# Dynamic Oligopoly and Price Stickiness

Olivier Wang
NYU Stern

Iván Werning MIT

#### Imperfect Competition

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- Monopolistic competition: continuum of firms (Dixit-Stiglitz)
  - simple and tractable
  - reigns supreme: trade, macro, growth, ...

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- Monopolistic competition: continuum of firms (Dixit-Stiglitz)
  - simple and tractable
  - reigns supreme: trade, macro, growth, ...
- Oligopoly: finite number of firms
  - more realistic and complicated
  - extensive IO literature
  - "rise in market power": markups, concentration, superstar firms, ...
- Q: Oligopoly important for macro?

#### This Paper

- Standard macro model...
  - representative agent, infinite horizon
  - consumption, labor and money
  - nominal rigidities a la Calvo

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  - nominal rigidities a la Calvo
- Here:
  - oligopoly with any *n* firms
  - general demand structure (e.g. Kimball, not just CES)
- Results
  - 1. Sufficient statistics for M shocks
  - 2. Calibration and counterfactuals
  - 3. Inspecting the mechanism
  - 4. Phillips Curve

#### Literature

Mongey (2016)

Rotemberg-Saloner (1986), Rotemberg-Woodford (1992)

• IO Literature (dynamic): Ericson-Pakes (1995), Bajari-Benkard-Levin (2007), ...

Passthrough Literature (static): Goldberg (1985),
 Atkeson-Burstein (2008), Gopinath-Itskhoki (2010),
 Arkolakis-Costinot-Donaldson-Rodríguez Clare (2015),
 Amiti-Itskhoki-Konings (2019)

### Setup

- Households: consumption, labor, money
- Firms: continuum of sectors s...
  - $n_s$  firms within sector s
  - Calvo price rigidity: constant probability of price change  $\lambda_s$
- Equilibrium concepts for oligopoly game...
  - Markov: dominant equilibrium concept in IO

$$\int_0^\infty e^{-\rho t} U\left(C(t), L(t), \frac{M(t)}{P(t)}\right) dt$$

$$C(t) = G(\{C_s(t)\}_s)$$
  
 $C_s(t) = H(c_{s,1}(t), c_{s,2}(t), \dots, c_{s,n}(t))$ 

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Calvo pricing Poisson arrival  $\lambda$ 

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$$\{p_{j,s}\}_{j \neq i}$$

• Constant C, L, M, P, W, r

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  - household and market clearing

