Stock Market Spillovers via the Global Production Network: Transmission of U.S. Monetary Policy*

Julian di Giovanni Federal Reserve Bank of New York ICREA-Universitat Pompeu Fabra Barcelona GSE, CREI and CEPR Galina Hale
U.C. Santa Cruz
Federal Reserve Bank of San Francisco
CEPR

June 26, 2020

Abstract

We quantify the role of global production linkages in explaining spillovers of the U.S. monetary policy shocks to stock returns of 54 sectors in 26 countries. A simple open-economy production network model predicts a spillover pattern consistent with a spatial autoregression framework, which allows us to decompose the overall impact of U.S. monetary policy on stock returns into a direct and a network effect. We find that approximately 60% of the total impact of U.S. monetary policy shocks on average country-sector stock returns are due to the network effect of global production linkages. We further show that U.S. monetary policy shocks have a direct impact predominantly on U.S. sectors and then propagate to the rest of the world through the global production network. Our results are robust to extending our sample to 2000–16 and to controlling for other correlates of the global financial cycle.

Keywords: Global production network, asset prices, monetary policy shocks

JEL Codes: G15, F10, F36

^{*}We are grateful to Margaret Chen, Ted Liu and Youel Rojas, for expert research assistance. We thank the authors of Aquaro et al. (2019) for sharing their Matlab code, and Gianluca Benigno, Vasco Carvalho, Manuel Garcia-Santana, Andrei Levchenko, and Damian Romero for helpful comments. Di Giovanni gratefully acknowledges the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation programme (grant agreement No. 726168), and the Spanish Ministry of Economy and Competitiveness, through the Severo Ochoa Programme for Centres of Excellence in R&D (SEV-2015-0563) for financial support. The views expressed herein are those of the authors and not necessarily those of the Federal Reserve Banks of New York or San Francisco or any other person affiliated with the Federal Reserve System. E-mail (URL): juliandigiovanni@gmail.com (http://julian.digiovanni.ca), gbhale@ucsc.edu (https://sites.google.com/view/galinahale/).

1 Introduction

The recent era of globalization has witnessed (i) greater cross-country integration as firms' production chains have spread across the world (Hummels et al., 2001; Yi, 2003),¹ and (ii) stock market returns becoming more correlated across countries (Dutt and Mihov, 2013). While research has predominantly focused on how *financial* integration has impacted the propagation shocks, such as changes in U.S. monetary policy, across international financial markets (e.g., via a global financial cycle, Rey, 2013), *real* integration also influences these cross-border spillovers. In this paper, we fill a gap in the literature by analyzing how the global production network impacts the transmission of U.S. monetary policy shocks across world stock markets.

To guide our empirical work, we first extend the static production network model proposed by Ozdagli and Weber (2017) to a multi-country setting. In this setting, shocks induced by changes in monetary policy propagate upstream from customers to suppliers. The model structure delivers an empirical specification where the international shock transmission pattern follows a spacial autoregression (SAR) process. We next construct a novel dataset that combines production linkages information from the World Input-Output Database (WIOD, Timmer et al., 2015) with firm-level stock returns worldwide. Using these data, we document a positive relationship between production linkages and stock market co-movements across countries at the country-sector level. We then use a panel SAR to quantify the role of the global production network in transmitting U.S. monetary policy shocks across international stock markets.

U.S. monetary policy shocks through the global production network is statistically significant and accounts for more than half of the total impact. Specifically, average monthly stock returns increase by 0.10 percentage points in response to one percentage point expansionary surprise in the U.S. monetary policy rate, and 60% of this stock return increase is due to the spillovers via global production linkages. U.S. monetary shocks impacts most prominently the domestic sectors – 0.17 percent vs. 0.10 percent for the foreign sample of countries. The impact of the shocks then spills over from the U.S. to foreign markets as U.S. sectors' increased demand propagates upstream to their foreign suppliers. This finding is robust to different time periods and to controlling for other variables that may drive a common financial cycle across markets, such as the VIX, 2-year Treasury rate, and the U.S. dollar Broad Index.

Our static multi-country multi-sector production framework follows the standard closed-economy setup (Acemoglu et al., 2012). Markets are competitive and each sector consists of a representative firm producing with labor and sourcing intermediate inputs from potentially all country-sector cells around the world. To generate non-zero profits (thus stock returns), we build on the closed-economy

¹Johnson and Noguera (2012, 2017) show that as trade barriers declined in recent decades, the share of value added in trade dropped, also indicating longer supply chains.

framework of Ozdagli and Weber (2017) and assume that firms produce using decreasing returns to scale technology and face fixed costs of production. Further, in order to generate monetary non-neutrality, we follow these authors by assuming that money is introduced via a cash-in-advance constraint and wages are preset. To close the model in the multi-country setting, we make two additional assumptions: there is balanced trade and all goods are traded with iceberg trade costs creating a wedge between domestic and foreign sectoral prices.

This theoretical framework delivers the result that firms in all countries will be affected by a monetary shock in a given country. The relative magnitude of the shock's impact will be proportional to a firm's production linkages with the rest of the world and the importance of intermediate products in its production function. Unlike models that focus on technology shocks, which generally propagate downstream from supplier to customer via changes in marginal costs, our model predicts that shocks to the money supply propagate upstream from customer to supplier given changes in customers' demand induced by the monetary policy shock. This change in demand in turns impacts firms profits and thus equity returns.² Finally, we take the input-output (IO) matrix as given, both in the model and in our empirical analysis. We view this assumption as realistic given that we are studying a demand-side shock and the level of aggregation (sector) that we use in our empirical analysis.³

To conduct our regression analysis we make use of the 2016 version of WIOD for input-output data and Thompson Reuters Eikon for stock market information. WIOD provides domestic and global input-output linkages for 56 sectors across 43 countries and a rest of the world aggregate annually for 2000–14. From Eikon we obtain firm-level stock prices, market capitalization, and firms' sector classification. Using the market capitalization as a weight, we construct our own country-sector stock market indexes by aggregating firm-level information to the same industrial sector level as WIOD for 26 of the countries available in WIOD.⁴ The final merged dataset contains monthly country-sector stock returns and annual input-output matrices.⁵ Finally, our baseline analysis uses the 30-minute window U.S. monetary policy shock measures calculated from Federal Funds futures data by Jarociński and Karadi (2020). Because of the global trade collapse in 2008–09 followed by the period of unconventional monetary policy, we limit our analysis to 2000–07 for the baseline analysis. However, our results are robust to other periods.

Using the raw stock market and input-output data, we show that country-sector cells that are

²Our baseline setup assumes Cobb-Douglas production, but using CES production does not change any of the analytical predictions.

³Our empirical results are consistent with this assumption.

⁴We have to start from the firm-level data because there is no one-to-one correspondence between WIOD sector definitions and any of the standard classifications that could be matched to Eikon. The 26 countries in our final sample cover a majority of world production and trade. See Appendix A for details.

⁵While the IO matrices only exist up to 2014, we further extend stock returns data through 2016 given the availability of these data and our baseline monetary policy shock variable. This approach works since we keep fixed the IO matrix for a pre-determined year for the empirical analysis.

more closely connected in the global production network also have more correlated stock returns. This observation remains true even if we exclude same-country cross-sector correlations from this analysis. This empirical regularity suggests that input-output linkages may provide an important channel of shock transmission across global stock markets.

The theoretical framework delivers a SAR structure for our empirical analysis (LeSage and Pace, 2009), where the spatial distance is represented by the coefficients in the global IO matrix. The SAR specification we use, however, is different from a standard one in two ways. First, in addition to the spatial dimension, country-sector in our case, we have a time dimension.⁶ Thus, we have a panel spatial autoregression. Second, we estimate country-sector specific coefficients, which is possible thanks to the time dimension in our panel setting. We estimate this heterogeneous-coefficient panel SAR model using the maximum likelihood methodology in Aquaro et al. (2019), and approximate standard errors using a wild bootstrap procedure.

We find a very robust and quantitatively important role of the global production network in the transmission of the U.S. monetary policy shocks across countries and sectors. Quantitatively, about 60% the total effect of the U.S. monetary policy shock on global stock returns is due to input-output linkages, while the rest is a direct effect. This finding is consistent with the Acemoglu et al. (2016) study that shows that the network-based shock propagation can be larger than a direct effect, as well as similar to what Ozdagli and Weber (2017) find for the response of U.S. stock returns to monetary policy shocks. Both of these studies focus only on the U.S. in a closed-economy setting, while ours incorporates global production linkages. By separating the estimates for sectors in the U.S. from those of foreign sectors, we show that the direct impact of the U.S monetary policy shock is mostly affecting U.S. stock returns, while the magnitude of the direct impact of the U.S monetary policy on foreign stock returns is small and only marginally statistically significant. Foreign stock returns respond to U.S. monetary policy shocks mostly through the network of customer-supplier linkages.

Our results are not sensitive to the choice of a specific time period, especially if we exclude 2008 from the sample. We also show that the year in which the IO matrix is sampled does not affect the result, suggesting very limited, if any, endogenous response of global supply chains to monetary and financial shocks. This result justifies the assumption of an exogenous trade structure in our theoretical framework.

We extend our results by exploring the impact of three global financial cycle correlates: (i)

⁶Because input-output coefficients do not change much over time, we use a static, beginning-of-period IO matrix. We are implicitly assuming that market participants react on the intensive margin of production networks, rather than to the expected changes in production linkages. This assumption is arguably more justifiable at the sector than the firm level. However, trade patterns have changed over time, so we also experiment by varying the weighting matrix for different time periods in our empirical analysis and find that results are not sensitive to these changes.

⁷Note that we use a much coarser level of sectoral aggregation than Ozdagli and Weber (2017), who use detailed U.S. IO matrices from the BEA. Therefore, it should not be surprising that the network contribution in our results tend to be smaller than what they find.

VIX, (ii) 2-year Treasury rate, and (iii) U.S. dollar Broad Index. All three variables, whether included individually or together, have a statistically significant direct and network effects on stock returns worldwide. We find that including the VIX in our spatial autoregression reduces the direct effects of monetary policy shocks on foreign stock returns, while not affecting the direct effect on U.S. domestic returns. This is consistent with the robust evidence in the literature of the global nature of VIX shocks. However, the network effect of the monetary policy shock on foreign returns does not change when including VIX, indicating that the model does a good job in capturing the upstream demand effects generated by the shock. Interestingly, the size of the direct and network effects of VIX is nearly the same for U.S. domestic and foreign stock returns. Furthermore, the 2-year Treasury rate and the U.S. dollar Broad Index do not affect the impact of the U.S. monetary policy shocks.

We explore the cross-country and cross-sector heterogeneity of our estimates of monetary policy shock spillovers. We find that there are no individual countries or sectors in which the spillover effects are concentrated. We document that sectors that are more financially dependent experience total effects from changes in U.S. monetary policy, but the share of the network effect is *smaller* for these sectors. We do not find a strong correlation between the size of spillovers across countries and countries' size, financial openness, or current account, or other country characteristics.

Our finding of the quantitative importance of the global production network in international transmission of U.S. monetary policy shocks to global stock returns at the sector level contributes to several strands of the literature. The first is the growing literature on the international transmission of shocks through production linkages. For example, Burstein et al. (2008), Bems et al. (2010), Johnson (2014), and Eaton et al. (2016), Auer et al. (2019), among others, model and quantify international shock transmission through input trade. Baqaee and Farhi (2019b) and Huo et al. (2020) develop theoretical and quantitative treatments of the international input network model. Boehm et al. (2019) and Carvalho et al. (2016) use a case study of the Tōhoku earthquake to provide evidence of real shock transmission through global and domestic supply chains, while di Giovanni et al. (2018) show the importance of firms' international trade linkages in driving cross-country GDP comovement. None of these studies focus on the transmission of monetary policy shocks, nor stock markets' comovement.

Our paper also contributes to broader literature on international spillovers of U.S. monetary policy by documenting and quantifying the importance of real linkages. Miranda-Agrippino and Rey (2020), among many others, provide evidence which shows that U.S. monetary policy shocks induce comovements in international asset returns. Most analysis of the spillover channels focus on bank lending and, more generally, global bank activity (see, among others, Cetorelli and Goldberg, 2012; Bruno and Shin, 2015b; Avdjiev et al., 2018; Temesvary et al., 2018; Buch et al., 2019; Morais et al., 2019) and a survey by Claessens (2017). Another large group of papers study, more generally,

the impact of U.S monetary policy on international capital flows (see, among others, Bruno and Shin, 2015a; Avdjiev and Hale, 2019). Much less attention has been devoted to real channels, such as international and domestic input-output linkages. Yet we know that real linkages across sectors play an important role in domestic shock transmission (see, among others, Foerster et al., 2011; Acemoglu et al., 2012; Atalay, 2017; Grassi, 2017; Baqaee and Farhi, 2019a). A recent paper by Ozdagli and Weber (2017), to which our paper is most closely related, shows that input-output linkages are quantitatively important for monetary policy transmission in the United States. 9

We bridge the gap between these strands of the literature by showing the importance of real linkages in the international transmission of monetary policy shocks across asset markets. Our paper adds to this literature by showing, on the global scale, the importance of the trade channel in transmitting the U.S. monetary policy shocks, and providing a quantitative estimate of its contribution as well as transmission pattern: from U.S. monetary policy directly to domestic stock returns and through the production network to the rest of the world.

We present a stylized global production model with cross-country monetary policy shock transmission in Section 2, which motivates the empirical model outlined in Section 3. We then describe our data in Section 4, before presenting our empirical results in Section 5. Section 6 concludes.

2 Theoretical Framework

In this section we provide a simple framework to motivate our estimation strategy for studying the transmission of U.S. monetary policy shocks to stock returns internationally via production linkage. The core model is based on the static closed-economy model of sectoral linkages of Acemoglu et al. (2012). In addition, we incorporate three features in order to study the impact of monetary policy shocks on stock returns, as in Ozdagli and Weber (2017): (i) firms produce with decreasing returns to scale and face fixed costs of production, (ii) wages are preset and do not adjust given monetary shocks, and (iii) consumers have cash-in-advance constraints.

We take the technology and trade structure as fixed since we are studying the short run. We make two further assumptions to solve the model analytically. First, we assume that trade is balanced across countries. Second, we assume that prices in a given sector are equal across countries after adjusting for an iceberg trade cost, which varies at the sector and country-pair level.

The world is comprised of N countries and J sectors. Countries are denoted by m and n, and sectors by i and j. The notation follows the convention that for trade between any two country-

⁸Notable exceptions are Brooks and Del Negro (2006), who demonstrate that sensitivity of stock returns to global shocks is related to firms' foreign sales; Todorova (2018), who analyzes the network effect on monetary policy transmission in the European Union; and Du et al. (2019) who study the transmission how countries' (aggregate) trade networks impact asset prices using information from the sovereign CDS market.

⁹Moreover, Bigio and La'O (2019) and Alfaro et al. (2020) show the importance of production linkages in transmitting sectoral shocks and financial frictions to the aggregate economy.

sectors, the first two subscripts always denote exporting (source) country-sector, and the second subscript the importing (destination) country-sector.

2.1 Model Setup

Households. There is a representative household in each country n, which consumes a bundle of goods across all sectors i produced across countries m, and supplies labor in country n, l_n . Its maximization problem is

$$\max_{\{c_{mi,n}\}, l_n} \sum_{i=1}^{J} \sum_{m=1}^{N} b_{mi,n} \log c_{mi,n} - l_n$$

s.t.

$$\sum_{i=1}^{J} \sum_{m=1}^{N} p_{mi,n} c_{mi,n} = w_n l_n + \pi_n + f_n,$$

where $b_{mi,n}$ is a preference parameter for which we assume $\sum_{i=1}^{J} \sum_{m=1}^{N} b_{mi,n} = 1$. Besides wage income, the domestic household's income includes aggregate profits, π_n and aggregate fixed costs, f_n , which firms must pay to produce. Note that in writing the budget constraint we assume balanced trade. Note that aggregate labor supply, profits, and fixed costs are additive across sectors: $l_n = \sum_{j=1}^{J} l_{nj}$, $\pi_n = \sum_{j=1}^{J} \pi_{nj}$, $f_n = \sum_{j=1}^{J} f_{nj}$. Maximization yields the standard first-order conditions, and the consumption-labor trade off: $b_{mi,n}w_n = p_{mi,n}c_{mi,n} \ \forall \ mi, n$.

Technology. There are $j=1,\ldots,J$ sectors in each country $n=1,\ldots,N$. Firms in country-sector nj have the following Cobb-Douglas production function:

$$y_{nj} = z_{nj} l_{nj}^{\alpha_{nj}} X_{nj}^{\lambda_{nj}}, \tag{1}$$

where z_{nj} is a Hicks-neutral technology term, l_{nj} is labor, X_{nj} is a composite intermediate good, and $\alpha_{nj} + \lambda_{nj} < 1$ implying decreasing returns to scale. Given our focus on monetary policy shocks, we simplify notation by assuming that $z_{nj} = 1 \,\forall nj$.

