

Monetary Policy, Capital Controls, and International Portfolios

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Motivation

- Large literature on optimal monetary policy in open economies...
 - Terms-of-trade management
 - Currency of pricing
 - Financial frictions
- Yet, little about the role of **asset market structure**...
 - Most studies have a single bond or complete markets
 - Potentially relevant! Large increase in size of external balance sheets across many asset classes, valuation effects...

This paper

- Small open economy model
 - ① Incomplete markets + Home asset → insurance objective
 - ② Nominal rigidities → demand-management objective
 - ③ More than one asset → portfolio problem
- Analytical characterization using a small-risks approximation of
 - Optimal monetary policy
 - Optimal portfolio
 - Taxes on financial assets
- Quantitative model: Deviate from inflation targeting?

Related Literature: Contributions

- Optimal Monetary Policy in Open Economies with Incomplete Markets
 - **Closest:** Benigno (2009a, 2009b) and Senay and Sutherland (2017)
- ⇒ Fully optimal policy with portfolio choice; interaction with capital controls
- Joint monetary and portfolio/macprudential policy problem
 - **Closest:** Farhi-Werning (2016), Engel and Park (2017), Ottonello and Perez (2017)
- ⇒ Tighter characterization using approximation; problem with commitment
- Solving DSGE models with portfolio choice
 - **Closest:** Judd and Guu (2001), Devereux and Sutherland (2011), Tille and van Wincoop (2010)
- ⇒ equivalence result; role of portfolio tax

Model

- Today: Two period model
 - Specific preferences, technology & shocks
 - Two assets (home and foreign currency bonds)
- Results are much more general
 - Dynamic, general preferences, technology & shocks
 - Arbitrary asset market structure
- Important assumption: Perfect stabilization under complete markets
 - No financial friction, exogenous terms-of-trade, no mark up shocks, single nominal rigidity...

Preferences

- Home households

$$\mathbb{E} \ln \left(C_{Ts}^\alpha C_{Ns}^{1-\alpha} - \frac{1-\alpha}{1+\psi} L_s^{1+\psi} \right)$$

- Own firms and tradable endowment $\{Y_{Ts}\}$

- Foreign households

$$\mathbb{E} \ln(C_{Ts}^*)$$

- Foreign is large: C_{Ts}^* taken as given

Technology and Market Structure

- Technology

$$Y_{Ns} = Z_s Y_s^I$$
$$Y_s^I(i) = L_s(i)$$

- Y_{Ns} : competitive
- Y_s^I : fixed price $P_s^I(i) = 1 \forall s$

Financial Markets

- 1 Foreign-currency bond B^*

$$1 \rightarrow R^*$$

- 2 Domestic-currency bond B

$$1 \rightarrow RE_0 E_s^{-1}$$

- Free access to all markets by all agents (i.e., no financial friction)

Financial Markets

- 1 Foreign-currency bond B^*

$$1 \rightarrow 1$$

- 2 Domestic-currency bond B

$$1 \rightarrow RE_s^{-1}$$

- Free access to all markets by all agents (i.e., no financial friction)

Government Tools

① Monetary policy: exchange rate rule $\{E_s\}_{s \in S}$

▶ money rule

② Capital controls: portfolio tax τ_B on home asset

$$(1 + \tau_B)B + B^* + T_0 = 0$$

③ Lump-sum subsidies $T_0 \rightarrow$ rebate tax revenue

• Problem under **commitment**

Equilibrium conditions

- Simplifying,

$$\frac{\alpha L_s}{(1 - \alpha) C_{T_s}} = E_s$$

$$Y_{T_s} + (R E_s^{-1} - 1) B = C_{T_s}$$

$$\mathbb{E}((1 + \tau_B)^{-1} R E_s^{-1} - 1) u_T(s) = 0$$

$$\mathbb{E}(R E_s^{-1} - 1) C_s^{*-1} = 0$$

- Note that using the first equation we may write

$$\{C_{N_s}(C_{T_s}, E_s), L_s(C_{T_s}, E_s)\}$$

Planning problem

$$\max_{\{C_{T_s}, E_s^{-1}\}_{s \in S}, R, B} \mathbb{E} \underbrace{V(C_{T_s}, E_s; Z_s)}_{\text{indirect utility}}$$

subject to

$$Y_{T_s} + \underbrace{(RE_s^{-1} - 1)B}_{\text{transfer}} - C_{T_s} = 0$$
$$\mathbb{E} \underbrace{(RE_s^{-1} - 1)B}_{\text{transfer}} C_s^{*-1} = 0$$