$$C = L$$

$$\frac{U_C}{P} = \frac{U_L}{W} = \frac{U_m}{rP}$$

$$r = \rho$$

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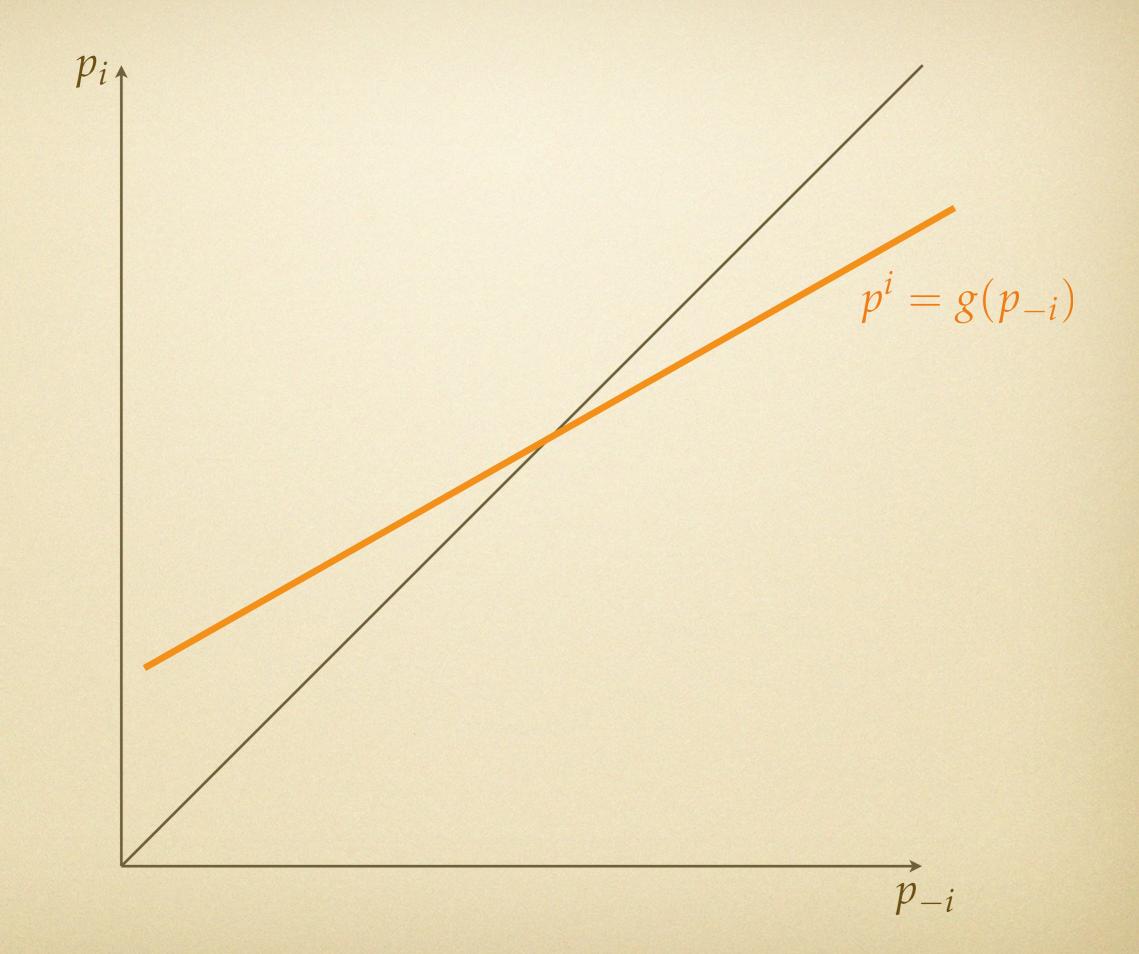
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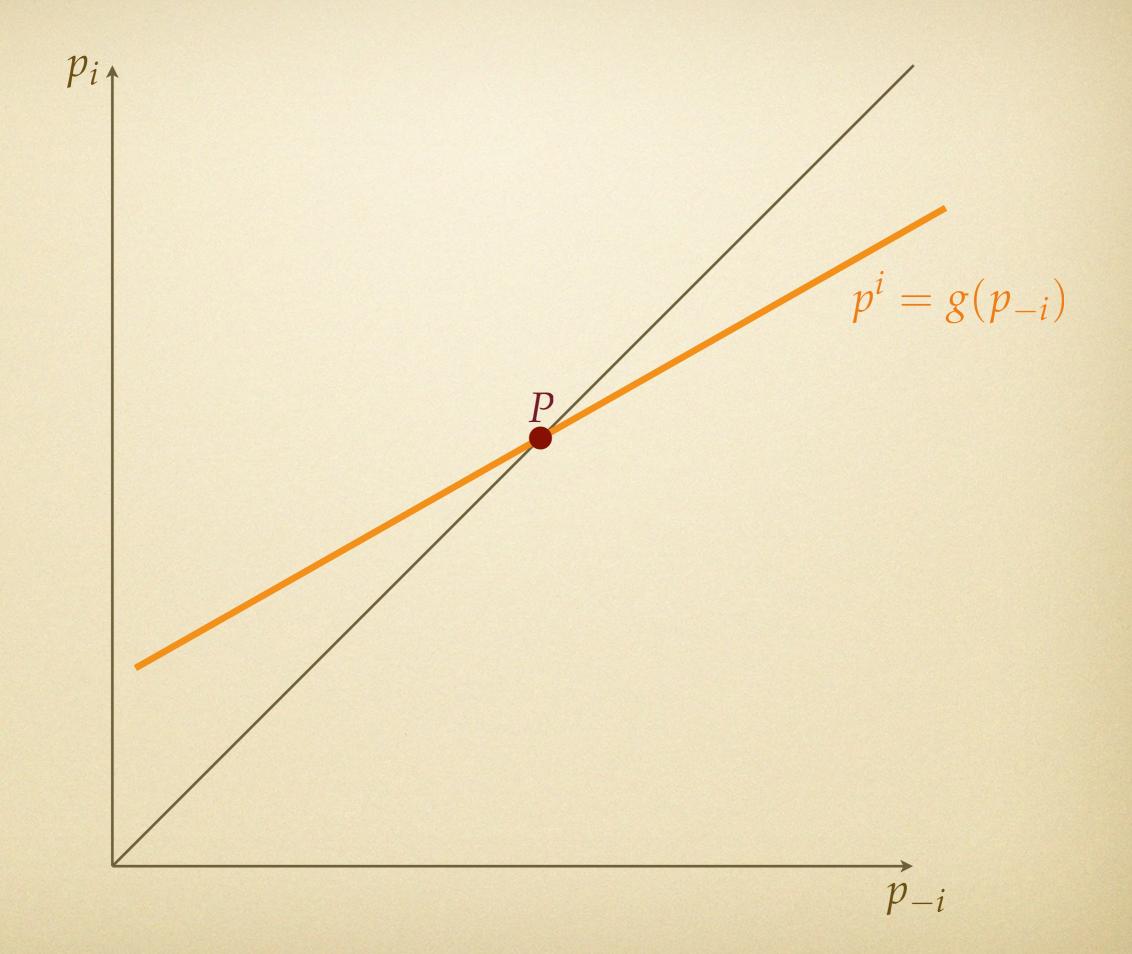
