

# When Does Procompetitive Entry Imply Excessive Entry?

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## Introduction

- **Dixit-Stiglitz Monopolistic Competition under CES**, widely used as a building block in applied GE
- **Two remarkable (but knife-edge) features:**
  - **Markup Rate Invariance**, particularly with respect to market size of the sector
  - **Optimality of Free-Entry Equilibrium**, efficient resource allocation within an MC sector.  
(Intersectoral allocation is generally inefficient even if all sectors are CES.)
- Departure from CES could make equilibrium entry to the sector *either*
  - **Pro- or Anti-competitive**: Market expansion → more product varieties → markup rate **down or up**
  - **Excessive or Insufficient**: too many varieties produced too little *or* too few varieties produced too much
- What do we know about
  - The condition for pro- vs. anti-competitive entry?
  - The condition for excessive vs. insufficient entry?
  - The relation between the two conditions?
- **Generally, all  $2 \times 2 = 4$  combinations are possible.**
  - Comparative static questions like “pro- vs. anti-competitive” hinge on the *local* property of the demand system
  - Welfare questions like “excessive vs. insufficient” hinge on the *global* property

But, there are some close connections between the two conditions.

- **Two Sources of Externalities in Entry** (Introduction of a new product variety)
  - **Negative externalities (business stealing)**, entry reduces the profit of other firms → excessive entry
  - **Positive externalities (imperfect appropriability)**, entrants do not fully capture social surplus created → insufficient entry

CES: *one* of the demand systems under which the two sources of externalities exactly cancel out at any market size.

- Starting from the knife-edge CES benchmark, introducing
  - **Procompetitive effect** *amplifies* negative externalities (business stealing), tips the balance for **excessive entry**
  - **Anticompetitive effect** *mitigates* negative externalities (business stealing), tips the balance for **insufficient entry**

Only *suggestive*, because positive externalities (imperfect appropriability) may also be affected.

- That is why we ask: *When (i.e., under what additional restrictions)*
  - Is procompetitive entry excessive?
  - Is anticompetitive entry insufficient?

### Three Classes of Homothetic Demand Systems: Matsuyama-Ushchev (2017)

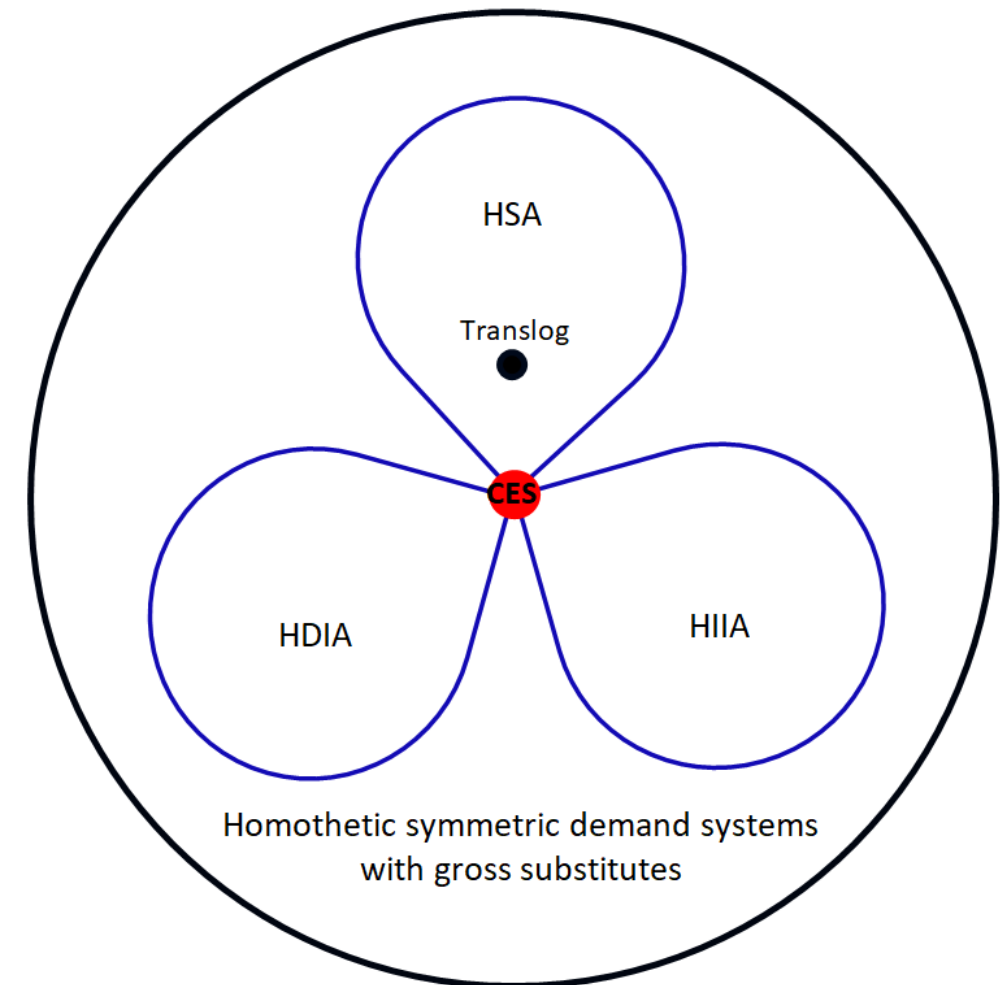
- **H.S.A.** (Homotheticity with a Single Aggregator)
- **HDIA** (Homotheticity with Direct Implicit Additivity)
- **HIIA** (Homotheticity with Indirect Implicit Additivity)

