# Confidence and the Propagation of Demand Shocks

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July 7, 2020

# Outline



2 Element 1: Variable Utilization  $\Rightarrow$  AS Responds to AD

### 3 Element 2: Rational Confusion $\Rightarrow$ Confidence Multiplier



# Popular Narrative

- Household deleveraging or other AD shocks
  - $\implies$  Consumers spend less
  - $\implies$  Firms produce and hire less
  - $\implies$  Consumers lose confidence and spend even less
  - $\implies$  Firms produce and hire even less
  - $\implies \cdots$
  - $\implies$  The Great Recession!

# Does It Make Sense?

In RBC: no

• In GE, interest rates adjust, offsetting AD shock

In NK: perhaps

- Only when MP does not replicate flexible price outcomes
- Effects of AD shock = monetary contraction
- Inflation and output co-move

BUT

- ZLB constraint not relevant in earlier recessions
- Philips curve elusive in the data (Mavroeidis et al., 14)
- Non-inflationary demand shocks prevalent
  - Beaudry & Portier (13), Angeletos et al. (20)

# This Paper

• A theory of demand driven fluctuations with flexible prices

Element 1:

• Variable utilization  $\Rightarrow$  AS responds to AD

Element 2:

- Rational confusion between idiosyncratic & agg. income fluctuations
- $\Rightarrow$  Confidence multiplier
  - feedback loop between output, consumer & investor expectations
- A broader bounded rationality interpretation

# Roadmap

Representative agent, complete info, version model

• Element 1: variable utilization  $\Rightarrow$  AS responds to AD

Introduce information frictions

• Element 2: rational confusion  $\Rightarrow$  confidence multiplier

Extensions

- Comovement of consumption, output, and investment
- Fiscal policy (front-loading vs back-loading)
- TFP Shock

## Outline



### 2 Element 1: Variable Utilization $\Rightarrow$ AS Responds to AD

### 3 Element 2: Rational Confusion ⇒ Confidence Multiplier



## Preferences and AD Curve

• Preference (representative agent & complete info)

$$U(c_t, n_t) + \beta_t U(c_{t+1}, n_{t+1}) + \beta_t \beta_{t+1} U(c_{t+2}, n_{t+2}) + \cdots,$$

where

$$\log \beta_t = (1 - \rho_\beta) \log \beta + \rho_\beta \log \beta_{t-1} - \bigcup_{\text{AD Shock}} \eta_t$$

• A positive  $\eta_t$  shock = urge to consume = positive AD shock

• AD curve (log-linearized, complete info)

$$y_t = -\sigma \{R_t + \beta_t\} + \mathbb{E}_t [y_{t+1}]$$

# Technology and AS Curve

Technology

$$y_t = (l_t)^{\alpha} (u_t k_t)^{1-\alpha}$$
$$k_{t+1} = (1 - \delta (u_t) + \Psi (\iota_t)) k_t,$$

• Tentatively: shut down  $\iota_t$  and drop  $\Psi(\iota_t)$ 

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$$k_{t+1} = (1 - \delta (u_t) + \Psi (l_t)) k_t,$$

- Tentatively: shut down  $\iota_t$  and drop  $\Psi(\iota_t)$
- AS curve (log-linearized):

$$y_t = (1 - \tilde{\alpha}) (u_t + k_t),$$
  
$$u_t = \frac{\beta}{\tilde{\alpha} + \beta \phi} R_t + \beta \mathbb{E}_t [u_{t+1}],$$
  
$$k_{t+1} = k_t - \kappa u_t,$$

where 
$$\tilde{\alpha} \equiv 1 - \frac{(1-\alpha)\left(1+\frac{1}{\nu}\right)}{1+\frac{1}{\nu}-\alpha+\frac{\alpha}{\sigma}}$$
 and  $\phi \equiv \frac{\delta''(u^*)u^*}{\delta'(u^*)}$ .

