Should Short-Term Shareholders Have Less Rights?

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Abstract

Public officials, business leaders, and academics have expressed concerned that allowing investors with short-term investment horizon to initiate and vote on changes in the governance of public companies can be expected to exacerbate short-termism, and have made influential proposals to eliminate or constrain the shareholder rights of such shortterm investors. We develop a model to study whether such proposals could be expected to enhance the long-term value of public companies. To this end, we extend the canonical Stein Model (Stein 1988 and Stein 1989) by allowing for governance structures, pay schemes, and director selection to be determined endogenously and influenced by shareholder preferences. Using this standard framework for analyzing short-termism, we find that governance structures that give rise to some level of corporate myopia can provide benefits to long-term investors that could lead to their adoption even when short-term investors are denied participation rights. Most importantly, we show that short-term investors have the same preferences with respect to governance structures, pay schemes, and director selections as long-term shareholders and, contrary to widely expressed concerns, short-term investors would not prefer choices making long-term shareholders worse-off. Our analysis indicates that the standard economic framework for studying short-termism does not provide a basis for eliminating or weakening the rights of short-term shareholders to participate in the governance of public companies. (JEL D74, D82, D83, G34, K22)

Keywords: Corporate Governance, Myopia, Short-termism, Long-Term Investments, Shareholder Rights, Hedge Fund Activism, Dual-Class, Tenure Voting

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1 Introduction

This paper develops a model to examine the effect that the presence of investors with short-term horizons ("short-term shareholders") has on problems of short-termism ("corporate myopia") and, in turn, on the performance and value of public companies. In particular, we study whether short-term shareholders can be expected to seek and support governance structures, pay arrangements, and board changes that would increase focus on short-term results, and thus exacerbate corporate myopia problems, at the expense of long-term value and long-term shareholders.

Our model seeks to contribute to two key debates – on short-termism and short-term share-holders. Prominent public officials and business leaders have expressed grave concerns about the adverse effects of short-term shareholders, and have advocated substantial policy measures to address them.¹ To begin, short-termism is widely viewed as a major problem for the performance of public companies and the economy. For example, corporate short-termism has been gravely described as "one of the greatest threats to America's enduring prosperity" by Vice-President Biden (Biden 2016), as "holding America back from reaching its full potential" by a bill sponsored by Senators Baldwin and Merkley (Baldwin and Merkley 2016), and as having "eroded faith in corporations continuing to be the foundation of the American free enterprise system, which has been, in turn, the foundation of our economy" by an Aspen Institute Task Force (Aspen Institute 2009).

Those concerned about short-termism have long viewed the presence and influence of short-term shareholders as a key contributor to myopic behavior by managers of public companies (see, e.g., Barton 2011). Delaware Chief Justice Strine explains the rationale for this position as follows: "[I]n corporate polities, unlike nation-states, the citizenry can easily depart and not 'eat their cooking.' As a result, there is a danger that activist shareholders will make proposals motivated by interests other than maximizing [long-term value]" (Strine 2010). Similarly, the Aspen Institute Task Force argued that "fund managers with a primary focus on short-term trading gains have little reason to care about long-term corporate performance or externalities, and so are unlikely to exercise a positive role in promoting corporate policies, including appropriate proxy voting and corporate governance policies, that are beneficial and sustainable in the long-term" (Aspen Institute 2009).

¹For surveys of these debates, see Bebchuk (2013) and Roe (2018).

Importantly, concerns that short-term shareholders exacerbate the myopia problems of public companies have motivated an array of proposals to limit the power, rights and influence of short-term shareholders relative to those of long-term shareholders. Indeed, to combat corporate myopia, various writers have advocated adopting tenure voting arrangements that would reduce the relative voting power of short-term investors (see, e.g., Fox and Lorsch 2012, Mayer 2013); others have proposed limits on the power of short-term investors to propose corporate changes (see, e.g., Strine 2010), with the SEC following such an approach when adopting a proxy access rule in 2010 (SEC, 2010); and Senators have put forward legislative proposed to curb the activities of hedge fund activists (Baldwin and Merkley 2016).²

We seek to study the impact of short-term shareholders on the problem of short-termism. To do so, we build on the well-known analytical framework for examining short-termism established by Jeremy Stein (Stein 1988 and Stein 1989, collectively "the Stein Model"). The Stein Model has shown how short-termism can arise in market equilibrium and has been key reference in financial economics. In this model, short-termism arises because of asymmetric information between corporate directors and managers ("the manager"). The manager may take some unobservable actions (such as making an unobservable investment that has payoff only in the long-term). The Stein Model shows that, whenever the managers care about the share value not only in the long-term but also in the short-term, the manager may take some inefficient unobservable actions that would improve short term results at the expense of the long term. This inefficiency, which is anticipated in equilibrium, adversely affects firm value. Furthermore, the larger the weight attached to short-term prices, the more sever the short-termism problem.

To contribute to the key policy debates on short-term shareholders, we extend the Stein Model to facilitate an examination of whether short-term shareholders would have an interest in pushing for governance structures, pay schemes, and leadership choices (e.g., appointing an

²In addition, concerns about the impact of short-term shareholders have motivated an array of policy proposals that seem to have gained substantial traction in policy debates. In particular, public officials and business leaders have called for measures to encourage a long-term horizon for institutional investors. For example, to combat corporate myopia, Hillary Clinton's presidential campaign, BlackRock's CEO Larry Fink, and economist Joseph Stiglitz advocated tax incentives to encourage long-term retention of stock (Clinton 2015, Fink 2017, Stiglitz 2015); others have called for reforming the compensation of portfolio managers to eliminate incentives for short-term focus (e.g., Strine 2016); and various researchers, organizations, and practitioners have advocated corporate arrangements that would encourage long-term investors by providing additional "loyalty" dividends to such investors at the expense of other investors (e.g., Bolton and Samama 2013).

³The Stein Model continues the work of Narayanan (1985) who showed that managerial myopia arises in equilibrium where prices reflect public information due to information asymmetry between insiders and market participants.

activist hedge fund to the board) that would disfavor long-term shareholders by exacerbating the short-termism problem. To this end, we introduce into the Stein Model shareholders with different horizons and examine the effects of shareholder horizons on various choices. Specifically, we allow for the governance structures, pay schemes, and leadership choices to be endogenously determined and influenced by the preferences of shareholders.⁴

We would like to clarify that our focus is not on analyzing the desirable level of influence shareholders of public companies ought to have. Rather, our focus is on the question whether, for any given level of influence that shareholders have with respect to governance, pay structure, and leadership choices, the presence of short-term shareholders would adversely affect these choices. In the course of our analysis, we do examine the long-term costs and benefits of governance arrangements that expand shareholder power to replaced directors. However, our focus is on examining whether short-term and long-term shareholders would have different preferences on such matters.

Our analysis is organized as follows. In Section 2 we present our framework of analysis. Similar to the Stein Model, we have a company that operates in two periods and that can take unobservable actions that would inefficiently improve results in the first period at the expense of the results in the second period. We add a time prior to the first period in which governance structures, pay schemes, and the identity of the manager – choices that will affect the subsequent level of short-termism in the first period – are determined. We allow for these choices to be influenced by shareholders, and we introduce two types of shareholders; short-term shareholders, which plan to sell their shares after the results of the first period are known, and long-term shareholders, which plan to hold their shares through the second period. Our primary question is whether short-term shareholders would prefer and seek different arrangements than those that would be desirable for long-term shareholders.

In Section 3 we analyze how the governance structure choice is expected to affect the level of myopia. For concreteness we examine the governance arrangements that affect how

⁴The Stein Model, which has attracted more than 3500 citations on Google Scholar, has provided a basis for may theoretical papers (including by us). Papers extending this model in various ways include, for example, Aghion and Stein 2008; Benmelech, Kandel, and Veronesi 2010; Bizjak, Brickley, and Coles 1993; Edmans et al. 2012; Goldman and Slezak 2006; Kumar and Langberg 2009; Marinovic and Varas 2018; Von Thadden 1995; Zhu 2018. To the best of our knowledge, however, this body of work has not provided our key insights. In addition, unlike the Stein Model and the papers that builds on its framework, there is another line of work that studies managerial myopia in settings in which market prices deviate from fundamental values for prolonged periods of time due to limits to arbitrage, investor overconfidence, and other reasons (e.g., Bolton et al. 2006; Shleifer and Vishny 1990).

easy/difficult it would be to replace the manager after the results of the first period with a new manager that will run the firm in the second period. The results of the first period might provide shareholders with information about the ability of the manager, and this information might indicate that replacing the manager with a new manager will be value-increasing (on an expected value basis). As long as the probability of replacement decreases with improvement in first-period results, any change in governance structure that makes it easier (harder) to replace the manager after the first period results are known increases (decreases) the manager's incentive to take unobservable myopic actions that inefficiently improve short-term results.

In Section 3.4, we identify the governance structure that would best serve the interests of long-term shareholders. The optimal choices for such investors will trade off two effects of enabling manager replacement – the expected benefit of enabling efficient replacement and the expected cost from incentivizing myopic behavior. Thus, even from the perspective of long-term investors a governance structure that fully insulates the manager from replacement to eliminate any incentives to engage in short-termism arising from the fear of replacement might not be optimal.

Section 4.1 then identifies the choice of governance structure that would be optimal for short-term investors. Our main result demonstrates that, although these investors expect to sell their shares at the end of the first period, they would not favor a governance structure that would induce more short-termism than the long-term investors. The reason is that, while the myopic actions taken by managers are assumed to be unobservable in the Stein model, the choice of governance structure is clearly observable. Thus, the inefficiency costs of choosing a governance structure that would inefficiently exacerbate the problem of myopic actions would be expected to be reflected in the market prices that would be received by short-term investors.

Thus, even assuming that short-term shareholders would be interested in the manager's taking unobservable myopic actions, the short-term shareholders would not be able to benefit from using the observable instrument of an inefficient governance structure to obtain such actions. Recall Chief Justice Strine's concern about short-term shareholders push for changes without having "to eat their own cooking." The intuition behind our result is that, because governance structure changes are observable, short-term investors that push for inefficient changes that can be expected to have an adverse effect on the myopia problem, they will have to eat their cooking when they sell their shares after making such changes.

Section 4.2 extends the analysis to the choice of executive pay schemes. Pay schemes that

induce managers to increase the weight they attach to short-term prices, such as by allowing short-term unloading of shares, can be expected to increase incentives to take unobservable myopic corporate actions. Again, however, we show that short-term investors would not have an interest in pushing for or encouraging myopic pay schemes disfavored by long-term investors. Doing so would decrease, not increase, the short-term prices that they would be able to obtain when they sell their shares.