The composite intermediate good is a Cobb-Douglas aggregate of intermediate goods sourced both domestically and abroad from all sectors. Specifically:

$$X_{nj} = \prod_{i=1}^{J} \prod_{m=1}^{N} x_{mi,nj}^{\omega_{mi,nj}},$$
(2)

where $x_{mi,nj}$ is the amount of sector *i*'s good produced in country m used by country-sector nj in final production, and $\omega_{mi,nj}$ is the associated input-output coefficient for country-sector nj usage of the intermediate good from country-sector mi in the aggregate intermediate good, where $\sum_{i=1}^{J} \sum_{m=1}^{N} \omega_{mi,nj} = 1.^{10}$

¹⁰We have also solved the model assuming a CES production structure in labor and the aggregate intermediate good, as well as as CES aggregator underlying intermediate goods. The main results needed to motivate the empirical approach setup do not change qualitatively. The model solution is available upon request.

Given a competitive market structure with wages preset and prices taken as given by each firm, profit maximization for country-sector nj is

$$\max_{l_{nj},\{x_{mi,nj}\}} p_{nj}y_{nj} - \sum_{i=1}^{J} \sum_{m=1}^{N} p_{mi,n}x_{mi,nj} - w_n l_{nj} - f_{nj} \quad \text{s.t. } (1), (2),$$

where p_{nj} is the price of the good produced by sector j in country n, $\{p_{mi,n}\}$ is a vector of prices of goods sold in country n, w_n is the wage in country n, and f_{nj} is a fixed cost of production. We do not model these costs but they may include access to credit or bureaucratic costs, for example. Further, we do not differentiate between fixed costs of production and fixed costs of accessing foreign markets, as is common in the international trade literature.

Solving the firm's maximization problem we can write profits as

$$\pi_{nj} = (1 - \lambda_{nj} - \alpha_{nj})R_{nj} - f_{nj}, \tag{3}$$

where total revenue $R_{nj} = p_{nj}y_{nj}$.

Goods Market Clearing. Global goods market clearing condition for any good mi is given by

$$y_{mi} = \sum_{n=1}^{N} c_{mi,n} + \sum_{j=1}^{J} \sum_{n=1}^{N} x_{mi,nj},$$
(4)

where the first term capture final consumption of good mi across n destination countries, and the second term captures intermediate consumption across nj country-sector destinations. To simplify the market clearing condition we first use the household first-order condition, $\frac{b_{mi,n}}{c_{mi,n}} = \theta p_{mi,n}$ (θ is the Lagrange multiplier), and its budget constraint to express consumption as

$$c_{mi,n} = \frac{b_{mi,n} \sum_{j=1}^{J} (1 - \lambda_{nj}) p_{nj} y_{nj}}{p_{mi,n}}.$$
 (5)

Combining this term and the firm's first-order condition, $\lambda_{nj}\omega_{mi,nj}R_{nj}=p_{mi,n}x_{mi,nj}$, the market clearing condition is

$$y_{mi} = \sum_{j=1}^{J} \sum_{n=1}^{N} \frac{b_{mi,n} (1 - \lambda_{nj}) R_{nj}}{p_{mi,n}} + \sum_{j=1}^{J} \sum_{n=1}^{N} \frac{\lambda_{nj} \omega_{mi,nj} R_{nj}}{p_{mi,n}}.$$
 (6)

Next, multiplying (6) by p_{mi} , and assuming iceberg trade costs $\tau_{mi,n}$ that vary by sector and country pair $(p_{mi,n} = \tau_{mi,n}p_{mi})$, where $\tau_{mi,n} \geq 1$, ¹¹ we express revenues in country-sector mi as:

$$R_{mi} = \sum_{j=1}^{J} \sum_{n=1}^{N} \frac{b_{mi,n} (1 - \lambda_{nj})}{\tau_{mi,n}} R_{nj} + \sum_{j=1}^{J} \sum_{n=1}^{N} \frac{\lambda_{nj} \omega_{mi,nj}}{\tau_{mi,n}} R_{nj}.$$
 (7)

¹¹Note that $\tau_{mi,n}$ may differ depending on the direction of trade; i.e., $\tau_{mi,n}$ need not equal $\tau_{ni,m}$. However, given our empirical definition of trade costs described in Section 4.1, the constructed trade costs are in fact symmetric and are equal to one for trade within the same country.

The above equation characterizes a recursive relationship between sectors' revenues across countries, as well as the the role of different parameters in the model. Note that we are implicitly assuming that these revenues are denominated in a common currency. While we do not incorporate the exchange rate explicitly in this framework, we address this issue in our regression analysis.

Stacking (7) across country-sectors leads to a matrix formulation of the global system of country-sector revenues:

$$(I - \widetilde{\mathbf{\Omega}} \mathbf{\Lambda}) \mathbf{R} = \sum_{j=1}^{J} \sum_{n=1}^{N} \frac{b_{mi,n} (1 - \lambda_{nj})}{\tau_{mi,n}} R_{nj},$$
(8)

where

$$\mathbf{R} \equiv (R_{11}, \dots, R_{NJ})', \qquad NJ \times 1,$$

$$\mathbf{\Lambda} \equiv \operatorname{diag}(\{\lambda_{nj}\}), \qquad NJ \times NJ,$$

$$\widetilde{\mathbf{\Omega}} \equiv \widetilde{\boldsymbol{\tau}} \circ \mathbf{\Omega}, \qquad NJ \times NJ,$$

$$\mathbf{\Omega} \equiv \begin{pmatrix} \omega_{11,11} & \dots & \omega_{11,NJ} \\ \vdots & \ddots & \vdots \\ \omega_{NJ,11} & \dots & \omega_{NJ,NJ} \end{pmatrix}, \qquad NJ \times NJ,$$

$$\widetilde{\boldsymbol{\tau}} \equiv \begin{pmatrix} \left(\frac{1}{\tau_{11,1}}\right) \circ 1_{1 \times J} & \dots & \left(\frac{1}{\tau_{11,N}}\right) \circ 1_{1 \times J} \\ \vdots & \ddots & \vdots \\ \left(\frac{1}{\tau_{NJ,1}}\right) \circ 1_{1 \times J} & \dots & \left(\frac{1}{\tau_{NJ,N}}\right) \circ 1_{1 \times J} \end{pmatrix}, \qquad NJ \times NJ,$$

where \circ represents the Hadamard product, and Ω is the global input-output matrix, where each element of the matrix, $\omega_{mi,nj}$, is the associated input-output coefficient for country-sector nj usage of the intermediate good from country-sector mi in nj's aggregate output.

Money Supply. We introduce money by assuming that consumers face a cash-in-advance constraint as in Ozdagli and Weber (2017); they justify this approach by assuming that firms enter into trade credit relationships, and thus there is no such constraint in the trade of intermediate goods.¹² Specifically, for a given economy n total final consumption is given by

$$\sum_{i=1}^{J} \sum_{m=1}^{N} p_{mi,n} c_{mi,n} = \sum_{i=1}^{J} \sum_{m=1}^{N} b_{mi,n} \sum_{j=1}^{J} (1 - \lambda_{nj}) R_{nj} = \mathcal{M}_n,$$

where \mathcal{M}_n is the domestic money supply in country n and we again see the result of our assumption of balanced trade. Recalling that $\sum_{i=1}^{J} \sum_{m=1}^{N} b_{mi,n} = 1$, we re-write the cash-in-advance constraints

¹²This assumption may be more tenuous in the open-economy context given potential frictions in international trade credit. Given the differences in these frictions across sectors and countries, they are partly incorporated in our iceberg trade costs (Antràs and Foley, 2015; Caballero et al., 2018; Niepmann and Schmidt-Eisenlohr, 2017). The remaining part, not reflected in the model, gives us heterogeneity across countries and sectors in our regression analysis.

for country n as

$$\sum_{j=1}^{J} (1 - \lambda_{nj}) R_{nj} = \mathcal{M}_n. \tag{9}$$

Next, substitute (9) into (8) to arrive at

$$(I - \widetilde{\Omega} \Lambda) \mathbf{R} = \widetilde{b} \mathcal{M}, \tag{10}$$

where $\tilde{\boldsymbol{b}}$ is a $NJ \times N$ matrix composed of elements $\{\tilde{b}_{mi,n}\}$, where $\tilde{b}_{mi,n} \equiv \frac{b_{mi,n}}{\tau_{mi,n}}$, and $\mathcal{M} \equiv (\mathcal{M}_1, \dots, \mathcal{M}_N)'$.

2.2 Network Effects of Money Shocks on Global Stock Returns

To determine the impact of money shocks on global stock returns we will examine deviations of firm profits around their deterministic steady state and only consider a shock to the money supply of one country n (the U.S.).¹³

In particular, for any variable x, define the log deviation from steady-state $\widehat{x} = \log(x) - \log(\overline{x})$ so that $x = \overline{x} \exp(\widehat{x}) \approx \overline{x}(1+\widehat{x})$, where \overline{x} is the steady-state value of x. Further define π to be a $NJ \times 1$ vector composed of elements $\{\pi_{mi}\}$, λ to be a $NJ \times 1$ vector composed of elements $\{\alpha_{mi}\}$, and \mathbf{f} to be a $NJ \times 1$ vector composed of elements $\{f_{mi}\}$. Stacking country-sector profits in (3):

$$\pi = (1 - \lambda - \alpha) \circ \mathbf{R} - \mathbf{f}. \tag{11}$$

Log-linearizing (11) and using (10), we arrive at

$$\widehat{\boldsymbol{\pi}} = \left(I - \widetilde{\boldsymbol{\Omega}} \boldsymbol{\Lambda} \right)^{-1} \boldsymbol{\beta} \widehat{\boldsymbol{\mathcal{M}}}, \tag{12}$$

where $\beta \equiv \operatorname{diag}\left(\left\{\frac{(1-\lambda_{nj})\bar{\mathcal{M}}_n}{\bar{\pi}_{nj}}\tilde{b}_{mi,n}\right\}\right)$ is a $NJ \times N$ matrix.

Allowing for shocks only to the U.S. monetary supply, write (12) as

$$\widehat{\boldsymbol{\pi}} = \left(I - \widetilde{\boldsymbol{\Omega}} \boldsymbol{\Lambda} \right)^{-1} \boldsymbol{\beta}_{US} \widehat{\mathcal{M}}_{US}, \tag{13}$$

where $\beta_{US} \equiv \text{diag}\left(\left\{\frac{(1-\lambda_{US\,j})\bar{\mathcal{M}}_{US}}{\bar{\pi}_{US\,j}}\tilde{b}_{mi,US}\right\}\right)$ is a $NJ \times 1$ vector.

3 Regression Framework

Under the efficient markets hypothesis, a change in stock returns reflects expected change in profits. Thus, the model predicts that a monetary policy shock affects all stock returns in the amount

¹³In equating stock returns with changes in profits, we apply the efficient market hypothesis. Appendix B derives the solution for changes in real output.

proportional to their input-output distance (scaled by trade costs) from the source of the shock. The empirical counterpart to this propagation pattern is a spatial autoregression.

Specifically, holding the parameters of the model fixed, and defining $\mathbf{W} \equiv \widetilde{\mathbf{\Omega}} \mathbf{\Lambda}$, the empirical counterpart of Equation (13) for a given country-sector observation is

$$\widehat{\pi}_{mi,t} = (I - \rho \mathbf{W})^{-1} \beta_{mi} \widehat{\mathcal{M}}_{US,t}, \tag{14}$$

where the subscript t is for the year-month in which a monetary policy shock occurs.¹⁴ ρ and β_{mi} are coefficients that will be estimated. While we can derive an analytical value β_{mi} from the model, we cannot measure it directly. Moreover, the estimate of β_{mi} can be affected by factors that are outside of the model, such as financial openness, level of financial developments, sector's dependence on external financing, and institutional factors. Such factors may also add resistance to the shock transmission through the production network. While the system of equations (13) predicts the pass-through of monetary policy shocks to stock returns perfectly ($\rho = 1$), this need not be the case in practice, which is why we let the data determine the empirical estimate of ρ .

Equation (14) is a representation of a spatial autoregressive process, and can be written in the following vector form:

$$\widehat{\boldsymbol{\pi}}_t = \boldsymbol{\beta} \, \widehat{\mathcal{M}}_{US,t} + \rho \, \mathbf{W} \widehat{\boldsymbol{\pi}}_t,$$

or, adding an error term,

$$\widehat{\boldsymbol{\pi}}_t = \boldsymbol{\beta} \, \widehat{\mathcal{M}}_{US,t} + \rho \, \mathbf{W} \widehat{\boldsymbol{\pi}}_t + \boldsymbol{\varepsilon}_t, \tag{15}$$

where ρ is the spatial autoregressive coefficient, and $\boldsymbol{\beta}$ is a vector of β_{mi} 's.

To allow for barriers to shock propagation to vary across sectors and countries, we extend the SAR model to allow for heterogeneity in the autoregressive coefficient. In particular, like β , we can allow ρ to vary at the mi level:

$$\widehat{\boldsymbol{\pi}}_t = \boldsymbol{\beta} \, \widehat{\mathcal{M}}_{US,t} + \boldsymbol{\rho} \mathbf{W} \, \widehat{\boldsymbol{\pi}}_t + \boldsymbol{\varepsilon}_t, \tag{16}$$

where β and ρ are $NJ \times 1$ vectors of the coefficients to estimate and ε is the $NJ \times 1$ vector of error terms. The time dimension of our data allows us to estimate individual parameters for every country-sector pair. Finally, note that the regression model also includes a set of country-sector specific intercepts.

Additional Controls. The panel SAR model (16) can be extended to include additional controls:

$$\widehat{\boldsymbol{\pi}}_t = \boldsymbol{\beta}_1 \, \widehat{\mathcal{M}}_{US,t} + \boldsymbol{\beta}_2 \, \mathbf{X}_t + \boldsymbol{\rho} \mathbf{W} \, \widehat{\boldsymbol{\pi}}_t + \boldsymbol{\varepsilon}_t, \tag{17}$$

¹⁴FOMC announcements do not occur every month, and at times multiple times within a month. We only include in our sample months with FOMC announcements, but the results are robust to including all months. For moths with multiple announcements, we aggregate all announcement by adding up measures of monetary policy shock.

where \mathbf{X}_t is matrix of additional independent variables. This specification assumes that additional shocks may also impact stock returns both directly and indirectly via the global input-output matrix. We use this specification to examine the robustness of results by including variables related to the global financial cycle that have been found to both correlate with U.S. monetary policy shocks and drive global asset prices.

Inference. Because of the recursive nature of the spacial autoregression model, coefficient β is not equal to the marginal impact of the monetary shock $\widehat{\mathcal{M}}_{US,t}$ on stock returns $\widehat{\pi}_{mi,t}$. Instead, from (14), the $NJ \times 1$ vector of marginal effects is given by

$$Total = (I - \rho W)^{-1} \beta. \tag{18}$$

Following LeSage and Pace (2009) this marginal effect for each mi can be decomposed into a direct effect of the shock and the network effect as

$$Direct = diag(I - \rho W)^{-1}\beta, \tag{19}$$

$$Network = Total - Direct$$
 (20)

where **Direct** and **Network** are $NJ \times 1$ vectors.

Reporting and standard errors. We present our results by reporting simple average values of β , ρ , direct, and network effects across all country-sectors. We also examine the cross-country transmission of monetary policy shocks by splitting the effects into the domestic and international components. Specifically, we compute *international* direct and network effects as averages of the elements of **Direct** and **Network** across all the non-U.S. country-sectors. We take averages of the elements of **Direct** and **Network** over only U.S. sectors in order to compute the U.S.-only direct and network effects.

We compute standard errors for each element of β , ρ , **Direct**, and **Network** as well as their overall, international, and U.S. average values using a wild bootstrap procedure proposed by Mammen (1993). To do so, for each iteration k of the 500 repetitions we replace our dependent variable with a synthetic one that is equal to the fitted values from the main estimation plus a random perturbation ν of the fitted error term:

$$\widehat{\pi}_{mi,t}^{k} = \widehat{\beta}_{mi} \, \widehat{\mathcal{M}}_{US,t} + \widehat{\rho}_{mi} \, \mathbf{W} \widehat{\boldsymbol{\pi}}_{t} + \nu_{mi,t}^{k} \, \varepsilon_{mi,t}.$$

We use a continuous distribution from which we draw perturbations

$$\nu_{mi,t}^{k} = \frac{u_{mi,t}^{k}}{\sqrt{2}} + \frac{1}{2} \left[(v_{mi,t}^{k})^{2} - 1 \right],$$

where u and v are drawn from independent standard normal distributions. We then estimate our regression model replacing true dependent variable with synthetic one and retain estimation results. Standard deviations of each estimated parameter across 500 repetitions are reported as standard errors.

