

# Bank Heterogeneity and Financial Stability

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# Motivation

## **Financial system is densely interconnected**

- ▶ Technologies: securitization, interbank trading, syndicated loans...
- ▶ Problem: common risk exposures and systemic risk

## **Our focus: Bank runs in the interconnected financial system**

- ▶ The literature mostly studies individual banks' fragility...
- ▶ ...or abstracts from fragility and focuses on interconnections

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- ▶ ...or abstracts from fragility and focuses on interconnections
- ▶ Our model emphasizes how cross-bank interactions amplify individual fragilities in a homogeneous financial system

# Preview

## Setting: Banking sector with fire-sale externalities

- ▶ Within-bank strategic complementarity a-la Diamond and Dybvig (1983)
- ▶ Cross-bank strategic complementarity due to fire sales
- ▶ *Two complementarities are mutually reinforcing*
  - ▶ When prices are low, depositors are more sensitive to runs within their banks

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- ▶ Asset portfolios are less correlated  $\Rightarrow$  weaker complementarity amplification
- ▶ Increasing heterogeneity (to a certain extent) is Pareto improving
  - ▶ Policy debate: individual insolvencies vs systemic risk (Haldane, 2009)
  - ▶ Existing theory: optimal heterogeneity depends on the size of the shocks (e.g. Acemoglu et al., 2015; Cabrales et al., 2017)

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- ▶ Ring fencing, M&A regulation, crises resolution, bank disclosure...

## Asset commonality and systemic risk

- ▶ Theories: Wagner (2010, 2011), Ibragimov, Jaffee and Walden (2011), Allen, Babus and Carletti (2012), Cabrales, Gottardi and Vega-Redondo (2017)
- ▶ Empirics: Adrian and Brunnermeier (2016), Acharya et al. (2017)

## Panic runs

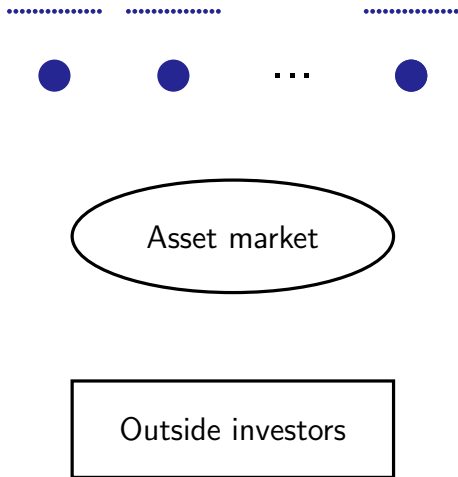
- ▶ Classics: Diamond and Dybvig (1983), Rochet and Vives (2004), Goldstein and Pauzner (2005)
- ▶ Panic runs with fire sales: Eisenbach (2017), Liu (2018), Luo and Yang (2019)

## Global games with heterogeneous agents

- ▶ Frankel, Morris and Pauzner (2003), Sakovics and Steiner (2012), Choi (2014)



# Structure of the economy



$t = 0$

Investors finance banks

$t = 1$

Shocks are realized  
Some investors choose to run  
Fire sales; cross-bank spillovers