Section 5 considers the case in which short-term investors seek to take over leadership of the firm before the first period in which myopic actions may be taken. This case is important to analyze because over the past decade, activist hedge funds have been increasingly able to get individuals associated with them elected to boards of directors (Bebchuk et al. 2017). In the setting that we analyze, if an investor with short-horizon takes on leadership of the firm in the first period, such a leader will have increased incentives to take unobservable myopic actions that exacerbate the costs of short-termism. However, because the introduction of a leadership with a short-term focus would be observable and reflected in subsequent market prices, such a leadership change would be in the best interest of short-term investors only when it would serve the interests of long-term investors – that is, when the expected benefits from superior leadership ability (if any) would exceed the expected costs from enhanced short-termism.

Section 6 extends the analysis in several directions. First, we highlight the key and valuable role played by disclosure requirements. We explain that corporate myopia levels could be adversely affected by the presence of activist hedge funds (or other short-term investors) if corporate managers could have a secret channel with hedge fund activists that (i) enabled the managers to provide such hedge fund managers with short-term horizons with information about myopic actions not observable to other, and (ii) enabled the managers to agree to do so. By preventing such secret channels, securities laws play a beneficial role. Second, we consider the possibility that insiders have superior information about the effects of governance structures on firm value. We show that our main result extends to this case, and highlight that the key issue is not whether outside shareholders are as informed as insiders, but rather whether all shareholders have access to the same information. Third, we consider situations in which short-term shareholders have governance expertise that enables them to facilitate changes to the management of the firm at a lower cost than other shareholders. We show that our main point remains unchanged; short-term shareholders will propose and vote for only governance changes that will be optimal for long-term shareholders. Finally, we discuss how our main

result could be extended to cases with substantial heterogeneity in the investment horizon of different investors.

Section 7 makes concluding remarks. Our analysis has substantial implications for the ongoing heated debates on corporate myopia problem and the contribution of short-term investors to this problem. We show that certain key channels – the influence of short-term investors on governance arrangements, pay schemes, and board composition – cannot be expected to have the adverse effect on corporate myopia that is often suggested in policy debates. To be sure, our analysis does not preclude short-term investors from having adverse effect through some other channel, and future work could investigate whether such channels exist. In the meantime, however, policy discussions regarding investor horizons and corporate myopia should be informed by our analytical results, and our framework of analysis can provide a solid foundation for such discussions.

2 Framework of Analysis

We consider a public firm which is run by a manager and owned by shareholders. We follow the Stein Model with two periods, where the first period represents the short-term and the second and final period represents the long-term. We have the following sequence of events, which is summarized in Figure 1 below:

- t = 0, choice of governance structure
- t=1, short term period:

a: choice of myopic actions level

b: realization and disclosure of first period profits

c: market trading

d: vote whether to replace the manager

• t=2, long term period:

a: second period operations

b: realization of second period profits

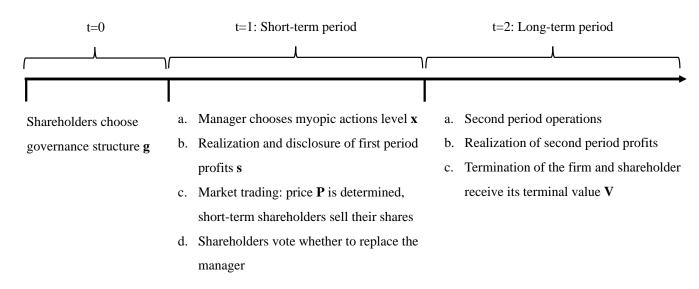


Figure 1 - Timeline of the model

Manager. The company is run by an incumbent team of directors and executives. Following the Stein Model, we view them for convenience as one agent and refer to that agent as the manager. We denote by $a_I \sim N(\mu, \sigma_a^2)$ the ability of the manager (i.e., skills, expertise, and talent). The manager's ability affects the terminal value of the firm, which we denote by V. We assume that shareholders and the manager are symmetrically uninformed about a_I , but they share the same prior.

Shareholders. We consider two types of shareholders. The first type of shareholders have long investment horizon; they hold onto their shares until the terminal period. The utility of these shareholders, which we denote by u_{LT} , is the terminal value of the firm net of compensation to the manager, which we specify below. The second type of shareholders have a short investment horizon; they must sell their shares before the terminal value is realized (later on we discuss cases with more than two types of shareholders in terms of investment horizon). We denote the interim share price that short-term shareholders receive when they sell their shares by P. Therefore, the utility of these shareholders, which we denote by u_{ST} , is proportional to the interim share price. Both types of shareholders are diversified and are not exposed to the idiosyncratic risk of the firm. Effectively, shareholders are assumed to be risk neutral.

Governance structure choice. At the outset, the firm has a governance structure in place that can be potentially influenced by shareholders (e.g., by submitting a shareholder proposal). In particular, at time t=0, shareholders vote on a governance structure of the firm $g\in[0,\overline{g}]$, where $\overline{g} > 0$. A change to the governance structure requires the approval of the majority of the shareholders in a vote. We interpret q as the level of insulation of corporate insiders from the market, where higher g implies higher insulation. More specifically, the level of g determines the cost that the firm must incur to replace a manager at the end of the first period. The cost is affected by takeover defenses, legal challenges, and search costs. We assume these costs are drawn from the resources of the firm. Therefore, a larger q is also a larger commitment not to fire the manager even if it is efficient to do so ex-post. Since in practice the governance structure of public companies is observable, we assume that the choice of q is public. The focus of the paper is on the optimal level of q that is set at the initial voting stage by shareholders. As we discuss below, the assumption that q is observable will play a key role in our analysis. We start by assuming that short-term shareholders have no rights to vote or make proposals, and we will relax this assumption later on and introduce participation rights to assess the effect of their introduction on share value.

Choice of myopic actions level. After the governance of the firm is determined by share-holders, the manager decides on $x \in [0, \overline{x}]$, which affects the profitability of the firm. It will become clear below that this decision can be interpreted as the allocation of resources between short-term and long-term projects, or simply earning management. Therefore, we refer to x as the level of myopic actions. We assume the expected increase in the profitability of the firm at the first period is given by x, whereas the expected decline in the profitability of the firm at the second period is given by K(x), where K(0) = 0, K'(0) = 1, and $K''(\cdot) > 0$ for all $x \in [0, \overline{x}]$. Intuitively, the myopic actions are inefficient with this inefficiency increasing in the amount of short-termism. Importantly, as in the Stein Model, the decision x is unobserved by the market.

First period profits. While the choice x is unobserved by the market, the profitability of the firm at the first period becomes public immediately after the manager makes his decision. The first period profit, which we denote by s, depends on the incumbent manager's ability a_I , the level of myopic actions x, and luck $\varepsilon \sim N(0, \sigma_{\varepsilon}^2)$ which is independent of a_I . Specifically,

$$s = a_I + x + \varepsilon. \tag{1}$$

Therefore, good performances in the short-term can be attributed to luck (ε) , high ability of the incumbent manager (a_I) , or high level of myopic actions (x). Action x is myopic in the sense that it inflates the current performances of the firm at the cost of its future.

First period trading. After the first period profits are realized and disclosed, there will be trading of the firm's share. At this point the short-term investors unload their shares and sell. The share price of the firm is determined by the expectations of the market about the terminal value of the firm. The market does not directly observe the level of myopic actions chosen by the manager, although it will have the correct expectations in equilibrium as in the Stein Model. Instead, the market bases its expectations on the available public information which includes the first period profits s and the initial decision of shareholders about s. To reflect this dependence, we denote the interim share price as s0 and s1.

Vote whether to replace the manager. Given the realization and disclosure of the first period profits, shareholders either retain the incumbent manager (e = retain) or replace him with a new manager that will run the firm in period 2 (e = fire). How difficult it is to replace the manager, and therefore, how likely it is to happen, will depend on the governance structure g that is chosen at time 0. To fire the manager, the firm must incur a cost of g. If the incumbent manager is removed, then a new manager with ability $a_R \sim N(\mu, \sigma_a^2)$ is hired, where a_R is independent of a_I .

Second period profits and terminal value. At this stage, the second period profits are realized. If the ability of the manager who is running the firm at that point is a_{LT} , and the level of myopic actions is x, then the second period profits are given by $\lambda a_{LT} - K(x)$, where $\lambda > 0$ captures the importance of the manager's ability to the long-term firm value relative to the short-term. Therefore, the value of the firm, gross of the cost of replacing the manager, is

$$\Pi\left(a_{LT}, x\right) = \underbrace{a_I + x + \varepsilon}_{\text{short-term}} + \underbrace{\lambda a_{LT} - K\left(x\right)}_{\text{long-term}}.$$
(2)

Finally, the terminal value of the firm is realized according to the initial level of x and the talent of the manager in office, net of the cost of firing the manager, if the incumbent manager

⁵The same result holds if instead the share price is determined after shareholders decide whether to fire the manager.

 $^{^{6}}$ In practice, shareholders do not vote directly on the replacement of CEOs; it is the responsibility of the board of directors. Instead, shareholders elect directors. Therefore, a higher g implies that it is harder to remove incumbent directors from office.

was fired. The terminal value of the firm is⁷

$$V(g, x, e, a_I, a_R) = \begin{cases} \Pi(a_I, x) & \text{if } e = retain \\ \Pi(a_R, x) - g & \text{if } e = fire. \end{cases}$$
 (3)

Management compensation and private benefits. The incumbent manager receives a monetary compensation that is proportional to the terminal value of the firm. Specifically, he receives $\omega_1 V$ for his work in period 1 and $\omega_2 V$ for his work in period 2, if he is still running the firm at that time. For simplicity, we assume $\omega_1 = 0$ and denote $\omega = \omega_2 \in [0, 1)$. Adding a fixed salary to the manager's compensation would not qualitatively change the main results. The total payoff of the incumbent manager, who is risk neutral, is

$$u_{M} = \mathbf{1}_{e=retain} \cdot \left[\omega V \left(g, x, retain, a_{I}, a_{R} \right) + b \right]. \tag{4}$$

Notice that the manager's compensation is not tied directly to the interim share price. We relax this assumption in Section 4.2, where we consider the affect of short-term compensation. Also note that, in addition to his monetary compensation, the manager has non-pecuniary private benefit b > 0 from keeping his job until the terminal period (e.g., the publicity and prestige that comes with the status of being a CEO of a public firm). If the manager is fired, then he loses his monetary compensation for the second period and private benefits, but he receives his outside option which we normalize to zero. We assume the private benefits are sufficiently large so the incumbent manager never resigns his job voluntarily if shareholders prefer him to stay.⁸ Finally, we assume the new manager is compensated by the same amount as the incumbent at the second period, so shareholders' decision to replace the manager is not motivated by their desire to reduce managerial compensation. Moreover, the new manager enjoys the same private benefits from his job as the incumbent manager, so the social welfare is not directly affected by the decision to replace the incumbent.

⁷Notice that the cost g is deducted from the resources of the firm. Similar results hold if the cost is privately incurred by shareholders.