# Equilibrium

Prop. Demand-driven business cycle without nominal rigidity

$$rac{\partial y_t}{\partial \eta_t} = \gamma \;\; ext{and} \;\; rac{\partial R_t}{\partial \eta_t} = rac{\sigma}{\sigma+arsigma},$$

where

$$\gamma \equiv \frac{\varsigma \sigma \beta}{\sigma + \varsigma} \frac{1}{1 - \rho_\beta \beta} \ \, \text{and} \ \, \varsigma \equiv \frac{1 - \tilde{\alpha}}{\tilde{\alpha} + \beta \phi}.$$

•  $\gamma$  increases with variability of u (decreases with  $\phi \equiv \frac{\delta''(u^*)u^*}{\delta'(u^*)}$ )

- Baseline NK: natural rate of output fixed ( $\gamma = 0$  because  $\phi = \infty$ )
- Here: natural rate of output responsive to AD

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### 4 Extensions

# Full Model with Information Frictions

Supply side

• Complete info, same as above

Demand side

- Islands & idiosyncratic shocks
- Know own discount rate, current local income & interest rates
- Incomplete info of, or inattention to, the aggregate
- Rational confusion of idiosyncratic & agg. income fluctuations

# AD Curve

### Prop. The AD Curve

$$y_t = -\sigma \{R_t + \beta_t\} + \mathbb{E}_t [y_{t+1}] + (\mathscr{B}_t + \mathscr{G}_t).$$

•  $\mathcal{B}_t$  captures misperception of permanent income

$$\mathscr{B}_{t} \equiv \frac{1-\beta}{\beta} \sum_{k=0}^{+\infty} \beta^{k} \int \left( E_{t}^{h} [y_{h,t+k}] - \mathbb{E}_{t} [y_{h,t+k}] \right) dh,$$

where  $y_{h,t} = y_t + \xi_{h,t}$  is the local income at t.

•  $\mathcal{G}_t$  captures misperception of future interest rates

$$\mathscr{G}_{t} \equiv -\sigma \sum_{k=1}^{+\infty} \beta^{k} \int \left( E_{t}^{h} [R_{t+k}] - \mathbb{E}_{t} [R_{t+k}] \right) dh$$

# $\mathcal{B}_t$ : Misperception of Permanent Income

Hulten's theorem: agg permanent income  $\sum_{k=0}^{+\infty} \beta^k \int y_{t+l}$  invariant to AD

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Hulten's theorem: agg permanent income  $\sum_{k=0}^{+\infty} \beta^k \int y_{t+l}$  invariant to AD

Prop. Pro-cyclical perceived permanent income

$$\mathscr{B}_t \equiv \frac{1-\beta}{1-\beta\rho_{\xi}} (1-\lambda) y_t,$$

- $ho_{\xi}$  is the persistence of the idiosyncratic income shock  $\xi_{h,t}$
- $1 \lambda$  : degree of confusion between idiosyncratic & agg.

**Mechanism:** current aggregate income  $y_t$  drops

- $\implies$  rationally confused as drop in idiosyncratic income  $\xi_{h,t}$
- $\implies$  drop in perceived permanent income

# Confidence Multiplier



# Confidence Multiplier

Focus on the impact of  $\mathscr{B}_t$  (as if  $\mathscr{G}_t = 0$ )

#### Prop. Equilibrium Impact of Confidence Multiplier

$$\frac{\partial y_t}{\partial \eta_t} = \gamma \cdot m^{\operatorname{conf}} \big( \lambda, \rho_{\xi} \big),$$

where the confidence multiplier

$$m^{\operatorname{conf}}\left(\lambda,
ho_{\xi}
ight)\equivrac{\zeta+\sigma}{\zeta+\sigma-\zetarac{1-eta}{1-eta
ho_{\xi}}\left(1-\lambda
ight)}>1$$

• Increases with the persistence of idiosyncratic income  $ho_{\mathcal{E}}$ 

• Increases with the confusion  $1-\lambda$ 

# 𝒴<sub>t</sub>: Dampening GE of Interest Rate Adjustments

### Prop. Misperception of Future Interest Rate Adjustment

$$egin{split} \mathscr{G}_t &= (1\!-\!\lambda)\sigma\sum_{k=1}^{+\infty}eta^krac{\partial\mathbb{E}_t[R_{t+k}]}{\partial\eta_t}\eta_t \ &= (1\!-\!\lambda)rac{\sigma^2}{\sigma\!+\!arsigma}rac{eta
ho_eta}{1\!-\!eta
ho_eta}\eta_t \end{split}$$

Persistent negative AD shock

- Neoclassical GE: future interest rate  $R_{t+k}$  drops
  - goes against the impact of the AD shock
- Here: cannot fully perceive  $R_{t+k}$  drop
  - $\mathscr{G}_t$  negative
  - Further amplifies the impact of the AD shock