4 Data

We source data from two main datasets: the global production network data are from the World Input-Output Database (WIOD), and the stock market information is from the Thompson-Reuters Eikon database (TREI). The WIOD provides annual data for input-output linkages across 56 sectors and 43 countries and a rest of the world aggregate for 1996–2014. For our analysis, we limit the data to 26 countries with active stock markets and 54 sectors that are connected to each others.¹⁵

From TREI, we obtain end-of-period monthly stock prices, stock market capitalization, and industrial classification for individual companies. We then construct our own stock return indexes for the same sector definitions as used in WIOD, using stock market capitalization of the firm as a weight. This is not straightforward, given that the TREI sector classification uses Thomson-Reuters Business Classification (TRBC), while the World Input-Output Tables are constructed under International Standard Industrial Classification (ISIC) Revision 4. Fortunately, in addition to TRBC, TREI also reports North American Industry Classification System (NAICS) 2007 sector codes for each firm, which we use to create a crosswalk to ISIC Rev. 4. This then allows us to aggregate firms' stock market indices into WIOD-based sectors. ¹⁶ For each of the resulting country-sector cells we construct monthly stock returns as a log change in weighted average of stock prices of all firms in that country-sector cell.

Table A1 presents cross-country sector coverage of monthly returns for the months where there are monetary surprise shocks over 2000–16. Given cross-country differences in size, industrial specialization patterns, and stock market depth we see that larger countries (e.g., the United States) have a larger coverage of sectors, while some countries only cover a few sectors (e.g., Portugal and Russia). These differences motivate a flexible empirical approach, where we allow for country-sector fixed effects as well as country-sector specific coefficients for the effect of the monetary policy shock variable.

4.1 Input-Output Coefficient Construction

The construction of the global input-output matrix using WIOD data is standard and follows from the literature. Denote countries as $m, n \in [1; N]$ and sectors as $i, j \in [1; J]$. WIOD provides infor-

¹⁵The remaining two sectors, household production ("T" in WIOD codes) and extraterritorial organization ("U") are not sufficiently connected to the rest of the network.

¹⁶Even with these data, there is not always 1-to-1 correspondence between the TREI and WIOD codes, and we rectify such instances in a variety of ways as described in Appendix A.

mation of output produced in a given country-sector and where it flows to – both geographical and what sector of the economy (including government and households). We first use this information to build a matrix \mathbf{W} , which is $NJ \times NJ$, where each element $\mathbf{w}_{mi,nj}$ represents the use of inputs from country m sector i as a share of total output of sector j in country n:

$$\mathbf{w}_{mi,nj} = \frac{Sales_{mi \to nj}}{Sales_{nj}}.$$

In network terminology, **W** is the adjacency matrix that gives us direct linkages between each pair of country-sector cells. Because by construction $w_{mi,nj} \in [0;1]$ and $w_{mi,nj} \neq w_{nj,mi}$, the network is weighted and directed. Note that we use all countries and sectors when constructing the adjacency matrix, but only exploit the sub-matrix where we have stock returns in the estimation below. This requires a re-normalization of the matrix for estimation purposes, but all preliminary statistics are based on manipulating the adjacency matrix without this re-normalization.

The W matrix differs from the model-based input-output matrix, Ω , because Ω is constructed using sectors' total input usage rather than total sales. In particular, each element of the matrix Ω is

$$\omega_{mi,nj} = \frac{Sales_{mi \to nj}}{Inputs_{nj}} = \frac{\mathbf{w}_{mi,nj}}{\lambda_{nj}},$$

where recall that λ_{nj} is a country-sector's input share used in production. In other words, $\mathbf{W} = \mathbf{\Omega} \mathbf{\Lambda}$, which is the theoretical and empirical weighting matrices (ignoring trade costs) in (13) and (14).¹⁷

Figure 1 presents the empirical counter cumulative distribution function (CCDF) of the weighted outdegree of \mathbf{W} for WIOD data, where we use the average input-output coefficients over the sample period 2000–14. The weighted distribution for a given country-sector pair mi is defined as:

$$out_{mi} = \sum_{n=1}^{N} \sum_{j=1}^{J} \mathsf{w}_{mi,nj}.$$

The weighted outdegree measures how important a given country-sector's inputs are for production use across all possible country-sector pairs. It is informative to look at this distribution, since a skewed one implies the potential for shocks to propagate and amplify across the production network (Acemoglu et al., 2012). Panel (a) plots the distribution using all possible input-output linkages in the world including both domestic and international linkages in computing the weighted outdegree, while panel (b) exploits only the international linkages. As can be seen in both figures, the distributions are very skewed. The curves were fitted using a Pareto distribution and as can be seen the slopes of the tail are steep, implying that the distributions are fat-tailed. This finding is along the lines of what Carvalho (2014) shows for the U.S. economy using detailed input-output tables from the BEA. In comparing panels (a) and (b), it's worth noting that the x-axis are on two

 $^{^{17}}$ Note that the matrix **W** is initially constructed using the full WIOD sample of countries and sectors. However, only a subset of the matrix will be used for estimation purposes given the availability of returns data, where this spatial matrix is row-normalized to equal one for estimation purposes.

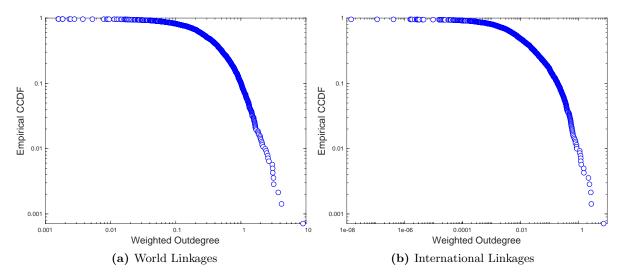


Figure 1. Distribution of Weighted Outdegree for WIOD

Notes: This figure plots the counter cumulative distribution function of the weighted outdegree using the average of the WIOD annual database over 2000–14. The panel with World Linkages is based on the full WIOD table, while the International Linkages panel uses only internationally connected country-sector cells (i.e., we omit the domestic-only linkages across sectors) in constructing the weighted outdegree measure.

different scales. In particular, the international weighted outdegree measures tend to be smaller on average than those using the full world input-output table (which includes domestic linkages) as several country-sector cells are not used as intermediate inputs (or in very tiny amounts) abroad.

Trade Costs. We construct a matrix of trade costs using the methodology of Head and Ries (2001), which relies on observed trade flows. In particular, the index is constructed based on total trade – intermediate and final consumption goods – for a given sector between two countries. The Head-Reis index is a bilateral measure that imposes symmetry in trade costs between countries. Specifically, using the notation from Section 2, we define bilateral iceberg trade costs of good i between countries m and n as

$$\tau_{mi,n} = \sqrt{\frac{X_{mi,n} \times X_{ni,m}}{X_{mi,m} \times X_{ni,n}}},$$

where $X_{mi,n}$ is m's exports to n of good i, and $X_{mi,m}$ is m's internal trade of good i. Similarly for exports from country n.

We calculate $\tau_{mi,n}$ for every country-sector pair in WIOD and create trade cost matrix τ , which we adjust the input-output matrix (**W**) by to create the final weighting matrix for the spatial autoregressions. We use the WIOD trade data for the sample period in constructing both the τ and **W** matrices. Further, note that to eliminate some outliers in τ , we winsorize the final sample matrix at the one percent level.

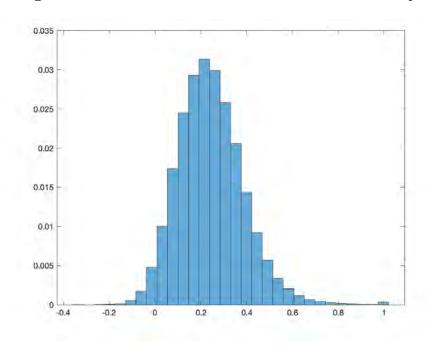


Figure 2. Correlation of Stock Returns over the Entire Sample

Notes: This figure plots the distribution of pairwise correlations of monthly stock returns over 2000–16 across 26 countries and 54 sectors.

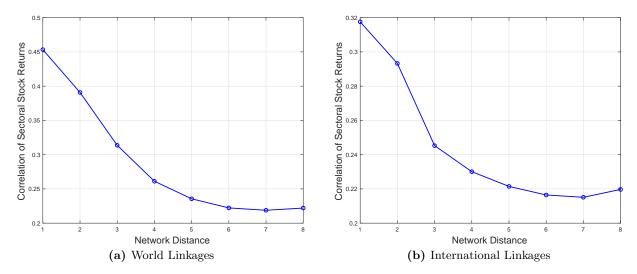
4.2 Returns Data

We next explore our data and show that there is a relationship between stock return correlations and input-output linkages. As described previously, a unit of observation in our data is monthly stock returns in country m and sector i. Because not all sectors are present in all countries, we have stock indexes for 671 out of possible 1404 country-sector cells for each month from January 2000 through December 2016.¹⁸ Figure 2 presents the distribution of pairwise correlations between each possible pair of the 671 time series of stock returns. We can see that most correlations are positive and that the mass of the distribution is between 0 and 0.5.

Returns and the Input-Output Network. Our main goal is to explore whether these stock market correlations are associated with production linkages. To do so, we first compute a measure of distance between each pair of cells. The concept of distance is better defined for binary networks. Thus, for illustrative purposes, we replace $w_{mi,nj} < 0.05$ with 0, and the rest of the cells with 1, converting our network into binary one. In a such a network, the distance between two cells is defined as the length of the shortest path (geodesic).

 $^{^{18}}$ Recall that we have potentially a maximum of 54 sectors and 26 countries. The number of possible country-sectors is further restricted to insure that \mathbf{W} is full rank for estimation purposes, even if stock returns data may exist for some of these country-sectors.

Figure 3. WIOD Network Distance and Correlation of Stock Returns: Supplier Linkages



Notes: This figure plots correlations of monthly stock returns over 2000–16 across 26 countries and 54 sectors on the y-axis, across network distance bins based on the direct bilateral supply linkage using the average of the WIOD annual database over 2000–14. The elements of IO matrix are defined as country-sector mi's usage of country-sector nj's good as an intermediate divided by mi's gross output. The panel with World Linkages is based on the full WIOD table, while the International Linkages panel extracts the correlation and distance variable for only internationally connected country-sector cells (i.e., we omit the domestic-only linkages across sectors).

We use this concept of for each pair of country-sector cells and compare it to the correlation of stock returns for this pair of country-sector cells. Figure 3 plots this relationship, where we compute the average directional distance between any two country-sector cells (i.e., the average distance from $mi \to nj$ and $nj \to mi$) per correlation. Even though the diameter, the longest distance, of the input-output network averaged over time is 23, we only plot distances up to 8 because for any distances longer than that the decline in stock price correlation levels off.

Panel (a), which uses the full set of country-sector cells, we can see that pairs most closely connected through input-output linkages exhibit the highest correlation of stock returns (correlation coefficient of 0.45). The larger is the distance, the lower is the correlation. We can see that it tapers out just below 0.25 for any distance over 4. Panel (b) shows that a similar pattern holds when we exclude from the analysis all domestic sector pairs. This alleviates a concern that our results are driven entirely by domestic input-output linkages and stock return correlations. We can see that even excluding domestic linkages, the country-sector cells that are most highly connected exhibit a strong correlation of stock returns (correlation coefficient of 0.33).

These two figures provide prima facie evidence that two sectors which rely more heavily on each other for the supply of inputs in productions also have more strongly correlated stock returns. However, these bilateral correlations may be driven by numerous transmission channels and are silent on how shocks are transmitted via the overall network.

4.3 Monetary Policy Shocks and Global Financial Cycle correlates

Our baseline measure of U.S. monetary policy shocks is sourced from Jarociński and Karadi (2020). They construct a measure of an interest rate surprise as the change in the 3-month Federal Funds future rate, which they interpret as the expected federal funds rate following the next policy meeting. The change in the futures rate is calculated in the 30-minute window around the time of the Federal Open Market Committee (FOMC) press release, which is 2 p.m. East Coast time on the day of a regular FOMC meeting.¹⁹

We explore robustness of our results to including in the regression other correlates of the global financial cycle, namely VIX, 2-year U.S. Treasury rate, and Broad Dollar Index. VIX is obtained from Federal Reserve Economic Data (FRED). 2-year Treasury rate and Broad U.S. Dollar Index are obtained from the Board of Governors of the Federal Reserve (series H.15 and H.10, respectively).

5 Empirical Results

5.1 Linear regression results

To establish a benchmark, we estimate a simple linear regression that ignores any spatial network effects:

$$\widehat{\pi}_{mi,t} = \alpha + \beta^{LS} \widehat{\mathcal{M}}_{US,t} + \varepsilon_{mi,t}, \tag{21}$$

where α represents either a constant or different sets of fixed effects.

The results of the estimation for the Jarociński and Karadi (2020) shock for 2000–07 sample period are reported in Table $1.^{20}$ The simple OLS estimate in column (1) implies that a one percentage point surprise in the monetary policy shock results in a 0.1 percentage points rise in the average country-sector monthly stock return. The standard errors increase substantially when we cluster them at the monthly (t) level, as reported in column (2), which should be expected given that the monetary policy shock is being repeated for each country-sector return in a given time period of the panel. The magnitude of the effect does not change much whether we control for country, sector, or country-sector fixed effects (column (3)).²¹ We use the country-sector fixed effect specification as our benchmark for linear regression.

Keeping in mind that the model predicts different β s for each mi, we also allow for the β s to vary across country-sectors. This is possible because of the time dimension of our data. First, we estimate a random coefficients model with β s varying across country-sector panels. We find

¹⁹This measure of monetary surprise shocks is common in the literature, and follows the work of Gertler and Karadi (2015).

²⁰The results for other monetary shock measures and other time periods are nearly identical and can be obtained from the authors upon request. The exception is including 2008, which lowers the magnitude of the effect. Because the dependent variable is the stock return, including lagged dependent variable in these regression does not alter the results.

²¹Only results with country-sector fixed effects are reported.

Table 1. Linear Regression Estimation Results, Full Sample

 $\widehat{\pi}_{mi,t} = \alpha + \beta^{LS} \widehat{\mathcal{M}}_{US,t} + \varepsilon_{mi,t}$

	(1)	(2)	(3)	(4)	(5)	(6)
MP shock	-0.102***	-0.102**	-0.103**	-0.083***	-0.098***	-0.136***
(β^{LS})	(0.008)	(0.044)	(0.044)	(0.011)	(0.009)	(0.049)
Constant	0.010***	0.010**	0.010^{*}	0.010***	0.010***	0.010^{*}
	(0.000)	(0.005)	(0.005)	(0.001)	(0.001)	(0.005)
Estimator	OLS	OLS	LS	Random coeffs	Mean Group	LS - country
Fixed effects	None	None	mi	Random	mi	m
St. errors	Regular	Cluster	red on t	Conventional	Group-specific	Clustered on t

Notes: This table reports coefficients from linear regressions where the dependent variable $\widehat{\pi}_{mi,t}$ is the country-sector monthly stock return (country average in column (6)) over 2000–07 in month with FOMC announcements, and the independent variable $\widehat{\mathcal{M}}_{US,t}$ is the measure of the monetary policy shock taken from Jarociński and Karadi (2020). There are 49,667 observations in columns (1)-(5), and 1,716 observations in column (6). Standard errors are in parentheses with *, **, and *** denoting coefficients significantly different from zero at the 1, 5 and 10% levels, respectively.

that the coefficient estimate declines slightly, as shown in column (4). Second, we use a Mean Group estimator (Pesaran and Smith, 1995) with groups defined as country-sector. In this case, the average β is nearly identical to the OLS estimate (column (5)).

Finally, we aggregate stock returns at the country level and estimate a country fixed effects linear regression, reported in column (6). We find that the coefficient for this country-time panel specification is slightly larger (in absolute value).

Table 2 reports the same sets of regressions, splitting the samples to all foreign countries (Panel A) and only the United States (Panel B). The overall point estimate for the international sample is similar to the baseline estimates using the whole sample of Table 1. However, the point estimates for the United States (Panel B) are substantially larger. The fixed effect coefficient in column (3) implies that a one percentage point surprise in monetary loosening is associated with a 0.17 percentage point increase in the average monthly returns across U.S. sectors.²²

The linear regression does not allow for the network structure and therefore β^{LS} combines both direct and network effects. We next turn to the spatial autoregression setup to be able to measure these two effects separately.

²²Note that this point estimate is substantially smaller than the implied impact in Ozdagli and Weber (2017), as well as other event-type studies on the impact of U.S. monetary policy shocks on stock returns. We believe this is due to higher level of aggregation in our data (fewer industries) and possibly attenuation due to our use of monthly frequency data, rather than looking at the returns around the 30-minute window of the FOMC announcement.

