
$$\mathbf{v}_t = \mathbf{o}_t \cdot \mathbf{A}^{-1} \mathbf{\Lambda}_t^{0.5} \boldsymbol{\varepsilon}_t \quad \boldsymbol{\varepsilon}_t \sim \mathbf{N}(\mathbf{0}, \mathbf{I})$$

- Maybe ok for selected variables during COVID-19
- Less plausible for broader set of variables
- For example, FE vol decomposition for real income:

SV-o



SVO

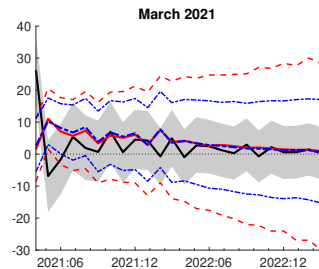
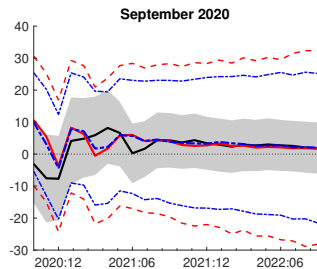
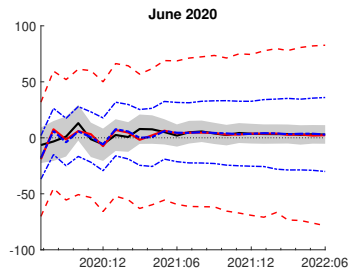
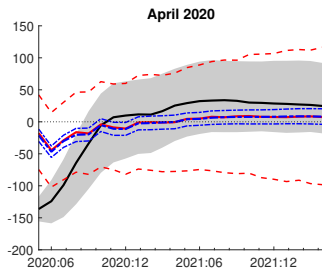


APPENDIX

- Outliers in post-war data
- Individual vs common outliers
- **Payroll forecasts in 2020/2021**
- Forecast errors since COVID-19
- Ordering of Variables

PAYROLL GROWTH FORECASTS

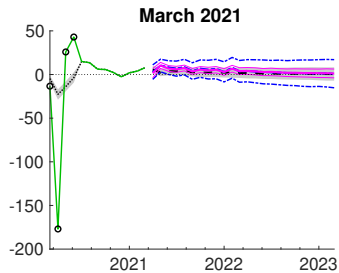
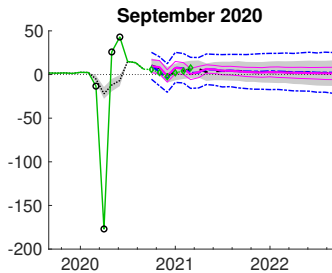
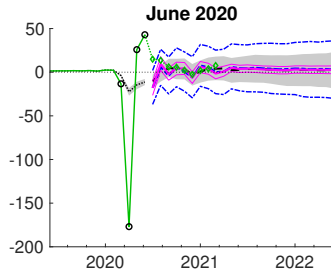
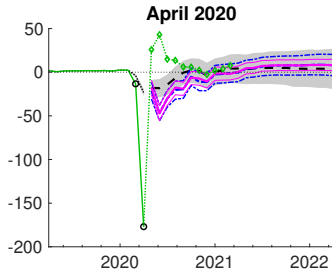
SVO-t (blue), SV (red), CONST (black)



Note: Medians and 68% bands

PAYROLL GROWTH FORECASTS W/KNOWN OUTLIERS

SVO-t (blue), SV-OutMiss (black), SV-Dummies (purple), realized (green)



Medians and 68% bands. Circles depict pre-identified past outliers

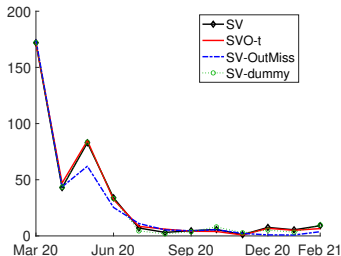
APPENDIX

- Outliers in post-war data
- Individual vs common outliers
- Payroll forecasts in 2020/2021
- **Forecast errors since COVID-19**
- Ordering of Variables