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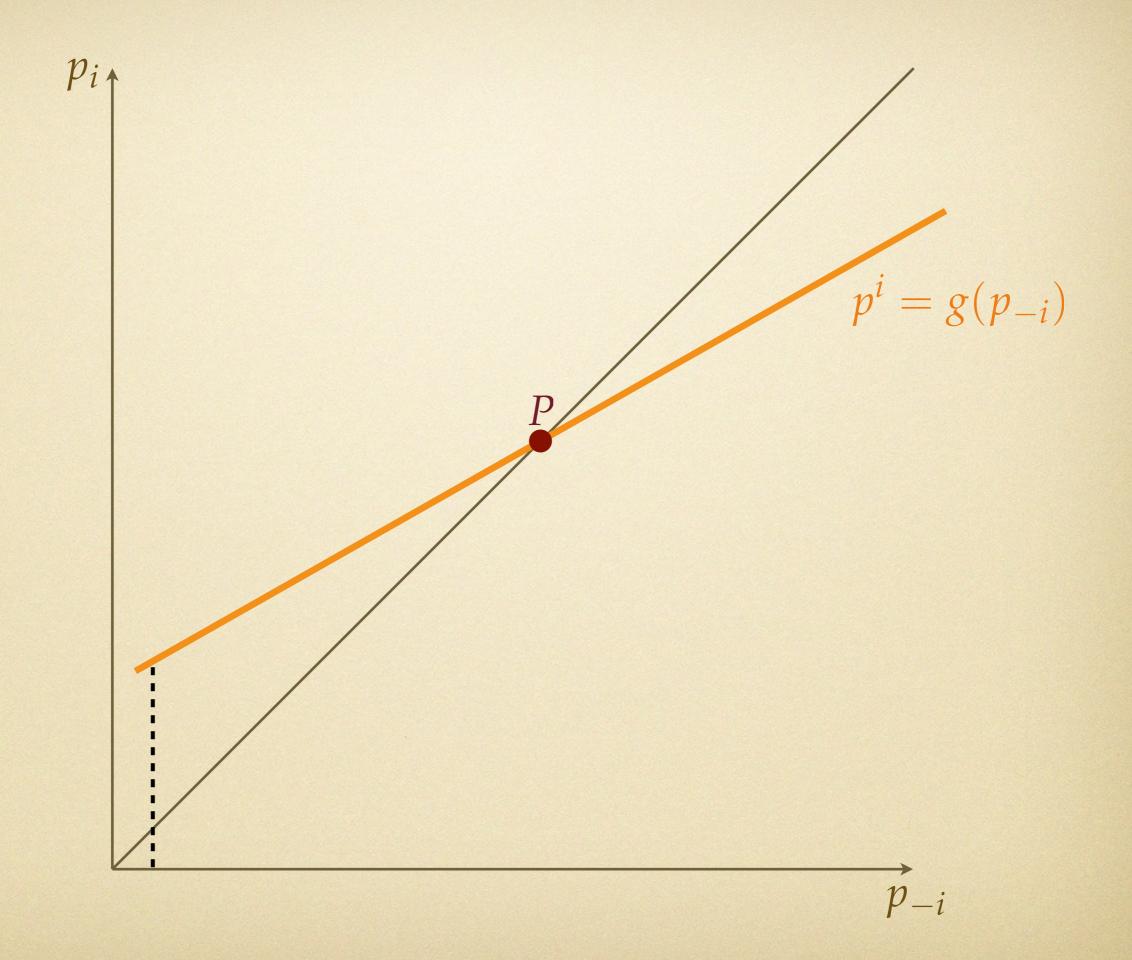
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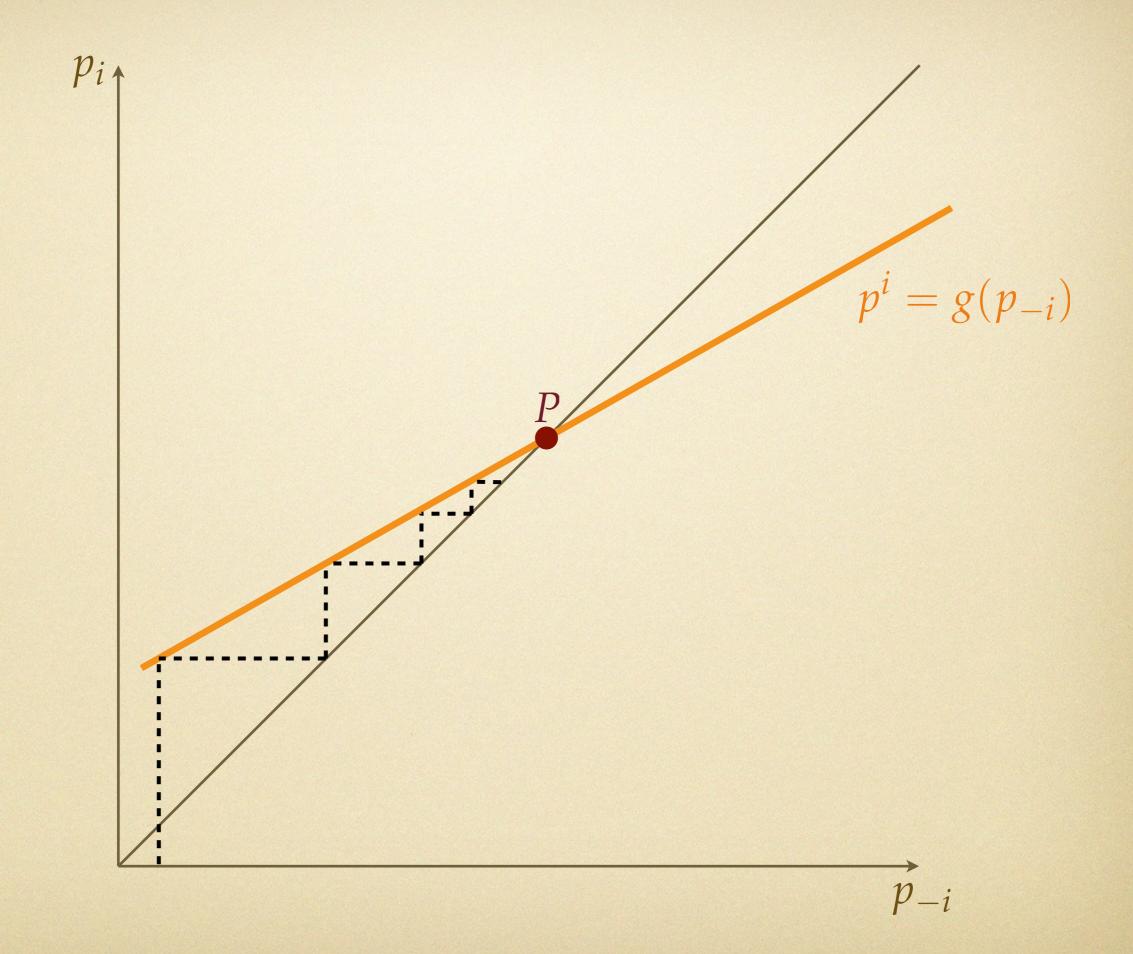
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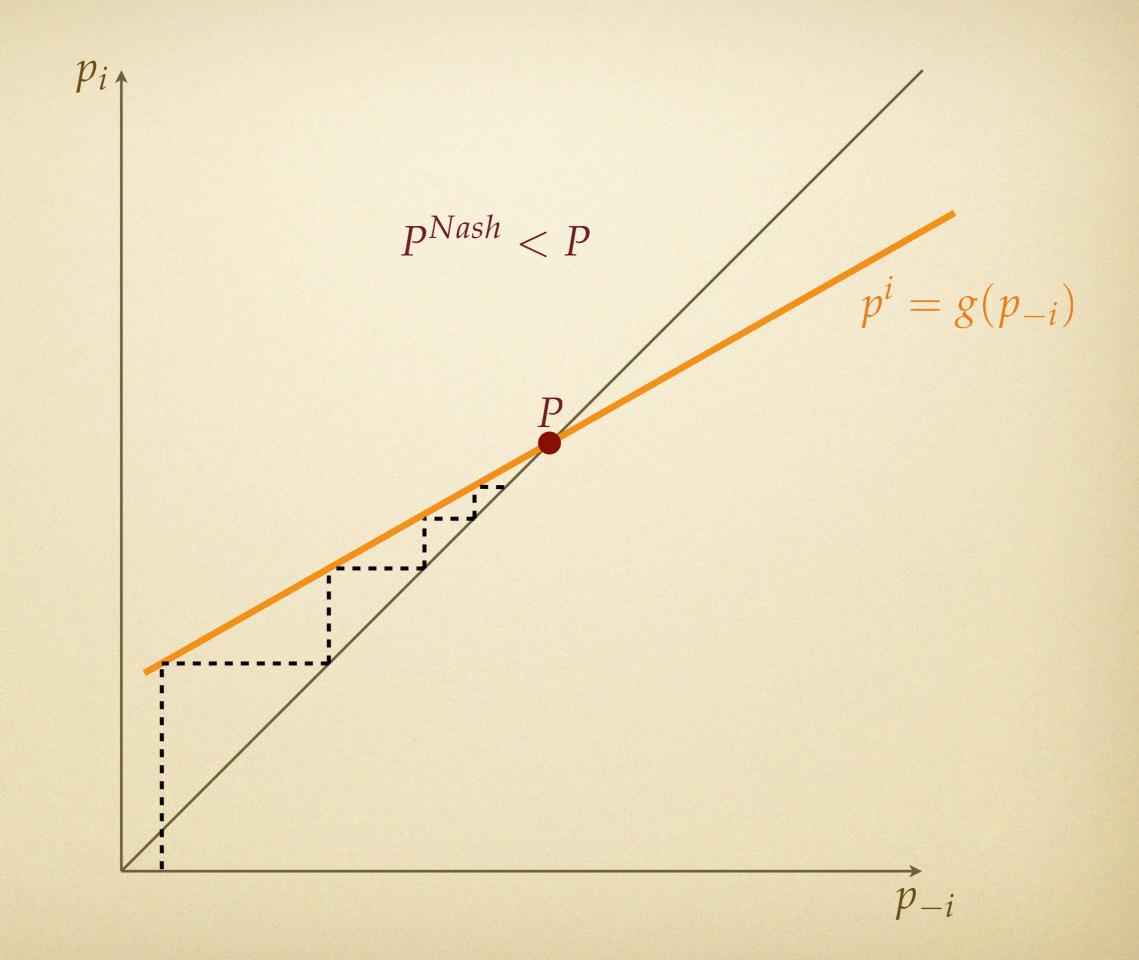
• steady state price vector P = g(P, P, ..., P)