$t = 2$

Banks repay late withdrawers

Outside investors

# Structure of the economy



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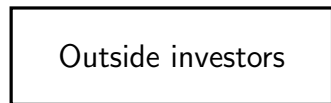
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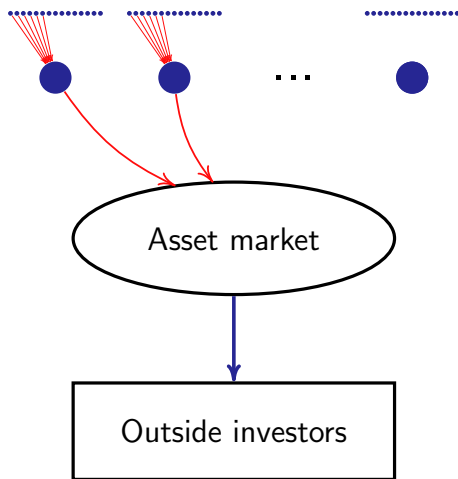
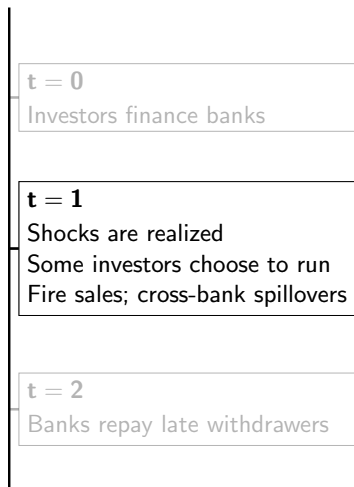
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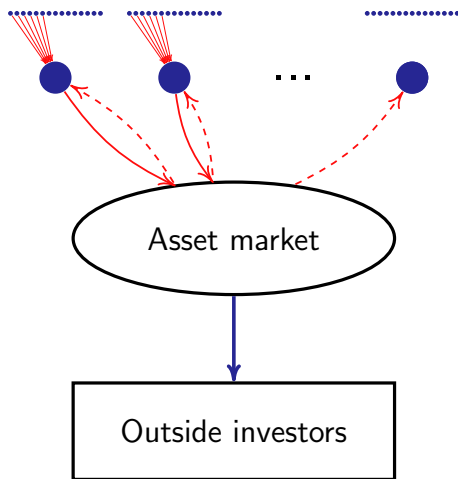
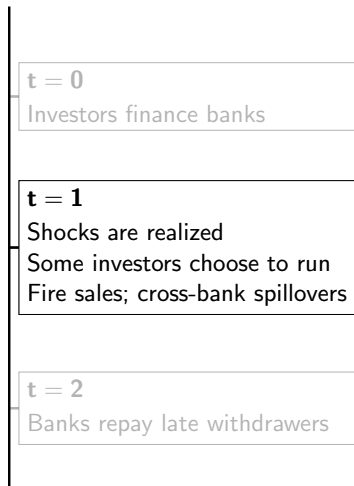
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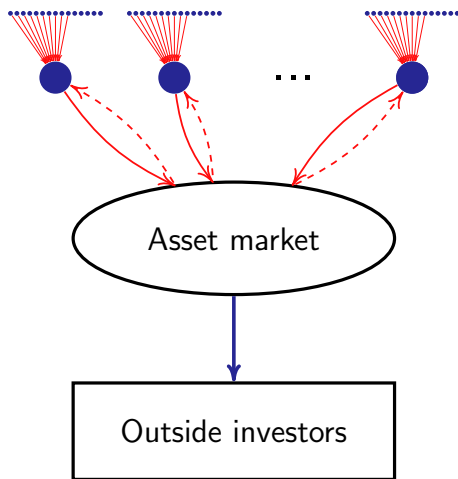
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Some investors choose to run  
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**t = 2**

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Asset market

Outside investors

# Model outline I

- ▶ Dates:  $t \in \{0, 1, 2\}$ . Three types of agents: banks, investors, outsiders

**t = 0**

- ▶ A continuum of ex-ante identical banks  $i \in [0, 1]$  with long-term asset return

$$z_i = \theta + \eta_i$$

- ▶ Aggregate productivity:  $\theta \sim F(\cdot)$ ,  $\mathbb{E}\theta > 1$

- ▶ Bank-specific productivities are i.i.d.:  $\eta_i = \begin{cases} \Delta & \text{w.p. } 0.5 \\ -\Delta & \text{w.p. } 0.5 \end{cases}$

- ▶  $\Delta$  is the degree of heterogeneity between (ex post) strong and weak banks
- ▶ Bank  $i$  has no wealth but receives funding from a unit mass of investors

# Model outline II

**t = 1**

- ▶ Payoff from early withdrawal (run):  $\pi_{run} = 1$ 
  - ▶ Fraction  $\bar{m} < 1$  can withdraw funds early (e.g. due to limited attention)
- ▶ Given the mass of runners  $m_i$ , bank  $i$  sells  $\frac{m_i}{p_i}$  units of assets to outsiders
  - ▶  $p_i < 1$  is determined by market-clearing condition
  - ▶  $\frac{\bar{m}}{p_i} \leq 1$ : no bankruptcy