Table 2. Linear Regression Estimation Results, International and United States Sub-Samples

$\widehat{\pi}_{mi,t} = \alpha + \beta$	$^{LS}\widehat{\mathcal{M}}_{US,t} +$	$arepsilon_{mi,t}$				
	(1)	(2)	(3)	(4)	(5)	(6)
			Panel	A. Excluding th	e U.S.	
MP shock (β^{LS}) Constant	-0.097*** (0.008) 0.010*** (0.000)	-0.097** (0.045) 0.010** (0.005)	-0.134** (0.045) 0.010* (0.005)	-0.076*** (0.012) 0.010*** (0.001)	-0.092*** (0.010) 0.010*** (0.001)	-0.134*** (0.050) 0.010* (0.005)
			P	anel B. U.S. onl	У	
MP shock (β^{LS}) Constant	-0.171*** (0.019) 0.007*** (0.001)	-0.171*** (0.040) 0.007 (0.004)	-0.171*** (0.040) 0.007* (0.004)	-0.156*** (0.029) 0.007*** (0.001)	-0.179*** (0.023) 0.007*** (0.001)	-0.173*** (0.039) 0.005 (0.004)
Estimator Fixed effects St. errors	OLS None Regular	OLS None Cluste	$\begin{array}{c} \text{LS} \\ mi \\ \text{red on} t \end{array}$	Random coeffs Random Conventional	Mean Group mi Group-specific	LS - country m Clustered on t

Notes: This table reports coefficients from linear regressions where the dependent variable $\widehat{\pi}_{mi,t}$ is the country-sector monthly stock return (country average in column (6)) over 2000–07 in month with FOMC announcements, and the independent variable $\widehat{\mathcal{M}}_{US,t}$ is the measure of the monetary policy shock taken from Jarociński and Karadi (2020). Panel A includes all countries but the United States (25 countries in total, 46,357 observations in columns (1)-(5), 1,650 observations in column (6)), and Panel B includes only the United States (3,310 observations in columns (1)-(5), 66 observations in column (6)). Standard errors are in parentheses with *, **, and *** denoting coefficients significantly different from zero at the 1, 5 and 10% levels, respectively.

5.2 SAR results

We now allow for network effects by estimating a spatial autoregression model (SAR). Effectively, it removes the restriction, imposed by the linear regression framework, of independent panels, i.e. $\rho = 0$ in Equation (15).

The baseline results of the estimation of the SAR model with heterogeneous coefficients (Equation (16)) are presented in Table 3. We allow for country-sector fixed effects following Elhorst (2014). We estimate the regression with maximum likelihood and bootstrap standard errors for all parameters as well as for decompositions, using a wild panel bootstrap with 500 repetitions.

Panel A of Table 3 shows the average values of β , ρ , Direct, Network, and the share of Network in Total across country-sectors. We report averages across all country-sectors, for country-sectors outside of the U.S., and for the U.S. sectors only. The full distribution of these estimates

Table 3. Spatial Autoregression Panel Estimation Results

	Avg. β	Avg. ρ	Avg. Direct	Avg. Network	Network/Total
	(1)	(2)	(3)	(4)	(5)
		Panel	A. Weighting M	Matrix with Trade	Costs
Full sample	-0.027*	0.675***	-0.035**	-0.053***	60%***
	(0.020)	(0.157)	(0.020)	(0.012)	(0.164)
International	-0.023	0.681^{***}	-0.031*	-0.052***	$62\%^{***}$
	(0.020)	(0.158)	(0.019)	(0.020)	(0.045)
USA	-0.080***	0.600***	-0.087***	-0.065**	$42\%^{***}$
	(0.034)	(0.154)	(0.034)	(0.034)	(0.008)
		Panel B	. Weighting Ma	trix without Trad	e Costs
Full sample	-0.019	0.748***	-0.026*	-0.093***	78%***
_	(0.021)	(0.179)	(0.020)	(0.018)	(0.197)
International	-0.016	0.746***	-0.023	-0.091***	80%***
	(0.020)	(0.179)	(0.019)	(0.020)	(0.084)
USA	-0.056*	0.768***	-0.066**	-0.122***	65%***
	(0.005)	(0.010)	(0.000)	(0.005)	(0.047)

Notes: This table reports results from heterogeneous coefficient spatial panel autoregressions where the dependent variable is the country-sector monthly stock return over 2000–07 over month with FOMC announcements, and the independent variable is the measure of the monetary policy shock taken from Jarociński and Karadi (2020). There are 44,286 observations total comprised of 671 country-sectors over 66 months. In Panel B autoregressive weighting matrix \mathbf{W} is replaced with the one that sets all trade costs τ to 1. Standard errors (in parentheses) are obtained via wild bootstrap with 500 repetitions and *, **, and *** denote coefficients significantly different from zero at the 1, 5 and 10% levels, respectively.

(0.033)

(0.035)

(0.047)

(0.035)

(0.212)

are reported in Figure A1. In addition to our benchmark, which accounts for trade costs τ , we estimate an alternative specification, in which τ is set to one for all country-sectors. Effectively, the second specification uses an unweighed input-output matrix, while the benchmark specification weighs the input-output matrix by trade costs. This second specification is reported in Panel B.

We find that for the full sample, about 40% of the average total effect is due to the direct impact of the U.S. monetary policy shock while the rest is due to the production network shock transmission. This is due to a high coefficient of shock propagation ρ , which is on average 0.68. As we would expect, average ρ is less than one, as implied by the model, due to unmodelled resistance to transmission of stock market shocks across the global production network.

Computing the averages for foreign country-sectors and for the U.S. sectors separately, we can see the pattern of transmission of the U.S. monetary policy shock to stock returns globally. We can see a much stronger (2.5 times stronger) direct effect of U.S monetary policy shock on U.S. sectors, which is expected. This direct effect is then propagated through the production network, both globally and domestically. The share of the production network effect for U.S. sectors is only 42%, while for foreign country-sectors it is 62%. In fact, the direct effect of the U.S. monetary policy shock on stock returns in foreign countries is only marginally statistically significant. These results are very intuitive and show that production linkages are very important in transmitting demand shocks at the sector level.²³

Panel B shows that setting all τ to 1 increases the autoregressive coefficient and lowers the direct effect overall as well as for international and U.S. subsamples. That is, not accounting explicitly for trade costs exaggerates the share of shock transmission that is due to the global production network on average. By looking at the distribution of direct and network effects across country-sectors for both sets of estimates reported in panels A and B, as shown in Figure 4, we can see that the amplification of the network effect is due to larger proportion of country-sectors with negative network effects in case when τ is set to 1.

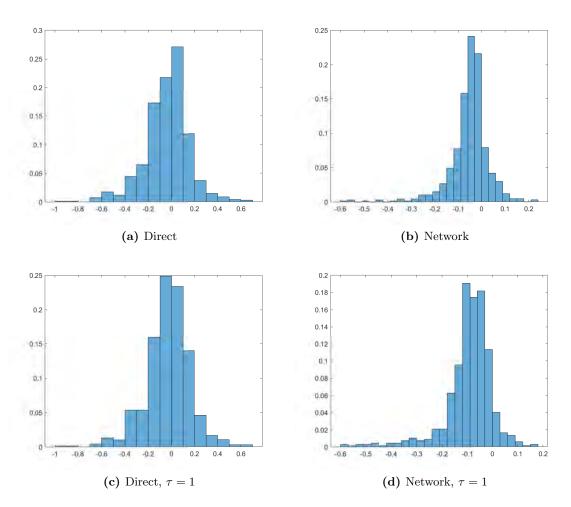
We conjecture that there are two potential reasons that the network effects decline when including trade costs in the spatial weighting matrix. First, the trade costs place greater weights on countries that have larger bilateral trade in a given sector with respect to their total output – i.e., a measure of bilateral sectoral integration. This integration may not match up to how intensely intermediate goods are used for total production, and may therefore dampen the input-output weights. Second, the trade costs are symmetric for a given sector, while the input-output weights are asymmetric. Therefore, introducing the trade costs may create some noise, which will attenuate the estimated impact of the production network.

5.3 Sensitivity to Time Period

So far we have limited our analysis to the 2000–07 time period. Our benchmark estimates are through 2007 for three reasons: first, this period includes a full cycle of monetary policy actions but excludes the effective lower bound period; second, this period ends well prior to the Great Trade Collapse that occurred during the Global Financial Crisis in 2008:H2–2009:H1; third, this period does not include the dramatic decline in global stock prices that followed the collapse of Lehmann Brothers. In our benchmark analysis, as in our model, we take the global production network as given, and therefore we use the input-output coefficients from 2000. It is possible, however, that a rapid increase in trade globalization and the lengthening of global supply chains in the early 2000s may affect our results. Therefore, we want to explore the evolution of our results as we vary the time period and the year from which we sample matrix **W**.

²³We will show that the direct effect on foreign sectors declines further when we explicitly allow for other financial shocks to affect foreign stock returns.





Notes: This figure plots the distribution of **Direct** and **Network** across mi from the estimation of equation $\widehat{\boldsymbol{\pi}}_t = \boldsymbol{\beta} \widehat{\mathcal{M}}_{US,t} + \boldsymbol{\rho} \mathbf{W} \widehat{\boldsymbol{\pi}}_t + \boldsymbol{\varepsilon}_t$ for 2000–07, using Jarociński and Karadi (2020) monetary policy shocks for $\widehat{\mathcal{M}}_{US}$. The averages of these distributions are reported in Table 3.

Table 4 reports just the share of network effect across different variations of the sample for our benchmark regression reported in Panel A of Table 3. A full set of estimates is reported in Table A3. We can see that replacing W measured in 2000 with the average W for 2000–07 does not change the results. This is not surprising given that elements of W are driven by production technologies and a trade structure that do not change very fast.

Next we extend our time period through 2016.²⁴ We can see that the share of the network effect increases dramatically in this extended sample, especially for foreign sectors. However, we can tell that this is driven by the coincidence of monetary policy shocks, stock market crashes, and global

 $^{^{24}}$ While WIOD is only available through 2014, we gather information on all other variables through the end of 2016. To compute average **W** for 2000–16 we simply assume that the WIOD for 2015 and 2016 would be the same as the average 2000–14 WIOD matrix.

Table 4. Spatial Autoregression Panel Estimation Results: Variation over time

Time period	Observations	Year for \mathbf{W}	Share	of network effective	ct
			Full sample	International	USA
2000-07	$44,\!286$	Average 2000–07	59%	62%	40%
			(0.141)	(0.013)	(0.007)
2000-16	$92,\!598$	2000	74%	80%	44%
			(0.349)	(0.240)	(0.124)
2000-16	$92,\!598$	Average 2000–14	77%	84%	43%
			(0.364)	(0.202)	(0.106)
2000-07,09-16	87,230	2000	65%	68%	45%
			(0.181)	(0.101)	(0.108)
2000 - 07,09 - 16	87,230	Average 2000–14	63%	66%	42%
	,		(0.172)	(0.099)	(0.087)

Notes: This table reports networks shares calculated from heterogeneous coefficient spatial panel autoregressions where the dependent variable is the country-sector monthly stock return over 2000–07 over month with FOMC announcements, and the independent variable is the measure of the monetary policy shock taken from Jarociński and Karadi (2020). There are 44,286 observations total comprised of 671 country-sectors over 66 months. In Panel B autoregressive weighting matrix \mathbf{W} is replaced with the one that sets all trade costs τ to 1. Standard errors (in parentheses) are obtained via wild bootstrap with 500 repetitions. All network shares are significant at the 1% level. Full regression results are reported in Table A3.

trade collapse in 2008 – once we exclude 2008 from the sample, our results become very similar to the benchmark. Furthermore, in this extended sample, using average \mathbf{W} instead of \mathbf{W} for 2000 does not make much difference.

5.4 Exploring other Shocks

There is clear evidence in the literature that global stock prices respond to a global financial cycle (Miranda-Agrippino and Rey, 2020). Some movements of the global financial cycle are due to changes in the U.S. monetary policy, while others are market-driven. Here we show the robustness of our results to controlling for such shocks. In our analysis we focus on three variables that are not highly correlated with each other and are easily available: the VIX, the U.S. 2-year Treasury rate, and the U.S. dollar Broad Index. We conduct both LS and SAR analysis and include these variables one at a time and then all together.

Table 5 shows the results of the fixed effects least square regressions for the full sample as well as for subsamples of foreign country-sectors and for the U.S. only. In the interest of space we only present the results with all three additional control variables included for the subsamples – the results do not vary much if we include them individually.²⁵

²⁵The full set of regressions is available upon request.

Table 5. Least-Squares Panel Estimation Results: Other Shocks

 $\widehat{\pi}_{mi,t} = \beta_{MP}^{LS} \widehat{\mathcal{M}}_{US,t} + \beta_X^{LS} \mathbf{X}_t + \varepsilon_{mi,t}$

		Full S	ample		International	USA
	(1)	(2)	(3)	(4)	(5)	(6)
MP shock	-0.061	-0.117**	-0.107**	-0.076	-0.070	-0.152***
	(0.046)	(0.046)	(0.044)	(0.047)	(0.048)	(0.040)
VIX	-0.162***			-0.146***	-0.148***	-0.123***
	(0.037)			(0.036)	(0.036)	(0.031)
T2y		0.146^{*}		0.091^*	0.090^*	0.113^{***}
		(0.077)		(0.047)	(0.049)	(0.035)
USD			-0.546	-0.338	-0.332	-0.417
			(0.363)	(0.290)	(0.297)	(0.281)
R^2	0.060	0.030	0.02	0.070	0.070	0.14
Observations		49,	667		46,357	3,310

Notes: This table reports coefficients from linear regressions where the dependent variable $\widehat{\pi}_{mi,t}$ is the country-sector monthly stock return over 2000–07 in month with FOMC announcements. The independent variables include the measure of the monetary policy shock taken from Jarociński and Karadi (2020) (MP shock), the monthly change in the VIX index (VIX); the 2-year Treasury rate (T2y), and the Broad U.S. Dollar Index (USD). Robust clustered standard errors are in parentheses with *, **, and *** denoting coefficients significantly different from zero at the 1, 5 and 10% levels, respectively.

VIX is shown to be highly correlated with the global financial cycle (Bruno and Shin, 2015a; Miranda-Agrippino and Rey, 2020) and is therefore likely to affect global stock returns given changes in risk aversion and the behavior of financial intermediaries. To the extent that some movements in VIX are correlated with U.S. monetary policy shocks, our benchmark regressions may be attributing some of the effect of VIX to the demand-channel effect of the monetary policy shock that our input-output model predicts. Indeed, when we include VIX in the regression, we find that the impact of the monetary policy shock is smaller than in the benchmark and is no longer statistically significant for the full sample or for foreign country-sectors. The effect of monetary policy shock does remain significant for the U.S. sectors. Consistent with the literature, increases in VIX lower stock market returns worldwide, and by about the same amount in the U.S. and in foreign countries.

Monetary policy can affect stock returns through surprises but it may also have an effect through the level of interest rates, which would not be necessarily reflected in monetary policy shocks. This second effect is likely to be reflected in capital flows (Avdjiev and Hale, 2019). According to the authors, an increase in the policy rate during the lending boom is likely to increase capital flows worldwide, which would imply increases in stock returns globally. Indeed, we find that an increase in the 2-year Treasury rate increases stock returns during our sample period of 2000-07, which

corresponds to a lending boom. Controlling for the 2-year Treasury rate, however, does not change much the impact of the monetary policy shock relative to the benchmark.

In our benchmark analysis we assumed away the explicit effect of exchange rates. Given that the value of the dollar can be affected by monetary policy shocks (Inoue and Rossi, 2019), we want to separate the impact of monetary policy surprises that is orthogonal to exchange rate changes from reaction to the change in the value of the dollar. To do so, we control for the U.S. dollar broad index. We find that the value of the dollar does not have an effect on global stock returns and that controlling for the dollar index does not change our benchmark results. Combining the three additional control variables produces results that are similar to the regression with VIX only, showing, consistent with the literature, that VIX is the dominant driver of the global financial cycle when it comes to global stock returns.

The least-square analysis, as before, does not allow us to separate direct impact from the effect of the global production chain. We would expect that the drivers of the global financial cycle, when omitted, may appear as the direct effect of the U.S. monetary policy. Thus, we include these additional control variables in our benchmark spatial autoregression. The results of this analysis are reported in Table 6. In the interest of space, we only show decomposition into foreign and U.S. sectors for the regression that includes all three controls at once. We also only report **Direct** and **Network** estimates.²⁶

When we control for the VIX, we find that both direct and network effects of monetary policy shocks are reduced and that the impact of the VIX is roughly equally split between direct and network effects. This implies that (a) some of the impact of monetary policy shocks on global stock prices is due to the U.S. monetary policy shocks affecting the global financial cycle, and (b) global production networks are important in stock market shock transmissions regardless of the origin of these shocks even when we control for correlates of the global financial cycle.²⁷ Importantly, when controlling for the VIX, we find that direct effect of the U.S. monetary policy shock is only significant for the U.S. stock returns, and not for full sample or international subsample. However, the network impact of the monetary policy shock remains significant and similar to the baseline results of Table 3. This finding highlights the mechanism of monetary policy shock transmission through customer linkages described in our model, and it suggests that the direct effect for the foreign sample of countries that we found in our benchmark estimation is primarily due to the effect of the U.S. monetary policy on global financial cycle variables, such as the VIX.