⁸Specifically, we assume $b/\omega + \overline{x} - K(\overline{x}) + (1+\lambda)(\mu - \overline{g}/\lambda - \overline{x}) \ge 0$. This assumption is needed since, in principle, the ability of the manager, which is normally distributed, can be low enough to justify a voluntary resignation. The wedge between the shareholders' and the manager's preferences stems from the assumption that the manager has private information about the level of myopic actions x, and therefore, his inference about his own ability from the first period profit s could be different from the inference of shareholders. If the manager is more pessimistic about his ability than shareholders (since the actual level of myopic actions is higher than anticipated by shareholders), he may prefer resigning and consuming his outside options over retaining his job.

3 Governance and Myopia with No Participation Rights for Short-Term Shareholders

As in the Stein model, the threat of replacement can induce the manager to choose myopic actions. In this section we analyze how the equilibrium level of myopic action, which we denote by x^* , depends on the chosen governance structure g. We solve the model backwards. In Subsection 3.1 we examine how the decision of shareholders to replace the manager is affected by the level of myopic actions and the initial governance structure. In Subsection 3.2 we analyze the manager's expected payoff for any given level of myopic action and governance structure. In Subsection 3.3, we characterize the level of myopic action chosen by the manager for any given initial governance structure. Last, in Subsection 3.4 we study the optimal choice of the governance structure g by long-term shareholders. All proofs not in the main text are given in the Appendix.

3.1 The choice to replace the manger after the first period

Consider the decision of shareholders to fire the manager given the first period profits s. At this stage, the governance structure is fixed at g and the level of myopic action x is no longer reversible. Therefore, the decision of shareholders to retain the incumbent manager depends only on their inference about his ability relative to a potential replacement. We establish the following result.

Lemma 1 Given governance structure g, realized first period profit s, and an expected level of myopic action x^* , shareholders retain the incumbent manager if and only if

$$\hat{\mu}\left(s, x^*\right) > \mu - g/\lambda. \tag{5}$$

where

$$\hat{\mu}(s, x^*) \equiv \frac{\sigma_{\varepsilon}^2}{\sigma_{\varepsilon}^2 + \sigma_a^2} \mu + \frac{\sigma_a^2}{\sigma_{\varepsilon}^2 + \sigma_a^2} (s - x^*).$$
 (6)

To understand Lemma 1, note that, in equilibrium, shareholders expect the level of myopic action to be x^* , and the first period profit to satisfy $s = a_I + x^* + \varepsilon$. Given the normality

⁹The solution concept is Perfect Bayesian Equilibria.

assumptions for a_I and ε , it follows from a standard normal learning model that shareholders' posterior inference for the ability of the incumbent manager is normally distributed with mean $\hat{\mu}(s, x^*)$ and variance $(\frac{1}{\sigma_{\varepsilon}^2} + \frac{1}{\sigma_a^2})^{-1}$, where the former is given by Expression (6) in Lemma 1. Intuitively, shareholders' posterior beliefs about the manager's ability are the weighted average of their prior μ and what their best estimate of ability would be if they only observed s and had a diffuse prior. A higher realization of first period profits implies that the manager has a higher ability, and shareholders update their beliefs accordingly. Notice that shareholders believe that the first period profits s are inflated by s, and account for that. The weights that are put on the prior versus the new estimate depend on the signal to noise ratio—that is, if the prior is very noisy (high σ_s^2), more weight is put on the new information, while if the new information is very noisy (high σ_s^2), more weight is put on the prior. This explains Expression (6).

Since the sensitivity of firm value to the ability of the manager in the long-term is λ , and since firing the manager cost shareholders g, shareholders retain the incumbent if and only if $\lambda \hat{\mu}(s, x^*) > \lambda \mu - g$, which is exactly Condition (5). This proves Lemma 1.

3.2 The manager's payoff given the myopia level

Before analyzing the choice of the manager on the level of myopic action, we derive the manager's expected payoff in closed form. For this purpose, let ϕ and Φ represent the density function and the cdf of the standard normal distribution, respectively. We have the following result.

Lemma 2 Suppose shareholders expect the level of myopic action to be x^* but the manager decides on x. The manager's expected payoff is

$$U_M(x, x^*; g) = (b + \omega \Pi(\mu, x)) (1 - \Phi(\tau(x - x^*))) + \omega(1 + \lambda) \Sigma \phi(\tau(x - x^*))$$
(7)

where $\Sigma \equiv \sqrt{\frac{\sigma_a^4}{\sigma_\varepsilon^2 + \sigma_a^2}}$ and

$$\tau (x - x^*) \equiv \frac{1}{\Sigma} \left(-g/\lambda - \frac{\sigma_a^2}{\sigma_\varepsilon^2 + \sigma_a^2} (x - x^*) \right). \tag{8}$$

The closed form of $U_M(x, x^*; g)$ has an intuitive interpretation. The first term in Expression (7), $b+\omega\Pi(\mu, x)$, is the payoff of the manager if he is retained by shareholders. The payoff of the

manager is composed of his private benefits b and the equity share in the firm's terminal value, $\omega\Pi(\mu, x)$. Notice that the manager is initially uninformed about his ability, and therefore, the terminal firm value is evaluated at the expected ability μ .

The second term in Expression (7), $1-\Phi\left(\tau\left(x-x^*\right)\right)$, is the probability the manager ascribes to the event that shareholders retain him if in equilibrium he is expected to choose x^* but in fact he was choosing x. That is, $1-\Phi\left(\tau\left(x-x^*\right)\right)$ is the probability of $\hat{\mu}\left(s,x^*\right)\geq\mu-g/\lambda$ given $s=a_I+x+\varepsilon.^{10}$ Notice that $1-\Phi\left(\tau\left(x-x^*\right)\right)$ is increasing in g and $x-x^*$. The effect of g is obvious; a higher cost of replacing the manager implies a lower probability of being fired. To understand the effect of $x-x^*$, notice that if the manager chooses a higher level of myopic action than what is anticipated (i.e., $x-x^*>0$ is large), shareholders will attribute high realizations of the first period profits to a high managerial ability (and in part to a bad draw of luck, ε) rather than myopic actions, and as a consequence, they are more likely to retain the manager. This observation also implies that the manager will have incentives to inflate the first period profits of the firm by choosing a larger x.

The third term in Expression (7) is a bit more subtle. Shareholders retain the manager if and only if his inferred ability is sufficiently high, that is, $\hat{\mu}(s, x^*) \ge \mu - g/\lambda$. Therefore, conditional on being retained, the manager believes that his ability is higher, and as a consequence, his equity compensation is also higher in those cases. This informational effect is captured by the term $\omega(1 + \lambda) \Sigma \phi(\tau(x - x^*))$.

3.3 The equilibrium myopia level

Given g and x^* , the manager chooses x that maximizes his expected payoff $U(x, x^*; g)$. In equilibrium, shareholders correctly anticipate the decision of the manager, even though they

¹⁰Notice that we invoked the assumption that the manager does not resign voluntarily when shareholders choose to retain him. If the manager resigns voluntarily, he obtains his outside option, which is zero. However, if shareholders retain the manager and the manager does not resign, conditional on realization of s, the manager gets $\omega\Pi\left(x,\hat{\mu}\left(s,x\right)\right)+b$. Notice that similar to shareholders, the manager also learns about his ability from s. However, unlike shareholders, the manager does not need to form expectations about the level of x; he directly observes it. In principle, the manager may choose a different x than what is anticipated by shareholders (i.e., $x \neq x^*$ is possible off the equilibrium path). Therefore, from the manager's perspective, his expected ability conditional on choosing x and the realization of s is $\hat{\mu}\left(s,x\right)$. The manager resigns voluntarily if and only if $\omega\Pi\left(x,\hat{\mu}\left(s,x\right)\right)+b<0$. Assuming $b/\omega+\overline{x}-K\left(\overline{x}\right)+\left(1+\lambda\right)\left(\mu-\overline{g}/\lambda-\overline{x}\right)\geq 0$ guarantees that Condition (5) implies $\omega\Pi\left(x,\hat{\mu}\left(s,x\right)\right)+b\geq 0$.

do not observe it directly. That is, $x = x^*$. Therefore, $x^*(g)$ must solve

$$\frac{\partial U_M(x, x^*; g)}{\partial x}|_{x=x^*} = 0. \tag{9}$$

The next result characterizes the equilibrium level of myopic actions.

Proposition 1 For any governance structure g, the equilibrium level of myopic actions $x^*(g)$ is strictly positive and decreasing in g and ω . Moreover, if $x^*(g) < \overline{x}$ then $x^*(g)$ is given by the unique solution of

$$\omega (K'(x^*) - 1) (1 - \Phi(\tau(0))) = (b + \omega \Pi (\mu - g/\lambda, x^*)) \phi(\tau(0)) (\sigma_{\varepsilon}^2 + \sigma_a^2)^{-\frac{1}{2}}.$$
 (10)

Proposition 1 implies that level of myopic actions in equilibrium is decreasing with the level of market insulation (i.e., the weakness of the governance structure) and the managerial skin in the game. The intuition is the following. The only reason the manager chooses inefficient myopic actions is to reduce the probability that shareholders replace him after the profits of the first period are realized. As g increases, the likelihood that shareholders find it optimal to replace the manager decreases. Therefore, the benefit from inefficiently inflating the first period profits decreases as well. In general, because $\omega > 0$, the manager at least partially internalizes the negative effect of myopic actions on the terminal value of the firm. Therefore, a larger ω implies that the manager will make fewer inefficient investments.

More specifically, Equation (10) has the following intuitive meaning. The left hand side is the marginal cost of choosing myopic actions from the perspective of the manager, while the right hand side is the marginal benefit. To understand these expressions, consider first the left hand side. If shareholders retain the manager, which happens with probability $1 - \Phi(\tau(0))$, then the manager will receive as compensation his share of the terminal value. Since K' > 1, myopic actions reduces the terminal value of the firm, which the manager at least partly internalizes as long as $\omega > 0$. Therefore, the left hand side of Equation (10) is the negative effect of myopic actions on the manager's payoff.

Consider the right hand side of Equation (10). The only benefit of the manager from myopic actions is the higher likelihood that shareholders will retain him. In equilibrium, however, the manager cannot fool the shareholders; they have the correct expectations about x. But since shareholders do not observe directly the actual level of myopic actions, the manager

cannot avoid the temptation to nevertheless increase x. The marginal effect of an increase of x on the decision of shareholders is inducing them to retain the manager when their inference about his ability is exactly $\mu - g/\lambda$. The first term in the right hand side of Equation (10), $b + \omega \Pi (\mu - g/\lambda, x^*)$, is the payoff to the manager from inducing shareholders to retain him when his ability is exactly $\mu - g/\lambda$. The second term, $\phi(\tau(0))$, is the probability that the shareholders will be exactly indifferent between firing and retaining the manager, which is the only event where a higher x could change their decision. The third term, $(\sigma_{\varepsilon}^2 + \sigma_a^2)^{-\frac{1}{2}}$, captures the sensitivity of the first period profits to the level of myopic actions. If σ_{ε}^2 or σ_a^2 are large, then shareholders ascribe variation in s to noise or to the ability of the manager, rather than to myopic actions. Therefore, the effect of x on shareholders' beliefs, and consequently on their decision to retain the manager, is smaller. The marginal benefit from myopic actions is weaker when $\sigma_{\varepsilon}^2 + \sigma_a^2$ is larger. This explains Equation (10).