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**t = 2**

- ▶ Late withdrawers receive  $\pi_{stay}(z_i, m_i, p_i) = \frac{z_i \left(1 - \frac{m_i}{p_i}\right)}{1 - m_i}$
- ▶ Within-bank strategic complementarity:  $\frac{\partial(\pi_{stay} - \pi_{run})}{\partial m_i} < 0$  iff  $p_i < 1$

# Liquidation

## Outsiders

- ▶ Deep-pocketed, competitive, less efficient than banks
- ▶ Purchase  $k_i$  unit of bank  $i$ 's asset to maximize expected payoff

$$\max_{\{k_i\}_{i \in [0,1]}} f\left(\int z_i k_i di\right) - \int p_i k_i di$$

where  $f(x) < x$ ,  $f'(\cdot) > 0$ ,  $f''(\cdot) < 0$ , and  $xf'(x)$  increases in  $x$

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## Liquidation prices

- ▶ Taking FOCs and imposing market-clearing conditions:  $p_i = \frac{z_i}{\lambda(m)}$
- ▶  $m = \int m_i di$  is total mass of runners in the economy
- ▶ Cross-bank complementarity:  $\lambda'(m) > 0$

# Complementarities

## Investors' incentive to stay

$$\pi_{stay} - \pi_{run} = \frac{z_i - \lambda(m)m_i}{1 - m_i} - 1$$

## Two mutually reinforcing complementarities

- ▶ Within-bank complementarity:  $\frac{\partial (\pi_{stay} - \pi_{run})}{\partial m_i} < 0$
- ▶ Cross-bank complementarity:  $\frac{\partial (\pi_{stay} - \pi_{run})}{\partial m} < 0$
- ▶ Complementarities reinforce each other:  $\frac{\partial^2 (\pi_{stay} - \pi_{run})}{\partial m \partial m_i} < 0$ 
  - ▶ When total amount of runs  $m$  is high, fire-sale discount  $\lambda(m)$  is high
  - ▶ Investors of bank  $i$  are more sensitive to run decisions of each other

# Bank runs

## Information structure

- ▶ Investor  $j$  in bank  $i$  observes  $\eta_i$  (can be relaxed)
- ▶ Investor  $j$  in bank  $i$  receives a noisy signal  $s_{ij}$  about aggregate fundamental  $\theta$

$$s_{ij} = \theta + \sigma \epsilon_{ij}, \quad \epsilon_{ij} \stackrel{\text{i.i.d.}}{\sim} \Phi(\cdot)$$

## Run decision

- ▶ An investor  $j$  in bank  $i$  withdraws early if

$$\mathbb{E} \left[ \pi_{\text{stay}}(z_i, m_i, p_i) \middle| s_{ij} \right] < \pi_{\text{run}} \Leftrightarrow \mathbb{E} \left[ \frac{z_i - \lambda(m) m_i}{1 - m_i} \middle| s_{ij} \right] < 1$$

# Global games

## Equilibrium uniqueness

- ▶ Focus on the limit of negligible signal noise:  $\sigma \rightarrow 0$
- ▶ Unique threshold equilibrium: investor  $j$  of bank  $i$   $\begin{cases} \text{runs if } s_{ij} \leq \theta_i^* \\ \text{stays if } s_{ij} > \theta_i^* \end{cases}$

## Marginal investor in bank $i$ : $s_{ij} = \theta_i^*$

- ▶ Indifference condition:  $\int_0^1 \frac{\theta_i^* + \eta_i - \lambda(m(x)) \bar{m}_x}{1 - \bar{m}_x} dx = 1$
- ▶ Mass of runner on investor's own bank  $i$ :  $\bar{m}_x$
- ▶ Mass of runners in the economy:  $m(x) = \bar{m} \int \Phi\left(\frac{\theta_k^* - \theta_i^*}{\sigma} + \Phi^{-1}(x)\right) dk$