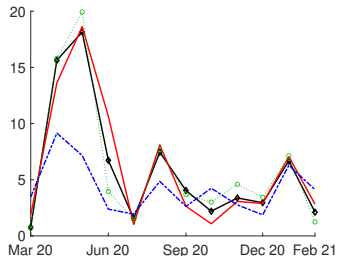
FORECAST ERRORS SINCE COVID-19

Absolute errors of one-step ahead forecasts made March 2020 to Feb 2021

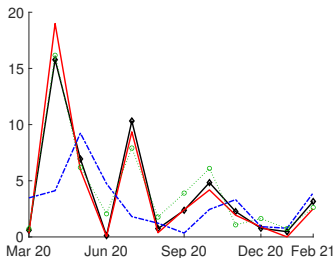
Payroll growth



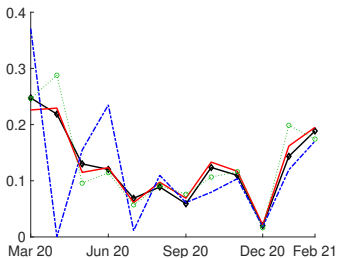
Hourly Earnings



PCE price inflation



Housing starts



APPENDIX

- Outliers in post-war data
- Individual vs common outliers
- Payroll forecasts in 2020/2021
- Forecast errors since COVID-19
- **Ordering of Variables**

CHANGES IN ORDER OF VARIABLES IN VAR

VAR-SV not invariant to order of elements in y_t

- Well-known concern: Inference on

$$v_t = A^{-1} \Lambda_t^{0.5} \varepsilon_t$$

not invariant to ordering of variables

- Primiceri (2005), Arias, Rubio-Ramirez, & Shin (2021)

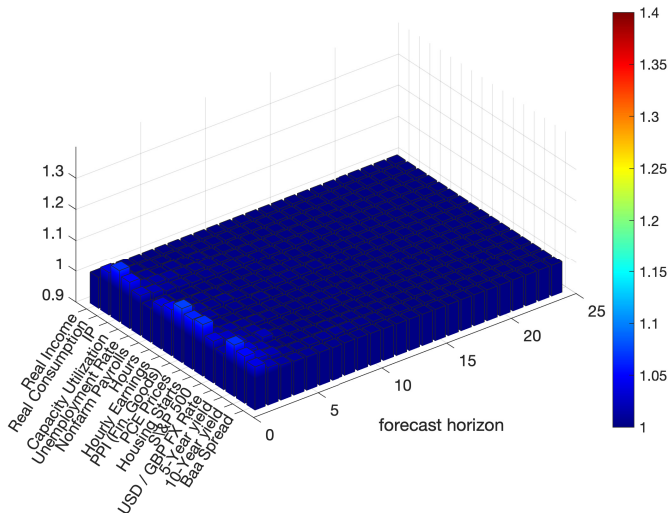
We consider random permutations

- N=640 permutations
- Two forecast origins: March 2021 and April 2020
- Compare predictive densities with “potential scale reduction factors” (PSRF) of Gelman & Rubin (1992)

**No significant differences per March 2021
only some per April 2020**

DISPERSION BETWEEN DENSITIES W/REORDERING

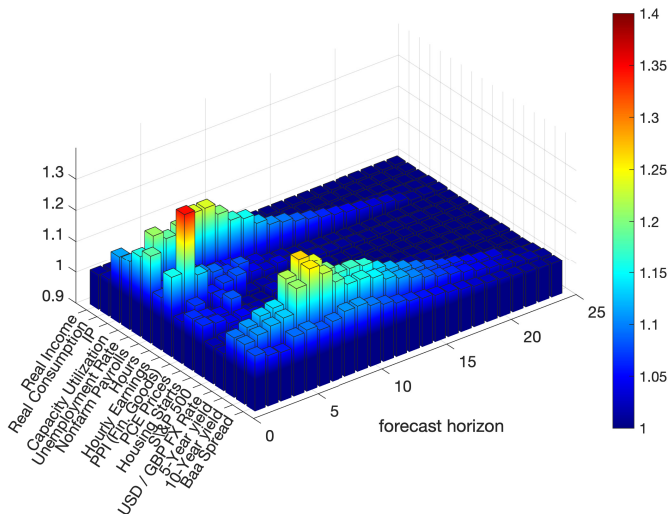
Forecast origin: March 2021



Gelman-Rubin PSRF across 640 permutations. Optimal value: 1.0

DISPERSION BETWEEN DENSITIES W/REORDERING

Forecast origin: April 2020



Gelman-Rubin PSRF across 640 permutations. Optimal value: 1.0

CONCLUSIONS

Benefits of outlier-adjusted SV in BVARs

- Detects outliers as random, not known, events
- Delineates transitory spikes from persistent changes in SV
- Pre-COVID-19: a little better, no worse than regular SV
- Since COVID-19: more plausible forecast densities
- Same pattern confirmed by log scores for GFC, G Inflation

Alternative: missing-data approach

- Require outliers to be known/identified ex-ante
- Outliers not modeled, densities assume standard VAR-SV
- Robust performance; but, neglect risk of future outliers

Makes BVARs work through turbulent times