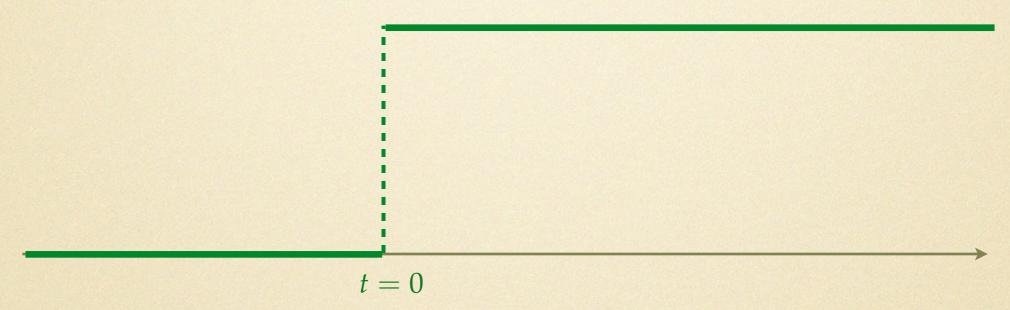


#### 1. Sufficient Statistics

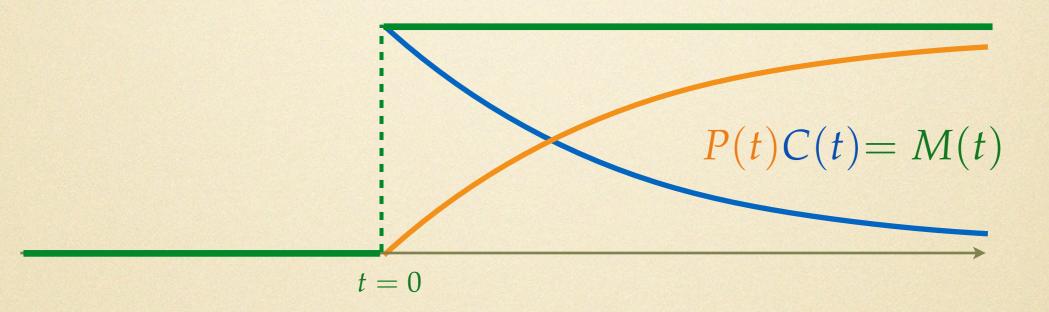
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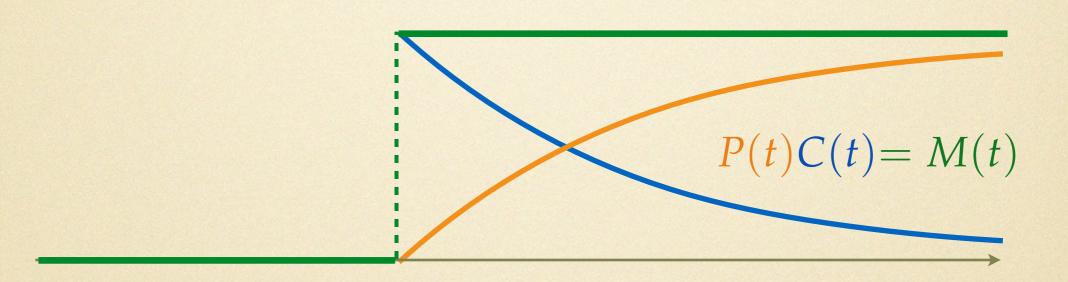
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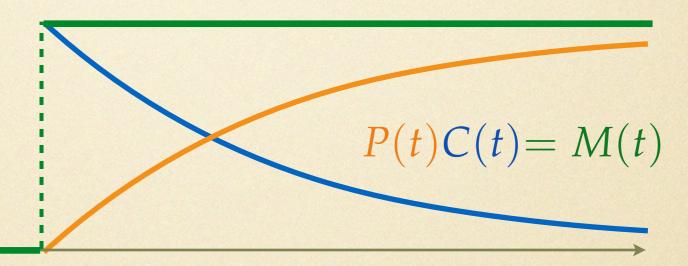


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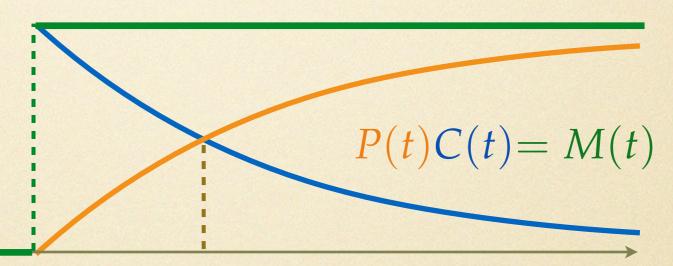
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$$\log \frac{P(t)}{P^*} \approx \log \frac{P(0)}{P^*} e^{-\lambda (1 - \sum_{n} (n-1)\beta_n \omega_n)t}$$

