# Customers and Retail Growth 

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#### Abstract

Using Visa debit and credit card transactions in the U.S. from 2016 to 2019, we document the importance of customers in accounting for sales variation across merchants, across stores within retail chains, and over time for individual merchants and stores. Customers, as opposed to transactions per customer or dollar sales per transaction, consistently account for about $80 \%$ of sales variation. The top $1 \%$ of growing and shrinking merchants account for about $70 \%$ of customer and sales reallocation in a given year. We write down an endogenous growth model with and without the customer margin. In this model, we find that the customer margin dramatically increases the size and growth contribution of the largest firms, but actually lowers the aggregate growth rate by diverting resources from research to marketing.


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## 1. Introduction

Over the last two decades, a stream of research has emphasized the role of customer acquisition in firm dynamics, trade, and growth. Influential models include Fishman and Rob (2003), Luttmer (2006), Arkolakis (2010, 2016), and Perla (2019). Gourio and Rudanko (2014) and Gilchrist, Schoenle, Sim and Zakrajšek (2017) argue that such frictions play a role in business cycle fluctuations, Eslava, Tybout, Jinkins, Krizan and Eaton (2015) present evidence and a customer search model of exporting firm dynamics, and Bernard, Dhyne, Magerman, Manova and Moxnes (2019) document the importance of the number of customers in Belgian inter-firm transactions. Bornstein (2018) argues that consumer aging interacts with customer inertia to explain the decline in both labor's share and firm entry in recent decades. Bagwell (2007) surveys models and evidence on the role of advertising in reaching and attracting customers.

In this paper, we use Visa debit and credit card transactions from 20162019 to bring new systematic and direct evidence to bear on the importance of customers in the U.S. retail sector. ${ }^{1}$ The Visa data covers a significant part of consumer spending in the U.S. Roughly $93 \%$ of households used at least one debit or credit card in 2018 (Foster, Greene and Stavins, 2019). Around $24 \%$ of all U.S. consumer spending flowed through Visa in 2019. ${ }^{2}$ If Visa's $60 \%$ share is representative of all debit and credit card spending, then Visa spending patterns are relevant for around $40 \%$ of all consumption. ${ }^{3}$

We start by decomposing Visa sales at the chain and store level into the number of unique credit and debit cards, transactions per card, and sales per transaction. We find that the number of customers dominates the decomposi-

[^1]tion across merchants and across stores within merchants, and over time within stores or merchants.

The customer margin is more important for brick-and-mortar transactions than for e-commerce. Focusing on offline retail, we show that about $80 \%$ of sales variation can be traced to the number of customers, and that the importance of customers per store plays an even bigger role than the number of stores for sales variation across merchants and over time for a given merchant. For only the largest merchants does the store margin play a big role. Perhaps surprisingly, the importance of customers is remarkably consistent across all retail categories, such as furniture, electronics, restaurants, or gas stations.

Our decomposition does not distinguish between adding low-spending vs. high-spending customers. If expanding stores and merchants tend to add lowspending customers, this will tend to overstate the contribution of new customers and understate the role of spending increases by retained customers. To address this, we show that retained customers do tend to increase their spending more at fast-growing merchants and stores. Even with a generous adjustment for the spending of gained and lost customers versus retained customers, however, we find that the extensive margin accounts for $60 \%$ of sales growth variation across merchants and stores.

We then continue by showing that around $70 \%$ of aggregate sales increases and decreases can be traced to the $1 \%$ fastest growing and shrinking merchants in a given year. This is consistent with a stream of results on the role of fastgrowing firms in aggregate job creation, such as Decker, Haltiwanger, Jarmin and Miranda (2016). We find that most of this tail behavior in the Visa data reflects adding or losing customers. Though in the retail sector rather than the manufacturing sector, our evidence of a large extensive margin for customers is in the spirit of findings by Foster, Haltiwanger and Syverson (2008, 2016) and Hottman, Redding and Weinstein (2016). These studies estimate that fast-growing manufacturers experience rising demand for their products, as opposed to selling a wider array of products more cheaply. One explanation
for this could be that such firms are attracting more customers, perhaps linked to the quality and variety of their products. Baker, Baugh and Sammon (2020) also analyze customers using debit and credit card transactions, specifically from 2010 to 2015. Their focus is on a smaller set of 550 firms, 420 of whom are publicly traded and hence have observable stock returns. Their analysis, like ours, emphasizes the importance of the customer margin. In concurrent work, Afrouzi, Drenik and Kim (2020) explore the relationship between pricecost markups and margins of consumer demand.

We next write down an endogenous growth model with firm dynamics that incorporates the customer extensive margin. In the model, firms invest in improving the quality of their products each period, which generates growth in the aggregate. Innovation outcomes are stochastic, so firms are heterogeneous in their quality levels and growth rates. Firms spend on marketing to access customers each period. Because they sell more to each customer they access, firms with higher quality products spend more to access more customers. Customer acquisition thereby amplifies size differences stemming from quality differences across firms. Customers are a static function of current year marketing efforts; firms do not lower markups early on to build their customer base dynamically. This is consistent with empirical evidence on Irish exporting firms and U.S. consumer goods manufacturers documented by Fitzgerald and Priolo (2018) and Fitzgerald, Haller and Yedid-Levi (2019).

In the model, customers dramatically amplify the effects of quality differences and therefore the market share and growth contribution of large firms. Yet, calibrating the model based on the empirical facts we document, we find that the customer margin actually undermines growth This is because it diverts resources from research to marketing.

The rest of the paper proceeds as follows. Section 2 describes the Visa dataset. Section 3 presents evidence on the importance of customers for sales variation. Section 4 lays out the growth model, its calibration, and its quantitative properties. Section 5 concludes.