$\Rightarrow V$ was obtained replacing $\{C_{N_s}(C_{T_s}, E_s), L_s(C_{T_s}, E_s)\}$

- 1 Monetary policy $\{E_s\}$
- 2 Portfolio B (i.e., decentralized via the portfolio tax τ_B)

Approximation Method

- Parametrize shocks $\zeta_s = \bar{\zeta} + \epsilon u_s$ and study limit $\epsilon \rightarrow 0$
- Two steps
 - 1 Derive standard LQ problem (as in Benigno Woodford 2012) around arbitrary steady-state portfolio
 - 2 Maximize over steady-state portfolio
- FOC of approximate problem coincide with perturbation approach on FOCs of nonlinear problem [▶ more](#)
 - This is true **only** if you have a portfolio tax (or if you do not need it)
 - Otherwise: Additional **quadratic** constraint (see paper)

Approximate Welfare

- Around arbitrary \bar{B} ,

$$\mathbb{E}_0 V(s) = -k_0 \mathbb{E}_0 \left[\frac{1}{2} \chi (1 + \bar{B}\mu)^2 \underbrace{\left(e_s - \frac{e_s^{dm}(0)}{1 + \bar{B}\mu} \right)^2}_{\text{demand-management}} + \frac{1}{2} \underbrace{(\bar{B}e_s + \mathcal{T}_s)^2}_{\text{insurance}} \right] + t.i.p. + O(\epsilon^3)$$

- Two key statistics:

- Desired transfer under complete markets and flexible prices

$$\mathcal{T}_s = \alpha y_{T_s} + c_{T_s}^*$$

- Exchange rate that closes the output gap without home-currency bonds

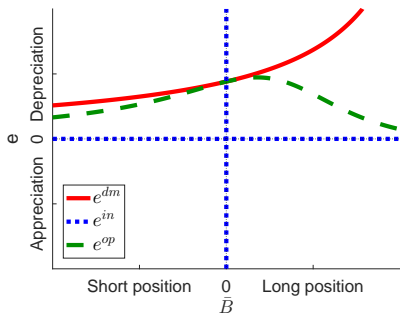
$$e_s^{dm}(0) = \frac{1 - \alpha}{\alpha + \psi} z_s - \frac{\psi}{\alpha + \psi} y_{T_s}$$

- Two important parameters:

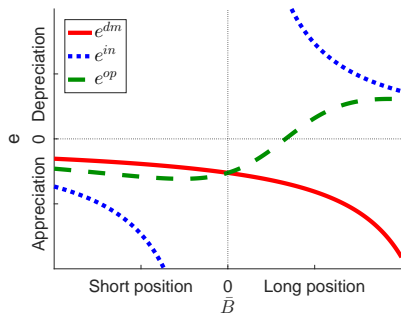
- $\chi = (1 - \alpha)\alpha(\psi + \alpha) > 0$: insurance vs. demand-management