Illustration

# Heterogeneity: Run thresholds

## Two groups of banks: strong and weak

$$\theta_i^* = \begin{cases} \theta_s^* & \text{if } \eta_i = \Delta, \\ \theta_w^* & \text{if } \eta_i = -\Delta \end{cases}$$

$$\int_0^1 \frac{\theta_s^* + \Delta - \lambda (0.5\bar{m}x + 0.5\bar{m}\Phi(t + \Phi^{-1}(x))) \bar{m}x}{1 - \bar{m}x} dx = 1$$

$$\int_0^1 \frac{\theta_w^* - \Delta - \lambda (0.5\bar{m}x + 0.5\bar{m}\Phi(-t + \Phi^{-1}(x))) \bar{m}x}{1 - \bar{m}x} dx = 1$$

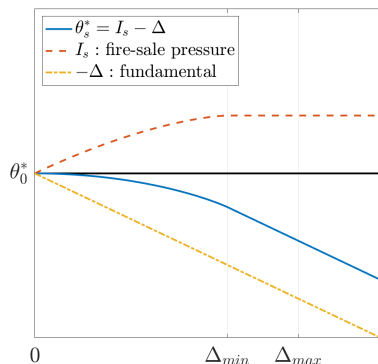
- ▶  $t = \lim_{\sigma \rightarrow 0} \frac{\theta_w^* - \theta_s^*}{\sigma}$  is a distance between run thresholds

## Two effects of larger heterogeneity $\Delta$

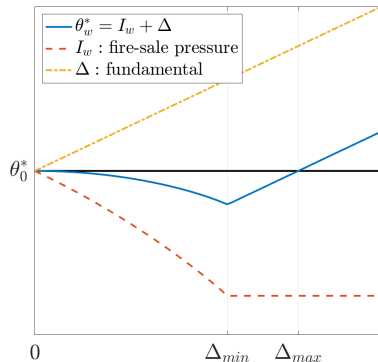
- ▶ *Fundamentals*: strong banks become stronger
- ▶ *Fire-sale pressure*: strong banks suffer from a higher fire-sale pressure

# Heterogeneity and fragility I

Strong banks



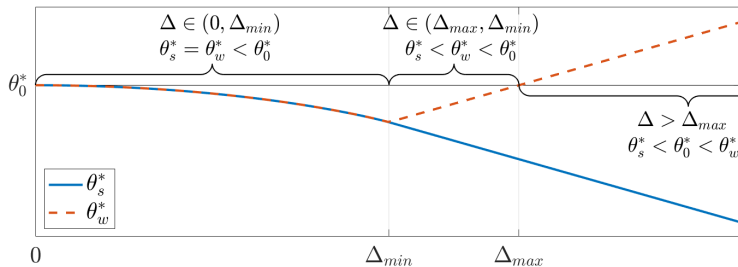
Weak banks



- ▶  $\Delta < \Delta_{min}$ : strategic uncertainties across investors of different banks
  - ▶ Weak bank investors perceive runs on strong banks as possible
  - ▶ Strong bank investors believe that weak banks might avoid runs
- ▶  $\Delta > \Delta_{min}$ : no more strategic uncertainties



# Heterogeneity and fragility II



- ▶ Heterogeneity is Pareto-improving if  $\Delta < \Delta_{min}$

Nonzero noise

# Heterogeneity and fragility III

## The effect of increasing heterogeneity $\Delta$

	Weak banks	Strong banks
Fundamental	$\downarrow (-)$	$\uparrow (+)$
Fire-sale pressure	$\downarrow (+)$	$\uparrow (-)$

- ▶ Impact of  $\Delta$  on run threshold  $\theta^*$ :
  - ▶ Fundamental: zero net effect (by construction)
  - ▶ Fire-sale pressure: net benefit due to reinforcing complementarities
- ▶  $\Delta > \Delta_{min}$ : fire-sale pressure is constant
  - ▶ Weak banks' investors are certain that strong banks are not liquidating
  - ▶ Strong banks' investors are certain that weak banks are liquidating

Why

# Robustness and extensions

- ▶  $N$  types of banks
- ▶ Uncertain bank-specific productivities
- ▶ General payoff functions
- ▶ No aggregate uncertainty