Controlling for the 2-year Treasury rate and Broad U.S. dollar Index does not alter our benchmark results, even though both direct and network effects of these controls are statistically significant with the effects going in the same direction as in the linear regression and roughly equally

²⁶Full regression results are available in Tables A4, A5, and A6.

²⁷Note that we only estimate one autoregression coefficient ρ for each country-sector, which them implies transmission of all shocks through the production network.

Table 6. Spatial Autoregression Panel Estimation Results: Other Shocks

 $\widehat{\pi}_{mi,t} = \beta_{MP} \, \widehat{\mathcal{M}}_{US,t} + \beta_X \, \mathbf{X}_t + \boldsymbol{\rho} \, \mathbf{W} \, \widehat{\boldsymbol{\pi}}_t + \varepsilon_{mi,t}$

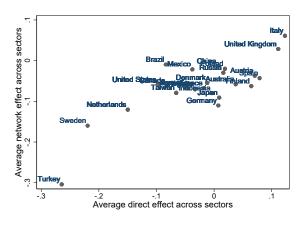
		Full S	ample		International	USA
	(1)	(2)	$\overline{(3)}$	(4)	(5)	(6)
Direct effect of MP	-0.014	-0.035**	-0.029	-0.020**	-0.014	-0.089***
	(0.010)	(0.017)	(0.023)	(0.011)	(0.011)	(0.019)
Network effect of MP	-0.036***	-0.068***	-0.064***	-0.045***	-0.045***	-0.050***
	(0.013)	(0.019)	(0.015)	(0.018)	(0.018)	(0.020)
Direct effect of VIX	-0.063***			-0.058***	-0.058***	-0.051***
	(0.024)			(0.019)	(0.019)	(0.017)
Network effect of VIX	-0.079***			-0.068***	-0.068***	-0.063***
	(0.016)			(0.016)	(0.016)	(0.016)
Direct effect of T2y		0.060**		0.042^{***}	0.041^{***}	0.051^{***}
		(0.027)		(0.014)	(0.013)	(0.016)
Network effect of T2y		0.077^{***}		0.045^{***}	0.045^{***}	0.048***
		(0.027)		(0.013)	(0.017)	(0.019)
Direct effect of USD			-0.150**	-0.101**	-0.091**	-0.212***
			(0.082)	(0.050)	(0.051)	(0.079)
Network effect of USD			-0.343***	-0.155^*	-0.155^*	-0.156*
			(0.088)	(0.106)	(0.106)	(0.118)

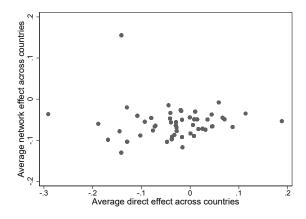
Notes: This table reports direct and network effects from heterogeneous coefficient spatial panel autoregressions where the dependent variable is the country-sector monthly stock return over 2000–07 over month with FOMC announcements, and the independent variable is the measure of the monetary policy shock taken from Jarociński and Karadi (2020). There are 44,286 observations total comprised of 671 country-sectors over 66 months. Standard errors (in parentheses) are obtained via wild bootstrap with 500 repetitions and *, **, and *** denote coefficients significantly different from zero at the 1, 5 and 10% levels, respectively. Full regression results are reported in Table A4-Table A6.

split between direct and network components (once we control for the VIX). As with the linear regression, we find that including all three variables at once produces results similar to those with VIX only. As in our benchmark, we continue to find that for foreign country-sectors most of the monetary policy shock transmission is due to the production network, while for the U.S. sectors the role of the direct effect is larger.

Overall, we find that, while there is clearly some contamination of our benchmark results that arises from omitting correlates of the global financial cycle, especially VIX, our description of the pattern of the monetary policy shock transmission through the global production network remains unchanged: U.S. monetary policy shock has a direct impact predominantly on the U.S. stock returns, which then spreads through production linkages internationally.

Figure 5. Distribution of Direct and Network Effects across Countries and Sectors





- (a) Distribution across countries, sector averages
- (b) Distribution across sectors, country averages

Notes: This figure plots averages of **Direct** and **Network** across i, plotted for each m and averages across m plotted for each i from the estimation of equation $\widehat{\boldsymbol{\pi}}_t = \boldsymbol{\beta} \widehat{\mathcal{M}}_{US,t} + \boldsymbol{\rho} \mathbf{W} \widehat{\boldsymbol{\pi}}_t + \boldsymbol{\varepsilon}_t$ for 2000–07, using Jarociński and Karadi (2020) monetary policy shocks for $\widehat{\mathcal{M}}_{US}$. The overall averages of these distributions are reported in Table 3.

5.5 Heterogeneity of Estimates

We next explore drivers of the observed heterogeneity in the importance of network effects across countries and sectors. Our approach is to analyze the country-sector cross-section of the decomposition of the total effect into direct and network components. We observe that large direct and network effects are not concentrated in specific sectors nor specific countries: Figure 5 plots the average network effect against the average direct effect, where panel (a) computes the average across sectors within countries, and panel (b) computes averages across countries within sectors.

We next consider an important source of sectoral heterogeneity, which may impact the estimated contribution of the network on the total effect of monetary policy: sectoral financial external dependence. To study this issue, we correlate the network effects to a measure of sectoral financial external dependence based on the extension of Rajan and Zingales (1998) to non-manufacturing sectors and computed for 2002–06 by Catão et al. (2009). We find that the network effect is in fact larger for sectors that are *less* financially dependent (Figure 6), indicating that our network estimates are isolating the upstream pass-through of the monetary policy shocks, independently of potential financial shock transmission.

Analyzing the heterogeneity across countries, we did not find any significant correlation of either total, direct, or network effects with country size, financial openness, current account, or other variables we considered. We also compared the average total, direct, and network effects for 16 advanced and 10 emerging economies separately, and found that the differences are not very large and are not statistically significant, with the exception of direct effect, which is twice as large

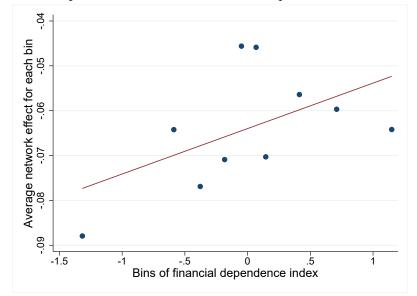


Figure 6. Relationship between External Financial Dependence and Shock Transmission

Notes: This figure plots a bin scatter of the average of the Network from the estimation of equation $\widehat{\boldsymbol{\pi}}_t = \boldsymbol{\beta} \widehat{\mathcal{M}}_{US,t} + \boldsymbol{\rho} \mathbf{W} \widehat{\boldsymbol{\pi}}_t + \boldsymbol{\varepsilon}_t$ for 2000–07, using Jarociński and Karadi (2020) monetary policy shocks for $\widehat{\mathcal{M}}_{US}$ across bins of the Financial Development index from Catão et al. (2009).

on average for emerging economies and the difference is statistically significant at 10% level.

5.6 Robustness Tests

We test for the robustness of our results to alternative measures of stock returns and monetary policy shocks. As a benchmark for our robustness tests we take SAR reported in Panel A of Table 3. In interest of space, we report only the share of network effect in Table 7, with full regression results reported in Table A7.

We begin by replacing nominal stock returns with real stock returns. To do so, we use last quarter's inflation rate for each observation in our sample in order to avoid incorporating any response of inflation to monetary policy shocks into our returns data. We compute real returns as $\widehat{r}\widehat{\pi}_{mi,t} = (1+\widehat{\pi}_{mi,t})/(1+infl_{m,t-1})-1$, where $\widehat{r}\widehat{\pi}_{mi,t}$ is the real stock return, and $infl_{m,t-1}$ is the inflation rate. The results are reported in the top row of Table 7. We find that the share of network effect of monetary policy increases slightly, across all subsamples, but the differences are not large or statistically significant.

Next, we consider three alternative measures of monetary policy shock: those proposed by Bu et al. (2019); Ozdagli and Weber (2017); Nakamura and Steinsson (2018). We find that the share of network effect for the U.S. sectors is slightly larger if we use BRW shocks, but qualitatively our results are very similar to the benchmark.

Table 7. Spatial Autoregression Panel Estimation Results, Robustness

 $\widehat{\pi}_{mi,t} = oldsymbol{eta} \widehat{\mathcal{M}}_{US,t} + oldsymbol{
ho} \, \mathbf{W} \widehat{oldsymbol{\pi}}_t + arepsilon_{mi,t}$

Specification	Share	of network effe	ct
	Full sample	International	USA
Real returns, JK shock	66%	69%	48%
	(0.156)	(0.070)	(0.055)
Nominal returns, BRW shock	67%	69%	60%
	(0.247)	(0.204)	(0.177)
Nominal returns, OW shock	57%	58%	54%
	(0.138)	(0.065)	(0.068)
Nominal returns, NS shock	59%	60%	52%
	(0.188)	(0.145)	(0.117)

Notes: This table reports the network shares calculated from heterogeneous coefficient spatial panel autoregressions where the dependent variable is the country-sector monthly stock return over 2000–07 over month with FOMC announcements, and the independent variable is a measure of the monetary policy shock. The first row uses real equity returns and the 'JK' monetary policy shock from Jarociński and Karadi (2020). Rows two to four use nominal returns but use a different measure of the monetary policy shock taken from: 'BRW' (Bu et al., 2019), 'OW' (Ozdagli and Weber, 2017), and 'NS' (Nakamura and Steinsson, 2018). There are 44,286 observations total comprised of 671 country-sectors over 66 months. Standard errors (in parentheses) are obtained via wild bootstrap with 500 repetitions. All network shares are significant at the 1% level. Full regression results are reported in Table A7.

6 Conclusion

In this paper we quantitatively evaluate the propagation of the U.S. monetary policy shocks to stock returns worldwide through the global production network. Basing our analysis on a multi-country production network model, we estimate a spatial autoregression in a panel setting, which allows for coefficients to vary across countries and sectors. The model predicts country-sectors that are more closely linked to the U.S. via supply linkages will be more affected by U.S. monetary policy shocks.

We find a very robust and quantitatively important role of the production network – over 60% of total impact of U.S. monetary policy shocks on global stock returns is due to production linkages. Among U.S. sectors, the share of the network effect is smaller and the magnitude of the direct effect is substantially larger than for foreign sectors. Our findings thus suggest that U.S. monetary policy shocks directly affect predominantly domestic stock returns and the resulting changes in stock returns propagate globally mainly through production linkages. These findings contribute to the growing literature on the spillovers of the U.S. monetary policy internationally by documenting and quantifying the role of real linkages in global transmission of financial shocks. The pattern we uncover is not affected by allowing for financial channel of U.S. monetary policy shock transmission studied in the literature, namely the global financial cycle.

While our analysis focuses on the transmission of demand shocks along the global production

network, other general equilibrium features of the transmission mechanism of monetary policy shocks, such as the impact of associated exchange rate movements – propagated both upstream and downstream – may play an important role. Examining such issues will require enriching both the current theoretical and empirical frameworks, which we leave for future work.

References

- Acemoglu, Daron, Ufuk Akcigit, and William Kerr, "Networks and the Macroeconomy: An Empirical Exploration," NBER Macroeconomics Annual 2015, 2016, 30, 276–335.
- _ , Vasco M. Carvalho, Asuman Ozdaglar, and Alireza Tahbaz-Salehi, "The Network Origins of Aggregate Fluctuations," *Econometrica*, September 2012, 80 (5), 1977–2016.
- Alfaro, Laura, Manuel García-Santana, and Enrique Moral-Benito, "On the Direct and Indirect Real Effects of Credit Supply Shocks," January 2020. Forthcoming, *Journal of Financial Economics*.
- Antràs, Pol and C. Fritz Foley, "Poultry in Motion: A Study of International Trade Finance Practices," *Journal of Political Economy*, 2015, 123 (4), 853–901.
- Aquaro, Michele, Natalia Bailey, and M. Hashem Pesaran, "Estimation and Inference for Spatial Models with Heterogeneous Coefficients: An Application to U.S. House Prices," October 2019. USC Dornsife Institute of New Economic Thinking Working Paper No. 19-07.
- Atalay, Enghin, "How Important Are Sectoral Shocks?," American Economic Journal: Macroeconomics, October 2017, 9 (4), 254–280.
- Auer, Raphael A., Andrei A. Levchenko, and Philip Sauré, "International Inflation Spillovers through Input Linkages," *Review of Economics and Statistics*, July 2019, 101 (3), 507–521.
- Avdjiev, Stefan and Galina Hale, "U.S. monetary policy and fluctuations of international bank lending," *Journal of International Money and Finance*, 2019, 95, 251 268.
- _ , Cathérine Koch, Patrick McGuire, and Goetz von Peter, "Transmission of monetary policy through global banks: whole policy matters?," August 2018. BIS Working Paper No 737.
- Baqaee, David Rezza and Emmanuel Farhi, "The Macroeconomic Impact of Microeconomic Shocks: Beyond Hulten's Theorem," *Econometrica*, July 2019, 87 (4), 1155–1203.
- _ and _ , "Networks, Barriers, and Trade," August 2019. mimeo, UCLA and Harvard.
- Bems, Rudolfs, Robert C Johnson, and Kei-Mu Yi, "Demand Spillovers and the Collapse of Trade in the Global Recession." *IMF Economic Review*, December 2010, 58 (2), 295–326.
- Bigio, Saki and Jennifer La'O, "Distortions in Production Networks," August 2019. Forthcoming, Quarterly Journal of Economics.
- Boehm, Christoph E., Aaron Flaaen, and Nitya Pandalai-Nayar, "Input Linkages and the Transmission of Shocks: Firm-Level Evidence from the 2011 Tōhoku Earthquake," The Review of Economics and Statistics, 2019, 101 (1), 60–75.
- Brooks, Robin and Marco Del Negro, "Firm-Level Evidence on International Stock Market Comovement," Review of Finance, January 2006, 10 (1), 69–98.
- Bruno, Valentina and Huyn Song Shin, "Capital Flows and the Risk-Taking Channel of Monetary Policy," *Journal of Monetary Economics*, 2015, 71, 119–132.
- $_$ and $_$, "Cross-border banking and global luquidity," Review of Economic Studies, 2015, 82, 525–564.

- Bu, Chunya, John Rogers, and Wenbin Wu, "A Unified Measure of Fed Monetary Policy Shocks," 2019. Finance and Economics Discussion Series 2019-043.
- Buch, Claudia M., Matthieu Bussierè, Linda Goldberg, and Robert Hills, "The international transmission of monetary policy," *Journal of International Money and Finance*, 2019, 91, 29 48.
- Burstein, Ariel, Christopher Kurz, and Linda L. Tesar, "Trade, Production Sharing, and the International Transmission of Business Cycles," *Journal of Monetary Economics*, 2008, 55, 775–795.
- Caballero, Julian, Christopher Candelaria, and Galina Hale, "Bank linkages and international trade," *Journal of International Economics*, 2018, 115, 30 47.
- Carvalho, Vasco M., "From Micro to Macro via Production Networks," *Journal of Economic Perspectives*, Fall 2014, 28 (4), 23–48.
- _ , Makoto Nirei, Yukiko U. Saito, and Alireza Tahbaz-Salehi, "Supply Chain Disruptions: Evidence from the Great East Japan Earthquake'," December 2016. CEPR Discussion Paper DP11711.
- Catão, Luis, Carmen Pagés, and María Fernanda Rosales, "Financial Dependence, Fromal Credit and Informal Jobs: New Evidence from Brazilian Household Data," 2009. IDB Working Paper Series No. IDB-WP-118.
- Cetorelli, Nicola and Linda S. Goldberg, "Banking Globalization and Monetary Transmission," *The Journal of Finance*, 2012, 67 (5), 1811–1843.
- Claessens, Stijn, "Global Banking: Recent Developments and Insights from Research," Review of Finance, 09 2017, 21 (4), 1513–1555.
- di Giovanni, Julian, Andrei A. Levchenko, and Isabelle Mejean, "The Micro Origins of International Business Cycle Comovement," *American Economic Review*, January 2018, 108 (1), 82–108.
- Du, Huancheng, Dong Lou, Christopher Polk, and Jinfan Zhang, "Trade Networks and Asset Prices: Evidence from the SCDS Market," March 2019. Mimeo, Princeton, LSE and Chinese University of Hong Kong.
- Dutt, Pushan and Ilian Mihov, "Stock Market Comovements and Industrial Structure," Journal of Money, Credit and Banking, 2013, 45 (5), 891–911.
- Eaton, Jonathan, Samuel Kortum, Brent Neiman, and John Romalis, "Trade and the Global Recession," *American Economic Review*, November 2016, 106 (11), 3401–38.
- Elhorst, J. Paul, "MATLAB Software for Spatial Panels," *International Regional Science Review*, 2014, 37 (3), 389–405.
- Foerster, Andrew T., Pierre-Daniel G. Sarte, and Mark W. Watson, "Sectoral vs. Aggregate Shocks: A Structural Factor Analysis of Industrial Production," *Journal of Political Economy*, February 2011, 119 (1), 1–38.
- Gertler, Mark and Peter Karadi, "Monetary Policy Surprises, Credit Costs, and Economic Activity," American Economic Journal: Macroeconomics, 2015, 7(1), 44–76.
- Grassi, Basile, "IO in I-O: Size, Industrial Organization, and the Input-Output Network Make a Firm Structurally Important," December 2017. mimeo, Bocconi.
- Head, Keith and John Ries, "Increasing Returns versus National Product Differentiation as an Explanation for the Pattern of U.S.-Canada Trade," *American Economic Review*, September 2001, 91 (4), 858–876.
- Hummels, David, Jun Ishii, and Kei-Mu Yi, "The Nature and Growth of Vertical Specialization in World Trade," *Journal of International Economics*, June 2001, 54, 75–96.