- $\mu = -\frac{\psi}{\alpha(\psi + \alpha)} < 0$: wealth effect

Response to NT productivity and endowment shocks



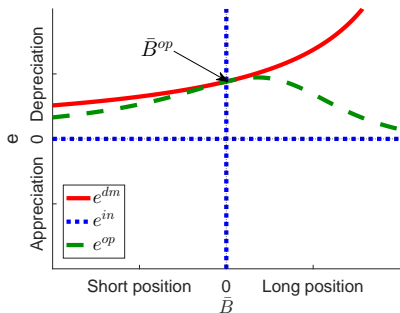
(a) Productivity shock



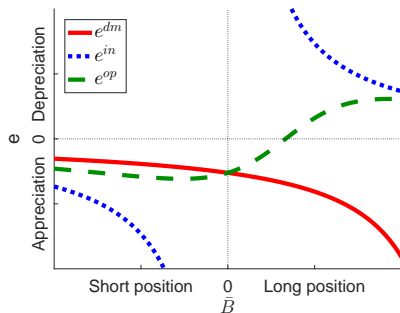
(b) Endowment shock

▶ portfolio

Response to NT productivity and endowment shocks



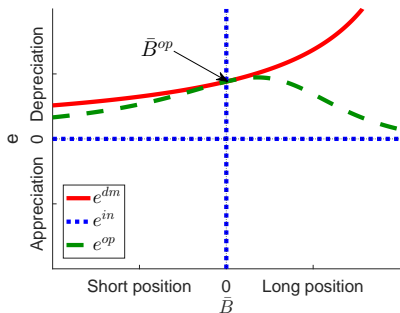
(c) Productivity shock



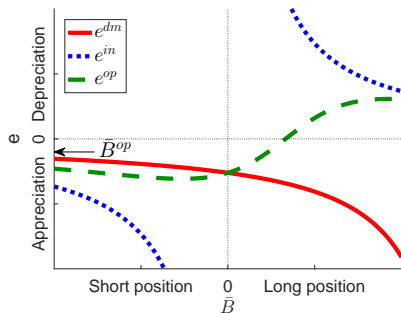
(d) Endowment shock

▶ portfolio

Response to NT productivity and endowment shocks



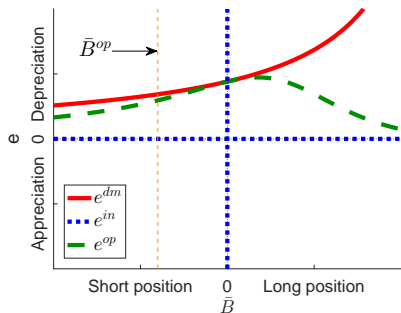
(e) Productivity shock



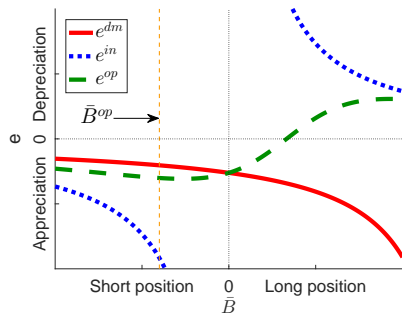
(f) Endowment shock

▶ portfolio

Response to NT productivity and endowment shocks



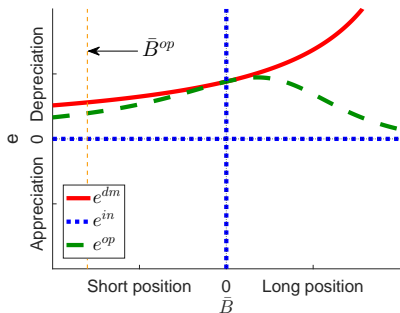
(g) Productivity shock



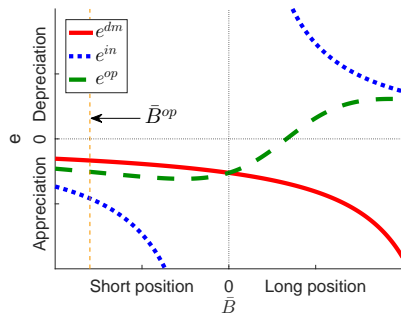
(h) Endowment shock

▶ portfolio

Response to NT productivity and endowment shocks



(i) Productivity shock



(j) Endowment shock

▶ portfolio

Optimal portfolio

Proposition: Optimal portfolio

If μ is not too large, positions become **larger** (in absolute value) when the insurance motive becomes more important ($\uparrow \sigma_T^2 / \sigma_{e^{dm}(0)}^2$ or $\downarrow \chi$)

- Shocks map differently to statistics $e_s^{dm}(0)$ and \mathcal{T}_s
 - High $|B| \Rightarrow$ costly to accomodate $e_s^{dm}(0)$
 - High $|B| \Rightarrow$ easy to create \mathcal{T}_s
- General asset structure: *sensitivity of portfolio to MP* (see paper)