$$\beta_n \equiv \frac{\partial}{\partial p_j} g(P^*)$$

extensions: heterogeneous  $\lambda$ , productivity, costs

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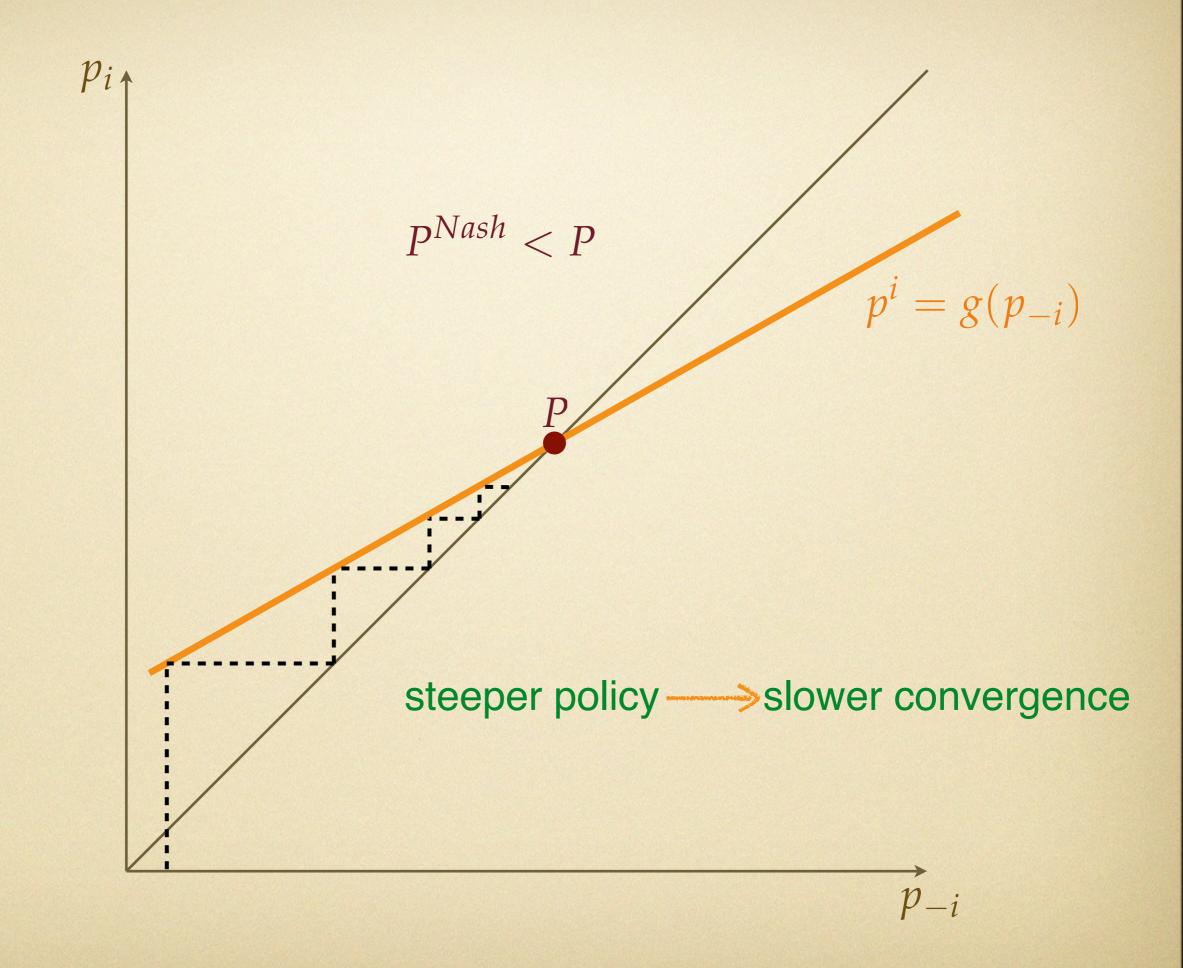


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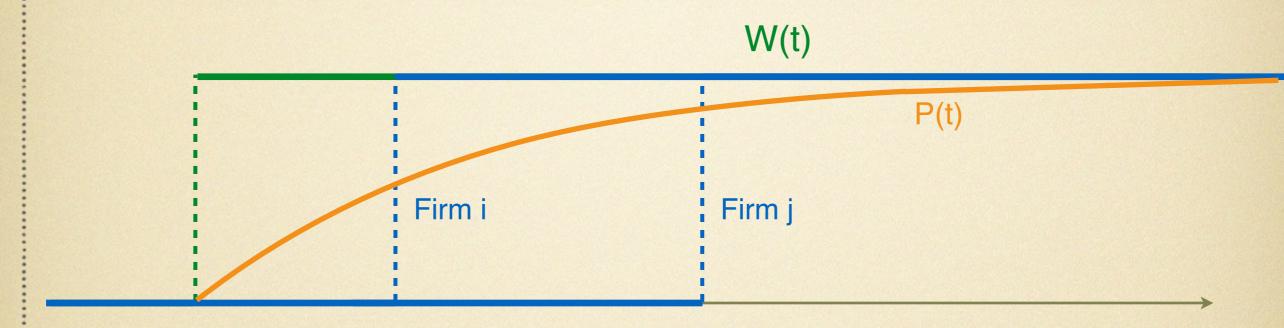


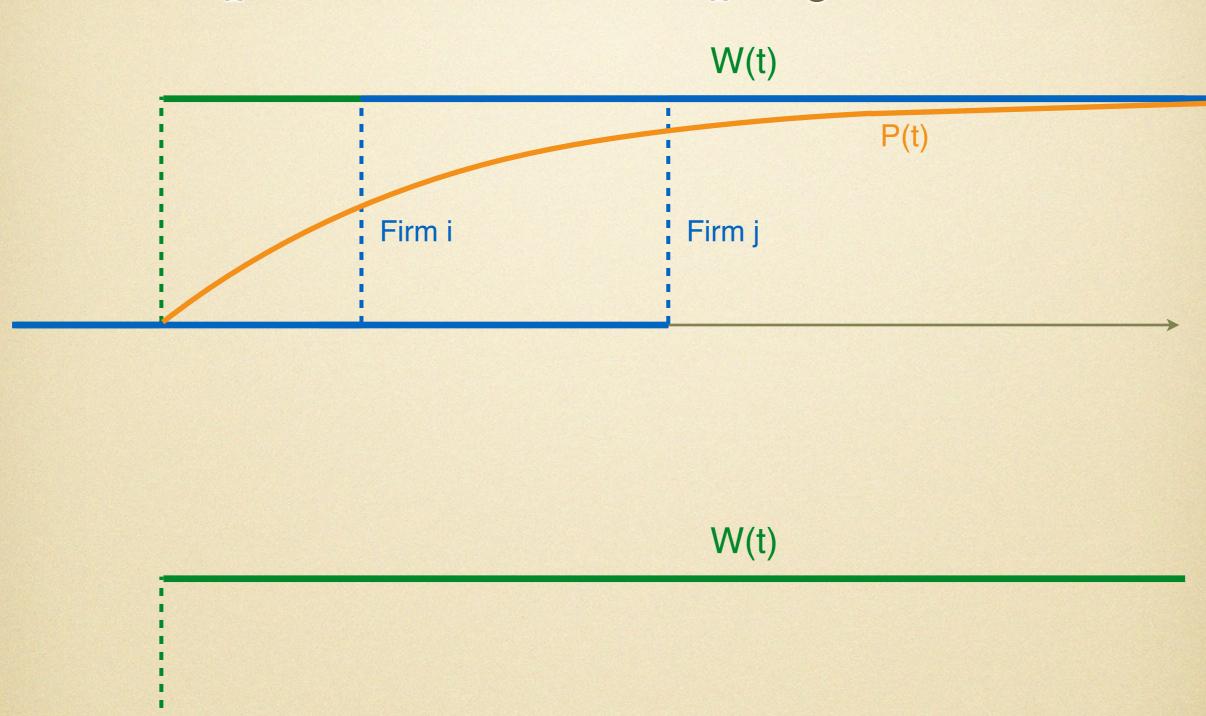
W(t)

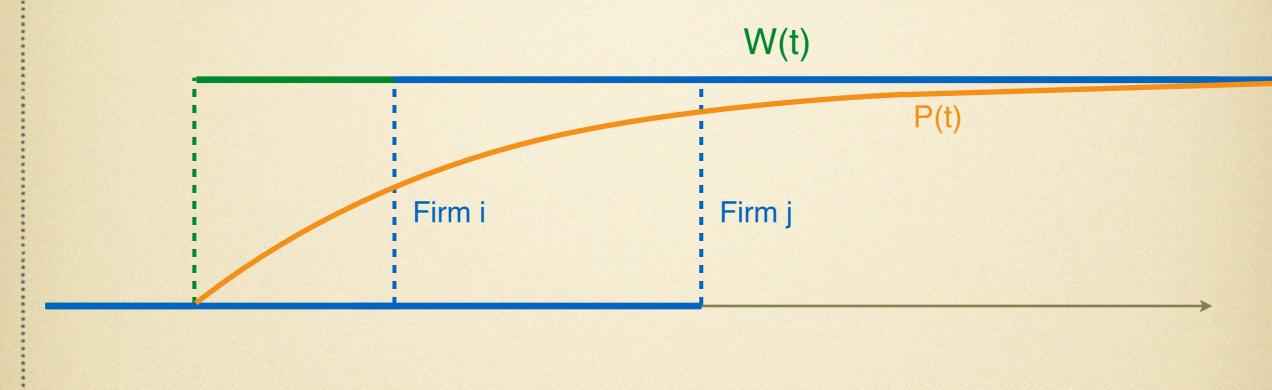
W(t)