3.4 Governance Structure Preferred by Long-Term Shareholders

Form the perspective of long-term investors, the optimal governance structure is the one that maximizes the terminal value of the firm. Based on the analysis in the previous section, the expected terminal value of the firm as a function of g is

$$E[V(g)] = x^*(g) - K(x^*(g)) + \mu + E[\max\{\lambda \hat{\mu}(s, x^*(g)), \lambda \mu - g\}].$$
 (11)

Equation (11) can be explained intuitively as follows. The first two terms embed the effect of myopic actions on firm value. The last two terms embed the effect of managerial ability on firm value. In particular, the last term is the option value from replacing the incumbent manager if it turns out that his ability is low. Notice that, in equilibrium, shareholders have correct expectations about the level of myopic actions, and therefore, $\hat{\mu}(s, x^*(g)) = \hat{\mu}(a_I + \varepsilon, 0)$. In other words, the option value of replacement is independent of $x^*(g)$, but it does decrease in g, which is effectively the strike price of this option.

Since $u_{LT} = (1 - \omega) V$, long-term shareholders prefer the governance structure that maximizes Equation (11). Therefore, the optimal governance structure from the perspective of

long-term investors is formally defined as¹¹

$$g_{LT}^{*} \in \arg\max_{g \in [0,\overline{g}]} E\left[V\left(g\right)\right]. \tag{12}$$

The analysis indicates that the optimal governance structure from the perspective of long-term shareholders may still induce some level of managerial myopia, that is, $g_{LT}^* < \overline{g}$ is possible. To understand this observation, recall that according to Proposition 1, $x^*(g)$ is decreasing in g. Therefore, $x^*(g) - K(x^*(g))$ is increasing in g. By providing the manager with insulation from market pressure (i.e., g > 0), long-term shareholders can reduce managerial myopia and thereby increase the terminal value of the firm. At the same time, a higher g also reduces the value of the option to replace the incumbent manager if shareholders learn he is unskilled. The optimal governance g_{LT}^* trades off these two opposing effects. Therefore, in general, even from the perspective of long-term shareholders, it may be optimal to induce some level of managerial myopia by ensuring that the option to replace the manager is in the money. 12

4 Right of Short-Term Shareholders to Participate in Governance Changes

4.1 Right to Make and Vote on Proposals

In this subsection we introduce the right of short-term shareholders to make proposals and to vote on them. Form the perspective of short-term investors, who sell their shares after the first period profits are realized, the optimal governance structure is the one that maximizes the expected share price at that point of time. Since the governance structure g is observable, in general, the interim stock price will depend on the initial choice of g. Therefore, the optimal governance structure from the perspective of short-term investors is formally defined as

$$g_{ST}^* \in \arg\max_{g \in [0,\overline{g}]} E\left[P\left(s,g\right)\right]. \tag{13}$$

¹¹ Since E[v(g)] is continuous on the closed interval $[0, \overline{g}]$, a maximum always exists (although its uniqueness is not guaranteed).

¹²For example, if λ is sufficiently large, then the shareholder value is mostly driven by the ability of the manager at the second period; the impact of myopic actions is a second order. In those cases, the optimal governance structure will be a low g, reflecting the desire of shareholders to increase the value of the option to replace a low ability manager.

Notice that the market correctly believes that the equilibrium level of myopic actions is $x^*(g)$. Therefore, conditional on s,

$$P(s,g) = x^{*}(g) - K(x^{*}(g)) + \hat{\mu}(s, x^{*}(g)) + E[\max{\{\lambda \hat{\mu}(s, x^{*}(g)), \lambda \mu - g\}} | s = a_{I} + x^{*}(g) + \varepsilon].$$
(14)

The interpretation of Equation (14) is very similar to the interpretation of Equation (11). The key difference is that, in the former, the estimation of the terminal value is conditional on the realization of the first period profits, s. Indeed, at the time when the interim share price is determined, the first period profits are realized and disclosed to the market.

The next proposition is our main result.

Proposition 2 The optimal governance structure from the perspective of long-term and short-term shareholders is the same, that is,

$$g_{ST}^* = g_{LT}^*. (15)$$

To prove Proposition 2, simply note P(s,g) = E[V(g)|s], and therefore, by the law of iterated expectations,

$$E[P(s,g)] = E[V(g)], \qquad (16)$$

where E[V(g)] is given by Equation (11). That is, shareholders who sell their share at the interim period get the same expected value as shareholders who keep their shares until the terminal value is realized.¹³ Since long-term and short-term shareholders solve the same optimization problem, they have identical preferences over the governance structure, as required.

Intuitively, since the governance structure on which shareholders vote is observed by the market, governance structures that are expected to harm the terminal value of the firm will be correctly priced by the market to reflect these lower valuations. Therefore, the policy the maximizes the expected interim share price also maximizes the expected terminal value of the firm, and short-term shareholders will prefer exactly the same governance structure that will be preferred by the long-term shareholders. As a result, if the investment horizon is the only source of heterogeneity in the shareholder base, shareholders will always reach a consensus on

Notice that the expected terminal value of the firm, E[v(g)], is a mean-preserving spread of the expected interim share price, E[p(s, q)].

the optimal governance mechanism.

Our result that short-term shareholders would not prefer to push for governance structures that put more pressure on the short-term unless these structures have long-term benefits that make them also attractive for long-term shareholders has empirical implications. Consistent with this observation, we note that active funds like Fidelity, T.RowePrice, and American have been supportive of moves from staggered board to annual director elections (Bebchuk et al. 2013). Annual elections make all directors come for a vote each year and thereby could arguably increase short-term pressure on incumbents. However, we note that the move to annual elections has been widely supported by investors with long investment horizon such as Vanguard, BlackRock and State Street (Bebchuk et al. 2013).

More generally, our analysis predicts that, all else equal,¹⁴ voting decisions on governance arrangements that put short-term pressure on incumbents should not be associated with the investment horizon of the institutional investors. Governance arrangements that put short-term pressure on incumbents include shareholders proposals to lower threshold on calling for special shareholder meeting and introducing shareholder rights to act by written consent.

4.2 Right to Affect Compensation Structure

Thus far we treated the compensation structure of the manager as given and assumed that the choices of shareholders at time 0, when they can exert influence, are limited to the governance structure of the firm. However, the incentives of the manager might be influenced not just by the governance structure but also by the compensation arrangement, on which shareholders may also have influence. Indeed, in the United States shareholders in most companies vote annually on say-on-pay proposals and it is widely viewed that these votes as well as the positions that shareholders express have significant influence on compensation structures (e.g., see Ertimur et al. 2013).

Therefore, in this section we extend the model and consider the preferences of long-term and short-term shareholders over the compensation structure of the manager. However, we do not examine the full range of compensation arrangements, instead, we focus on the preferences of investors over long-term and short-term compensation structure. In the baseline model the

¹⁴There could be other factors that affect voting behavior, for example, the extent to which institutional investors derive revenues from managing 401K plans for public companies (e.g., Cvijanoviet et al. 2016). These factors should be controlled for in the empirical analysis.

compensation of the manager was long-term in the sense that it was tied to the terminal value of the firm. Here, we also consider cases where the compensation of the manager is tied to the short-term, that is, to the interim share price (or alternatively, the compensation contract allows the manager to sell a fraction of his shares at the short-run). Specifically, the manager's payoff is

$$u_{M} = \eta P\left(g, s\right) + \mathbf{1}_{e=retain} \cdot \left[\left(\omega - \eta\right) V\left(g, x, retain, a_{I}, a_{R}\right) + b\right], \tag{17}$$

where $\eta \in [0, \omega]$ measures the fraction of the compensation that is short-term. We assume the compensation structure of the manager is observable. Since the total amount of compensation that the manager receives is ω , the payoff of long-term and short-term shareholders is the same as in the baseline model. Notice that the baseline model is a special case where $\eta = 0$. If $\eta = \omega$ then all the compensation of the manager is short-term. This formulation abstracts from the optimal level of managerial compensation, as captured by parameter ω . Many factors outside of our model can affect this choice. Instead, our main focus is on the optimal allocation between short-term and long-term compensation, that is, the optimal η .

We denote by $x^*(\eta)$ the equilibrium level of myopic actions as a function of short-term managerial compensation. Similar to the analysis in Section 4.1 we can prove the following result.

Proposition 3

- (i) The equilibrium level of myopic actions, $x^*(\eta)$, is increasing in η where $x^*(\omega) = \overline{x}$.
- (ii) The compensation structure that is most preferred by short-term shareholders is the same as the one that is most preferred by long-term shareholders, and it is given by

$$\eta_{ST}^* = \eta_{LT}^* = 0. {18}$$

Part (i) of Proposition 3 describes how the short-term compensation affects the manager's choice of myopic actions. It shows that with short-term compensation, the manager has stronger incentives to in crease x. Intuitively, with short-term compensation, a higher x not only reduces the likelihood that shareholders will fire the manager (given their expectations about the level of myopic actions), but the interim share price is also likely to be higher, which increases the manager's payoff due to $\eta > 0$. Therefore, as expected, a larger η induces more managerial

myopia. In the limit, when all the managerial compensation is short-term (i.e., $\eta = \omega$), the manager only cares about influencing market expectations, he does not internalize the adverse effect of myopic actions on the terminal value of the firm. In equilibrium, the manager cannot avoid the temptation to inflate the first period profits as much as possible, and as a result, $x^* = \overline{x}$.

Part (ii) of Proposition 3 states that both long-term and short-term shareholders have the same preferences over the compensation structure of the manager. Moreover, it states that both types of shareholders prefer the manager's compensation to be as long-term as possible.

Long-term shareholders. To understand the perspective of long-term shareholders, notice that a higher η induces a higher level of myopic actions, but it has no benefit to shareholders (unlike a lower g which intensifies managerial myopia but also increases the option value of replacing an incompetent manager). Indeed, the expected long-term shareholder value, E[V(g)], which is given by Expression (11), depends on η only indirectly, through its effect on x^* . All else equal, E[V(g)] decreases with x^* , and therefore, long-term shareholders prefer is $\eta = 0$, as required.¹⁵

Short-term shareholders. To understand the perspective of short-term shareholders, notice that the reasoning of Section 4.1 also applies here: since in equilibrium the market has the correct expectations about the level of myopic actions, for a given level of η , the expected interim share price is the same as the expected terminal value of the firm, that is, $E[P(s,\eta)] = E[V(\eta)]$. Moreover, since the compensation structure of the manager is observable to the market, and a larger η implies a higher and inefficient level of myopic actions, short-term shareholders also prefer $\eta = 0$, as required. Therefore, as long as the compensation structure of the manager is observed by the market, short-term shareholders have incentives to set a compensation that minimizes the effect of short-termism.¹⁶

The analysis of this section has empirical implications. For example, it suggests that, all else equal, the tendency to vote against compensation packages that provide short-term incentives in the company's say-on-pay vote should not depend on the of institutional investor's investment

¹⁵The goal of the analysis is not to explain the existence of short-term compensation arrangements in practice. Short-term compensation could be part of an optimal contract if one augments our model with a moral hazard problem or managerial liquidity needs. Instead, our goal is to emphasize that short-term shareholders will have the same preferences as long-term shareholders over the compensation arrangements.