## 2. The Visa dataset

Our primary source of data relies on all credit and debit card transactions that were processed through Visa's electronic payments network in the US between January 2016 and December 2019. The Visa network is the largest network in the market, accounting for about $50 \%$ of the credit card transaction volume and about $70 \%$ of the debit card volume over this period, with Mastercard, American Express, and Discover sharing the rest. ${ }^{4}$

The unit of observation is a transaction, which includes a merchant identifier, an anonymized card identifier, the time and date of the transaction, and the transaction amount. We do not see the specific items purchased, nor their prices or quantities. The merchant details include an exact store location, so each merchant's store can be uniquely identified.

We apply standard filters used by Visa's data analytics team. We exclude PINdebit transactions (as opposed to signature-debit transactions) because their volume flowing through Visa fluctuates substantially with regulatory changes during our sample period. We also exclude transactions that are not sales drafts (these would include chargebacks, failed transactions, or payment holds, which would not culminate in an actual transaction), those coming from prepaid gift cards, and those conducted by cards that transacted at fewer than five merchants during the lifetime of the card (these are likely specialized merchantspecific rewards cards). We also exclude transactions associated with merchants located outside the US (which would flow through the US Visa network if the card is issued by a US bank). Online Appendix A provides more detail.

We further restrict the analysis to merchants who are (self) classified as operating in the retail sector (Census Bureau NAICS 44 and 45) or as restaurants (NAICS 722), and we limit our primary analysis to in-person transactions where the card was used in a brick-and-mortar store. Thus, our main sample drops NAICS code 454 ("Nonstore Retail"), which consists almost exclusively of online transactions. We also exclude Gas Stations (NAICS 447) when we decompose

[^2]aggregate time series changes, given that gasoline sales are heavily driven by price fluctuations (Levin, Lewis and Wolak, 2017).

Overall, the 2016-2019 Visa data contain an annual average of 428 million cards, 31.5 billion transactions, and $\$ 1.07$ trillion in sales for the retail sector plus restaurants. ${ }^{5}$ Of these sales, $60 \%$ (of the dollar volume) were credit transactions and $40 \%$ were debit transactions. Visa spending covers a similar share of sales and restaurant spending in 2019 as consumption overall. Thus, if other card transactions are similar in nature to Visa's, then Visa spending would be representative of approximately $40 \%$ of all retail and restaurant sales.

We analyze the Visa data at three levels of aggregation. First, we aggregate the transaction data to store-card-years to calculate each card's yearly spending in each store. Second, we aggregate to store-years. For every store-year we calculate the following: the number of distinct customer cards (accounts), the number of transactions (swipes), and the dollar volume of transactions. Third, we aggregate to merchant-years. We then calculate, for each merchant, the following variables: number of distinct locations (stores), number of distinct customer accounts (cards), number of transactions, and dollar volume.

Finally, we note that we also have access to Visa data before 2016, going back to 2007, but it is less granular with respect to stores and merchants. For the largest merchants (which covers about $70 \%$ of the transactions and $60 \%$ of the dollar volume during these years), pre-2016 data do not provide exact location for each transaction, but only a 5-digit zip code, which makes it infeasible to distinguish stores of the same merchant within a zip. Smaller merchants in these earlier years are grouped by NAICS, so it is also infeasible to distinguish different stores of different small merchants within a NAICS-zip combination, rendering them mostly unusable for our purpose. Therefore, in our main analysis we use the complete complete set of merchants and stores uing data from 2016-2019, but we also report results that use larger merchants only for this longer panel of 2007-2019 (see Online Appendix B).

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## 3. The empirical importance of customers

### 3.1. Sales Decompositions

Measurement. To gauge the importance of customers to a merchant's or store's sales, we decompose sales into three margins we can observe in the Visa data:

$$
\begin{equation*}
S=N \cdot \frac{V}{N} \cdot \frac{S}{V}, \tag{1}
\end{equation*}
$$

where $S$ denotes total merchant (or store) sales in dollars over a given period, $N$ is the number of unique customer cards that transact at the merchant or store over that period, and $V$ is the total number of visits (transactions) at the merchant or store in that period. The decomposition breaks down total sales into a customer extensive margin (the number of cards) and two intensive margins - the frequency at which customers visit the merchant or store, $V / N$, and the average transaction amount (the "ticket size"), $S / V$.

At the merchant level, we can further decompose how merchants reach customers into their number of locations (stores), $L$, and the number of unique customers per store, so that the total decomposition becomes:

$$
\begin{equation*}
S=L \cdot \frac{N}{L} \cdot \frac{V}{N} \cdot \frac{S}{V} . \tag{2}
\end{equation*}
$$

To operationalize this decomposition, we take logs of both sides in equation (1) or (2) and regress each right-hand-side component on log sales. These coefficients add up to 1 by construction. The coefficients are equivalent to a variance decomposition in which the covariance terms are split equally.

Overall results. Table 1 presents this decomposition at the merchant level using different subsamples of merchants in 2019. Panel A reports results from all sectors (that is, not only retail), covering over two million different merchants. In this broad sample, the customer margin accounts for $74 \%$ of sales variation across merchants, transactions per card around $4 \%$, and the ticket size accounts for the remaining $22 \%$. When we look at only online transactions
(Panel B), the customer margin falls to $67 \%$ of variation in online sales across merchants. In contrast, the customer margin accounts for $81 \%$ of variation in offline sales across about 1.8 million merchants in 2019 . Of this $81 \%, 71 \%$ comes from cards per store and only around $10 \%$ from the number of stores.

Our primary focus is on offline retail (plus restaurants), a sector that contains almost a million distinct merchants in 2019. The results (in Panel D) are very similar to those obtained using the broader set of offline merchants. For comparison, the bottom panel (Panel E) shows that for the much smaller set of 2,700 large "named" merchants, which Visa tracks all the way back to 2007, the store margin is much more important, accounting for $56 \%$ of the variation in sales vs. only $35 \%$ that is accounted for by cards per store.