Firm i

Firm i Firm j

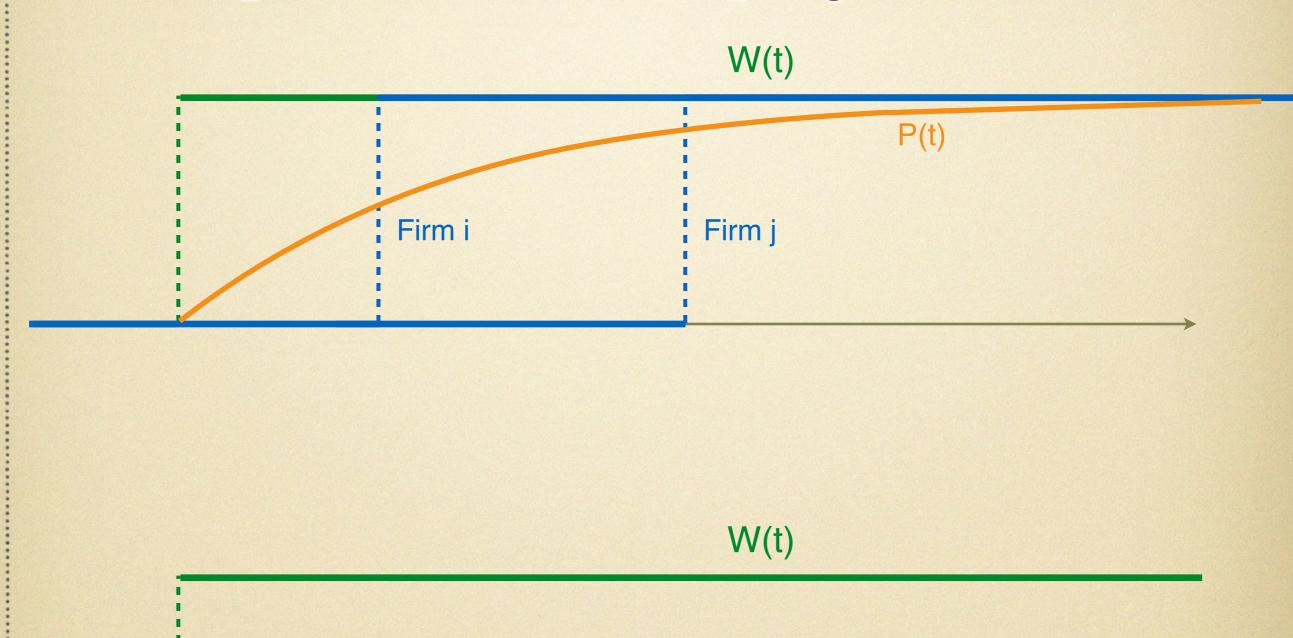






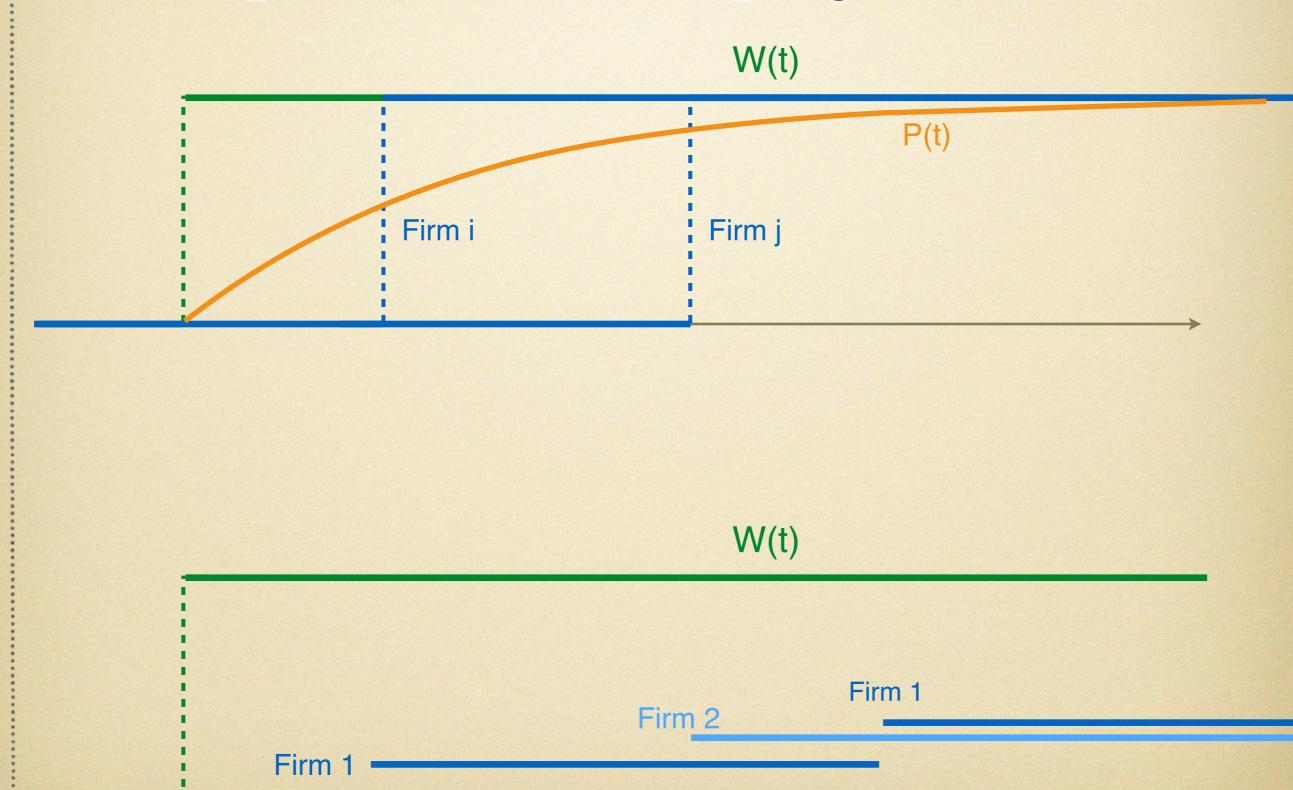


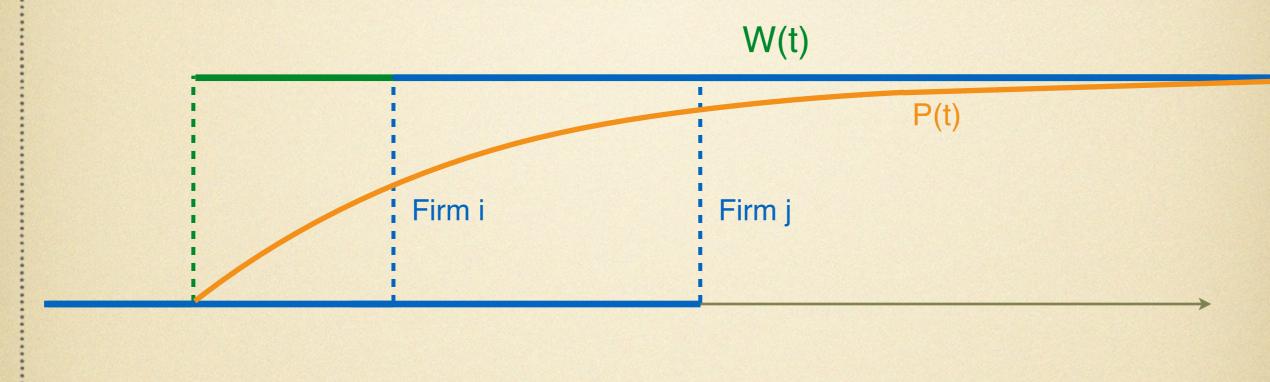
Firm 1

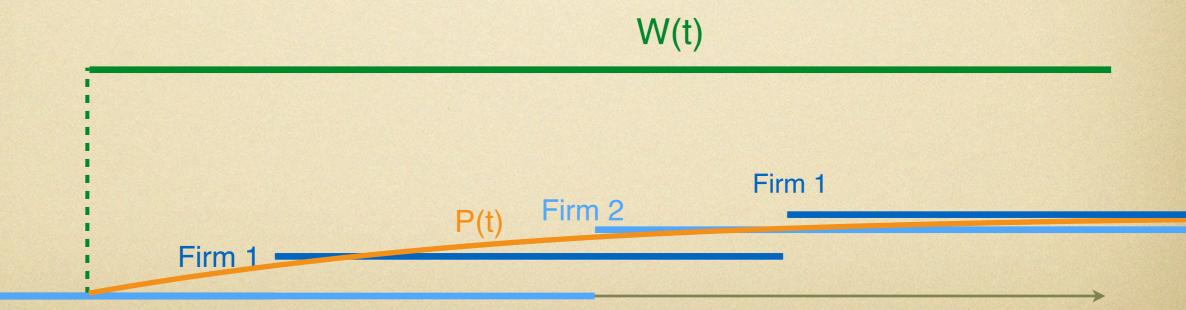


Firm 2

Firm 1







## Sufficient Statistic

#### Proposition.

$$(n-1)\beta_n = \frac{\rho + \lambda}{\lambda} \frac{n-1}{n-2 + \frac{\epsilon_i^i - 1}{\epsilon_i^i - \frac{\mu}{\mu - 1}}} \quad \epsilon_i^i = \frac{-\partial \log D^i}{\partial \log p_i}$$

$$\mu = \frac{P}{W}$$

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- Intuition... (reverse causality  $\beta \rightarrow \mu$ )
  - Nash markup  $\iff \beta = 0$
  - higher markup  $\iff$  rivals mimic my price (high  $\beta$ )

## Sufficient Statistic

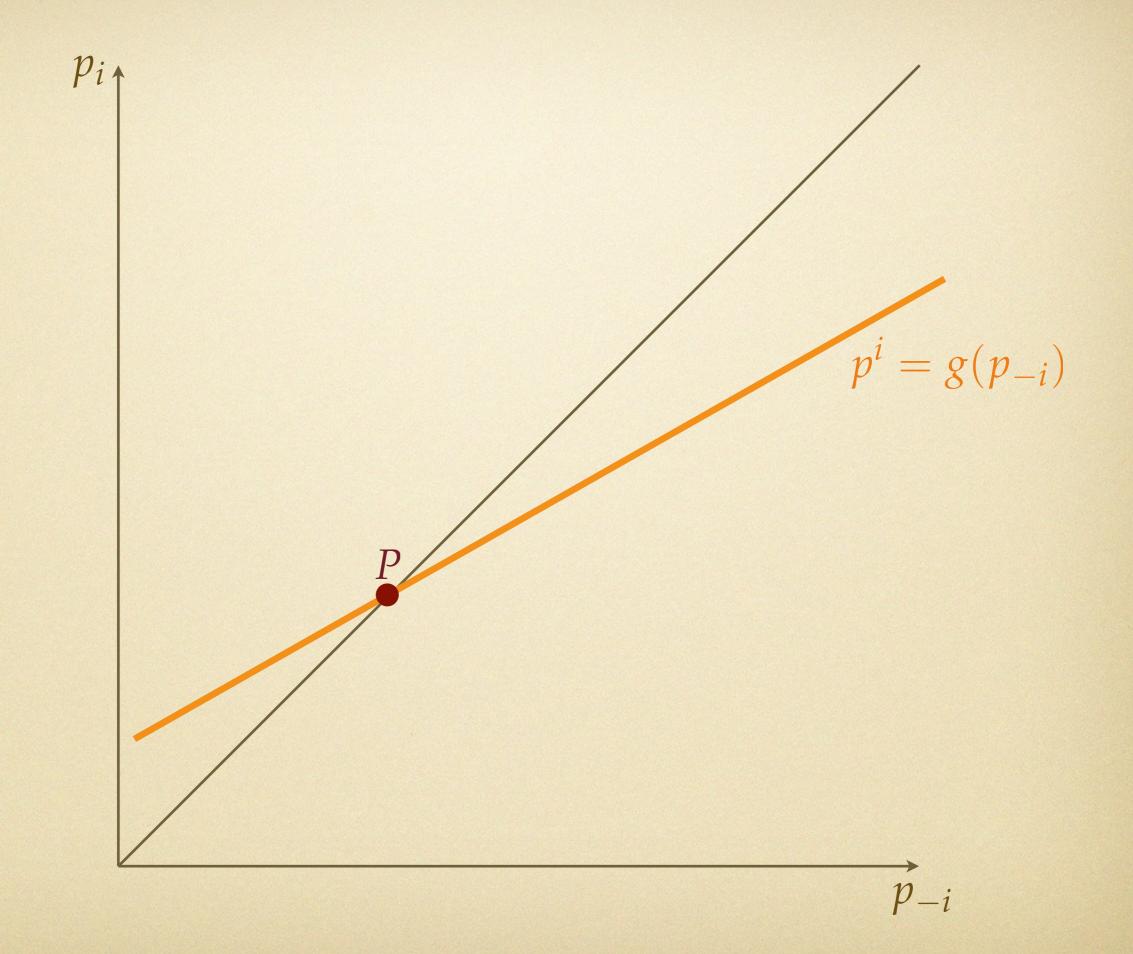
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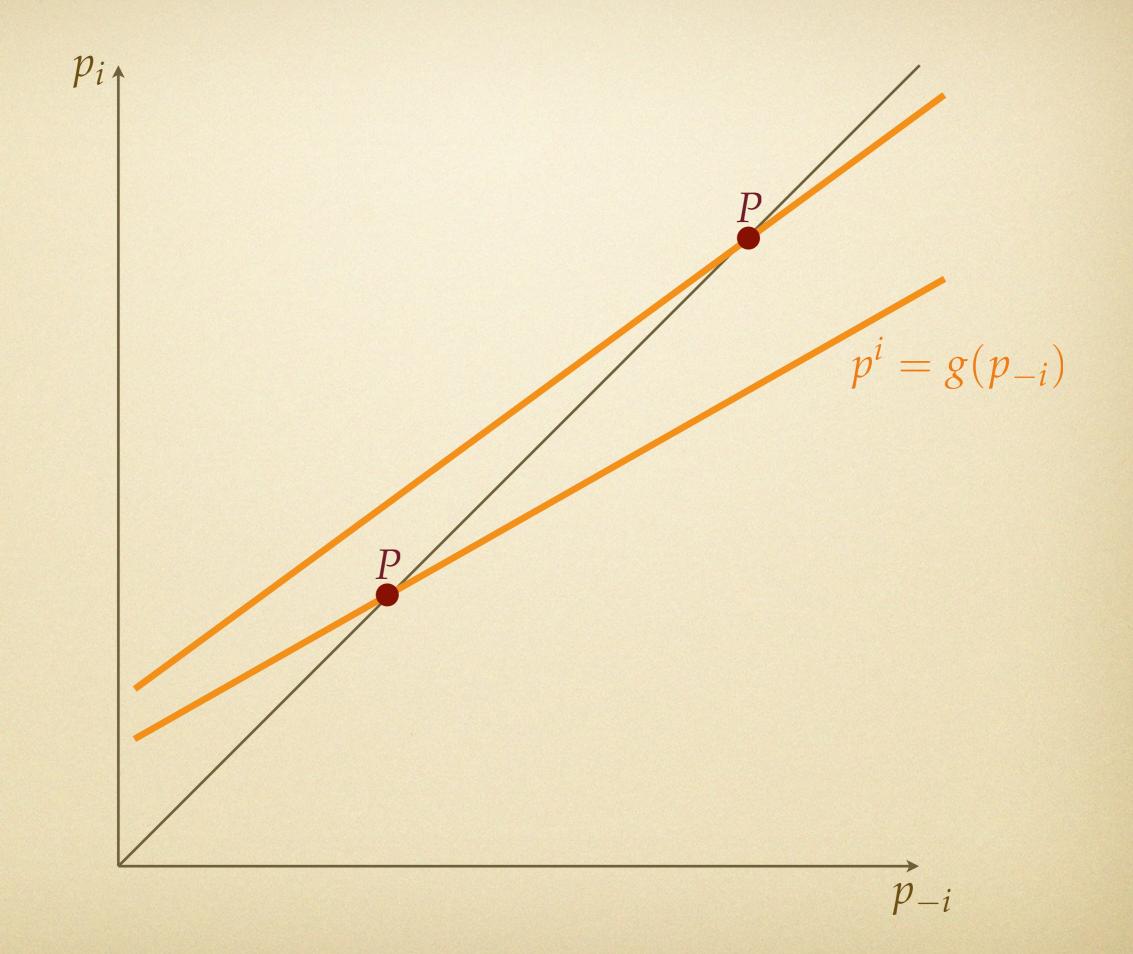
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- Intuition... (reverse causality  $\beta \rightarrow \mu$ )
  - Nash markup  $\iff \beta = 0$
  - higher markup  $\iff$  rivals mimic my price (high  $\beta$ )
- Very few statistics needed!
  - markup observable? maybe
  - elasticity observable? maybe