Implications for exchange rate volatility

Proposition: Optimal exchange rate volatility

- 1 Suppose the portfolio decision is constrained (i.e. $|\bar{B}| = \bar{K}$). Then exchange rate volatility $\sigma_e^2 / \sigma_{e^{dm}(0)}^2$ **increases** with the importance of the insurance motive ($\uparrow \sigma_T^2 / \sigma_{e^{dm}(0)}^2$ or $\downarrow \chi$)
 - 2 Suppose $\mu \bar{B} \geq 0$ and the optimum \bar{B} is interior. Then, exchange rate volatility $\sigma_e^2 / \sigma_{e^{dm}(0)}^2$ **decreases** with the importance of the insurance motive. If $\mu \bar{B} < 0$, the result is ambiguous.
- General asset structure: *sensitivity of excess returns to MP* (see paper)

▶ example

Portfolio choices are approximately efficient

Proposition

Private portfolio decisions are efficient in the limit, i.e., $\tau_B = O(\epsilon^3)$

- No differential tax on home vs. foreign-currency bond
- **Key:** Economy would be **efficient** if markets were **complete**
- **Not key:** Simple asset structure; static model \rightarrow result much more general

Conclusion

- Framework to study joint optimal monetary policy and portfolio choice
 - Much more general than this particular setup!
 - *Caveat*: “Steady-state” portfolio tax important for tractability in general
- When market incompleteness is important...
 - ↑ sensitivity of external balance sheet to MP
 - Lowers cost of creating transfers ex post
 - Prevents accommodating demand to avoid undesirable transfers
- Market incompleteness **alone**: weak argument for portfolio taxes

Optimal monetary policy given \bar{B}

Proposition: Optimal exchange rate

The optimal exchange rate is given by

$$e_s^{op}(\bar{B}) = (1 - \omega(\bar{B}))e_s^{dm}(\bar{B}) + \omega(\bar{B})e_s^{in}(\bar{B}) + O(\epsilon^2)$$

where where e_s^{dm} and e_s^{in} are the **demand-management** and **insurance** targets,

$$e_s^{dm}(\bar{B}) = \frac{1}{1 + \mu\bar{B}} e_s^{dm}(0)$$

$$e_s^{in}(\bar{B}) = -\frac{1}{\bar{B}} \mathcal{T}_s$$

and ω is given by

$$\omega = \frac{\bar{B}^2}{\bar{B}^2 + \chi(1 + \mu\bar{B})^2}.$$

More in the paper...

- Dynamic model
 - Everything goes through analytically
 - New “cost-minimization problem”: Solve optimal way of creating excess-return at 0 (use savings taxes!)
- Calibration for Canada
 - Weight on insurance target: around 8% (sensitive to cost of inflation)
 - Welfare gains of completing markets (including an additional financial asset) significantly larger under optimal policy relative to inflation targeting

More in the paper I

- Solution under cooperation (when $m < \infty$)
 - Analytical: as-if m was twice as large ($\uparrow |B|$, $\downarrow \sigma_{rr}^2$) and no portfolio tax
 - Large quantitative gains due to small m
- General asset structures
 - Model with equity in non-tradable sector: χ increases with price flexibility
 - Any: Sufficient statistic of “exposure” to monetary policy in static model
 - No portfolio tax result ($m = \infty$) robust

More in the paper II

- Solution without time-varying capital controls
 - Results go through, but $\uparrow \chi$ (higher cost of providing insurance)
 - Quantitatively similar due to long bond duration
- Solution with no capital controls whatsoever
 - If $m < \infty$, need to solve additional degree of indeterminacy (Lagrange multiplier)

Money supply rule

- Modify utility to

$$\max_{\{C_{Ts}, C_{Ns}, M_s, B\}} \mathbb{E}\{u(C_{Ts}, C_{Ns}, L_s, s) + \nu L(M_s/E_s)\}$$