which are pairwise disjoint with the sole exception of CES.

Here, we apply these 3 classes to **the Dixit Stiglitz environment** by imposing

- **Symmetry**
- **Gross Substitutability**

across a **continuum** of product varieties.



## The Dixit-Stiglitz Environment: A General Case

A Sector consists of

- **Monopolistic competitive firms:** produce a continuum of differentiated *intermediate inputs varieties*,  $\omega \in \Omega$ 
  - Fixed cost of entry,  $F$
  - Constant marginal cost,  $\psi$

*We can also allow multi-product MC firms, as long as they do not produce a positive measure of products.*

- **Competitive firms:** produce a single good by assembling intermediate inputs, using **CRS technology**

**CRS Production Function:**

$$X = X(\mathbf{x}) \equiv \min_{\mathbf{p}} \left\{ \mathbf{p}\mathbf{x} = \int_{\Omega} p_{\omega} x_{\omega} d\omega \mid P(\mathbf{p}) \geq 1 \right\}$$

**Unit Cost Function:**

$$P = P(\mathbf{p}) \equiv \min_{\mathbf{x}} \left\{ \mathbf{p}\mathbf{x} = \int_{\Omega} p_{\omega} x_{\omega} d\omega \mid X(\mathbf{x}) \geq 1 \right\}$$

**Duality Principle:** Either  $X = X(\mathbf{x})$  or  $P = P(\mathbf{p})$  can be used as a primitive of the CRS technology, as long as linear homogeneity, monotonicity and quasi-concavity are satisfied.

**Demand Curve for  $\omega$** 

$$x_{\omega} = X(\mathbf{x}) \frac{\partial P(\mathbf{p})}{\partial p_{\omega}}$$

**Inverse Demand Curve for  $\omega$** 

$$p_{\omega} = P(\mathbf{p}) \frac{\partial X(\mathbf{x})}{\partial x_{\omega}}$$

**Market Size of the Sector**  
*taken as exogenous*

$$\mathbf{p}\mathbf{x} = \int_{\Omega} p_{\omega} x_{\omega} d\omega = P(\mathbf{p})X(\mathbf{x})$$

**Revenue Share of  $\omega$** 

$$s_{\omega} = \frac{p_{\omega} x_{\omega}}{\mathbf{p}\mathbf{x}} = \frac{p_{\omega} x_{\omega}}{P(\mathbf{p})X(\mathbf{x})}$$

$$s_{\omega}(p_{\omega}, \mathbf{p}) = \frac{\partial \ln P(\mathbf{p})}{\partial \ln p_{\omega}}; \quad s_{\omega}(x_{\omega}, \mathbf{x}) = \frac{\partial \ln X(\mathbf{x})}{\partial \ln x_{\omega}}$$