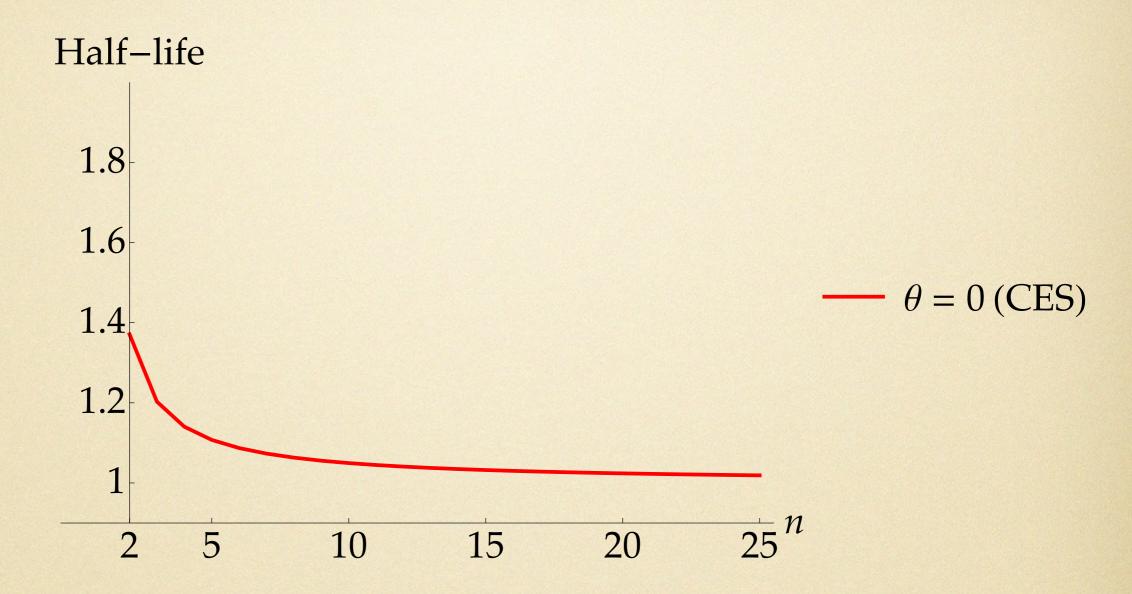


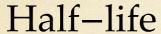
## 2. Counterfactuals

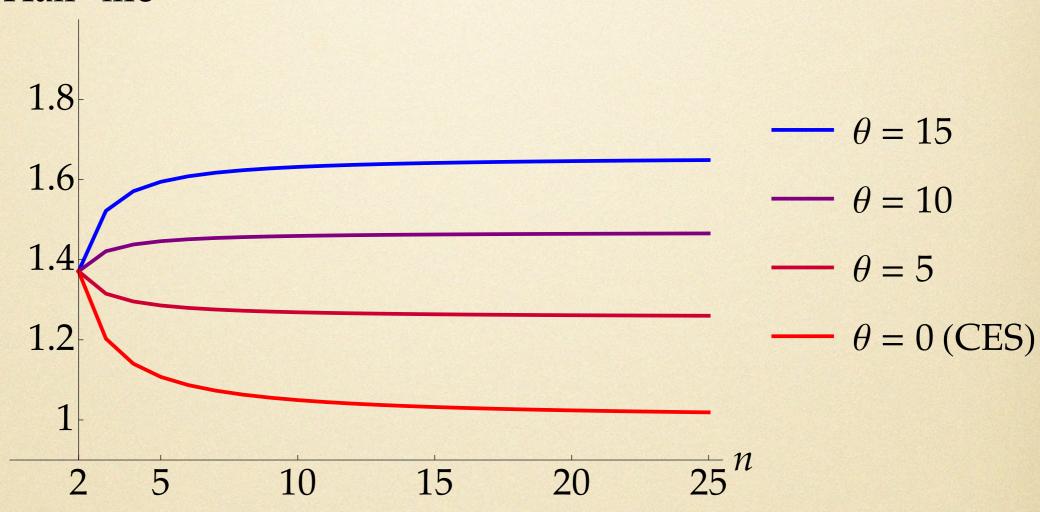
$$\frac{1}{n} \sum \Psi(\frac{c_i}{C}) = 1$$

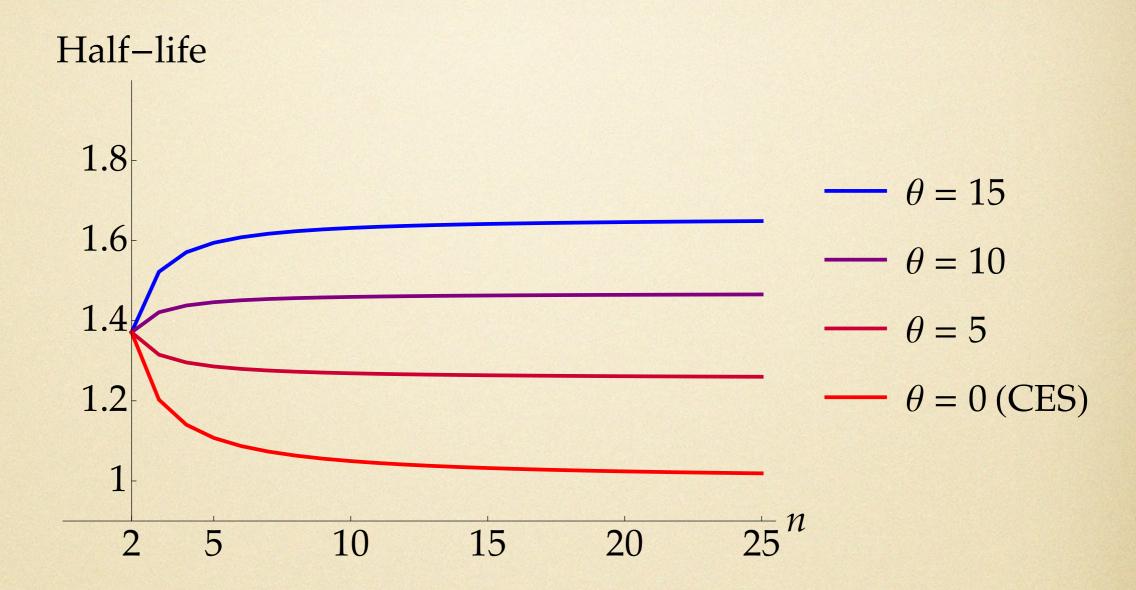
$$\Psi'(x) = \frac{\eta - 1}{\eta} \exp\left(\frac{1 - x^{\theta/\eta}}{\theta}\right) \quad \text{(Klenow-Willis)}$$

- Under monopolistic competition
  - $\rightarrow$  elasticity  $\eta$
  - $\rightarrow$  superelasticity  $\theta$
- Oligopoly: elasticities also depend on *n*









- Low  $\theta$  similar to CES: slowest convergence at n=2
- But with high enough  $\theta$ , fastest convergence at n=2!
- Duopoly is knife-edge: half-life stuck at CES level... in contrast:  $n \ge 3$  arbitrarily large as  $\theta$  increases