 $^{^{16}}$ If η is hidden, it will have no effect on the optimal choice of long-term shareholders, but it would affect the optimal choice of short-term shareholders; they will be tempted to use short-term managerial compensation to inflate the short-term price. For more details see Section 6.1.

5 Right of Short-Term Shareholders to Participate in Leadership Changes

Over the last decade there has been a large number of cases in which activist hedge funds, which are often viewed as having a short-term investment horizon, obtained seats on corporate boards by winning proxy fights or negotiating settlements (Bebchuk et al. 2017). This empirical evidence raises the question whether short-term shareholders have incentives to take over corporate boards and use its power to inflate the short-term performances of the firm.

Introducing the possibility of short-term leadership. To examine this channel of influence, we extend the model as follows. We assume that at time 0, before the level of myopic actions is determined by the manager, shareholders have the power to put a hedge fund activist on the board. Electing the activist to the board costs g to the firm. For simplicity we assume the governance structure g is given exogenously. The activist joins the board together with other nominees and obtains enough influence such that the incumbent manager has effectively the same preferences as the activist. The activist always leaves the board after the first period profits are realized (so there is no need to fire the activist and incur an additional cost of g at that point of time), and his objective is to maximize the interim share price P.

We assume that by joining the board, the hedge fund activist may also bring expertise and new ideas how to unlock additional shareholder value. Specifically, the strategic plan of the activist can potentially increase shareholder value by $q\theta$ where $\theta \sim (\mu_{\theta}, \sigma_{\theta}^2)$ and $q \in \{0, 1\}$ such that $\Pr[q = 1] = \gamma \in (0, 1)$. Thus, under the leadership of the activist, the first period profit is $s + q\theta$. We assume that the activist privately knows θ but he does not know q. The incumbent manager privately knows q but he does not know θ . Intuitively, the incumbent manager has private information about the likelihood that the strategic plan of the activist will succeed (i.e., q = 1), and the activist has private information about the value of his strategic plan conditional on the plan being successful. We assume that the activist first declares his intention to change the leadership of the firm, then the manager's discloses his private information about q, and finally, shareholders decide whether to appoint the activist to the board.

The effect of leadership changes on the myopia level. Under the influence of the activist, the

manager behaves as if his only objective is to maximize the interim short-term stock price. As one might expect, such preferences lead to a higher level of myopic actions than before (as in Section 4.2). Indeed, once the activist has the ability to secretly influence the manager from inside the board, he cannot resist the temptation to pressure the manager to inflate the interim share price as much as possible, even though in equilibrium the market will have correct expectations about it.

Lemma 3 The change of leadership by an activist induces the manager to choose $x^* = \overline{x}$ in equilibrium.

The circumstances under which an activist initiates a leadership change. The activist initiates a change in leadership only if he expects it to increase the interim stock price. The change in leadership will have two effects. First, it will increase the expected level of myopic actions as described by Lemma 3 above. Second, it will add value of $q\theta$ to the firm. If the manager discloses q=0, then the activist's idea is futile. The activist will necessarily withdraw his campaign, even though a leadership position will give him the power to control the level of myopic actions. If instead the manager discloses q=1 (or remains silent, where silence is interpreted as not being able to fend off the activist), then the activist will pursue his campaign as long as the expected interim share price under his leadership is higher.

Lemma 4 There exists $\mu_{\theta}^* > 0$ such that if and only if $\mu_{\theta} > \mu_{\theta}^*$ and q = 1 the activist initiates a change in leadership.

To understand Lemma 4, notice that since θ is the private information of the activist, the interim share price only depends on the beliefs of the market about θ , rather than its actual realization. The activist, who is a short-termist, will change the leadership of the firm only if the market believes that under his leadership the share value is higher. Therefore, the decision of the activist to change firm's leadership is independent of the actual realization of θ (it only depends on the market beliefs), and the activist cannot credibly reveal information about θ in equilibrium. As a result, in equilibrium, the market believes that the added value by the activist is μ_{θ} , its unconditional expectations. Against this added value, the market expects the change in leadership to increase the level of myopic actions to \overline{x} and costs additional g from the resources of the firm. Therefore, the interim share price under the activist's leadership is

higher than before only if $q\mu_{\theta}$ is positive and sufficiently large, that is, q=1 and $\mu_{\theta} > \mu_{\theta}^*$. These are the circumstances under which the activist will initiate a change in leadership.

Notice that Lemma 4 implies that the activist will pursue a change in leadership only if the market expects his strategic plan to increase value (q = 1 and $\mu_{\theta} > 0$). However, since the activist does not stay for the long-term to "eat his cooking", he will pursue a change in the leadership of the firm even if his strategic plan in fact destroys value (q = 1 and $\theta < 0$), and in spite of the expectations of the market of a higher level of myopic actions ($x^* = \overline{x}$).

Lemmas 3 and 4 raise the critical question whether shareholders would prefer appointing the short-term hedge fund activist to the board, and if so, whether there is a wedge between the preferences of long-term and short-term investors. We obtain the following result.

Proposition 4 There exists $\mu_{\theta}^* > 0$ such that:

- (i) If and only if $\mu_{\theta} > \mu_{\theta}^*$ and q = 1 then the expected terminal value of the firm under the control of the short-term hedge fund activist is higher than under the control of the incumbent manager.
- (ii) The change of leadership will be preferred by short-term shareholders and the activist under exactly the same circumstances that it will be preferred by the long-term shareholders.

To understand the logic of Proposition 4, notice that by following the reasoning of Section 4.1, we can conclude that the expected interim share price is equal to the expected terminal value of the firm. Therefore, the long-term shareholders will always agree with the short-term shareholders on whether to grant the hedge fund activist the control of the board. Both types of shareholders will benefit from doing so as long as the expected interim share price is larger than E[V(g)], which is explicitly given by Expression (11).

Moreover, Proposition 4 states that short-term shareholders will not always seek to appoint the activist to the board, and when they do, long-term shareholders will benefit from that as well. To understand these observations, notice that short-term shareholders face the following trade-off: if they let the activist control the board, the activist will not be able to resist the temptation to inflate the first period profits, in attempt to boost the interim share price. Therefore, the activist will choose a high level of myopic actions, higher than what the manager would have chosen in the absence of the activist's intervention. Since the market observes the appointment of an activist to the board, in equilibrium, the market will anticipate the high level

of myopic actions, and accordingly, will price the share at a low level. Therefore, appointing a short-term hedge fund activist to the board has a the cost of a fully anticipated high level of myopic actions, which is inefficient. Unless the hedge fund activist brings additional expertise and value to the leadership of the company (i.e., if q = 0 or $\mu_{\theta} \leq \mu_{\theta}^*$), even the short-term shareholders will not support his appointment.

On the other hand, if q=1 and μ_{θ} is sufficiently large, then short-term shareholders can increase firm value by deploying the expertise of the activist to board of the company. Since the market observes the appointment of the activist and his expected expertise, it will be reflected in the interim share price. If this expertise is high enough to compensate for the expected high level of myopic actions (i.e., $\mu_{\theta} > \mu_{\theta}^*$), both types of shareholders would benefit from appointing the hedge fund activist to the board.

Notice that although not every arrival of an activist will lead to value-increasing leadership change, the arrival of an activist will have on average a positive expected effect on firm value, consistent with the evidence on 13D filings. Indeed, since in equilibrium the activist pursues a successful change to the leadership of the company if and only if he is expected to increase the terminal value of the firm, the arrival of the activist is always positive news in spite of the activist being short-termist.

The analysis of this section has testable empirical implications. In particular, the analysis suggests that in companies where a majority of shareholders have short-term investment horizon and bring about a leadership change, the leadership change would not adversely affect the value of long-term shareholders.¹⁷ Again, we hope that future empirical work will investigate this issue.

¹⁷Some suggestive evidence in this regard is provided by Bebchuk et al. (2017). This study show that the introduction of directors favored by hedge fund activists into the boardroom, presumably because the issuer expects the hedge fund activist to have a good chance in wining a proxy fight, is not associated with adverse affect on long-term shareholder value down the road.

6 Extensions and discussion

6.1 Pressure from outside the board and the key role of disclosure obligations

An implicit assumption of our analysis is that the manager and short-term shareholders do not have a "secret" channel through which managers can secretly communicate to short-term shareholders the level of myopic actions or agree to adopt compensation or governance arrangements that would be unknown to other shareholders or the market. In practice, Regulation Fair Disclosure (FD) prohibits managers from sharing private information with investors that is not provided to the market at large. Moreover, securities laws require disclosure of governance structures and compensation arrangements, as well as any material agreement between hedge fund activists and managers. For this reason, as long as hedge fund activists do not take over the leadership of the company through board seats, they do not have superior information about myopic unobservable actions relative to other investors that has to be disclosed.

In principle, if such disclosure obligations did not exist or were not tightly enforced, managers would be able to privately share with hedge fund activists information about the level of myopic actions, and one could imagine how this information might have been exploited by short-term investors outside the boardroom. For example, the activist and the manager could reach a secret agreement in which the manager increases the level of myopic actions in return for secret compensation benefits or in order to avoid the pressure from the activist (e.g., publication of adverse information about the manager if he does not comply with the activist's demand). The agreement can be enforced by the manager secretly showing the activist the level of the myopic actions. Therefore, in this world, the presence of short-term investors such as activist hedge funds who have secret channels to managers could lead to an increase in the level of myopic actions and the reduction of long-term firm value. Nowadays, however, this state of affairs is largely precluded by the existing and long-standing disclosure requirements. Our analysis therefore highlights the value and important role of disclosure obligations.

Alternatively, the hedge fund activist may secretly pressure the manager to increase the level of myopic actions, even without obtaining private information from the manager, by making threats to replace the manager if the first period profits are not good in a broad set of circumstances. However, threatening to push for replacing the incumbent manager even when

this is not optimal after the first period will not be credible. Indeed, without private information about the actual level of myopic actions, the activist cannot be sure if the low first period profits are due to bad luck, low ability of the manager, or due to the manager's refusal to increase the level of myopic actions. Alternatively, such a threat can be backed up by the activist's desire to maintain and develop reputation of being able to force out incumbents from office. But if such reputation (or the desire to maintain it) exists, then it is observable and known by the market, and in this case, the market will correctly anticipate that the activist will successfully pressure the manager to increase the level of myopic actions, and as a result, the share price will be lower, making the hedge fund activist worse off. This discussion highlights, once again, that without private information about the level of myopic actions, the activist cannot or will not have the incentives to exacerbate managerial myopia above and beyond what long-term shareholders would prefer.