**Price Elasticity of  $\omega$ :**

$$\zeta_{\omega} = - \frac{\partial \ln x_{\omega}}{\partial \ln p_{\omega}}$$

$$\zeta_{\omega}(p_{\omega}, \mathbf{p}) = 1 - \frac{\partial \ln \left( \frac{\partial \ln P(\mathbf{p})}{\partial \ln p_{\omega}} \right)}{\partial \ln p_{\omega}}; \quad \zeta_{\omega}(x_{\omega}, \mathbf{x}) = \left[ 1 - \frac{\partial \ln \left( \frac{\partial \ln X(\mathbf{x})}{\partial \ln x_{\omega}} \right)}{\partial \ln x_{\omega}} \right]^{-1}$$

Under general CRS, little restrictions on  $\zeta_{\omega}$  beyond the homogeneity of degree zero in  $(p_{\omega}, \mathbf{p})$  or in  $(x_{\omega}, \mathbf{x})$ .  
Under CES,  $\zeta_{\omega}$  is constant, independent of  $(p_{\omega}, \mathbf{p})$  and of  $(x_{\omega}, \mathbf{x})$ .

**(Symmetric) H.S.A., HDIA, and HIIA: Definitions & Key Properties**

	$P(\mathbf{p})$ or $X(\mathbf{x})$	Revenue Share: $s_\omega$	Price Elasticity: $\zeta_\omega$	For CES
<b>H.S.A.</b> in two equivalent representations	$\frac{P(\mathbf{p})}{cA(\mathbf{p})} = \exp \left[ - \int_{\Omega} \left[ \int_{p_\omega/A(\mathbf{p})}^{\bar{z}} \frac{s(\xi)}{\xi} d\xi \right] d\omega \right]$	$s \left( \frac{p_\omega}{A(\mathbf{p})} \right)$ with $\int_{\Omega} s \left( \frac{p_\omega}{A(\mathbf{p})} \right) d\omega \equiv 1$	$\zeta \left( \frac{p_\omega}{A(\mathbf{p})} \right) \equiv 1 - \frac{zs'(z)}{s(z)} \Big _{z=\frac{p_\omega}{A(\mathbf{p})}} > 1$	$\frac{P(\mathbf{p})}{A(\mathbf{p})} = \frac{A^*(\mathbf{x})}{X(\mathbf{x})} = \text{const.}$ $\Leftrightarrow s(\cdot)$ or $s^*(\cdot)$ is a power function.
	$\frac{X(\mathbf{x})}{cA^*(\mathbf{x})} = \exp \left[ \int_{\Omega} \left[ \int_0^{x_\omega/A^*(\mathbf{x})} \frac{s^*(\xi)}{\xi} d\xi \right] d\omega \right]$	$s^* \left( \frac{x_\omega}{A^*(\mathbf{x})} \right)$ with $\int_{\Omega} s^* \left( \frac{x_\omega}{A^*(\mathbf{x})} \right) d\omega = 1$	$\zeta^* \left( \frac{x_\omega}{A^*(\mathbf{x})} \right) \equiv \left[ 1 - \frac{ys^{*'}(y)}{s^*(y)} \Big _{y=\frac{x_\omega}{A^*(\mathbf{x})}} \right]^{-1} > 1$	
<b>HDIA</b> Kimball	$\int_{\Omega} \phi \left( \frac{x_\omega}{X(\mathbf{x})} \right) d\omega \equiv 1$	$\frac{x_\omega}{C^*(\mathbf{x})} \phi' \left( \frac{x_\omega}{X(\mathbf{x})} \right)$ with $C^*(\mathbf{x}) \equiv \int_{\Omega} x_\omega \phi' \left( \frac{x_\omega}{X(\mathbf{x})} \right) d\omega$	$\zeta^D \left( \frac{x_\omega}{X(\mathbf{x})} \right) \equiv - \frac{\phi'(y)}{y\phi''(y)} \Big _{y=\frac{x_\omega}{X(\mathbf{x})}} > 1$	$\frac{C^*(\mathbf{x})}{X(\mathbf{x})} = \text{const.}$ $\Leftrightarrow \phi(\cdot)$ is a power function.
<b>HIIA</b>	$\int_{\Omega} \theta \left( \frac{p_\omega}{P(\mathbf{p})} \right) d\omega \equiv 1$	$\frac{p_\omega}{C(\mathbf{p})} \theta' \left( \frac{p_\omega}{P(\mathbf{p})} \right)$ with $C(\mathbf{p}) \equiv \int_{\Omega} p_\omega \theta' \left( \frac{p_\omega}{P(\mathbf{p})} \right) d\omega$	$\zeta^I \left( \frac{p_\omega}{P(\mathbf{p})} \right) \equiv - \frac{z\theta''(z)}{\theta'(z)} \Big _{z=\frac{p_\omega}{P(\mathbf{p})}} > 1$	$\frac{C(\mathbf{p})}{P(\mathbf{p})} = \text{const.}$ $\Leftrightarrow \theta(\cdot)$ is a power function.