In Table 2 we focus on the offline retail (plus restaurants) sector, now showing additional types of variation. The first row (Panel A) reproduces the corresponding cross-sectional analysis we already reported in Panel D of Table 1. The second row (Panel B of Table 2) uses the same set of merchants, over the four years of data (2016-2019), but now focusing on variation in sales over time within each merchant. To do so, we aggregate observation at the merchant-year level (there are 3.9 million observations at this aggregation level) and include in all regressions merchant and year fixed effects so that the variation is coming from merchants that grow faster or slower than the average for that year. The customer extensive margin is just as important here, accounting for $85 \%$ of the variation of sales within merchants. Much of this (68.5\%) is attributed to the changing number of cards per store, and the rest (16\%) to store closings and openings.

Panels C and D of Table 2 report a similar analysis at the single store (rather than the merchant) level, where we control for merchant fixed effect in all regressions so that the object of interest is variation in sales across stores within the same merchant. In Panel C we use a cross section of stores (in 2019), and again find that much ( $84 \%$ ) of the variation of sales across stores of the same merchant is accounted for by the customer margin. Finally, in Panel D we look

Table 1: Sales Decomposition for Different Merchant Samples

Stores Cards/Store Trans/Card Dollar/Trans

$\left.\begin{array}{lccc}\text { A. All Data } & 0.743 & 0.037 & 0.221 \\ (N=2,176,981) & & (<0.001) & (<0.001)\end{array}\right](<.001)$

Note: $N=$ the number of merchant observations. Cards $=$ the number of unique debit and credit cards; Trans = the number of transactions. Standard errors are reported in parenthesis, and RSquared values are in square brackets. Regressions are based on 2019 data. All Data covers all merchants with Visa transactions in consumer NAICS. The "named" merchants are the largest chains. Each regression includes NAICS fixed effects.
at variation in sales within a store over time by (similar to Panel B) using 20162019 data, aggregating variables at the store-year level (we have 8.2 million such observations), and adding store and year fixed effects. The customers margin continues to be the dominant factor ( $82 \%$ in this specification) that explains variation in store sales over time.

Taken together, whether we look across merchants or stores in 2019, or across time for merchants and stores from 2016 to 2019, the number of unique customers explains the vast majority ( $80 \%$ or more) of the variation in sales.

Heterogeneity across retail sectors. In some retail contexts, this general finding seems hardly surprising. For example, in the context of furniture stores, when purchases by a single customer are not frequent, it seems natural that sales are almost entirely driven by how many customers show up. Yet, in other retail contexts this general result is a-priory less obvious. For example, one can imagine that coffee shop sales would be driven not only by how many unique customers show up, but whether they show up once week or every day, or whether they add a pastry to the coffee.

To explore this, we repeat the decomposition exercise using the "within merchant over time", which is our preferred specification (as in Panel B of Table 2), but estimate it separately for different retail categories (defined by 3-digit NAICS). As before, the observation is at merchant-year level (using data from 2016 to 2019), and each regression includes merchant and year fixed effects.

The results are shown in Figure 1. Customers are the primary driver of merchant sales in all sectors. Customers explain at least $70 \%$ of the variation in merchant sales over time in every category except furniture and electronics. In the latter two NAICSs, customers account for about $60 \%$ of the variation in sales, and the average transaction amount accounts for much of the rest. The frequency of visits explains very little of sales variation in thee two, a well as all other retail categories.

Households vs. Cards. Cards could overstate the importance of the customer margin to the extent that households use multiple cards at the same

Table 2: Decomposing Sales in Offline Retail

Stores Cards/Store Trans/Card Dollar/Trans

| A. Across Merchants | 0.094 | 0.712 | 0.036 | 0.157 |
| :--- | :---: | :---: | :---: | :---: |
| $(N=891,289)$ | $[0.119]$ | $[0.597]$ | $[0.020]$ | $[0.057]$ |
| B. Within Merchants over Time | 0.170 | 0.676 | 0.097 | 0.057 |
| $(N=3,627,846)$ | $[0.798]$ | $[0.974]$ | $[0.941]$ | $[0.969]$ |
|  |  |  |  |  |
| C. Across Stores within Merchants |  | 0.841 | 0.077 | 0.082 |
| $(N=1,926,714)$ | $[0.972]$ | $[0.809]$ | $[0.933]$ |  |
|  |  | 0.817 | 0.134 | 0.049 |
| D. Within Stores over Time |  | $[0.995]$ | $[0.969]$ | $[0.987]$ |
| $(N=7,746,218)$ |  |  |  |  |

Note: All standard errors are less than 0.001 . R-Squared values are reported in square brackets. Across Merchant and Across Store within Merchant decompositions are based on 2019 data. Within Merchants over Time and Within Stores over Time are based on 2016-2019 data. Within Merchants over Time regressions include merchant and year fixed effects. Across Stores within Merchants regressions include merchant fixed effects. Within store over Time regressions include store and year fixed effects. See Online Appendix B for robustness with respect to a longer panel of merchant/store data.

Figure 1: Decomposing Merchant Sales Growth by Industry


Note: This figure displays the coefficients of the "Within Merchant over time" decomposition by industry. The regressions are run with Visa data from 2016 through 2019, and include merchant and year fixed effects.
merchant or store. In particular, if households use a greater number of cards at merchants or stores with higher overall sales. For Visa credit cards from 2016 to 2019 we can match cards to households for about $50 \%$ of cards. these households average 1.7 Visa cards, but $91 \%$ of them transact with a given merchant in a given year using a single card. More to the point, when we do a version of Table 2 in Appendix Table B2 with cards vs. households, we find the customer margin falls by only one percentage point.

Non-linearities. Our linear regressions may hide important non-linearities. We explore this in Figure 2. We partition merchants into 20 bins in terms of their
sales (Figure 2a) or sales growth (Figure 2b), with an equal number of merchants in each bin, and plot their components vs. sales (or sales growth) on a log-log base 10 scale. The first bin is normalized to one for all variables.