Here

Here

Here

Here

# Policies

## Ring fencing

- ▶ Service divisions: commercial banks vs investment banks
  - ▶ United States: Volcker rule
  - ▶ United Kingdom: Banking Reform Act 2013
- ▶ Geographic divisions
  - ▶ Europe: legal restrictions on intragroup cross-border asset transfers and limitations on the distribution of profits by foreign-owned subsidiaries
- ▶ Heterogeneity is crucial: splitting banks into identical clones will not help
- ▶ M&A regulation: increase risk weights of merging banks

## Bank support during crises

- ▶ U.S. Treasury forced all major banks to take the TARP money
- ▶ Avoid signaling and stigma
- ▶ Unintended (?) consequence: heterogeneity is preserved

# Conclusion

## Bank runs with common market for asset sales

- ▶ Two mutually reinforcing complementarities
- ▶ Aggregate uncertainty

## Key results

- ▶ A homogeneous financial system is suboptimal
- ▶ Increasing heterogeneity is Pareto improving

## Policy prescriptions

- ▶ Ring fencing, M&A regulation, support of banks in crises

# Appendix

# $N$ types of banks

- ▶ Same setting but bank-specific productivity can take  $N$  values

$$\eta_i = \Delta_i \text{ with prob. } w_i, \text{ where } \sum_{i=1}^N w_i = 1, \sum_{i=1}^N w_i \Delta_i = 0$$

## Proposition

*Starting from a homogeneous financial system ( $\Delta_i = 0 \forall i$ ), any sufficiently small heterogeneity reduces run thresholds for all banks.*

Back

# Uncertain bank-specific productivities

- ▶ Assume that bank  $i$  sends an imperfect signal  $d_i \in \{G, B\}$  about its type at  $t = 1$

$$\mathbb{P}(d_i = G | \eta_i = \Delta) = \mathbb{P}(d_i = B | \eta_i = -\Delta) = \alpha \in [0.5, 1]$$

## Proposition

The model is equivalent to the benchmark one with

$$w^{\text{eff}}(\alpha) = w\alpha + (1-w)(1-\alpha),$$
$$\Delta^{\text{eff}}(\alpha) = \frac{2\alpha - 1}{w\alpha + (1-w)(1-\alpha)} w\Delta.$$

Effective heterogeneity  $\Delta^{\text{eff}}(\alpha > 0)$ ,  $\Delta^{\text{eff}}(0.5) = 0$ , and  $\Delta^{\text{eff}}(1) = \Delta$ .

- ▶ Imperfect signals about bank-specific productivities reduce *effective* heterogeneity
- ▶ When  $\alpha = 0.5$ , banks are effectively homogeneous
- ▶ Main result holds as long as signals are informative,  $\alpha > 0.5$



# General payoff function

- ▶ Consider a general (net) benefit from staying

$$g(z_i, m_i, m), \text{ where } \frac{\partial g}{\partial z_i} > 0, \frac{\partial g}{\partial m_i} < 0, \frac{\partial g}{\partial m} < 0$$

## Proposition

*If  $\frac{\partial^2 g}{\partial m_i \partial m} \leq 0$ ,  $\frac{\partial^2 g}{\partial z_i \partial m} \geq 0$ ,  $\frac{\partial^2 g}{\partial z_i^2} \geq 0$ , a common run threshold  $\theta^*$  is not increasing when heterogeneity  $\Delta$  goes up (declines if any of the inequalities is strict).*

- ▶  $\frac{\partial^2 g}{\partial m_i \partial m} \leq 0$  — mutually reinforcing complementarities
- ▶  $\frac{\partial^2 g}{\partial z_i \partial m} \geq 0$  — (mechanically) asymmetric fire-sale pressure
- ▶  $\frac{\partial^2 g}{\partial z_i^2} \geq 0$  — (mechanically) beneficial heterogeneity