# Full Equilibrium

### Prop. Full Equilibrium

The equilibrium response of aggregate output is given by

$$\frac{\partial y_t}{\partial \eta_t} = \gamma \cdot \boldsymbol{m}^{\mathsf{conf}}\left(\boldsymbol{\lambda}, \boldsymbol{\rho}_{\boldsymbol{\xi}}\right) \cdot \boldsymbol{m}^{\mathsf{GE}}\left(\boldsymbol{\lambda}, \boldsymbol{\rho}_{\boldsymbol{\beta}}\right),$$

where

$$m^{\mathsf{GE}}(\lambda,\rho_{\beta}) \equiv 1 + \beta \rho_{\beta} \frac{\sigma}{\sigma+\varsigma} (1-\lambda) \geq 1$$

• Increases with the persistence of AD shock  $ho_{eta}$ 

• Increases with the confusion  $1 - \lambda$ 

# Bounded Rationality

Broader interpretation of confidence multiplier  $\mathcal{B}_t$ 

- Key: the response of  $c_{h,t}$  to  $y_{h,t}$  independent from idio. vs agg.
- Rule of thumb (Kahnman, 11)
- Extrapolation (Barberis Greenwood, Jin, Shleifer, 14)
- One-factor representation (Molavi, 19)

Broader interpretation of GE dampening  $\mathscr{G}_t$ 

- Lack of common knowledge (Angeletos & Lian, 18)
- Level-k thinking (Farhi & Werning, 19; Garcia-Schmidt & Woodford, 19)
- Cognitive discounting (Gabaix, 20)

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### Investment

$$k_{t+1} = \left[1 - \delta\left(u_t\right) + \Psi\left(\iota_t\right)\right] k_t.$$

Complete info (with small wealth effect on labor supply)

- Positive AS & comovement between c and y
- Negative comovement between *i* and *c* 
  - ▶ negative AD shock,  $c \downarrow$ ,  $R \downarrow$ ,  $i \uparrow$

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Complete info (with small wealth effect on labor supply)

- Positive AS & comovement between c and y
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  - ▶ negative AD shock,  $c \downarrow$ ,  $R \downarrow$ ,  $i \uparrow$

Our resolution:

- Investment subject to confidence multiplier too
- Feedback between  $y_t$  & investor expectations of returns

#### Prop. Investment comovement

With strong enough info friction, (c, i, y) all co-move

# **Fiscal Multiplier**

Q: How does confidence multiplier impact fiscal policy?

Here, for simplicity, shut down wealth effect of  ${\sf G}$  on labor supply

• Same AS as above

AD:

$$y_t = -\sigma R_t + G_t - E_t [G_{t+1}] + E_t [y_{t+1}] + (\mathscr{B}_t + \mathscr{G}_t)$$

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$$y_{t} = -\sigma R_{t} + G_{t} - E_{t} [G_{t+1}] + E_{t} [y_{t+1}] + (\mathscr{B}_{t} + \mathscr{G}_{t})$$

**Front-loading**  $G_t \implies$  positive AD shock  $\implies$  confidence multiplier

### Prop. Front-loading government spending

With strong enough info friction,  $G_t$  can crowd in  $c_t$ 

**Back-loading**  $G_t \implies$  negative AD shock  $\implies$  negative multiplier

# **TFP Shock**

$$y_t = -\sigma R_t + E_t [y_{t+1}] + (\mathscr{B}_t + \mathscr{G}_t),$$

#### No confidence multiplier

- Actual permanent income moves with aggregate TFP
- Rational confusion  $\implies$  Ambiguous  $\mathscr{B}_t$
- Useful benchmark  $\mathscr{B}_t \approx 0 \ (\rho_{\xi} \approx \rho_A)$
- Dampening of GE has reverse effect
  - Negative TFP Shock  $\Longrightarrow$  positive  $R_t \Longrightarrow$  **Positive**  $\mathscr{G}_t$

#### Prop. TFP Shock

Info friction dampens the relative impact of AS vs AD shock

• Consistent with the importance of non-inflationary AD shock

# Main Business Cycle Shock (Angeletos, Collard, Dellas, 20)



• u, y, h, c, i comove without TFP &  $\pi$ 

- Utilization accounts for pro-cyclicality in labor prod
- Non-accommodative MP and procyclical real R
- Intertemporal substitution in production

- $\bullet\,$  A theory why & how the natural output responds to AD shock
- Main insights go through sticky prices
- Additional mechanism: misperception of output gaps (MP)
  - existing literature on forward guidance etc.

# Conclusion

Two contributions:

- A theory of demand-driven fluctuations without sticky prices
- A theory of amplifications for AD shock (but not AS shocks)