In the cross section of merchants in 2019 (Figure 2a), the number of unique customers is even more important across larger merchants, with visits per customer and average transaction amount being less important across the largest merchants. When we look at sales variation over time within a merchant (Figure $2 b)$, after residualizing merchant and year fixed effects, the relationship look approximately linear.

Figure 2: Decomposing Merchant Sales

(a) across Merchants (b) within Merchants over time

Note: Panel (a) is based on a cross section of all merchants in 2019. In panel (a), we group the x-axis into 20 bins, and report averages by bin, normalizing each variable by its average for the first bin. Panel (b) repeats the same exercise, but for the panel of merchant-years over 2016-2019. For (b) we de-mean each variable by its merchant average and its year average, so the plot reflects fast vs. slow-growing merchants over time. Both panels are plotted on a log (base 10) scale.

Figure 3 further decomposes the number of unique customers into the number of stores and the number of unique cards per store, respectively. It shows
that, both in the cross section and over time, the number of stores is not an important source of sales variation for the bottom half (in terms of sales) of merchants, which may be natural as many smaller merchants only have a single store. For larger merchants stores become more important, in particular for the largest set of merchants (top ventile). This is similar to the role of establishments in firm size more generally, as documented by Moscarini and PostelVinay (2012) for example. That is, most variation in firm size comes from its employment per establishment, except for the largest firms which have many more establishments.

Figure 3: Stores vs. Cards Per Store


Note: Panel (a) is based on a cross section of all merchants in 2019. In panel (a), we group the xaxis into 20 bins, and report averages by bin, normalizing each variable by its average for the first bin. Panel (b) repeats the same exercise, but uses the panel of merchant-years from 2016-2019. For (b), we de-mean each variable by its merchant average and its year average. Both panels are plotted on a log (base 10) scale.

Figure 4 repeats this exercise at the store (rather than merchant) level, both for a cross section of stores in 2019 (Figure 4a) and within store over time (Figure 4b). The pattern is remarkably similar for stores and for merchants, except that at the store level the relationships are approximately linear throughout.

Figure 4: Decomposing Store Sales


Note: Panel (a) uses a cross section of stores in 2019 and de-means each store by its merchant average. We group the $x$-axis into 20 bins, and report averages by bin, normalizing each variable by its average for the first group. Panel (b) repeats the same exercise, but uses a panel of stores from 2016-2019, de-meaning each variable by its store average and its year average. All panels are plotted on (base 10) log scale.

Results by store age. In Online Appendix B we repeat this analysis for the much smaller set of large merchants who linked back to 2007 in the Visa data. The results look qualitatively similar, with the exception that the number of stores is much more important across large merchants and, to a lesser extent, over time within large merchants.

An advantage of a longer panel is that we can look at whether store dynamics differ by firm age. In Online Appendix B, we decompose the sources of store growth separately for stores in their first two years since entry, years 3-5, and stores that have been open for 6+ years. Customers remain the primary driver of revenue growth for all three age groups $(77 \%, 81 \%$, and $85 \%$, respectively), but new stores rely more than established stores on the average transaction amount to grow their sales ( $15 \%$ vs. $6 \%$, respectively).

Returning vs. newly acquired customers. One possible concern about the above analysis is that it confounds compositional effects. For example, we might be overstating the extensive margin if returning customers increase their spending a lot at growing stores, but average spending does not grow much because new customers spend less than returning customers. ${ }^{6}$

To address this concern, we regress the log change of spending per returning customer on the log change of total sales for merchant-years from 2016 to 2019 (adding year fixed effects). ${ }^{7}$ We report the coefficient for all retail (first bar) and separately by 3-digit NAICS in Figure 5. By this metric, returning customers account for $38 \%$ of the variance of sales growth in all NAICS. Their contribution ranges from $26 \%$ among clothing stores to almost $47 \%$ among food and beverage stores. This $38 \%$ is notably higher than the approximately $20 \%$ variation in sales that we attributed to the intensive margin earlier, when we did not adjust for composition. Still, we continue to find that the extensive margin accounts for most of sales growth variation (62\%) by this metric. In Online Appendix D we report similar results at the store level.

### 3.2. Customers and aggregate growth

Skewed individual contributions to aggregate retail growth. Having established the importance of the customer margin for growth at the merchant and store levels, we now explore how this translates to retail-wide aggregates. ${ }^{8}$

Let $S_{i t}$ denote merchant $i$ 's total sales in year $t$, and $\Delta S_{i t}=S_{i, t}-S_{i, t-1}$ be the change in merchant $i$ 's sales from year $t-1$ to year $t$. In each year $t$, we order

[^4]Figure 5: Spending per returning customer on firm sales growth


The figure reports the coefficient in the regression of annual log change of spending per returning customer on annual log change of total sales. An observation is a merchant-year level. The regression uses 2016-2019 data and includes a year fixed effect.
merchants by $\Delta S_{i t}$, and place them into groups, year by year, which account for the top or bottom $1 \%, 5 \%, 10 \%$, or $25 \%$ of merchants in terms of their sales change in that year. The top $1 \%$ saw the biggest increases in their sales, and the bottom $1 \%$ saw the biggest decreases in sales.

We next divide the total increases (or decreases) in each group by the sum of all increases (or decreases) across all merchants in the same year. This is analagous to breaking down the gross job creation and destruction rate as in Davis, Haltiwanger and Schuh (1998), only for the gross sales creation and destruction rates. That is, we trace how much of all sales creation and destruction, respectively, comes from the biggest increases and decreases.