- Huo, Zhen, Andrei A Levchenko, and Nitya Pandalai-Nayar, "International Comovement in the Global Production Network," February 2020. NBER Working Paper 25978.
- Inoue, Atsushi and Barbara Rossi, "The effects of conventional and unconventional monetary policy on exchange rates," *Journal of International Economics*, 2019, 118, 419 447.
- Jarociński, Marek and Peter Karadi, "Deconstructing Monetary Policy Surprises The Role of Information Shocks," American Economic Journal: Macroeconomics, April 2020, 12 (2), 1–43.
- Johnson, Robert C., "Trade in Intermediate Inputs and Business Cycle Comovement," *American Economic Journal: Macroeconomics*, October 2014, 6 (4), 39–83.
- _ and Guillermo Noguera, "Accounting for intermediates: Production sharing and trade in value added," Journal of International Economics, 2012, 86 (2), 224 236.
- _ and _ , "A Portrait of Trade in Value-Added over Four Decades," The Review of Economics and Statistics, 2017, 99 (5), 896–911.
- LeSage, James and Robert Kelley Pace, Introduction to Spatial Econometrics, 1 ed., New York, NY: CRC Press, January 2009.
- Mammen, Enno, "Bootstrap and Wild Bootstrap for High Dimensional Linear Models," Annals of Statististics, 03 1993, 21 (1), 255–285.
- Miranda-Agrippino, Silvia and Hélène Rey, "U.S. Monetary Policy and the Global Financial Cycle," May 2020. Forthcoming, Review of Economic Studies.
- Morais, Bernardo, José-Luis Peydró, Jessica Roldán-Pe na, and Claudia Ruiz-Ortega, "The International Bank Lending Channel of Monetary Policy Rates and QE: Credit Supply, Reach-for-Yield, and Real Effects," *Journal of Finance*, 2019, 74 (1), 55–90.
- Nakamura, Emi and Jón Steinsson, "High-Frequency Identification of Monetary Non-Neutrality: The Information Effect," *The Quarterly Journal of Economics*, 01 2018, 133 (3), 1283–1330.
- Niepmann, Friederike and Tim Schmidt-Eisenlohr, "International trade, risk and the role of banks," *Journal of International Economics*, 2017, 107, 111 126.
- Ozdagli, Ali and Michael Weber, "Monetary Policy through Production Networks: Evidence from the Stock Market," May 2017. NBER Working Paper No. 23424.
- Pesaran, M.Hashem and Ron Smith, "Estimating long-run relationships from dynamic heterogeneous panels," *Journal of Econometrics*, 1995, 68 (1), 79 113.
- Rajan, Raghuram and Luigi Zingales, "Financial dependence and growth," American Economic Review, June 1998, 88 (3), 559–586.
- Rey, Hélène, "Dilemma not Trilemma: The Global Financial Cycle and Monetary Policy Independence," 2013. Jackson Hole Conference Proceedings, Federal Reserve Bank of Kansas City.
- Temesvary, Judit, Steven Ongena, and Ann L. Owen, "A global lending channel unplugged? Does U.S. monetary policy affect cross-border and affiliate lending by global U.S. banks?," *Journal of International Economics*, 2018, 112, 50 69.
- Timmer, Marcel P., Erik Dietzenbacher, Bart Los, Robert Stehrer, and Gaaitzen J. de Vries, "An Illustrated User Guide to the World Input-Output Database: the Case of Global Automotive Production," *Review of International Economics*, August 2015, 23 (3), 575–605.
- Todorova, Zornitsa, "Network Effects of Monetary Policy: Evidence from Global Value Chains," 2018. Mimeo, Bocconi University.
- Yi, Kei-Mu, "Can Vertical Specialization Explain the Growth of World Trade?," *Journal of Political Economy*, February 2003, 111 (1), 52–102.

Appendix A Linking sector classifications

TREIs data are available under Thomson Reuters Business Classification(TRBC), but the World Input-Output Tables (WIOT) have been constructed under ISIC Revision 4.

We take advantage of the fact that TREI reports both 10-digit TRBC activity codes and 6-digit NAICS 2007 codes for all equity prices. With this information one can use a concordance from NAICS 2007 to ISIC Rev. 4 to match each firm's information to WIOT codes. In the next step, one can use the firm-level information from TREI data to construct alternative sector-specific stock price indices that are consistent with WIOT sector definitions.

However, a mapping from NAICS2007 to WIOT16 codes (2-digit ISIC Rev 4) is not perfect, as there can be many-to-many correspondences between NAICS 2007 and ISIC Rev. 4 codes. The following figure shows an example of a possible 'rear' overlapping of NAICS2007 sectors (3-digit code) in a WIOT2016 code.

wiot16code	wiot16 description	naics07_3d	naics07_3d_name	naics07_2d	naics07_2d_name
В	Mining and quarrying	211	Oil and Gas Extraction	21	Mining, Quarrying, and Oil and Gas Extraction
В	Mining and quarrying	212	Mining (except Oil and Gas)	21	Mining, Quarrying, and Oil and Gas Extraction
В	Mining and quarrying	213	Support Activities for Mining	21	Mining, Quarrying, and Oil and Gas Extraction
В	Mining and quarrying	311	Food Manufacturing	31-33	Manufacturing

In this example, the WIOT2016 Code B (Mining and quarrying) besides mining and oil sectors, it also contains the NAICS2007-Food Manufacturing sector. This occurs because the NAICS2007 sector "311942-Spice and Extract Manufacturing" from the Food Manufacturing includes the "mining and processing of table salt" activity, that is classified as a Mining activity in ISIC Rev. 4.

A.1 A reduced version of the NAICS 2007 to ISIC Rev. 4 correspondence

To limit similar occurrences as in the one in the previous example, a new version of the NAICS 2007 to ISIC Rev. 4 correspondence is constructed. The objective is to reduce the number of very different 4-digit ISIC Rev. 4 sectors per each 6-digit NAICS 2007 sector. With that in mind, the next steps were followed:

- 1. Work only on the set of 6-digit NAICS 2007 codes that (i) have more than one 2-digit ISIC Rev. 4 sector, and/or (ii) have more than one WIOT16 sector.
- 2. For a single 6-digit NAICS 2007 code, compute the frequency of its corresponding multiple 4-digit ISIC Rev. 4 sectors. When possible, the following principles were taken into consideration to assign one single NAICS 2007 code to a single 2-digit sector, the predominant sector.
- 3. Frequency criteria: If a 2-digit ISIC Rev. 4 sector represents more than 60 percent of the 6-digit NAICS 2007 sector in consideration, it is the called the predominant sector.

Example: The following example shows the corresponding multiple ISIC Rev. 4 codes for the single 6-digit NAICS 2007 sector "Paper (except Newsprint) Mill":

naics2007	naics2007_name	type match	isic4	isic4_name
322121	Paper (except	keep	1709	Manufacture of other articles of paper and paperboard
	Newsprint) Mills	keep	1701	Manufacture of pulp, paper and paperboard
		keep	1702	Manufacture of corrugated paper and paperboard and of containers of paper and paperboard
		delete	2399	Manufacture of other non-metallic mineral products n.e.c. (tar paper made in paper mills.)

The frequency of the 2-digit ISIC Rev. 4 sector "17-Manufacture of paper and paper products" is 75 percent and it is the predominant sector. The other 2-digit ISIC Rev. 4 sector, "23- Manufacture of other non-metallic mineral products", is not predominant and its deleted from the concordance. Note that for this sector its 2-digit ISIC Rev. 4 meaning is very different from the 3-digit NAICS 2007 meaning too ("322-Paper Manufacturing").

Closest sector criteria: When the frequency criteria is not sufficient, the predominant sector is chosen by a comparison of meanings between the single 6-digit NAICS 2007 code and its corresponding 4-digit ISIC Rev. 4 codes. Then, the ISIC Rev. 4 sector with the closest meaning to the NAICS 2007 sector is selected as the predominant sector. The meaning of aggregate codes (3-digit NAICS 2007 and 2-digit ISIC Rev. 4) helped also to decide, when the comparison of 6-digit NAICS and 4-digits ISIC Rev. 4 meanings were not clear enough to reach a decision.

Example: The following example shows the corresponding multiple 4-digit ISIC Rev. 4 codes for the single 6-digit NAICS 2007 sector "Carbon and Graphite Product Manufacturing"

naics2007		isic4		naics2007_3digit	isic4_2digit
	200	2790	Manufacture of other electrical equipment	Electrical Equipment, Appliance, and Component Manufacturing	Manufacture of electrical equipment
335991	Carbon and Graphite Product Manufacturing	2399	Manufacture of other non-metallic mineral products n.e.c.	Electrical Equipment, Appliance, and Component Manufacturing	Manufacture of other non-metallic mineral products

Although by frequency the two 4-digit (and 2-digit) ISIC Rev. 4 sectors are equally representative for this NAICS 2007 code, their sector meanings are different. In fact, the 6-digit NAICS 2007 "335991-Carbon and Graphite Product Manufacturing" is closest to the 4-digit ISIC Rev. 4 "2399-Manufacture of other non-metallic mineral products n.e.c." than to the 4-digit ISIC Rev. 4 "2790-Manufacture of other electrical equipment" sector. Then, the 2-digit ISIC Rev. 4 "27-Manufacture of electrical equipment" is denominated the predominant sector.

There was only one exception, NAICS 2007 "337920-Blind and Shade Manufacturing". As it can be observed below, none of the previous criteria worked; and it was hard coded arbitrarily based on its 3-digit NAICS 2007 meaning, "Furniture and Related Product Manufacturing", to the 2-digit ISIC Rev. 4 "3100-Manufacture of furniture" sector.

naics2007	isic4	isic4_name	naics2007_3digit	isic4_2digit
Blind and 337920 Shade Manufacturing	1392	Manufacture of made-up textile articles, except apparel		"Manufacture of textiles"
	1629	Manufacture of other products of wood; manufacture of articles of cork, straw and plaiting materials	Furniture and	"Manufacture of wood and of products of wood and cork, except furniture; manufacture of articles of straw and plaiting materials"
	2220	Manufacture of plastics products	Related Product Manufacturing	"Manufacture of rubber and plastics products"
	2593	Manufacture of cutlery, hand tools and general hardware		"Manufacture of fabricated metal products, except machinery and equipment"
	2599	Manufacture of other fabricated metal products		"Manufacture of fabricated metal products, except machinery and equipment"

Once this new NAICS 2007 to ISIC Rev. 4 concordance was finished, it was easy to go from NAICS 2007 to WIOT16. In the final NAICS 2007-WIOT16 concordance:

- 1020 correspondences were tagged based on the official NAICS 2007-ISIC Rev. 4 concordance.
- 37 correspondences were tagged based on the frequency criteria.
- 122 correspondences were tagged based on the closest sector criteria.
- 1 correspondence was arbitrarily hard coded.

Table A1 presents cross-country sector coverage of monthly returns for the months where there are monetary surprise shocks over 2000–14. Given cross-country differences in size, industrial specialization patterns, and stock market depth we see that larger countries (e.g., the United States) have a larger coverage of sectors, while some countries only cover a few sectors (e.g., Portugal and Russia). These differences motivate a flexible empirical approach, where we allow for country-sector fixed effects as well as country-sector specific coefficients for the effect of monetary policy surprise variable.

Table A2 presents coverage of monthly returns for the months where there are monetary surprise shocks along the sector dimension. This table shows how the distribution of sector returns varies across countries. For example, all countries have returns for the 'Construction,' 'Telecommunication,' and 'Financial service activities, except insurance and pension funding' sectors. Meanwhile, sectors like 'Forestry and logging,' 'Fishing and aquaculture,' and 'Repair and installation of machinery and equipment' have sparse stock returns coverage across countries.

Table A1. Monthly Country Stock Return Coverage for Months with Monetary Surprise Shocks

Country	No. Industries	Observations
Australia	38	5,893
Austria	15	2,477
Brazil	17	3,781
Canada	38	5,803
China	47	6,735
Germany	28	4,841
Denmark	17	2,525
Spain	24	3,783
Finland	22	3,410
France	38	$5,\!542$
United Kingdom	40	5,954
Greece	10	1,943
Indonesia	18	3,220
India	40	5,690
Italy	22	4,370
Japan	45	6,706
Korea	34	6,108
Mexico	14	2,401
Netherlands	20	2,895
Poland	17	3,266
Portugal	8	1,209
Russia	5	1,419
Sweden	29	$4,\!584$
Turkey	21	3,887
Taiwan	29	4,675
United States	50	6,982

Notes: This table presents information on the number of sectors and observation of monthly sector returns per country for dates where there are monetary surprise shocks (FOMC meetings or off-cycle meetings) over 2000–16. The data are constructed by merging stock returns data from TREI with the WIOD classification of sectors.

Table A2. Monthly Sector Stock Return Coverage for Months with Monetary Surprise Shocks

Industry	WIOD code	No. countries	Observations
Crop and animal production, hunting and related service activities	A01	13	1,614
Forestry and logging	A02	3	348
Fishing and aquaculture	A03	6	626
Mining and quarrying	В	19	2,593
Manufacture of food products, beverages and tobacco products	C10-C12	23	3,174
Manufacture of textiles, wearing apparel and leather products	C13-C15	16	2,167
Manufacture of wood and of products of wood and cork, etc	C16	10	1,196
Manufacture of paper and paper products	C17	19	2,504
Printing and reproduction of recorded media	C18	8	1,034
Manufacture of coke and refined petroleum products	C19	20	2,623
Manufacture of chemicals and chemical products	C20	25	3,251
Manufacture of basic pharmaceutical products and pharmaceutical preparations	C21	20	2,513
Manufacture of rubber and plastic products	C22	18	2,370
Manufacture of other non-metallic mineral products	C23	18	2,488
Manufacture of basic metals	C24	24	3,129
Manufacture of fabricated metal products, except machinery and equipment	C25	14	1,724
Manufacture of computer, electronic and optical products	C26	22	3,036
Manufacture of electrical equipment	C27	16	2,044
Manufacture of machinery and equipment n.e.c.	C28	19	2,519
Manufacture of motor vehicles, trailers and semi-trailers	C29	20	2,708
Manufacture of other transport equipment	C30	17	2,181
Manufacture of furniture; other manufacturing	C31-C32	17	2,219
Repair and installation of machinery and equipment	C33	1	84
Electricity, gas, steam and air conditioning supply	D35	22	2,874
Water collection, treatment and supply	E36	6	740
Sewerage; waste collection, treatment and disposal activities; etc	E37-E39	9	1,111
Construction	F	26	3,526
Wholesale and retail trade and repair of motor vehicles and motorcycles	G45	12	1,522
Wholesale trade, except of motor vehicles and motorcycles	G46	19	2,537
Retail trade, except of motor vehicles and motorcycles	G47	24	3,136
Land transport and transport via pipelines	H49	17	1,957
Water transport	H50	9	1,138
Air transport	H51	19	2,318
Warehousing and support activities for transportation	H52	19	2,245
Postal and courier activities	H53	8	796
Accommodation and food service activities	I	19	2,483
Publishing activities	J58	18	2,358
Motion picture, video and television programme production, etc	J59-J60	16	2,104
Telecommunications	J61	26	3,563
Computer programming, consultancy and related activities; info; etc	J62-J63	21	2,794
Financial service activities, except insurance and pension funding	K64	26	3,508
Insurance, reinsurance and pension funding, except compulsory social security	K65	21	2,613
Activities auxiliary to financial services and insurance activities	K66	22	2,491
Real estate activities	L68	23	2,930
Legal and accounting activities; activities of head offices; etc	M69-M70	10	1,036
Architectural and engineering activities; technical testing and analysis	M71	16	2,004
Scientific research and development	M72	13	1,575
Advertising and market research	M73	10	1,182
Other professional, scientific and technical activities; veterinary activities	M74-M75	7	848
Administrative and support service activities	N	18	2,248
Education	P85	7	831
Human health and social work activities	Q	13	1,445
Other service activities	R-S	17	2,037

Notes: This table presents information on the number of sectors and observation of monthly sector returns per sector for dates where there are monetary surprise shocks (FOMC meetings or off-cycle meetings) over 2000–16. The data are constructed by merging stock returns data from TREI with the WIOD classification of sectors.