with some additional restrictions on  $s(\cdot)$  or  $s^*(\cdot)$ ,  $\phi(\cdot)$ ,  $\theta(\cdot)$  for

- the integrability (i.e., monotonicity and quasi-concavity) of  $P(\mathbf{p})$  or  $X(\mathbf{x})$
- the gross substitutability to ensure the existence of the free-entry equilibrium.
- The uniqueness of the free-entry equilibrium

## Appealing Features of These Three Classes

### Homothetic:

- Without homotheticity, we would need to worry about the composition of market size.
- To *isolate* the efficiency effect of the markup rate response to market size, we need to avoid introducing the scale effect of market size due to nonhomotheticity
- can be given a cardinal interpretation, and hence useful for a *building block* in a *multi-sector* setting

### Nonparametric: To avoid functional form restrictions.

But we have many parametric examples to illustrate our results in the paper.

### Sufficient-statistic property; tractable, because entry and pricing behavior of other firms affect

- Revenue share only through a **single aggregator** under H.S.A; and **two aggregators** under HDIA & HIIA
- Price elasticity only through **a single aggregator under all three classes**
  - A single aggregator captures the effect of competition on the markup rate.
  - Comparative statics results dictated by the derivative of the price elasticity function

which help to find

- The conditions that guarantee the *existence* and *uniqueness* of free-entry equilibrium for any given market size
- The condition for **procompetitive vs. anticompetitive**
- The condition for **excessive vs. insufficient**
- the relation between the last two conditions