# Pass-Through

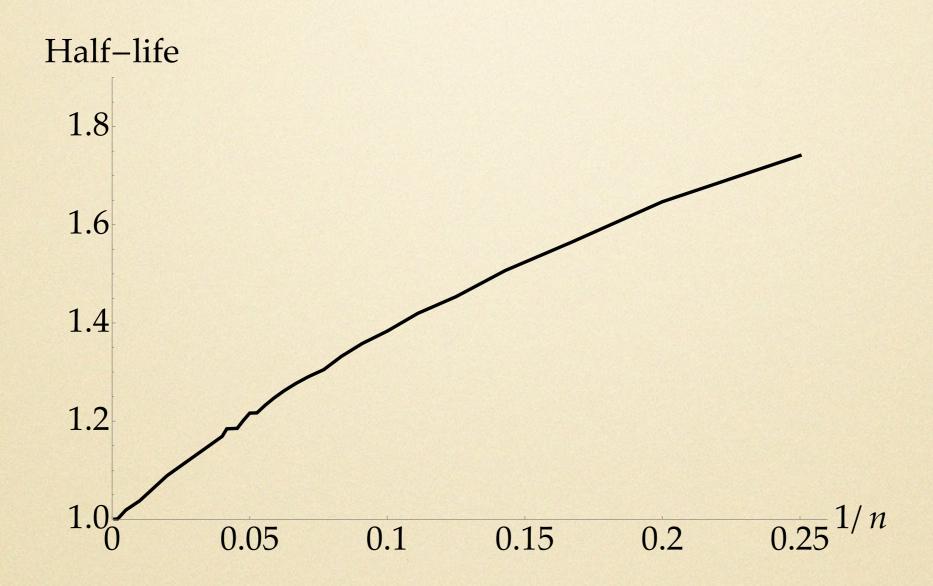
- Amiti-Itskhoki-Konings 19: own cost pass-through
  - high for small firms
  - low for large firms
  - consistent with CES Cournot but not Bertrand

Depart from CES to match

pass-through = f(market share)

in dynamic (Bertrand) model

## HHI and Half-life

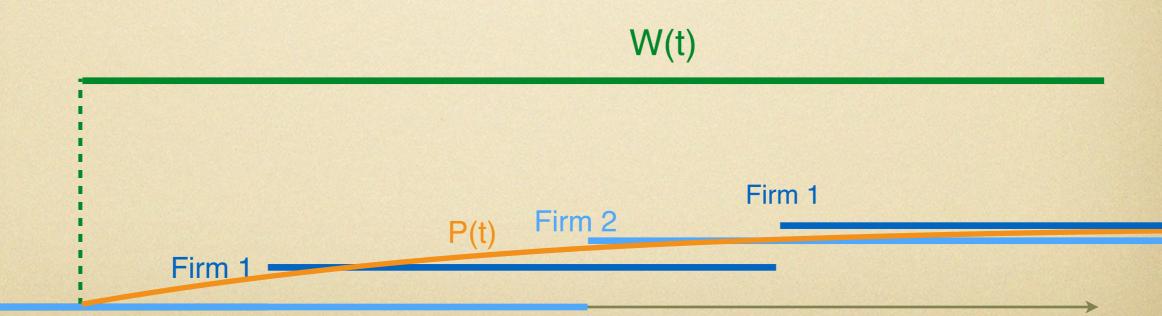


- National HHI 0.05 to 0.1 (e.g., Gutierrez-Philippon): MP 15% stronger
- Local HHI 0.15 to 0.05 (Rossi-Hansberg, Sarte, Trachter): MP 25% weaker

# 3. Inspecting the mechanism



- Two effects with finite *n*…
  - feedback: firm i cares about others' prices
  - strategic: firm i can affect others' prices



- Two effects with finite *n*…
  - feedback: firm i cares about others' prices
  - strategic: firm i can affect others' prices
- Feedback effect with  $n = \infty$ 
  - inputs from other firms
  - Kimball (1995) demand

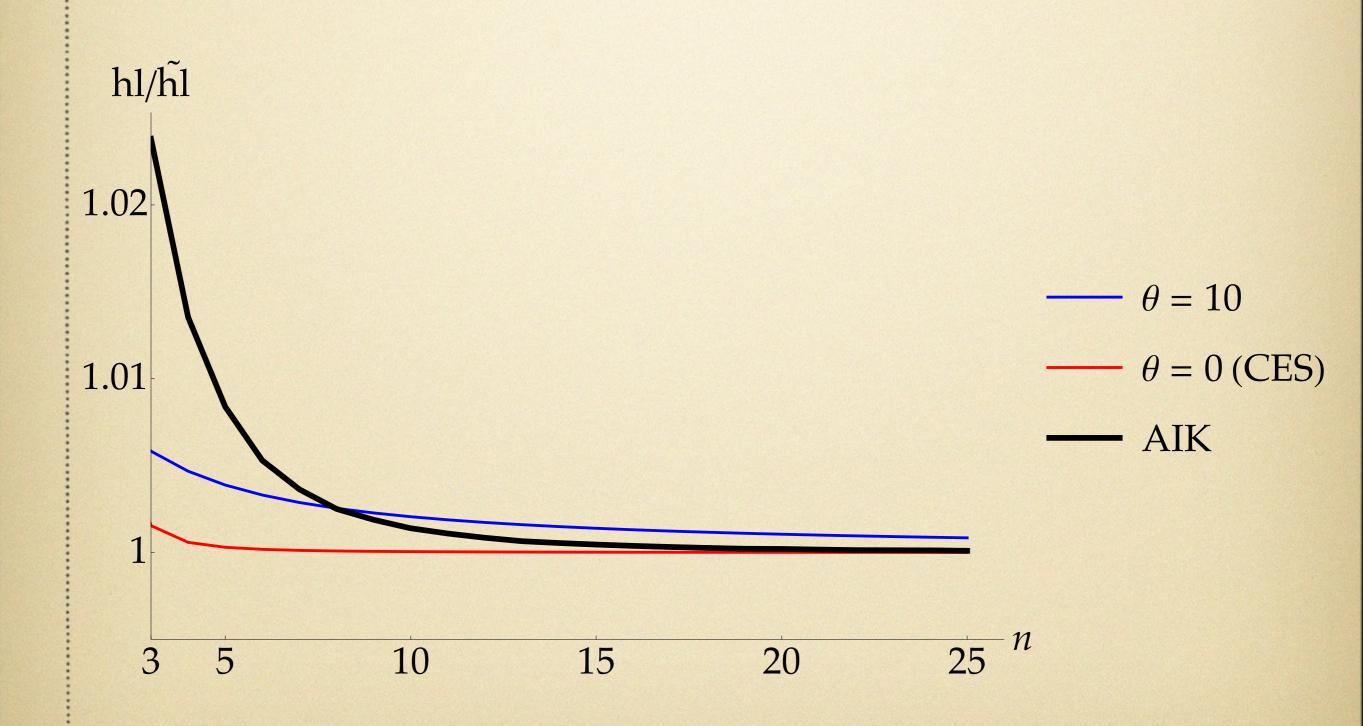


• Compare MPE with *n* firms to

#### as if monopolistic market

- $n = \infty$  and modified Kimball preferences to match elasticities
- $\Rightarrow$  equilibrium if *n* firms ignore how they affect rivals' pricing  $\Rightarrow$  "non-strategic" model

# Small strategic effects



# 4. Phillips Curve

# Phillips Curve

- Generalize preferences and allow arbitrary paths of
  - Interest rate shocks
  - Real shocks
- Monopolistic NKPC
  - First order ODE
  - Inflation only depends on future MC
  - Kimball  $\Leftrightarrow$  less frequent adjustment (lower  $\lambda$ )
- Oligopolistic NKPC
  - Higher order ODE: inflation persistence
  - Not just MC: demand, interest rates
  - Not equivalent to lower  $\lambda$

# Phillips Curve

Standard NKPC

$$\dot{\pi} = 0.05\pi - 1.05mc$$

- Oligopoly: Example with n = 3
  - MPE

$$\dot{\pi} = 0.07\pi - 0.28mc$$

$$+1.31\ddot{\pi} + 0.45mc + 0.03(r - \rho)$$

Non-strategic (= monopolistic Kimball)

$$\dot{\pi} = 0.05\pi - 0.27mc$$

# 3-Eq Oligopoly NK

Combine with Euler equation

$$\dot{c} = \sigma^{-1} \left( r - \pi - \rho - \epsilon^r \right)$$

Taylor rule

$$r = \rho + \phi \pi + \epsilon^m$$

• AR(1)  $\epsilon^r$ ,  $\epsilon^m$  shocks

n	Model	$\sigma$ (	$\sigma\left(\pi\right)$		$\sigma\left(c\right)$	
		$\epsilon^r$	$\epsilon^m$	$\epsilon^r$	$\epsilon^m$	
$\infty$	$\theta = 0 \text{ (CES)}$	2.2%	2.7%	0.8%	1.0%	
$\infty$	$\theta = 10$	2.0%	2.4%	1.0%	1.3%	
10	MPE Non-strategic	$2.3\% \\ 2.7\%$	2.8% $3.3%$	$1.1\% \\ 1.4\%$	1.4% 1.7%	

## Conclusions

Monopolistic competition used pervasively

- Our paper: oligopoly...
  - 1. sufficient statistics for micro to macro
  - 2. calibration: concentration amplifies non-neutrality
  - 3. for simple shocks: mostly driven by implied demand shape, rather than strategic interactions
  - 4. more differences with Phillips curve and general shocks