Appendix B Solving for Equilibrium Output

Solving for the Price Level We first derive the price level of a country-sector pair in two-stages given a firm's minimization problem, where the nested intermediate goods allow us to do this. The top-level minimization problem is:

$$\min_{l_{nj}, X_{nj}} P_{nj} X_{nj} + w_n l_{nj} \quad \text{s.t. } (1) = 1,$$

where P_{nj} is an aggregate price level of the underlying country-sector intermediates source by nj, which will be solved for in the second step.

The first-order-conditions are, given a Lagrangian multiplier, μ :

$$w_n = \mu \alpha_{nj} l_{nj}^{\alpha_{nj}-1} X_{nj}^{\lambda_{nj}}, \tag{B.1}$$

$$P_{nj} = \mu \lambda_{nj} l_{nj}^{\alpha_{nj}} X_{nj}^{\lambda_{nj}-1}, \tag{B.2}$$

$$y_{nj} = l_{nj}^{\alpha_{nj}} X_{nj}^{\lambda_{nj}}. \tag{B.3}$$

Dividing (B.1) by (B.2) and re-arranging:

$$\frac{w_n l_{nj}}{P_{nj} X_{nj}} = \frac{\alpha_{nj}}{\lambda_{nj}},$$

$$\Rightarrow X_{nj} = \left(\frac{w_n}{P_{nj}}\right) \left(\frac{\lambda_{nj}}{\alpha_{nj}}\right) l_{nj}.$$

Substituting X_{nj} into the production function we have:

$$y_{nj} = \left[\left(\frac{w_n}{P_{nj}} \right) \left(\frac{\lambda_{nj}}{\alpha_{nj}} \right) \right]^{\lambda_{nj}},$$

which solving for labor yields:

$$l_{nj} = y_{nj}^{\frac{1}{\alpha_{nj} + \lambda_{nj}}} \left[\left(\frac{P_{nj}}{w_n} \right) \left(\frac{\alpha_{nj}}{\lambda_{nj}} \right) \right]^{\frac{\lambda_{nj}}{\alpha_{nj} + \lambda_{nj}}}, \tag{B.4}$$

and plugging this value into the production function to solve out for the intermediate good:

$$X_{nj} = \left(\frac{w_n}{P_{nj}}\right)^{\frac{\alpha_{nj}}{\alpha_{nj} + \lambda_{nj}}} \left(\frac{\lambda_{nj}}{\alpha_{nj}}\right) y_{nj}^{\frac{1}{\alpha_{nj} + \lambda_{nj}}} \left(\frac{\alpha_{nj}}{\lambda_{nj}}\right)^{\frac{\lambda_{nj}}{\alpha_{nj} + \lambda_{nj}}}.$$
 (B.5)

Plugging (B.4) and (B.5) into the cost minimization function we have, where set $y_{nj} = 1$:

$$C(l_{nj}, X_{nj}) = y_{nj}^{\frac{1}{\alpha_{nj} + \lambda_{nj}}} \left(w_n^{\alpha_{nj}} P_{nj}^{\lambda_{nj}} \right)^{\frac{1}{\alpha_{nj} + \lambda_{nj}}} \left[\left(\frac{\alpha_{nj}}{\lambda_{nj}} \right)^{\frac{\lambda_{nj}}{\alpha_{nj} + \lambda_{nj}}} + \left(\frac{\lambda_{nj}}{\alpha_{nj}} \right)^{\frac{\alpha_{nj}}{\alpha_{nj} + \lambda_{nj}}} \right].$$
 (B.6)

The next step is to solve for P_{nj} as a function of the prices of the underlying intermediate goods. We do this by minimizing the cost of building on unit of the composite intermediate, X_{nj} . I.e.,:

$$\min_{\{x_{mi,nj}\}} \sum_{i=1}^{J} \sum_{m=1}^{N} p_{mn,i} x_{mi,nj} \quad \text{s.t. } (2) = 1.$$

The first-order-condition for every good $x_{mi,nj}$ given a Lagrange multiplier, μ , is:

$$p_{mn,i} = \mu \omega_{mi,nj} x_{mi,nj}^{\omega_{mi,nj}-1} \underbrace{\left(\prod_{k=1}^{J} \prod_{l=1}^{N} x_{kl,nj}^{\omega_{kl,nj}}\right)}_{lk \neq mi}$$
(B.7)

$$X_{nj} = \prod_{i=1}^{J} \prod_{m=1}^{N} x_{mi,nj}^{\omega_{mi,nj}}.$$
 (B.8)

Taking the ratio between (B.7) for $p_{mn,i}$ and $p_{ln,k}$ (as an example), we have:

$$\frac{p_{mn,i}}{p_{ln,k}} = \frac{\omega_{mi,nj}}{\omega_{mk,nj}} \frac{x_{ln,kj}}{x_{mn,ij}},$$

$$\Rightarrow x_{mi,nj} = \left(\frac{\omega_{mi,nj}}{\omega_{mk,nj}}\right) \left(\frac{p_{ln,k}}{p_{mn,i}}\right) x_{lk,nj}.$$

Substituting $x_{mn,ij}$ into the intermediate aggregate function we have:

$$X_{nj} = \frac{p_{ln,k} x_{lk,nj}}{\omega_{lk,nj}} \prod_{i=1}^{J} \prod_{m=1}^{N} \left(\frac{\omega_{mi,nj}}{p_{mn,i}} \right)^{\omega_{mi,nj}},$$

which solving for the input $x_{lk,nj}$ yields:

$$x_{lk,nj} = X_{nj} \frac{\omega_{lk,nj}}{p_{ln,k}} \prod_{i=1}^{J} \prod_{m=1}^{N} \left(\frac{\omega_{mi,nj}}{p_{mn,i}}\right)^{-\omega_{mi,nj}}.$$
(B.9)

We then multiply (B.9) by its respective price level and sum over all lk pairs to solve for the price-level (cost) of one unit of X_{nj} :

$$P_{nj} = \sum_{k=1}^{J} \sum_{l=1}^{N} p_{lk,n} x_{lk,nj}$$

$$= \prod_{i=1}^{J} \prod_{m=1}^{N} \left(\frac{p_{mn,i}}{\omega_{mi,nj}} \right)^{\omega_{mi,nj}}.$$
(B.10)

Finally, plugging (B.10) into (B.6) we have the final cost function, which equals marginal cost:

$$C(l_{nj}, \{x_{mi,nj}\}) = g(\alpha_{nj}, \lambda_{nj}) \left(y_{nj}^{\frac{1}{\alpha_{nj} + \lambda_{nj}}}\right) \left(w_n^{\alpha_{nj}} \left[\prod_{i=1}^J \prod_{m=1}^N \left(\frac{p_{mn,i}}{\omega_{mi,nj}}\right)^{\omega_{mi,nj}}\right]^{\lambda_{nj}}\right)^{\frac{1}{\alpha_{nj} + \lambda_{nj}}}, \quad (B.11)$$

where
$$g(\alpha_{nj}, \lambda_{nj}) = \left[\left(\frac{\alpha_{nj}}{\lambda_{nj}} \right)^{\frac{\lambda_{nj}}{\alpha_{nj} + \lambda_{nj}}} + \left(\frac{\lambda_{nj}}{\alpha_{nj}} \right)^{\frac{\alpha_{nj}}{\alpha_{nj} + \lambda_{nj}}} \right].$$

This implies that marginal costs are

$$MC_{nj} = \tilde{g}(\alpha_{nj}, \lambda_{nj}) \left(y_{nj}^{\frac{1 - \alpha_{nj} - \lambda_{nj}}{\alpha_{nj} + \lambda_{nj}}} \right) \left(w_n^{\alpha_{nj}} \left[\prod_{i=1}^J \prod_{m=1}^N \left(\frac{p_{mn,i}}{\omega_{mi,nj}} \right)^{\omega_{mi,nj}} \right]^{\lambda_{nj}} \right), \tag{B.12}$$

where $\tilde{g}(\alpha_{nj}, \lambda_{nj}) = \frac{1}{\alpha_{nj} + \lambda_{nj}} g(\alpha_{nj}, \lambda_{nj}).$

Firms in sector nj will set their price to equal (B.12). Further, given the assumption we make below on relative prices across countries, $p_{mn,i} = \tau_{mn,i}p_{mi}$, it follows that there will be $N \times J$ prices to solve for in equilibrium, along with N-1 wages.

Solving for Output First, set the price of a firm's good, p_{nj} equal to log of its marginal cost (B.12):

$$\ln p_{nj} = B_{nj} + \frac{1 - \alpha_{nj} - \lambda_{nj}}{\alpha_{nj} + \lambda_{nj}} \ln y_{nj} + \frac{\alpha_{nj}}{\alpha_{nj} + \lambda_{nj}} \ln w_n + \frac{\lambda_{nj}}{\alpha_{nj} + \lambda_{nj}} \sum_{i=1}^{J} \sum_{m=1}^{N} \omega_{mi,nj} \tau_{mn,i} \ln p_{mi},$$

where $B_{nj} = \ln \tilde{g}(\alpha_{nj}, \lambda_{nj}) + \frac{\lambda_{nj}}{\alpha_{nj} + \lambda_{nj}} \ln \left(\sum_{i=1}^{J} \sum_{m=1}^{N} \omega_{mi,nj}^{-\omega_{mi,nj}} \right)$, and we've applied the pricing assumption to relate prices across markets cum an iceberg trade cost.

Writing this expression in matrix form across all nj we have:

$$\ln \mathbf{p} = \mathbf{B} + \mathbf{\Gamma} \ln \mathbf{y} + \mathbf{\Phi} \ln \mathbf{w} + \mathbf{\Psi} \widehat{\mathbf{\Omega}}' \ln \mathbf{p}, \tag{B.13}$$

$$\ln \mathbf{p} \equiv (\ln p_{11}, \dots, \ln p_{NJ})', \qquad NJ \times 1,$$

$$\mathbf{B} \equiv (B_{11}, \dots, B_{NJ})', \qquad NJ \times 1,$$

$$\Gamma \equiv \operatorname{diag} \left(\left\{ \frac{1 - \alpha_{nj} - \lambda_{nj}}{\alpha_{nj} + \lambda_{nj}} \right\} \right), \qquad NJ \times NJ,$$

$$\ln \mathbf{y} \equiv (\ln y_{11}, \dots, \ln y_{NJ})', \qquad NJ \times NJ,$$

$$\Phi \equiv \operatorname{diag} \left(\left\{ \frac{\alpha_{nj}}{\alpha_{nj} + \lambda_{nj}} \right\} \right), \qquad NJ \times NJ,$$

$$\ln \mathbf{w} \equiv (1_{1 \times J} \circ \ln w_{1}, \dots, 1_{1 \times J} \circ \ln w_{N})', \qquad NJ \times NJ,$$

$$\Psi \equiv \operatorname{diag} \left(\left\{ \frac{\lambda_{nj}}{\alpha_{nj} + \lambda_{nj}} \right\} \right), \qquad NJ \times NJ,$$

$$\widehat{\Omega}' \equiv \tau \circ \Omega', \qquad NJ \times NJ,$$

$$\tau \equiv \begin{pmatrix} \{\tau_{11,\cdot}\}_{1 \times J} & \dots & \{\tau_{N1,\cdot}\}_{1 \times J} \\ \vdots & \ddots & \vdots \\ \{\tau_{N1,\cdot}\}_{1 \times J} & \dots & \{\tau_{NN,\cdot}\}_{1 \times J} \end{pmatrix}, \qquad NJ \times NJ,$$

where $\tau_{mn,\cdot} \equiv (\tau_{mn,1}, \dots, \tau_{mn,J})$.

Solving for the price level in (B.13) we have

$$\ln \mathbf{p} = (I - \Psi \widehat{\Omega}')^{-1} [\mathbf{B} + \mathbf{\Gamma} \ln \mathbf{y} + \mathbf{\Phi} \ln \mathbf{w}]. \tag{B.14}$$

Next, re-write (10) in logs as

$$\ln \mathbf{p} + \ln \mathbf{y} = \ln \left[(I - \widetilde{\mathbf{\Omega}})^{-1} \widetilde{\mathbf{b}} \mathbf{\mathcal{M}} \right].$$

Substituting (B.14) into this expression and solving for output yields

$$\ln \mathbf{y} = \ln \left[(I - \widetilde{\boldsymbol{\Omega}})^{-1} \widetilde{\mathbf{b}} \boldsymbol{\mathcal{M}} \right] - (I - \boldsymbol{\Psi} \widehat{\boldsymbol{\Omega}}')^{-1} [\mathbf{B} + \boldsymbol{\Gamma} \ln \mathbf{y} + \boldsymbol{\Phi} \ln \mathbf{w}],$$

which re-arranging gives

$$\ln \mathbf{y} = \left[I + (I - \mathbf{\Psi}\widehat{\mathbf{\Omega}}')^{-1} \mathbf{\Gamma} \right]^{-1} \left\{ \ln \left[(I - \widetilde{\mathbf{\Omega}})^{-1} \widetilde{\mathbf{b}} \mathbf{\mathcal{M}} \right] - (I - \mathbf{\Psi}\widehat{\mathbf{\Omega}}')^{-1} [\mathbf{B} + \mathbf{\Phi} \ln \mathbf{w}] \right\}.$$
(B.15)

Equations (B.14) and (B.15) highlight the interdependence of output on wages across countries that still needs to be solved for.

Fixed-Wage Solution In the case when wages are preset, the second term of (B.15) is simply and elaborate constant as wages will not adjust to shocks to the money supply, and breaking up the firm terms there are also numerous constants that are functions of parameters of the model. Ignoring these constants, we re-write the vector of country-sector outputs as

$$\ln \mathbf{y}_{fix} = \left[I + (I - \mathbf{\Psi}\widehat{\mathbf{\Omega}}')^{-1} \mathbf{\Gamma} \right]^{-1} \ln \mathbf{\mathcal{M}} + \mathbf{constant}.$$
 (B.16)

Taking the a first-order approximation of (B.16) around steady-state yields

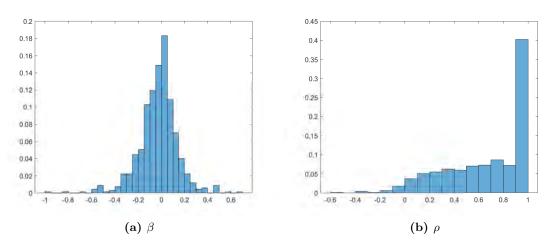
$$\widehat{\mathbf{y}}_{fix} = \left[I + (I - \mathbf{\Psi}\widehat{\mathbf{\Omega}}')^{-1} \mathbf{\Gamma} \right]^{-1} \widehat{\mathbf{\mathcal{M}}}, \tag{B.17}$$

which shows the positive relationship between an innovation in any country's money supply and sectoral output growth across countries. Given adjustments in prices and non-constant marginal costs, new output will adjust less than one-to-one to monetary shock. As supplies increase their prices, this will dampen the impact of monetary shock.

Appendix C Full Regression Tables and Additional Charts

Here we report additional information about our benchmark estimation as well as tables will full estimation results for all the tables in the paper.

Figure A1. Distribution of β and ρ across Country-Sectors



Notes: This figure plots the distribution of β and ρ across mi from the estimation of equation $\widehat{\boldsymbol{\pi}}_t = \beta \widehat{\mathcal{M}}_{US,t} + \rho \mathbf{W} \widehat{\boldsymbol{\pi}}_t + \boldsymbol{\varepsilon}_t$ for 2000–07, using Jarociński and Karadi (2020) monetary policy shocks for $\widehat{\mathcal{M}}_{US}$. The averages of these distributions are reported in Table 3.