Figure 6 plots the contribution of each group to aggregate sales increases or decreases, averaged across the three observations 2016-2017, 2017-2018, and 2018-2019. In a similar spirit to Decker et al. (2016), the figure illustrates that a small fraction of growing merchants is responsible for a large fraction of aggregate growth, and similarly a small number of shrinking merchants are re-
sponsible for a large fraction of the aggregate decline. The top $1 \%$ growers and shrinkers each contribute around $70 \%$ of aggregate sales increases and decreases, respectively. The top and bottom $5 \%$ contribute more than $80 \%$, the top and bottom $10 \%$ contribute about $90 \%$, and the top and bottom $25 \%$ contribute more than $99 \%$. The patterns appear to be fairly symmetric for growing and shrinking merchants. ${ }^{9}$

As we noted, in Figure 6 the grouping of firms is done year by year. This implies that the identity of tail firms is changing from year to year. How important are cumulative sales increases and decreases to the aggregate increases and decreases from 2016 to 2019? To find out we rank merchants based on their cumulative sales changes from 2016 to 2019. This includes entrants among the growers and exiting merchants among the shrinkers.

In Figure 7, we then show that tail firm contributions remain remarkably similar when looking at cumulative changes from 2016 to 2019. Evidently, many firms are growing and shrinking by large amounts over the three year period. This could reflect the short time horizon, but in Online Appendix B we document that the patterns are very similar when we use the longer (2007-2019) panel, which include a much smaller set of merchants.

[^5]Figure 6: Contribution to Aggregate Sales Changes


The figure reports the average contribution of each merchant group as defined in the text to aggregate sales change over year with the error bar extending one standard deviation up and down. An observation is a merchant-year and the figure uses a panel of merchants from 2016 to 2019. Each bar corresponds to a merchant group. TX refers to top X\% merchants and BX refers to the bottom X\% of merchants according to their absolute sales changes.

Figure 7: Persistence of Merchant Contributions


The figure reports the contribution of each firm group as defined in the text to aggregate sales change between 2016 and 2019. Each bar corresponds to a firm group. TX refers to top X\% firms and BX refers to bottom X\% firms by the absolute sales changes between 2016 and 2019.

Figure 8 reports the contributions of the top and bottom $1 \%$ of merchants for each 3-digit NAICS from 2016 to 2019. The importance of these tail merchants varies from around $40 \%$ in motor vehicles and parts to over $90 \%$ for general merchandise, but is mostly in the range of $50 \%$ to $80 \%$. Thus, this is a robust feature across retail NAICSs that extreme growers and shrinkers account for a large fraction of aggregate sales changes.

Figure 8: Contribution to Aggregate Sales Changes By NAICS


The figure reports the average contribution of top and bottom $1 \%$ merchants to within-NAICs aggregate sales change over year for each retail NAICs. An observation is a merchant-year and the figure uses a panel of merchants from 2016 to 2019. The calculation of each merchant group's contribution is described in the text.

The importance of customers for the tails. We now try to assess the extent to which the extensive margin of customers account for these tail patterns. To do so, we decompose merchant sales changes into two components: changes in the number of customers and changes in sales per customer. Let $N_{i t}$ denote the number of unique customers visiting merchant $i$ in year $t$ and $S_{i t} / N_{i t}$ denote the sales per customer for merchant $i$ in year $t$. Each merchant's sales changes
can be written as

$$
\Delta S_{i t} \equiv \Delta N_{i t} \cdot \overline{S / N}_{i t}+\Delta(S / N)_{i t} \cdot \bar{N}_{i t}
$$

where

$$
\bar{N}_{i t} \equiv \frac{N_{i t}+N_{i, t-1}}{2}
$$

and

$$
\overline{S / N}_{i t} \equiv \frac{S_{i t} / N_{i t}+S_{i, t-1} / N_{i, t-1}}{2}
$$

Using this decomposition, we can tell how much of the aggregate sales changes in each group are attributed to changes in the number of unique customers versus changes in sales per customers. Figure 9 shows that the change in customers accounts for around $80 \%$ of sales changes in the tails (modestly under $80 \%$ for increases, and modestly above $80 \%$ for decreases). Thus, the (now familiar) pattern prevails even we focus on the tails of the growth/decline distribution: customer growth accounts for most of the extremes we see in overall sales growth across merchants from year to year.

## 4. A model of growth with customer acquisition

Having shown that the customer margin is quantitatively important, we present a model of growth that incorporates this margin to see how it may matter.

### 4.1. Customers

Consider a unit mass of customers with identical preferences:

$$
U=\sum_{t=0}^{\infty} \beta^{t} \frac{C_{t}^{1-1 / \sigma}}{1-1 / \sigma}
$$

Figure 9: Customers vs. sales/customer and firm sales changes


The figure reports the average share of sales changes in each firm group that can be attributed to changes in number of customers and changes in sales per customer respectively from 2016 to 2019. By construction, the two shares sum to 1. Each bar corresponds to a firm group. TX refers to top X\% firms and BX refers to bottom X\% firms by firms' absolute sales changes.

Their composite consumption $C$ is a CES aggregate of varieties:

$$
C_{t}=\left(\int_{0}^{1} n_{i t}\left(q_{i t} c_{i t}\right)^{\frac{\theta-1}{\theta}} \mathbf{d} i\right)^{\frac{\theta}{\theta-1}}
$$

where $n_{i t} \in[0,1]$ is the probability that a customer purchases variety $i$ and $q_{i t}$ is the quality of variety $i . \theta>1$ is the elasticity of substitution between varieties and $0<\beta<1$ is the discount factor. Note there is a fixed unit measure of varieties. Finally, we assume that $n_{i t}$ is identical across consumers, so it is also the fraction of consumers who buy variety $i$ in period $t$. Demand (per customer) conditional on access to variety $i$ is given by:

$$
c_{i t}=\left(\frac{P_{t}}{p_{i t}}\right)^{\theta} q_{i t}^{\theta-1} C_{t}, \quad \forall i \in[0,1]
$$

where the ideal consumer price index is:

$$
P_{t} \equiv\left(\int_{0}^{1} n_{i t}\left(\frac{p_{i t}}{q_{i t}}\right)^{1-\theta} \mathrm{d} i\right)^{\frac{1}{1-\theta}} .
$$