6.2 Uncertainty about the effects of governance structures

In the body of the paper we assumed that shareholders have the same information as insiders about the effects of governance structures on firm value. But in reality, insiders might have a better idea about the consequences of governance structures, for example, because they have better information about the investment technology and the extent to which myopic actions harm the long-term value of the firm.

Could the information asymmetry between insiders and outside shareholders change the main conclusions of our analysis? The answer is no. To illustrate this point, suppose that myopic actions reduce the terminal value of the firm by $K_1(x)$ with probability $\varphi \in (0,1)$, and by $K_2(x)$ with probability $1 - \varphi$. We assume $K_1(x) \neq K_2(x)$, but these functions have the same generic properties as in the baseline model.¹⁸ The manager knows whether it is $K_1(x)$ or $K_2(x)$, whereas both long-term and short-term shareholders, as well as the market, only know the prior probability of each form. We show that Proposition 2 holds in this setup as well.

Proposition 5 The optimal governance structure from the perspective of long-term and short-term shareholders is the same, that is,

$$g_{ST}^* = g_{LT}^*. (19)$$

¹⁸ Specifically, for i = 1, 2, we assume $K_i(0) = 0$, $K'_i(0) = 1$, and $K''_i(\cdot) > 0$ for all $x \in [0, \overline{x}]$.

To prove Proposition 5, note that in this setup the manager's choice of x will in general depend on his private information. That is, given the governance structure g, the manager will choose in equilibrium $x_1^*(g)$ if the form is $K_1(\cdot)$, and $x_2^*(g)$ if it is $K_2(\cdot)$. Since long-term and short-term shareholders have the same (imperfect) information about the true state of nature, from their perspective, the equilibrium effect of the myopic action on the profit in the first and the second period is $\hat{x}^*(g) \equiv \varphi x_1^*(g) + (1-\varphi)x_2^*(g)$ and $\hat{K}^*(g) \equiv \varphi K_1(x_1^*(g)) + (1-\varphi)K_2(x_2^*(g))$, respectively. Similarly, the expected value of the option to replace the manager at the interim period is $E\left[\max\left\{\lambda\hat{\mu}\left(s,x_1^*(g),x_2^*(g)\right),\lambda\mu-g\right\}\right]$, where $\hat{\mu}\left(s,x_1^*(g),x_2^*(g)\right)$ is the inference about the ability of the manager given realization s of the first period profits. Therefore, and for the same reason as in Section 4.1, the expected terminal value of the firm is the same as the expected interim share price as a function of g. Since the governance structure is observable, long-term shareholders and short-term shareholders will have the same preferences over the choice of g.

This result highlights that the key issue is not whether outside shareholders are perfectly informed, but rather whether all shareholders have access to the same information. As long as this is the case, our work shows that the suspected divergence of interest between long-term and short-term shareholders would not arise in the canonical Stein Model.

6.3 Governance expertise

Our analysis implicitly assumes that all shareholders, regardless of their investment horizon, have the same governance expertise, and therefore, the same ability to change the governance structure. However, some short-term shareholders, especially hedge fund activists, can affect the consequences of any given language of the governance documents. Therefore, an activist with expertise in running proxy fights might find it easier to facilitate a change with any given language.

In the context of our model, this assumption implies that the manager believes that given the governance structure in place, he is more likely to be fired at the end of the first period if short-term shareholders are present. For example, if the governance structure is g and shortterm shareholders with governance expertise are present, the manager will correctly anticipate them to behave as if the cost of replacement is $g - \Delta$, where $\Delta > 0$ captures their governance

¹⁹Notice that the inference about the manager's ability from the first period profit is more complex in this extension, since now shareholders have to account for the two different states of nature.

expertise. Under this assumption, short-term shareholders will induce more corporate myopia, perhaps more than desired by long-term shareholders. However, if short-term shareholders have the right to make and vote on proposals, the optimal governance structure from their perspective will be $g_{LT}^* + \Delta$. That is, short-term shareholders will choose the level of g to be such that the effective governance under their influence and given their expertise is g_{LT}^* . Intuitively, short-term shareholders will give more insulation to the incumbent manager as a means to protect him from their governance expertise. In this respect, our main point remains unchanged; short-term shareholders will propose and vote for only governance changes that will be optimal for long-term shareholders.

6.4 Different types of investment horizons

Our baseline analysis focuses on two types of shareholders; those who hold their shares until the value of the firm is realized, and those who sell everything they own in the interim period. In reality, there is substantial heterogeneity in the investment horizon of different investors. For example, some hedge fund activists such as Nelson Peltz of Trian, emphasize that their investment horizon is longer than the typical activist, and can be as long as 7-8 years. Our analysis can be extended to capture such heterogeneity. For example, one can assume that there is a continuum of types of shareholders who differ with respect to the investment horizon, which we parametrize by $y \in [0,1]$. Parameter y captures the likelihood the investor sells his shares immediately after the first period, or the fraction of shares sold at that point of time. Using the same reasons as in our baseline model, one can establish that the preferences of investors over the governance structure, compensation arrangement, and the potential of taking over the leadership of the company by short-term activists will not depend on the level of y.

7 Concluding Remarks

This paper has sought to contribute to a key and long-standing policy debate regarding public companies and their shareholders. Leading policymakers and business leaders have expressed concerns that the presence of shareholders with short-term investors exacerbates managerial myopia problems and thereby has adverse effects on long-term performance. These concerns have led to an array of proposals for limiting the rights and influence of short-term investors.

We have studied this question within the standard Stein Model that financial economists

have used to study managerial myopia. In this framework, myopia arises from informational asymmetry between corporate insiders and market participants, with the latter group being unable to observe some choices made by the former group. We have shown that, in this standard framework, the presence or share of short-term investors does not have adverse effects. To be sure, certain choices of governance arrangements, pay structures, and leadership changes could exacerbate managerial myopia and have adverse long-term effects. However, we show that short-term shareholders would not systematically prefer different choices from those favored by long-term investors and, in particular, would not push for choices that would involve a higher degree of myopia than the choices favored by long-term investors. A key insight is that when short-term investors influence choices that are observable – as governance arrangements, pay structures, and leadership changes are – they need to take into account that the expected effects of these observable choices will be taken into account also by others and reflected in short-term market prices. Thus, the securities laws that prevent outside short-term investors from having a secret channel to managers and getting privileged access to inside information about observables play an important role.

Of course, future work might examine whether it is possible to ground the expressed concerns about short-term investors in a model not developed within the standard framework. For example, short-term investors could have adverse effects if they were to have nonpublic information about the expected long-term effects of governance, pay, or leadership choices or if their information about these choices were public but still not expected to be reflected in market prices. Of course, if such models are developed, the question would arise whether their assumptions provide a plausible premise.²⁰ In any event, our analytical results within the standard framework should in the meantime inform the debate on short-term investors. We also hope that they will provide a useful starting point and benchmark for any subsequent work on short-term shareholders.

²⁰For early models of myopia problems with public information that not fully reflected in market prices, which can be used as a starting point of such work, see Shleifer and Vishny (1990) and Bolton et al. (2006).

References

- [1] Aghion, Philippe, and Jeremy Stein, "Growth vs. Margins: Destabilizing Consequences of Giving the Stock Market What It Wants," Journal of Finance, 63 (2008), 1025–1058.
- [2] Aspen Institute, Overcoming Short-Termism: A Call for a More Responsible Approach to Investment and Business Management (2009).
- [3] Baldwin Tammy and Jeff Merkley, The Brokaw Act The Problem of Short-Termism & Active Hedge Funds, March 2016.
- [4] Barton Dominic, Capitalism for the Long Term, The Harvard Bus. Rev., (Mar. 2011).
- [5] Bebchuk, Lucian A., The Myth that Insulating Boards Serves Long-Term Value, 113 Colum. L. Rev. 1637 (2013).
- [6] Bebchuk, Lucian A., Brav, A., Jiang, W., Keusch, T., 2017. Dancing with Activists, Working Paper
- [7] Bebchuk, Lucian A., S. Hirst, and J. Rhee, Towards the Declassification of S&P 500 Boards, 3 Harvard Business Law Review 157 (2013).
- [8] Bebchuk, Lucian A. & Lars A. Stole, Do Short-Term Objectives Lead to Under- or Over-investment in Long-Term Projects?, 48 J. Fin. 719 (1993).
- [9] Benmelech, Efraim, Eugene Kandel, and Pietro Veronesi (2010): Stock-based compensation and CEO (dis)incentives. Quarterly Journal of Economics 125, 1769–1820.
- [10] Biden Joe, How Short-Termism Saps the Economy, WALL ST. J., (Sep. 28, 2016).
- [11] Bizjak, John M., James A. Brickley, and Jeffrey L. Coles (1993): Stock-based incentive compensation and investment behavior. Journal of Accounting and Economics 16, 349–372.
- [12] Bolton Patrick and Frederic Samama, L-Shares: Rearding Long-Term Investors, Journal of Applied Corporate Finance, Volume 25, 86-97.
- [13] Bolton, Patrick, Scheinkman, José, and Wei Xiong, 2006, Executive Compensation and Short-Termist Behaviour in Speculative Markets. Review of Economic Studies 73 (3), 577-610.

- [14] Clinton Hillary, Economic Speech Delivered at Warren, MI, Newsweek, (Aug. 11, 2016).
- [15] Cvijanovic, D., A. Dasgupta, and K. E. Zachariadis. 2016. Ties that bind: How business connections affect mutual fund activism. Journal of Finance 71:2933–66.
- [16] Edmans, Alex, Xavier Gabaix, Tomasz Sadzik, and Yuliy Sannikov (2012): Dynamic CEO compensation. Journal of Finance 67, 1603–1647.
- [17] Ertimur, Yonca, Fabrizio Ferri, and David Oesch, 2013, Shareholder votes and proxy advisors: Evidence from say on pay, Journal of Accounting Research 51, 951–996.
- [18] Fink Larry, BlackRock's Chairman CEO, 2017 Corporate Governance Annual Letter to CEOs, January 23, 2017, https://www.blackrock.com/corporate/literature/press-release/2017-ldf-ceo-letter.pdf (hereinafter, Fink 2017 Letter)
- [19] Fox, Justin and Jay W. Lorsch, The Big Idea: What Good Are Shareholders?, Harv. Bus. Rev., July-Aug. 2012, at 49.
- [20] Goldman, Eitan and Steve L. Slezak (2006): An equilibrium model of incentive contracts in the presence of information manipulation. Journal of Financial Economics 80, 603–626.
- [21] Kumar, Praveen, and Nisan Langberg, "Corporate Fraud and Overinvestment in Efficient Capital Markets," RAND Journal of Economics, 40 (2009), 144–172.
- [22] Marinovic, Iván and Felipe Varas (2018): CEO horizon, optimal pay duration, and the escalation of short-termism. Journal of Finance, forthcoming.
- [23] Mayer Colin, Firm commitment: Why the corporation is failing us and how to restore trust in it, Oxford University Press: Oxford, 2013 (2013)
- [24] Narayanan, M.P. (1985), "Managerial incentives for short-term results", Journal of Finance 40(5): 1469-1484.
- [25] Roe, Mark, Stock Market Short Termism's Impact (2018).
- [26] Securities and Exchange Commission, Facilitating Director Shareholder Nominations, 2010
- [27] Shleifer, Andrei, and Robert Vishny, 1990, Equilibrium short horizons of investors and firms, American Economic Review 80, 148–153.