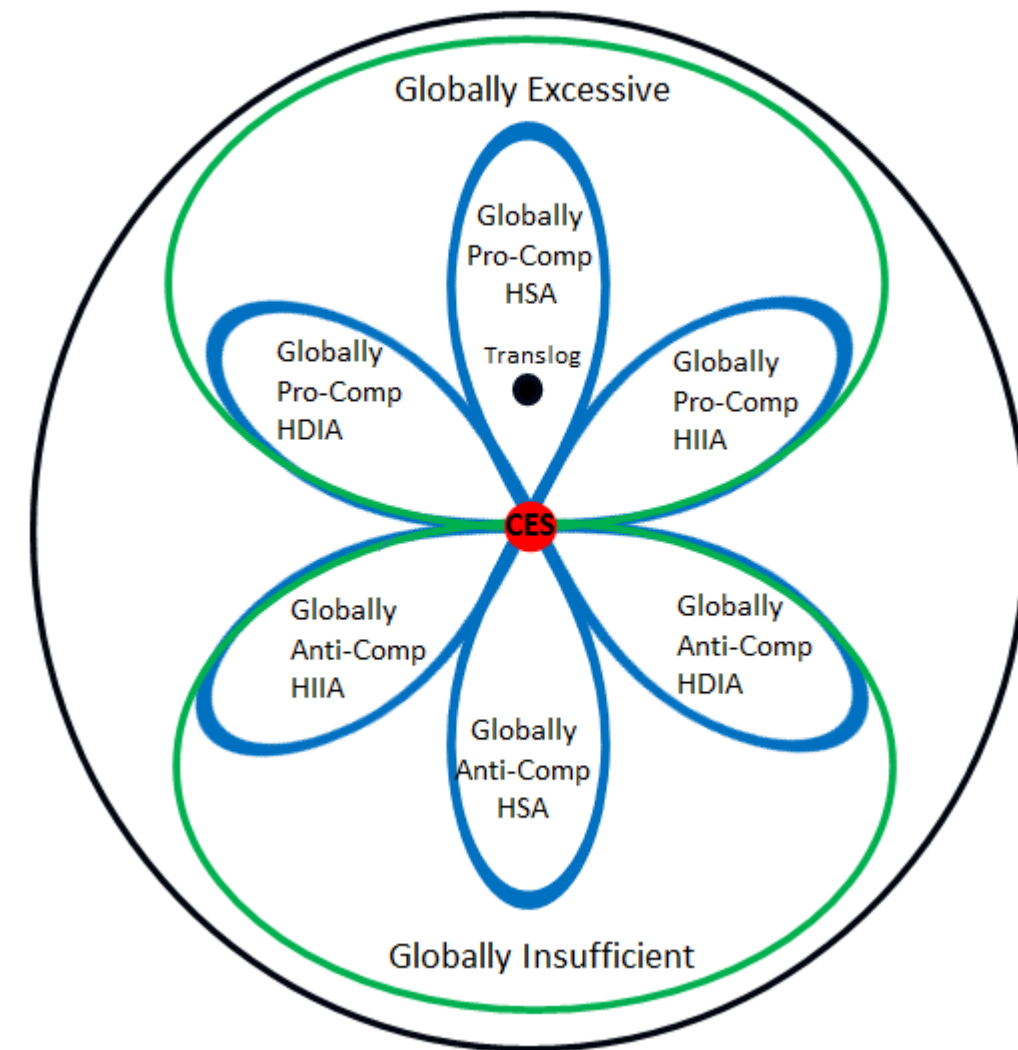


**Main Results:** In each of these three classes,

- CES *uniquely* ensures the optimality of free entry equilibrium.
- Procompetitive Entry  $\Leftrightarrow$  Strategic complementarity  $\Leftrightarrow$  Marshall's 2<sup>nd</sup> Law (Incomplete Pass-Through)  
*These equivalences do not hold in general, including many commonly used non-CES demand systems!!*
- Two *sufficient* conditions
  - Entry is *globally* excessive (insufficient) if *globally* pro-competitive (anti-competitive); see Figure.
  - Entry is procompetitive & excessive for a *sufficiently large market size in the presence of the choke price*.

*Cautionary Notes on interpreting these results*

- We model a MC sector as a *building block in a multi-sector model*
  - We do *not* assume that an economy has only one MC sector.
  - The MC sector we model may coexist with other sectors, which may not have to be MC.
  - We study distortion of *intra-sectoral* allocation *conditional* on the size of the sector.
  - In a multisector setting, *inter-sectoral* allocation is generally distorted even if all sectors are MC under CES.
- Excessive entry result may not justify an entry restriction, *in the presence of other sources of distortions*.



## One Frequently Asked Question

*What are the relative advantages of the three classes for applications?*

We believe that H.S.A. has advantages over HDIA and HIIA, because

- **the revenue share function,  $s(\cdot)$ , is the primitive of H.S.A.** and hence it can be readily identified by typical firm level data, which has revenues but not output. Kasahara-Sugita (2020)
- **With free-entry**, easier to ensure the existence and uniqueness of equilibrium, to characterize the equilibrium and to conduct comparative statics under H.S.A., because
  - For H.S.A., the interaction across products operates through **only one aggregator** in each sector.
    - An easy characterization of the free-entry equilibrium, as it minimizes  $A(\mathbf{p})$ , not  $P(\mathbf{p})$
  - For HDIA and HIIA, the interaction across products operates through **two aggregators** in each sector, creating more room for the *multiplicity* and *non-existence* of equilibrium.