Total quantity demanded for variety $i$, summed across customers, is:

$$
y_{i t}=n_{i t} c_{i t}
$$

### 4.2. Firms

Each firm uses production labor $l_{i t}$ to produce its single variety:

$$
y_{i t}=l_{i t} .
$$

It uses marketing labor $m_{i t}$ to reach a random fraction $n_{i t}$ of customers:

$$
n_{i t}=\left(\frac{\gamma m_{i t}}{\phi M_{t}^{\delta}}\right)^{\frac{1}{\gamma}} \quad \text { where } \quad M_{t} \equiv \int_{0}^{1} m_{i t} \mathbf{d} i
$$

Here $\gamma>1$ and $\phi>0$, and $M$ is aggregate marketing labor across all firms. ${ }^{10}$ We note the built-in negative externality with respect to other firms' marketing efforts. Choosing labor as the numéraire, the firm's static profit maximization problem is:

$$
\max _{p_{i t}, m_{i t}}\left(p_{i t}-1\right) y_{i t}-m_{i t} .
$$

Assuming that firms engage in monopolistic competition, they set their price to a constant markup above unit marginal cost:

$$
p_{i t}=\mu \quad \text { where } \quad \mu \equiv \frac{\theta}{\theta-1} .
$$

[^6]Substituting the firm's price in its demand function yields:

$$
c_{i t}=\left(\frac{q_{i t} P_{t}}{\mu}\right)^{\theta-1} \cdot \frac{P_{t} C_{t}}{\mu}
$$

The firm's static marketing problem becomes:

$$
\max _{n_{i t}} n_{i t}\left(\frac{q_{i t} P_{t}}{\mu}\right)^{\theta-1} \cdot \frac{P_{t} C_{t}}{\theta}-\frac{\phi M_{t}^{\delta} n_{i t}^{\gamma}}{\gamma} .
$$

This marketing problem yields the following first order condition:

$$
n_{i t}=\min \left\{\left(\frac{q_{i t} P_{t}}{\mu}\right)^{\theta-1} \cdot \frac{P_{t} C_{t}}{\theta \phi M_{t}^{\delta}}, 1\right\}^{\frac{1}{\gamma-1}}
$$

Denoting $\Gamma \equiv \frac{\gamma}{\gamma-1}$, it follows that a firm's flow profits are:

$$
\pi_{i t}=\left[\left(\frac{q_{i t} P_{t}}{\mu}\right)^{\theta-1} \cdot \frac{P_{t} C_{t}}{\theta \phi M_{t}^{\delta}}\right]^{\Gamma} \cdot \frac{\phi M_{t}^{\delta}}{\Gamma} .
$$

It is useful to define an aggregate quality index as:

$$
Q_{t} \equiv\left(\int_{0}^{1} q_{i t}^{\Gamma(\theta-1)} \mathbf{d} i\right)^{\frac{1}{\Gamma(\theta-1)}}
$$

Defining a firm's relative quality as $z_{i t}=q_{i t} / Q_{t}$, we can use the market clearing conditions for the final good and labor to solve for profits as a function of aggregate production labor:

$$
\pi_{i t}=\frac{L_{t} z_{i t}^{\Gamma(\theta-1)}}{\Gamma(\theta-1)}
$$

### 4.3. Innovation

A firm with absolute quality $q_{i t}$ and relative quality $z_{i t}$ that hires research labor $s_{i t}$ sees its quality follow a controlled binomial process with probability $x_{i t} \in[0,1]$ :

$$
q_{i t+1}=\left\{\begin{array}{ll}
q_{i t} e^{\Delta} & \text { w/ prob. } x_{i t} \\
q_{i t} & \text { w/ prob. } 1-x_{i t}
\end{array} \quad \text { and } \quad s_{i t}=\lambda \log \left(\frac{1}{1-x_{i t}}\right) z_{i t}^{\zeta}\right.
$$

Here $\Delta, \lambda$ and $\zeta$ are all strictly positive. $\Delta$ is the step size of successful quality innovations, and $x_{i t}$ is the probability that a firm succeeds in innovating. $\lambda$ is a scalar for the level of research labor and $\zeta$ quantifies how much more research labor is necessary to innovate from a higher level of relative quality. Note the knowledge spillover in this formulation: the higher the quality of other firms, the lower the cost of successfully innovating $(\zeta>0)$. A firm's value function is given by:

$$
V_{t}(z)=\pi_{t}(z)+\max _{x \in[0,1]}\left\{R_{t}^{-1}\left[x V_{t+1}\left(z e^{\Delta-g_{t}}\right)+(1-x) V_{t+1}\left(z e^{-g_{t}}\right)\right]-s_{t}(z, x)\right\}
$$

where $R$ is the gross interest rate. The Euler equation produces the usual relationship between the growth rate $g$ (here of the aggregate quality index) and the consumer's discount factor in the absence of aggregate uncertainty:

$$
\left(1+g_{t}\right)^{1 / \sigma}=\beta R_{t} .
$$

The first-order condition of the firm's dynamic problem implies:

$$
x_{t}(z)=1-\frac{\lambda z^{\zeta} R_{t}}{v_{t}\left(z e^{\Delta-g}\right)+v_{t}\left(z e^{-g}\right)} .
$$

### 4.4. Labor market clearing

To recap, labor is used for production, marketing, and research:

$$
\begin{aligned}
L_{t} & =\int l_{t}(z) \mathrm{d} F_{t}(z) \\
M_{t} & =\int m_{t}(z) \mathrm{d} F_{t}(z) \\
S_{t} & =\int s_{t}(z) \mathrm{d} F_{t}(z)
\end{aligned}
$$