- [28] Stein, Jeremy C., Takeover Threats and Managerial Myopia, 96 J. Pol. Econ. 61 (1988).
- [29] Stein, Jeremy C., Efficient Capital Markets, Inefficient Firms: A Model of Myopic Corporate Behavior, 104 Q.J. Econ. 655 (1989).
- [30] Stiglitz Joseph E., Rewriting the Rules for the American Economy an Agenda for Growth and Shared Prosperity, Roosevelt Institute, (May, 2015).
- [31] Strine, Leo E., Jr., One Fundamental Corporate Governance Question We Face: Can Corporations Be Managed for the Long Term Unless Their Powerful Electorates Also Act and Think Long Term?, 66 Bus. Law. 1 (2010).
- [32] Strine, Leo E., Jr., Securing Our Nation's Economic Future: A Sensible, Nonpartisan Agenda to Increase Long-Term Investment and Job Creation in the United States, 71 BUS. LAW. 1081 (2016).
- [33] Von Thadden, E., 1995, Long term contracts, short term investment and monitoring, Review of Economic Studies 62, 557-575
- [34] Zhu. Y. John Myopic Agency Review of Economic Studies (2018) 85, 1352–1388

Appendix

Proof of Lemma 2. We prove the result for a general managerial preferences as given by (17). The proof has several steps. First, we prove the following claim: if shareholders expect the level of short-termism to be x^* , but the manager decides on x, then from the manager's perspective, $\hat{\mu}(s, x^*)$ is normally distributed with variance Σ^2 and mean

$$m(x - x^*) \equiv \mu + \frac{\sigma_a^2}{\sigma_\varepsilon^2 + \sigma_a^2} (x - x^*).$$

Indeed, by substituting (1) into (6) we get

$$\hat{\mu}(s, x^*) = \frac{\sigma_{\varepsilon}^2}{\sigma_{\varepsilon}^2 + \sigma_a^2} \mu + \frac{\sigma_a^2}{\sigma_{\varepsilon}^2 + \sigma_a^2} (a_I + x + \varepsilon - x^*).$$

Since $a_I \sim N(\mu, \sigma_a^2)$ and $\varepsilon \sim N(0, \sigma_\varepsilon^2)$ are uncorrelated, we have

$$\hat{\mu}(s, x^*) = \mu + \frac{\sigma_a^2}{\sigma_s^2 + \sigma_a^2} [x - x^* + \xi],$$

where ξ is a random variable distributed according to $N\left(0, \sigma_{\varepsilon}^2 + \sigma_a^2\right)$, which concludes the argument.

Second, let F(y) be the cumulative distribution function of $\hat{\mu}(s, x^*)$. Then, $F(y) = \Phi(\frac{y-m(x-x^*)}{\Sigma})$ and $F'(y) \equiv f(y) = \frac{1}{\Sigma}\phi\left(\frac{y-m(x-x^*)}{\Sigma}\right)$. We argue

$$\int_{\mu-g/\lambda}^{\infty} y dF(y) = m(x - x^*) (1 - \Phi(\tau(x - x^*))) + \Sigma \phi(\tau(x - x^*)).$$
 (20)

To see why, recall that for the normal distribution $\phi'(y) = -y\phi(y)$. Therefore, $f'(y) = -\frac{y-m(x-x^*)}{\Sigma^2}f(y)$, which implies by simple algebra

$$yf(y) = m(x - x^*) f(y) - \Sigma^2 f'(y).$$

Therefore,

$$\int yf(y) dy = \int \left[m(x - x^*) f(y) - \Sigma^2 f'(y) \right] dy$$

$$= m(x - x^*) \int f(y) dy - \Sigma^2 \int f'(y) dy$$

$$= m(x - x^*) F(y) - \Sigma^2 f(y)$$

$$= m(x - x^*) \Phi\left(\frac{y - m(x - x^*)}{\Sigma}\right) - \Sigma \phi\left(\frac{y - m(x - x^*)}{\Sigma}\right),$$

and

$$\int_{\mu-g/\lambda}^{\infty} y f(y) dy = \left[m(x-x^*) \Phi\left(\frac{y-m(x-x^*)}{\Sigma}\right) - \Sigma \phi\left(\frac{y-m(x-x^*)}{\Sigma}\right) \right]_{y=\mu-g/\lambda}^{y=\infty}$$
$$= m(x-x^*) \left(1 - \Phi\left(\tau(x-x^*)\right)\right) + \Sigma \phi\left(\tau(x-x^*)\right).$$

Third, let $P(x, x^*) \equiv E[P(g, s)]$ be the expected interim share price from the manager's perspective when shareholders' expected the equilibrium level of short-termism to be x^* but the manager chooses x. Notice that according to Equation (14),

$$P\left(s,g\right)=x^{*}\left(g\right)-K\left(x^{*}\left(g\right)\right)+\hat{\mu}\left(s,x^{*}\right)+\lambda E\left[\max\left\{\hat{\mu}\left(s,x^{*}\left(g\right)\right),\mu_{R}-g/\lambda\right\}|s=a_{I}+x^{*}\left(g\right)+\varepsilon\right].$$

Therefore,

$$\begin{split} P\left(x,x^{*}\right) &= x^{*} - K\left(x^{*}\right) + m\left(x - x^{*}\right) \\ &+ \lambda \int_{-\infty}^{\mu - g/\lambda} \left(\mu - g/\lambda\right) dF\left(y\right) + \lambda \int_{\mu - g/\lambda}^{\infty} y dF\left(y\right) \\ &= x^{*} - K\left(x^{*}\right) + m\left(x - x^{*}\right) + (\lambda\mu - g) \Phi\left(\tau\left(x - x^{*}\right)\right) + \lambda \int_{\mu - g/\lambda}^{\infty} y dF\left(y\right). \\ &= x^{*} - K\left(x^{*}\right) + m\left(x - x^{*}\right) + (\lambda\mu - g) \Phi\left(\tau\left(x - x^{*}\right)\right) \\ &+ \lambda \left[m\left(x - x^{*}\right)\left(1 - \Phi\left(\tau\left(x - x^{*}\right)\right)\right) + \Sigma \phi\left(\tau\left(x - x^{*}\right)\right)\right], \end{split}$$

which can be rewritten as

$$P(x - x^{*}) = x^{*} - K(x^{*}) + m(x - x^{*})(1 + \lambda)$$

$$+ (\lambda \mu - g - \lambda m(x - x^{*})) \Phi(\tau(x - x^{*})) + \lambda \Sigma \phi(\tau(x - x^{*})).$$
(21)

Fourth, since $\hat{\mu}(s,x) = \hat{\mu}(s,x^*) + \mu - m(x-x^*)$, the manager's expected payoff is

$$U_{M}(x, x^{*}; g, \eta) = \int_{\mu-g/\lambda}^{\infty} \left[b + (\omega - \eta) (x - K(x)) + (\omega - \eta) (1 + \lambda) (y + \mu - m(x - x^{*})) \right] dF(y) + \eta P(x, x^{*})$$

$$= (1 - \Phi(\tau(x - x^{*}))) \left[b + (\omega - \eta) (x - K(x)) + (\omega - \eta) (1 + \lambda) (\mu - m(x - x^{*})) \right] + (\omega - \eta) (1 + \lambda) \int_{\mu-g/\lambda}^{\infty} y dF(y) + \eta P(x, x^{*})$$

$$= (1 - \Phi(\tau(x - x^{*}))) \left[b + (\omega - \eta) (x - K(x)) + (\omega - \eta) (1 + \lambda) (\mu - m(x - x^{*})) \right] + (\omega - \eta) (1 + \lambda) \left[m(x - x^{*}) (1 - \Phi(\tau(x - x^{*}))) + \Sigma \phi(\tau(x - x^{*})) \right] + \eta P(x, x^{*})$$

$$= (1 - \Phi(\tau(x - x^{*}))) \left[b + (\omega - \eta) (x - K(x)) + (\omega - \eta) (1 + \lambda) \mu \right] + (\omega - \eta) (1 + \lambda) \Sigma \phi(\tau(x - x^{*})) + \eta P(x, x^{*})$$

Noting that $\Pi(\mu, x) = x - K(x) + (1 + \lambda)\mu$ and letting $\eta = 0$ gives Expression (7).

Proof of Proposition 1. First note that

$$\begin{split} \frac{\partial P\left(x,x^*\right)}{\partial x} &= \left(1+\lambda\right)\frac{\sigma_a^2}{\sigma_\varepsilon^2+\sigma_a^2} \\ &-\lambda\frac{\sigma_a^2}{\sigma_\varepsilon^2+\sigma_a^2}\Phi\left(\tau\left(x-x^*\right)\right)+\left(\lambda\mu_R-g-\lambda m\left(x,x^*\right)\right)\phi\left(\tau\left(x-x^*\right)\right)\frac{-\frac{\sigma_a^2}{\sigma_\varepsilon^2+\sigma_a^2}}{\Sigma} \\ &-\lambda\Sigma\phi\left(\tau\left(x-x^*\right)\right)\frac{-\frac{\sigma_a^2}{\sigma_\varepsilon^2+\sigma_a^2}}{\Sigma}\tau\left(x-x^*\right) \\ &= 1+\lambda-\lambda\Phi\left(\tau\left(x-x^*\right)\right)>0. \end{split}$$