Back

# No aggregate uncertainty

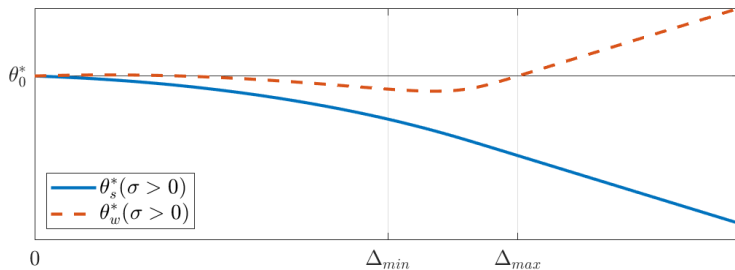
- ▶ Bank  $i$  is characterized by its position  $x_i \in [0, 1]$ :  $\eta_i = \begin{cases} \Delta, & \text{if } x_i > 0.5, \\ -\Delta, & \text{if } x_i \leq 0.5 \end{cases}$
- ▶ Assume that agents perfectly observe  $\theta$  but not  $x_i$  (i.e.,  $\eta_i$ ):  $s_{ij} = x_i + \sigma \epsilon_{ij}$

## Proposition

- ▶  $\theta > \theta_L$ : there exists a 'low-run' equilibrium with the run threshold  $x_L^* < 0.5$
  - ▶  $\theta < \theta_H$ : there exists a 'high-run' equilibrium with the run threshold  $x_H^* > 0.5$
  - ▶  $\theta_L(\Delta)$  is increasing and  $\theta_H(\Delta)$  is decreasing in  $\Delta$
- 
- ▶  $\eta_i$  is uncertain  $\Rightarrow$  multiplicity due to within-bank complementarities is resolved
  - ▶ Prices are certain  $\Rightarrow$  multiplicity due to cross-bank complementarity is preserved
  - ▶ Impact of heterogeneity depends on the type of equilibria being played

Back

# Finite noise

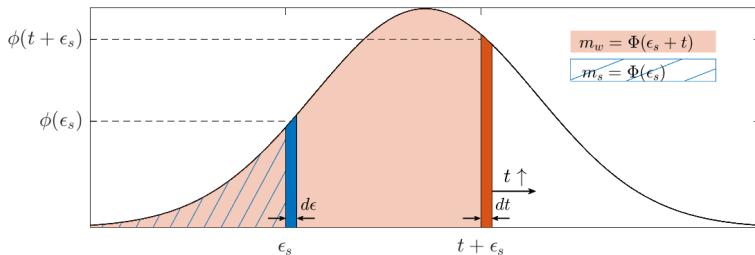


- ▶ Assume that signals are not infinitely precise
- ▶ Thresholds  $\theta_s^*$  and  $\theta_w^*$  are not infinitely close
- ▶ But overall pattern is preserved

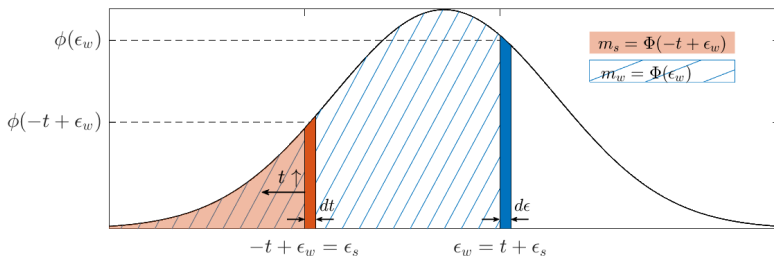
Back

# Asymmetric fire-sale pressure

## Fire-sale pressure on strong banks



## Fire-sale pressure on weak banks



# Fragility of a homogeneous financial system

- ▶ Consider a homogeneous financial system,  $\eta_i = 0 \forall i$

## Benchmark case: Interacting complementarities

- ▶ Synchronized runs across different banks  $\Rightarrow$  Threshold investor expects many runs on her bank when fire-sale discount is large
- ▶ Indifference condition: 
$$\int_0^1 \frac{\theta_0^* - \lambda(\bar{m}_x) \bar{m}_x}{1 - \bar{m}_x} dx = 1$$

## Fixed fire-sale discount: No complementarity interaction

- ▶ Fix fire-sale discount at its average level:  $\bar{\lambda} = \int_0^1 \lambda(\bar{m}_x) dx$
- ▶ Indifference condition: 
$$\int_0^1 \frac{\hat{\theta}_0^* - \bar{\lambda} \bar{m}_x}{1 - \bar{m}_x} dx = 1$$
- ▶ Banks are *less* fragile when complementarities do not interact:  $\hat{\theta}_0^* < \theta_0^*$