As each of the unit mass of consumers is endowed with one unit of labor that they supply inelastically, the labor market clearing condition is simply:

$$
L_{t}+M_{t}+S_{t}=1
$$

Solving for aggregate production and marketing labor yields:

$$
L_{t}=\frac{\gamma(\theta-1)\left(1-S_{t}\right)}{\gamma(\theta-1)+1} \quad \text { and } \quad M_{t}=\frac{L_{t}}{\gamma(\theta-1)} .
$$

### 4.5. Calibration

In Table 3 we set our baseline parameter values. A period in the model is one year. We set the intertemporal elasticity of substitution $\sigma=0.5$. We choose an elasticity of substitution between varieties of 3. This is at the lower end of estimates such as in Hottman et al. (2016), but this and other papers typically do not control for the customer margin. We set the discount factor to 0.992 so that, when the baseline growth rate is set to $2.9 \%$ per year, the steady state real interest rate is $6.7 \%$ per year. We also set the aggregate labor endowment to one. ${ }^{11}$

We set the level of marketing costs $\phi$ so that the firm with maximum relative quality reaches half of the customers. We set the elasticity of marketing labor with respect to customers to $\gamma=1.25$. The elasticity of sales with respect to

[^7]quality in the model is the sum of the elasticity of customers and elasticity of spending per customer with respect to quality:
$$
\xi_{y, q}=\xi_{n, q}+\xi_{c, q}=\frac{\theta-1}{\gamma-1}+\theta-1
$$

With $\gamma=1.25$ and $\theta=3$, the customer share of the sales elasticity is $80 \%$, which matches our finding in Section 3.

We choose an innovation step size of $6 \%$. With $\theta=3, \gamma=1.25$, and $\Delta=0.06$, sales grow by $29 \%$ for expanding firms and shrink by $29 \%$ for contracting firms:

Sales growth $=g \cdot \xi_{y, q}$.

We choose the innovation cost parameters to achieve a $2.9 \%$ growth rate and for the top $1 \%$ fastest growing firms to account for $70 \%$ of sales changes.

Table 3: Parameter Values

| Symbol | Parameter | Value |
| :---: | :--- | :---: |
| $\sigma$ | Intertemporal elasticity of substitution | 0.50 |
| $\theta$ | Elasticity of substitution between varieties | 3.00 |
| $\beta$ | Discount factor | 0.992 |
| $\phi$ | Scale of marketing costs | $3.57 \cdot 10^{37}$ |
| $\gamma$ | Elasticity of marketing costs wrt customers | 1.25 |
| $\Delta$ | Quality step size | 0.06 |
| $\lambda$ | Linear research cost | 0.094 |
| $\zeta$ | Research spillover parameter | 10.04 |
| $\delta$ | Marketing externality | 1.0 |

### 4.6. Results

We are now ready to characterize equilibrium outcomes. For contrast, we also show what happens in an economy with no customer margin. We achieve this by setting $\gamma=\infty$ and $\Gamma=1$, so that labor is not needed to access customers. We keep all other parameter values the same when we make this comparison. ${ }^{12}$

Figure E3 shows how $n$, the fraction of consumers the firm sells to, varies with the firm's relative quality $z$. It is log-linear with elasticity $\gamma /(\gamma-1)$ in the Baseline. This in turn makes the value of the firm much more convex with respect to $z$ in the Baseline than in the No Customers case - see the log-log scale in Figure E8.

Because the customer margin makes variable profits increase much faster in relative quality, it induces higher quality firms to do more innovation than they would otherwise do. This can be seen in Figure 10a. A corollary is that R\&D intensity (research spending as a share of sales) is slowly decreasing with respect to $z$ in the baseline case, whereas it falls quickly with $z$ in the model without a customer margin. As a result, the stationary distribution of relative qualities is much more dispersed with customer variation than without it (Figure E7). ${ }^{13}$

The distribution of sales ends up being much more dispersed with an extensive margin for customers in Figure E5. Higher quality firms have more customers, and this endogenously induces more quality dispersion.

[^8]
## Figure 10: Innovation



Note: This figure shows how the arrival rate of innovations $x$ varies with the firm's relative quality $z$. The Baseline features $\gamma=1.25$ and the "No customers" version uses $\gamma=\infty$, where $\gamma$ is the elasticity of marketing costs with respect to customers.

In Table 4 we compare some variables in steady state across the Baseline and No Customer cases. The endogenous growth rate of aggregate quality rises modestly from $2.9 \%$ in the baseline to $3.2 \%$ in the model without a customer margin. This is despite $27 \%$ of all labor being freed up from doing marketing when going from the Baseline to the model with no extensive margin for customers. Production labor does soar from $68 \%$ of all labor in the Baseline to $93 \%$ with no customer margin. But there is still room for research labor to rise from $4.9 \%$ in the baseline to $6.7 \%$ of all labor in the model with no extensive margin for customers.

Table 5 shows the importance of the covariance between sales changes and quality growth to aggregate growth. We calculate a Törnqvist approximation to the true growth rate, which is the weighted average of quality growth rates across firms. The Törnqvist weights are the firm's average sales share across the two years. The Table indicates that the Törnqvist second-order approximation is quite good. If we instead use initial sales shares as weights (a 1st order approximation), the approximated growth rate understates the true growth rate by about 50 basis points in the case with a customer margin. With no customers, in contrast, the second order term is much smaller. This breakdown illustrates the importance of customer acquisition in amplifying the growth contribution of the right tail of firm growers.

Just like in the data, we can calculate the contribution of the top $1 \%$ of firms (based on their sales increases) to aggregate sales increases. As depicted in Figure 11, our baseline model is calibrated to achieve a contribution of $70 \%$ from the top $1 \%$. Without a customer margin, in contrast, the top $1 \%$ of firms would account for less than $1 \%$ of all sales increases. Again, this comes from both the direct effect of acquiring customers in response to rising $z$, and the indirect effect of a much narrower $z$ distribution in the absence of a customer margin. In this economy, the growth contribution of top firms is the same as their contribution to aggregate sales increases. Therefore, the top $1 \%$ fastest growing firms also account for $70 \%$ of consumption growth.