Differentiating $U_{M}\left(x,x^{*};g,\eta\right)$ with respect to x, and rearranging terms (notice we use the

identity $\phi'(x) = -x\phi(x)$, yields

$$\begin{split} \frac{\partial U\left(x,x^{*};g,\eta\right)}{\partial x} &= \left(\omega-\eta\right)\left(1-K'\left(x\right)\right)\left(1-\Phi\left(\tau\left(x-x^{*}\right)\right)\right) \\ &-\left(b+\left(\omega-\eta\right)\Pi\left(\mu_{I},x\right)\right)\phi\left(\tau\left(x-x^{*}\right)\right)\frac{\partial\tau\left(x,x^{*}\right)}{\partial x} \\ &-\left(\omega-\eta\right)\left(1+\lambda\right)\Sigma\tau\left(x-x^{*}\right)\phi\left(\tau\left(x-x^{*}\right)\right)\frac{\partial\tau\left(x-x^{*}\right)}{\partial x}+\eta\frac{\partial P\left(x,x^{*}\right)}{\partial x} \\ &= \left(\omega-\eta\right)\left(1-K'\left(x\right)\right)\left(1-\Phi\left(\tau\left(x-x^{*}\right)\right)\right) \\ &+\left(\begin{pmatrix}b+\left(\omega-\eta\right)\left(x-K\left(x\right)\right)\\+\left(\omega-\eta\right)\left(1+\lambda\right)\left(\mu-g/\lambda-\frac{\sigma_{a}^{2}}{\sigma_{\varepsilon}^{2}+\sigma_{a}^{2}}\left(x-x^{*}\right)\right)\end{pmatrix}\phi\left(\tau\left(x-x^{*}\right)\right)\left(\sigma_{\varepsilon}^{2}+\sigma_{a}^{2}\right)^{-\frac{1}{2}} \\ &+\eta\left[1+\lambda-\lambda\Phi\left(\tau\left(x-x^{*}\right)\right)\right] \end{split}$$

and

$$\begin{split} \frac{\partial^2 U\left(x,x^*;g,\eta\right)}{\partial^2 x} &= -\left(\omega-\eta\right)K''\left(x\right)\left(1-\Phi\left(\tau\left(x-x^*\right)\right)\right)\\ &+ \left(\omega-\eta\right)\left(1-K'\left(x\right)\right)\phi\left(\tau\left(x-x^*\right)\right)\left(\sigma_{\varepsilon}^2+\sigma_a^2\right)^{-\frac{1}{2}}\\ &+ \left(\omega-\eta\right)\left(\left(1-K'\left(x\right)\right)-\left(1+\lambda\right)\frac{\sigma_a^2}{\sigma_{\varepsilon}^2+\sigma_a^2}\right)\phi\left(\tau\left(x-x^*\right)\right)\left(\sigma_{\varepsilon}^2+\sigma_a^2\right)^{-\frac{1}{2}}\\ &+ \left(\frac{b+\left(\omega-\eta\right)\left(x-K\left(x\right)\right)}{+\left(\omega-\eta\right)\left(1+\lambda\right)\left(\mu-g/\lambda-\frac{\sigma_a^2}{\sigma_{\varepsilon}^2+\sigma_a^2}\left(x-x^*\right)\right)}\right)\\ &\times\phi\left(\tau\left(x-x^*\right)\right)\tau\left(x-x^*\right)\left(\left(\sigma_{\varepsilon}^2+\sigma_a^2\right)^{-\frac{1}{2}}\right)^2\\ &+ \eta\lambda\phi\left(\tau\left(x-x^*\right)\right)\left(\sigma_{\varepsilon}^2+\sigma_a^2\right)^{-\frac{1}{2}}. \end{split}$$

The first order condition requires $\frac{\partial U(x,x^*;g,\eta)}{\partial x} = 0$. Plugging this condition into $\frac{\partial^2 U(x,x^*;g,\eta)}{\partial x^2}$

yields

$$\begin{split} \frac{\partial^{2}U\left(x,x^{*};g,\eta\right)}{\partial^{2}x} &= -\left(\omega-\eta\right)K''\left(x\right)\left(1-\Phi\left(\tau\left(x-x^{*}\right)\right)\right) \\ &+\left(\omega-\eta\right)\left(1-K'\left(x\right)\right)\left[\phi\left(\tau\left(x-x^{*}\right)\right)-\left(1-\Phi\left(\tau\left(x-x^{*}\right)\right)\right)\tau\left(x-x^{*}\right)\right]\left(\sigma_{\varepsilon}^{2}+\sigma_{a}^{2}\right)^{-\frac{1}{2}} \\ &+\left(\omega-\eta\right)\left(\left(1-K'\left(x\right)\right)-\left(1+\lambda\right)\frac{\sigma_{a}^{2}}{\sigma_{\varepsilon}^{2}+\sigma_{a}^{2}}\right)\phi\left(\tau\left(x-x^{*}\right)\right)\left(\sigma_{\varepsilon}^{2}+\sigma_{a}^{2}\right)^{-\frac{1}{2}} \\ &-\eta\left[1+\lambda-\lambda\Phi\left(\tau\left(x-x^{*}\right)\right)\right]\tau\left(x-x^{*}\right)\left(\sigma_{\varepsilon}^{2}+\sigma_{a}^{2}\right)^{-\frac{1}{2}} \\ &-\eta\tau\left(x-x^{*}\right)\left(\sigma_{\varepsilon}^{2}+\sigma_{a}^{2}\right)^{-\frac{1}{2}} \\ &+\eta\lambda\left(\phi\left(\tau\left(x-x^{*}\right)\right)-\left(1-\Phi\left(\tau\left(x-x^{*}\right)\right)\right)\tau\left(x-x^{*}\right)\right)\left(\sigma_{\varepsilon}^{2}+\sigma_{a}^{2}\right)^{-\frac{1}{2}} \end{split}$$

The first row is negative by K'' > 0, the third term is negative by K' > 1. The fourth and fifth terms are also negative. The second and the sixth terms are negative if and only if

$$\Lambda\left(\tau\left(x-x^*\right)\right) \ge \tau\left(x-x^*\right),\,$$

where $\Lambda(\cdot) = \frac{\phi(\cdot)}{1-\Phi(\cdot)}$ is the hazard rate of the normal distribution. Since the hazard rate of a normal distribution is an increasing function, then $\Lambda' \geq 0$. Note that $\Lambda'(y) = \Lambda(y) (\Lambda(y) - y)$, and hence, $\Lambda(y) - y \geq 0$ for all y. We conclude that any solution of the first order condition is a maximum point.

In equilibrium, $x = x^*$, and hence, $\tau\left(x^* - x\right) = \frac{-g/\lambda}{\Sigma}$. Therefore, x^* must solve $\frac{\partial U(x, x^*; g, \eta)}{\partial x}|_{x = x^*} = 0$, which can be rewritten as $\Gamma\left(x^*\right) = 0$ where

$$\Gamma\left(x^{*}\right) = \left(\omega - \eta\right)\left(1 - K'\left(x^{*}\right)\right) + \left(\begin{array}{c} b + \left(\omega - \eta\right)\left(x^{*} - K\left(x^{*}\right)\right) \\ + \left(\omega - \eta\right)\left(1 + \lambda\right)\left(\mu - g/\lambda\right) \end{array}\right) \frac{\phi\left(\tau\left(0\right)\right)}{1 - \Phi\left(\tau\left(0\right)\right)} \left(\sigma_{\varepsilon}^{2} + \sigma_{a}^{2}\right)^{-\frac{1}{2}} + \eta\left(\frac{1}{1 - \Phi\left(\tau\left(0\right)\right)} + \lambda\right).$$

Notice that if $\eta = 0$ then $\Gamma(x^*) = 0$ is equivalent to Equation (10). Since K'' > 0 and x - K(x) is a decreasing function (i.e., K' > 1), $\Gamma(x^*)$ is a decreasing function of x^* , which implies that the solution is unique.

The assumption that the incumbent manager does not resign voluntarily (i.e., $b/\omega + \overline{x}$ –

 $K(\overline{x}) + (1 + \lambda)(\mu - \overline{g}/\lambda - \overline{x}) \ge 0$ implies

$$b + (\omega - \eta) (x^* - K(x^*)) + (\omega - \eta) (1 + \lambda) (\mu - g/\lambda) \ge 0$$
 (22)

for all admissible values. Since $\tau(0) = \frac{-g/\lambda}{\Sigma}$ and the hazard rate of the normal distribution is an increasing function, $\Gamma(x^*)$ is decreasing in g, which implies that $x^*(g)$ is decreasing in g. Moreover, notice that $\Gamma(x^*)$ is increasing in η , which implies that $x^*(\eta)$ is decreasing in η . In fact, if $\eta = \omega$ then

$$\frac{\partial U\left(x,x^{*};g,\eta\right)}{\partial x}=b\phi\left(\tau\left(x-x^{*}\right)\right)\left(\sigma_{\varepsilon}^{2}+\sigma_{a}^{2}\right)^{-\frac{1}{2}}+\omega\left(1+\lambda-\lambda\Phi\left(\tau\left(x-x^{*}\right)\right)\right)>0,$$

that is, the manager has incentives to choose the largest x possible, and in equilibrium, it must be $x^* = \overline{x}$.

Finally, note that combined, (22) and K'(0) = 1 imply $\Gamma(0) > 0$, that is, $x^*(g) > 0$ for all $g \in [0, \overline{g}]$.

Proof of Proposition 3. The proof of Proposition 1 shows that $x^*(\eta)$ is decreasing in η and $\eta = \omega$ implies $x^* = \overline{x}$.

Proof of Lemma 3. Consider the notation of η in Section 4.2. Under the activist's control the manager behaves as if $\eta = \omega$ and b = 0 (recall the activist always leaves the company at the interim period). A corollary of Proposition 3 implies that, in equilibrium, the manager will choose $x^* = \overline{x}$ under the influence of the short-term activist.

Proof of Lemma 4. If the activist does not change the leadership of the firm then the expected share price is E[V(g)], which is given by Expression (11), and it is independent of θ and q. If the manager reveals q = 0 and the activist succeeds in changing the leadership of the firm, then the expected interim share price, denoted by P_A , will be

$$P_{A} = -g + \overline{x} - K(\overline{x}) + \mu + E\left[\max\left\{\lambda \hat{\mu}(s, \overline{x}), \lambda \mu - g\right\}\right], \tag{23}$$

which is strictly smaller than E[V(g)]. Indeed, based on Lemma 3, under the activist influence the manager chooses the highest level of myopic actions, which is expected by the market.

Moreover, a change in leadership costs additional g to the firm. For both of these reasons, the expected interim share price will be lower under the activist control if q = 0 (and regardless of the realization of θ and the beliefs of the market about θ). Notice that since the market correctly expects the level of myopic actions in equilibrium, the value of the option to replace the incumbent manager is not affected by the change in leadership.

Suppose the manager reveals q = 1. Let $\hat{\theta}$ be the beliefs of the market about the expected value of θ conditional on q = 1 and conditional on the activist pursuing a successful campaign. Then, the expected interim share price will be $P_A + \hat{\theta}$. Therefore, the activist benefits from pursuing a campaign and changing leadership if and only if

$$P_A + \hat{\theta} > E[V(g)].$$

Notice that this decision is independent of the actual realization of θ . Since $P_A < E[V(g)]$, notice that there is $\mu_{\theta}^* > 0$ such that $P_A + \hat{\theta} > E[V(g)]$ holds if and only if $\hat{\theta} > \mu_{\theta}^*$. Therefore, if $\hat{\theta} > \mu_{\theta}^*$ then the activist will pursue a campaign regardless of the realization of θ , which implies that $\hat{\theta} = \mu_{\theta}$. If $\hat{\theta} < \mu_{\theta}^*$ then the activist will not pursue a campaign, also regardless of the realization of θ . Similarly, shareholders will approve the campaign if and only if the activist is interested in pursuing it, that is, if and only if $P_A + \hat{\theta} > E[V(g)]$.

Proof of Proposition 4. The proof follows directly from Lemmas 3 and 4, and the main text. ■