## Related Literature

**Excessive entry in *homogeneous* good oligopoly:** Mankiw-Whinston (1986), Suzumura-Kiyono (1987)

**Macro Misallocation,** starting with Hsieh-Klenow (2009)

**MC under non-CES:** Thisse-Ushchev (2018) for a survey

- Parenti-Thisse-Ushchev (2017) studied the uniqueness, symmetry, and the “pro- vs. anti-competitive” under **general symmetric demand** *but only under the conditions given in reduced form, not in the primitives.*
- **MC under *nonhomothetic* non-CES**, *Blue compare the equilibrium and optimum.*
  - DEA:  $U = \int_{\Omega} u(x_{\omega})d\omega$ . Dixit-Stiglitz (1977), Zhelobodko et.al.(2012), Mrazova-Neary(2017), Dhingra-Morrow (2019), Behrens et.al.(2020). Under DEA, markup rate unaffected by market expansion through higher spending
  - Linear Quadratic: Ottaviano-Tabuchi-Thisse(2002), Melitz-Ottaviano(2008), Nocco et.al. (2014). Under LQ, markup rate goes up (down) due to market expansion through higher spending (more consumers).
- **MC under *homothetic* non-CES** *None compare the equilibrium and the optimum.*
  - Feenstra (2003)’s **translog**, a special case of H.S.A.
    - Functional form implies procompetitive entry and choke price.
    - Our analysis suggests excessive entry.
  - Kimball (1995) uses HDIA with **an exogenous set of firms** (no entry), Baqaee-Farhi (2020) introduces entry.
    - Under the popular functional form used in calibration study, non-existence of equilibrium under free entry
    - We identify the conditions for the existence & uniqueness of free-entry equil. for each of the 3 classes.
  - Bucci-Ushchev (2021) uses general **homothetic**, *again under the conditions given in reduced form.*

**This is a part of our big project!!**

**Matsuyama-Ushchev (2017)** “*Beyond CES: Three Alternative Classes of Flexible Homothetic Demand Systems*”

Propose **the same 3 classes** *more broadly*, which allow us to introduce **Asymmetric Demand Across Sectors** with

- a mixture of gross complements and gross substitutes
- a mixture of essential and inessential sectors, etc.

**Matsuyama-Ushchev (2020)** “*Constant Pass-Through*”

Propose and characterize **parametric families** within each of **the same 3 classes**

- with **firm heterogeneity** in *many* dimensions (market size, quality, substitutability, productivity, pass-through rate)
- MC firms operating at lower markup (not necessarily smaller firms) suffer more from tougher competition

**Matsuyama-Ushchev (2020)** “*Destabilizing Effects of Market Size in the Dynamics of Innovation*”

Replace CES with **H.S.A.** in a **dynamic** MC model of innovation cycles and show, under the procompetitive effect

- Under the procompetitive effect, large market size makes *the dynamics of innovation more volatile*

**Matsuyama-Ushchev (coming soon!)** “*Procompetitive Effect and Selection and Sorting of Heterogenous Firms*”

Replace CES with **H.S.A.** to introduce the procompetitive effect in a MC model with **Melitz-heterogeneity**

- Large market size leads to more selection of more productive firms in a closed economy
- More productive firms self-select to larger regions in a spatial model.

In the last two, we use H.S.A. not HDIA or HIIA, for the ease for ensuring the existence & the uniqueness of equilibrium.

## Summing Up:

### Dixit-Stiglitz under 3 classes of nonparametric homothetic demand systems

**H.S.A.** (Homotheticity with a Single Aggregator)

**HDIA** (Homotheticity with Direct Implicit Additivity)

**HIIA** (Homotheticity with Indirect Implicit Additivity)

- mutually exclusive except CES.
- **Sufficient-statistic property:** entry and behavior of other firms affect
  - revenue and profit of each firm only through one aggregator (for H.S.A.) or two aggregators (for HDIA and HIIA)
  - its price elasticity only through a single aggregator (for all three classes)
- flexibility and tractability allow us to identify the conditions for
  - the existence of the unique symmetric free entry equilibrium
  - the non-existence for an asymmetric free-entry equilibrium
  - procompetitive vs. anticompetitive
  - excessive vs. insufficient entry
 as well as the relation between the last two conditions

- Main findings: In these three classes
  - Optimal if and only if CES, **generally not true!!**
  - Procompetitive entry  $\Leftrightarrow$  Strategic complementarity  $\Leftrightarrow$  Marshall's 2<sup>nd</sup> Law (Incomplete pass-through).  
**generally not true!!**
  - Entry is *always* excessive (insufficient) if it is *globally* procompetitive (anticompetitive)
  - Entry is procompetitive and excessive for a large market size in the presence of the choke price