Table 4: Steady-state endogenous variables

| Symbol | Variable | Baseline | No customers | No customers <br> (scaled) |
| :---: | :--- | :---: | :---: | :---: |
| $g$ | Growth rate | $2.90 \%$ | $3.22 \%$ | $2.65 \%$ |
| $r$ | Interest rate | $6.70 \%$ | $7.36 \%$ | $6.19 \%$ |
| $L$ | Production labor | $67.9 \%$ | $93.3 \%$ | $93.2 \%$ |
| $M$ | Marketing labor | $27.2 \%$ | $0.0 \%$ | $0.0 \%$ |
| $S$ | Research labor | $4.9 \%$ | $6.7 \%$ | $6.8 \%$ |

Note: The scaled economy without customers has a total labor endowment of 0.728 instead of 1 .

Table 5: Törnqvist growth decomposition

|  | Baseline | No customers | No customers <br> (scaled) |
| :--- | :---: | :---: | :---: |
| True growth rate | $2.90 \%$ | $3.22 \%$ | $2.65 \%$ |
| Approximated growth rate | $2.95 \%$ | $3.26 \%$ | $2.70 \%$ |
| 1st order term | $2.49 \%$ | $3.17 \%$ | $2.61 \%$ |
| 2nd order term | $0.46 \%$ | $0.09 \%$ | $0.09 \%$ |

Note: The scaled economy without customers has a total labor endowment of 0.728 instead of 1.

Figure 11: Firm Contributions to Aggregate Sales Changes


## 5. Conclusion

Using Visa data on credit and debit card transactions at U.S. retail merchants from 2016 to 2019, we document the paramount importance of the extensive, customer relationship margin in driving variation in retail sales. Customers account for approximately $80 \%$ of the sales variation whether we look across merchants, across stores within merchants, or over time within merchants and stores.

We write down a simple growth model that incorporates the extensive margin and illustrates how and why the customer margin may matter for growth. In the model, firms pay marketing and research costs to acquire customers and improve their quality. The customer margin makes large firms drastically more important for sales and overall growth. The ability to increase profits by adding customers increases the returns to innovation and stimulates research, but marketing diverts resources away from research. The latter force dominates so that growth is modestly lower in the model with a customer margin than if all firms could access all customers.

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[^0]:    *Einav, Klenow, and Levin: Stanford University and NBER; Murciano-Goroff: Boston University. Conclusions expressed herein are those of the authors and do not necessarily represent the views of Visa, Inc. We are grateful to Sam Kortum and Sara Moreira for helpful discussions, and to Jean-Felix Brouillette, Yue Cao, and Mariana Guido for excellent research assistance.

[^1]:    ${ }^{1}$ The sample is anonymized. Neither the name, address, nor any personal information about the cardholder is observable, other than what can be inferred given a card's transaction history.
    ${ }^{2}$ Visa (2019)'s 2019 10-K filing reports $\$ 3.242$ trillion in nominal payments volume for consumer credit and debit. This is $24.4 \%$ of BEA nominal consumption in 2019 of $\$ 13.280$ trillion.
    ${ }^{3}$ Consistent with wide spending coverage, in Yelp data for seven mid-sized cities (Pittsburgh, Charlotte, Urbana-Champaign, Phoenix, Las Vegas, Madison, and Cleveland) in 2017, three quarters of the outlets who reported payment information and $93 \%$ of tem indicated that they accepted credit cards (https://www.yelp.com/dataset).

[^2]:    ${ }^{4}$ https://WalletHub.com/edu/market-share-by-credit-card-network/25531.

[^3]:    ${ }^{5}$ Appendix Table A2 provides these statistics for each year separately.

[^4]:    ${ }^{6}$ In the case of Pareto distribution of spending across customers, one might see the entry of new customers exactly offset the growing spending of returning customers.
    ${ }^{7}$ Unlike the earlier decomposition analysis, this is not a precise decomposition because due to turnover of cards - tracking returning vs. new customers requires us to limit attention to the subset of cards that are active over two consecutive years.
    ${ }^{8}$ Since the volume of transactions on the Visa network has been steadily increasing over time, throughout this section we measure both aggregate and merchant sales in 2012 CPI dollars and re-scale each of them by Visa's share of the debit and credit card market by dollar volume in the corresponding year (obtained from https://wallethub.com/edu/cc/market-share-by-credit-card-network/25531). As mentioned in Section 2, in this part of the analysis we also excluded gasoline sales.

[^5]:    ${ }^{9}$ In Figure B10 in the Appendix we should the share of initial sales at the top growers and shrinkers. It is notably smaller than their share of changes, for example only $45 \%$ of sales on average are at the top $1 \%$ of growing firms.

[^6]:    ${ }^{10}$ With $\gamma \rightarrow \infty$, we obtain the corresponding economy with no customer margin. One can see this by inverting the marketing labor function and taking its limit as $\gamma$ goes to infinity. For $n_{i t} \leq 1$, marketing labor marketing labor goes to zero.

[^7]:    ${ }^{11}$ The model features strong scale effects, but is invariant to the scale of the economy once re-calibrated to match the targeted moments.

[^8]:    ${ }^{12}$ With no customer margin, the elasticity of sales with respect to quality would be only $\xi_{y, q}=$ $\xi_{c, q}=\theta-1$. To achieve relative sales growth of $40 \%$ in a model without customers, relative quality would need to grow by $20 \%$ rather than by $4 \%$ as in the customer economy.
    ${ }^{13}$ Note that in both models, the probability of successfully innovating is equal to one for the smallest firms and zero for the largest ones, which delivers a stationary distribution of relative quality.