Table A3. Full Regression Results for Different Time Periods and Weighting Matrices

$\hat{\pi}_{mi.t} =$	$\widehat{eta}\widehat{\mathcal{M}}_{US,t}$	$+ \rho \mathbf{W} \hat{\boldsymbol{\pi}}_t$	$+\varepsilon_{mi.t}$
1100,0	1		1166,6

	Avg. β (1)	Avg. ρ (2)	Avg. Direct (3)	Avg. Network (4)	Network/Total (5)		
	Panel A. Full Sample						
2000–07, avg W	-0.026	0.673***	-0.033*	-0.050***	60%***		
,	(0.022)	(0.168)	(0.021)	(0.014)	(0.169)		
2000-16, 2000 W	-0.003	0.758***	-0.005	-0.048***	91%***		
	(0.012)	(0.205)	(0.011)	(0.020)	(0.421)		
2000-16, avg W	-0.006	0.728***	-0.008	-0.044	84%***		
, 3	(0.037)	(0.183)	(0.039)	(0.086)	(0.369)		
2000–16, 2000 W , no 2008	-0.016	0.725***	-0.022	-0.066***	75%***		
,	(0.020)	(0.183)	(0.020)	(0.018)	(0.229)		
2000-16, avg W , no 2008	-0.024	0.695***	-0.029*	-0.050***	63%***		
, ,	(0.020)	(0.164)	(0.020)	(0.020)	(0.188)		
			Panel B. Inter	national Sample			
2000–07, avg W	-0.021	0.681***	-0.027*	-0.061***	65%***		
, 3	(0.021)	(0.168)	(0.020)	(0.021)	(0.018)		
$2000-16,\ 2000\ \mathbf{W}$	0.001	0.765***	-0.001	-0.048***	99%***		
,	(0.011)	(0.207)	(0.011)	(0.011)	(0.337)		
2000-16, avg W	-0.002	0.737***	-0.004	-0.044	93%***		
, ,	(0.040)	(0.185)	(0.042)	(0.040)	(0.253)		
2000–16, 2000 W , no 2008	-0.011	0.730***	-0.017	-0.066***	80%***		
	(0.020)	(0.184)	(0.019)	(0.020)	(0.143)		
2000-16, avg W , no 2008	-0.018	0.704***	-0.023	-0.051***	69%***		
, ,	(0.019)	(0.166)	(0.019)	(0.019)	(0.052)		
	Panel C. USA Sample						
2000–07, avg W	-0.095***	0.581***	-0.104***	-0.039	27%***		
,	(0.034)	(0.168)	(0.034)	(0.034)	(0.009)		
2000-16, 2000 W	-0.053**	0.676***	-0.057**	-0.051**	47%***		
,	(0.025)	(0.191)	(0.025)	(0.025)	(0.047)		
2000-16, avg W	-0.063**	0.613***	-0.067***	-0.038	36%***		
,	(0.027)	(0.162)	(0.027)	(0.027)	(0.102)		
2000–16, 2000 W , no 2008	-0.076***	0.661***	-0.082***	-0.066**	45%***		
,	(0.032)	(0.179)	(0.031)	(0.032)	(0.012)		
2000–16, avg W , no 2008	-0.094***	0.590***	-0.101***	-0.035	26%***		
,	(0.032)	(0.148)	(0.032)	(0.032)	(0.008)		

 $\textbf{Notes:} \ \ \textbf{This table presents full regression results for the regressions reported in } \ \ \textbf{Table 4}. \ \ \textbf{See notes to } \ \ \textbf{Table 4}.$

 ${\bf Table~A4.~Full~Regression~Results~with~Additional~Shocks:~Full~sample}$

 $\widehat{\pi}_{mi,t} = oldsymbol{eta}_{MP} \, \widehat{\mathcal{M}}_{US,t} + oldsymbol{eta}_X \, \widehat{\mathbf{X}}_t + oldsymbol{
ho} \, \mathbf{W} \widehat{oldsymbol{\pi}}_t + arepsilon_{mi,t}$

	(1)	(2)	(3)	(4)
Average ρ	0.654***	0.681***	0.690***	0.647***
iivoiago p	(0.148)	(0.169)	(0.174)	(0.164)
Monetary shock	(01220)	(0.200)	(0.2, 2)	(0.202)
$\overline{\text{Average }\beta_{MP}}$	-0.009	-0.028*	-0.022	-0.015
0 / 1121	(0.011)	(0.019)	(0.024)	(0.013)
Direct effect of MP	-0.014	-0.035**	-0.029	-0.020**
	(0.010)	(0.017)	(0.023)	(0.011)
Network effect of MP	-0.036***	-0.068***	-0.064***	-0.045***
	(0.013)	(0.019)	(0.015)	(0.018)
Share of network effect (MP)	0.723***	0.663***	0.688***	0.693***
, ,	(0.235)	(0.184)	(0.183)	(0.232)
VIX				
$\overline{\text{Average }}\beta_{VIX}$	-0.009	-0.052***		
0 , , ===	(0.011)			(0.020)
Direct effect of VIX	-0.063***			-0.058***
	(0.024)			(0.019)
Network effect of VIX	-0.079***			-0.068***
	(0.016)			(0.016)
Share of network effect (VIX)	0.555***			0.541**
, ,	(0.007)			(0.286)
2-year Treasury rate				
$\frac{1}{\text{Average }\beta_{T2y}}$		0.054**		0.039***
O / 1 = 9		(0.027)		(0.014)
Direct effect of T2y		0.060**		0.042***
·		(0.027)		(0.013)
Network effect of T2y		0.077***		0.045***
•		(0.018)		(0.017)
Share of network effect (T2y)		0.561***		0.517***
, ,		(0.059)		(0.012)
USD Broad Index				
Average β_{USD}			-0.133*	-0.097**
0 / 022			(0.086)	(0.053)
Direct effect of USD			-0.150**	-0.101**
			(0.082)	(0.050)
Network effect of USD			-0.343***	-0.155*
			(0.088)	(0.106)
Share of network effect (USD)			0.696***	0.606**
\ /			(0.014)	(0.006)

Notes: This table presents full regression results for the regressions reported in Table 6. See notes to Table 6.

Table A5. Full Regression Results with Additional Shocks: International

 $\widehat{\boldsymbol{\pi}}_{mi,t} = \boldsymbol{\beta}_{MP} \, \widehat{\mathcal{M}}_{US,t} + \boldsymbol{\beta}_{X} \, \widehat{\mathbf{X}}_{t} + \boldsymbol{\rho} \, \mathbf{W} \widehat{\boldsymbol{\pi}}_{t} + \boldsymbol{\varepsilon}_{mi,t}$

	(1)	(2)	(3)	(4)
Average ρ	0.662***	0.688***	0.696***	0.655***
11.01@0 b	(0.149)	(0.170)	(0.175)	(0.166)
Monetary shock				
Average β_{MP}	-0.004	-0.022	-0.017	-0.009
	(0.011)	(0.018)	(0.024)	(0.012)
Direct effect of MP	-0.008	-0.029**	-0.024	-0.014
	(0.010)	(0.017)	(0.022)	(0.011)
Network effect of MP	-0.036***	-0.068***	-0.064***	-0.045***
	(0.013)	(0.019)	(0.015)	(0.018)
Share of network effect (MP)	0.812***	0.699***	0.731^{***}	0.757***
	(0.115)	(0.699)	(0.179)	(0.128)
<u>VIX</u>				
Average β_{VIX}	-0.057***			-0.052***
	(0.026)			(0.021)
Direct effect of VIX	-0.064***			-0.058***
	(0.025)			(0.019)
Network effect of VIX	-0.079***			-0.068***
	(0.015)			(0.016)
Share of network effect (VIX)	0.553^{***}			0.540***
	(0.009)			(0.061)
2-year Treasury rate				
$\overline{\text{Average } \beta_{T2y}}$		0.054**		0.038***
		(0.027)		(0.014)
Direct effect of T2y		0.060**		0.041***
, and the second				
		(0.027) $0.076***$		(0.013)
Network effect of T2y		(0.027) $0.076***$		(0.013) 0.045^{***}
Network effect of T2y		(0.027) 0.076*** (0.018)		(0.013) 0.045^{***} (0.017)
		(0.027) $0.076***$		(0.013) $0.045***$
Network effect of T2y Share of network effect (T2y)		(0.027) 0.076*** (0.018) 0.558***		(0.013) 0.045*** (0.017) 0.520**
Network effect of T2y Share of network effect (T2y) USD Broad Index		(0.027) 0.076*** (0.018) 0.558***	-0.127*	(0.013) 0.045*** (0.017) 0.520** (0.027)
Network effect of T2y Share of network effect (T2y)		(0.027) 0.076*** (0.018) 0.558***	-0.127* (0.086)	(0.013) 0.045*** (0.017) 0.520** (0.027) -0.089**
Network effect of T2y Share of network effect (T2y) USD Broad Index Average β_{USD}		(0.027) 0.076*** (0.018) 0.558***	(0.086)	(0.013) 0.045*** (0.017) 0.520** (0.027) -0.089** (0.054)
Network effect of T2y Share of network effect (T2y) USD Broad Index		(0.027) 0.076*** (0.018) 0.558***	(0.086) -0.144**	(0.013) 0.045*** (0.017) 0.520** (0.027) -0.089** (0.054) -0.091**
Network effect of T2y Share of network effect (T2y) USD Broad Index Average β_{USD} Direct effect of USD		(0.027) 0.076*** (0.018) 0.558***	(0.086) -0.144** (0.082)	(0.013) 0.045*** (0.017) 0.520** (0.027) -0.089** (0.054) -0.091** (0.051)
Network effect of T2y Share of network effect (T2y) USD Broad Index Average β_{USD}		(0.027) 0.076*** (0.018) 0.558***	(0.086) -0.144** (0.082) -0.341***	(0.013) 0.045*** (0.017) 0.520** (0.027) -0.089** (0.054) -0.091** (0.051) -0.155*
Network effect of T2y Share of network effect (T2y) USD Broad Index Average β_{USD} Direct effect of USD		(0.027) 0.076*** (0.018) 0.558***	(0.086) -0.144** (0.082)	(0.013) 0.045*** (0.017) 0.520** (0.027) -0.089** (0.054) -0.091** (0.051)

Notes: This table presents full regression results for the regressions reported in Table 6. See notes to Table 6.

Table A6. Full Regression Results with Additional Shocks: USA

 $\widehat{\boldsymbol{\pi}}_{mi,t} = \boldsymbol{\beta}_{MP} \, \widehat{\mathcal{M}}_{US,t} + \boldsymbol{\beta}_{X} \, \widehat{\mathbf{X}}_{t} + \boldsymbol{\rho} \, \mathbf{W} \widehat{\boldsymbol{\pi}}_{t} + \boldsymbol{\varepsilon}_{mi,t}$

	(1)	(2)	(3)	(4)
Average ρ	0.561***	0.601***	0.612***	0.548***
Tiverage p	(0.143)	(0.167)	(0.171)	(0.147)
Monetary shock				
Average β_{MP}	-0.074***	-0.092***	-0.087***	-0.083***
	(0.020)	(0.029)	(0.039)	(0.021)
Direct effect of MP	-0.080***	-0.100***	-0.095***	-0.089***
	(0.018)	(0.027)	(0.037)	(0.019)
Network effect of MP	-0.035***	-0.068***	-0.063***	-0.050***
	(0.016)	(0.023)	(0.019)	(0.020)
Share of network effect (MP)	0.302***	0.404***	0.399***	0.358**
	(0.102)	(0.056)	(0.066)	(0.183)
<u>VIX</u>				
Average β_{VIX}	-0.057***			-0.050***
	(0.022)			(0.018)
Direct effect of VIX	-0.058***			-0.051***
	(0.021)			(0.017)
Network effect of VIX	-0.079***			-0.063***
	(0.017)			(0.016)
Share of network effect (VIX)	0.574***			0.552***
	(0.005)			(0.007)
2-year Treasury rate				
Average β_{T2y}		0.058**		0.048***
S 7 = -9		(0.000)		
		(0.029)		(0.017)
Direct effect of T2y		(0.029) $0.061**$		(0.017) $0.051***$
Direct effect of T2y		0.061**		0.051***
		0.061** (0.029) 0.089***		0.051*** (0.016) 0.048***
Network effect of T2y		0.061** (0.029) 0.089*** (0.024)		0.051*** (0.016) 0.048*** (0.019)
Network effect of T2y		0.061** (0.029) 0.089***		0.051*** (0.016) 0.048***
Direct effect of T2y Network effect of T2y Share of network effect (T2y) USD Broad Index		0.061** (0.029) 0.089*** (0.024) 0.592***		0.051*** (0.016) 0.048*** (0.019) 0.485***
Network effect of T2y Share of network effect (T2y) USD Broad Index		0.061** (0.029) 0.089*** (0.024) 0.592***	-0.205*	0.051*** (0.016) 0.048*** (0.019) 0.485*** (0.008)
Network effect of T2y		0.061** (0.029) 0.089*** (0.024) 0.592***	-0.205* (0.132)	0.051*** (0.016) 0.048*** (0.019) 0.485*** (0.008)
Network effect of T2y Share of network effect (T2y) USD Broad Index Average β_{USD}		0.061** (0.029) 0.089*** (0.024) 0.592***	(0.132)	0.051*** (0.016) 0.048*** (0.019) 0.485*** (0.008) -0.192** (0.085)
Network effect of T2y Share of network effect (T2y) USD Broad Index Average β_{USD}		0.061** (0.029) 0.089*** (0.024) 0.592***	(0.132) -0.226**	0.051*** (0.016) 0.048*** (0.019) 0.485*** (0.008) -0.192** (0.085) -0.212***
Network effect of T2y Share of network effect (T2y) USD Broad Index Average β_{USD} Direct effect of USD		0.061** (0.029) 0.089*** (0.024) 0.592***	(0.132) -0.226** (0.123)	0.051*** (0.016) 0.048*** (0.019) 0.485*** (0.008) -0.192** (0.085) -0.212*** (0.079)
Network effect of T2y Share of network effect (T2y) USD Broad Index		0.061** (0.029) 0.089*** (0.024) 0.592***	(0.132) -0.226** (0.123) -0.361***	0.051*** (0.016) 0.048*** (0.019) 0.485*** (0.008) -0.192** (0.085) -0.212*** (0.079) -0.156*
Network effect of T2y Share of network effect (T2y) USD Broad Index Average β_{USD} Direct effect of USD		0.061** (0.029) 0.089*** (0.024) 0.592***	(0.132) -0.226** (0.123)	0.051*** (0.016) 0.048*** (0.019) 0.485** (0.008) -0.192** (0.085) -0.212*** (0.079)

Notes: This table presents full regression results for the regressions reported in Table 6. See notes to Table 6.

Table A7. Full Regression Results for Different Monetary Policy Shocks and Real Returns

 $\widehat{\pi}_{mi,t} = \boldsymbol{\beta} \, \widehat{\mathcal{M}}_{US,t} + \boldsymbol{\rho} \, \mathbf{W} \widehat{\boldsymbol{\pi}}_t + \varepsilon_{mi,t}$

	Avg. β	Avg. ρ	Avg. Direct (3)	Avg. Network	Network/Total
	(1)	(2)	(9)	(4)	(5)
			Panel A.	Full Sample	
Real	-0.024	0.681***	-0.031*	-0.060***	66%***
	(0.022)	(0.155)	(0.021)	(0.012)	(0.156)
Nom. returns, BRW shock	-0.019	0.672^{***}	-0.020	-0.042***	67%***
	(0.024)	(0.161)	(0.024)	(0.016)	(0.247)
Nom. returns, OW shock	-0.039	0.673***	-0.049*	-0.066**	57%***
	(0.031)	(0.149)	(0.031)	(0.017)	(0.138)
Nom. returns, NS shock	-0.046	0.674***	-0.058	-0.082	59%***
	(0.045)	(0.154)	(0.044)	(0.040)	(0.188)
			Panel B. Inter	rnational Sample	
Real returns	-0.019	0.686***	-0.026*	-0.058***	69%***
	(0.021)	(0.155)	(0.020)	(0.021)	(0.070)
Nom. returns, BRW shock	-0.017	0.678***	-0.018	-0.040**	69%***
	(0.024)	(0.162)	(0.023)	(0.024)	(0.204)
Nom. returns, OW shock	-0.038	0.679***	-0.048*	-0.066**	58%***
	(0.032)	(0.150)	(0.032)	(0.032)	(0.065)
Nom. returns, NS shock	-0.043	0.680***	-0.056	-0.082	60%***
	(0.046)	(0.154)	(0.045)	(0.046)	(0.145)
	Panel C. USA Sample				
Real returns	-0.080**	0.612***	-0.088***	-0.082**	48%***
	(0.040)	(0.154)	(0.040)	(0.040)	(0.055)
Nom. returns, BRW shock	-0.039	0.602***	-0.044	-0.065**	60%***
	(0.038)	(0.164)	(0.037)	(0.038)	(0.177)
Nom. returns, OW shock	-0.051**	0.602***	-0.057**	-0.068***	54%***
•	(0.028)	(0.151)	(0.027)	(0.028)	(0.068)
Nom. returns, NS shock	-0.075*	0.602***	-0.083*	-0.090**	52%***
	(0.054)	(0.169)	(0.053)	(0.054)	(0.117)

Notes: This table presents full regression results for the regressions reported in Table 7. See notes to Table 7.