- Yields money demand,

$$L'(M_s/E_s) \propto u_T(s)$$

⇒ Invert this to obtain E_s as a function of M_s

⇒ Take $\nu \rightarrow 0$ so that it does not enter planning problem

▶ back

Optimization: Consumers

- Home consumer

$$u_N(s)/u_T(s) = P_{Ns}/E_s \quad (1)$$

$$-u_L(s)/u_T(s) = W_s/E_s \quad (2)$$

$$\mathbb{E}((1 + \tau_B)^{-1} R E_s^{-1} - 1) u_T(s) = 0 \quad (3)$$

$$(1 + \tau_B) B + B^* = T_0 \quad (4)$$

$$E_s C_{Ts} + P_{Ns} C_{Ns} = E_s Y_{Ts} + W_s L_s + \Pi_s \\ + RB + E_s B^* + T_s \quad \forall s \quad (5)$$

- Foreign consumer

$$\mathbb{E}(R E_s^{-1} - 1) u_T^*(s) = 0 \quad (6)$$

$$B^f + B^{*f} = 0 \quad (7)$$

$$E_s C_{Ts}^* = E_s Y_{Ts}^* + R B^f + E_s B^{*f} \quad (8)$$

Optimization: Firms and government

- Firms

$$P_{Ns} F_{Yl}(s) = P_s^l \quad (9)$$

$$P_s^l(i) = \frac{\eta}{\eta - 1} (1 + \tau^l) W_s \forall i \in (\phi, 1] \quad (10)$$

- Government

$$T_0 + B^g + B^{g*} = \tau_B B \quad (11)$$

$$T_s = \tau_L W_s L_s + R B^g + E_s B^{g*} \quad (12)$$

Market clearing

$$Y_{Ns} = F(s) \quad (13)$$

$$B + B^g + mB^f = 0 \quad (14)$$

$$B^* + B^{g*} + mB^{*f} = 0. \quad (15)$$

- Ricardian equivalence holds $\rightarrow B^g = B^{g*} = 0$ wlog

▶ back

Applying the method

Proposition: Equivalence to perturbation approach

Suppose u , u^* and F are locally analytic functions around the steady state. Then, maximizing

$$\mathbb{E}_0 V(s) = k_0 \mathbb{E}_0 \left[-\frac{1}{2} \underbrace{(\bar{B}e_s + \mathcal{T}_s)^2}_{\text{insurance}} - \frac{1}{2} \chi \underbrace{((1 + \bar{B}\mu)e_s - e_s^{dm}(0))^2}_{\text{demand-management}} \right] + t.i.p. + O(\epsilon^3)$$

with respect to $\{e_s\}$ and \bar{B} yields a linear approximation of a solution to the first-order conditions of problem \mathcal{P} around $(\bar{B}, \epsilon = 0)$ for $\{e_s\}$ and a bifurcation point of the system \bar{B} .

Approximating the solution

- $m = \infty$ to simplify
- FOC:

$$V_{1s} - \lambda_s = 0 \quad (16)$$

$$V_2 + BR\lambda_s + \varphi BRu^*(s) = 0 \quad (17)$$

$$B\mathbb{E}_0 E_s^{-1} \lambda_s + B\varphi \mathbb{E}_0 E_s^{-1} u^*(s) = 0 \quad (18)$$

$$Y_{Ts} + B(RE_s^{-1} - 1) - C_{Ts} = 0 \quad (19)$$

$$\mathbb{E}_0(RE_s^{-1} - 1)\lambda_s = 0 \quad (20)$$

$$\mathbb{E}_0(RE_s^{-1} - 1)u^*(s) = 0 \quad (21)$$

- Apply IFT around (B, ϵ) to (16) - (20)

$$\Rightarrow \{C_T(B, \epsilon), E_s^{-1}(B, \epsilon), R_s^{-1}(B, \epsilon), \lambda_s(B, \epsilon), \varphi(B, \epsilon)\}$$

Approximating the solution

- Let

$$H(B, \epsilon) \equiv \mathbb{E}_0(R(B, \epsilon)E_s^{-1}(B, \epsilon) - 1)(\lambda_s(B, \epsilon) - \varphi(B, \epsilon)u^*(B, \epsilon))$$

- Can show

$$\begin{aligned}\frac{\partial H}{\partial B} &= 0 \\ \frac{\partial^2 H}{\partial B \partial \epsilon} &= 0\end{aligned}$$

- Solve singularity

$$\hat{H}(\theta, \epsilon) = \begin{cases} \frac{H(\theta, \epsilon)}{\epsilon} & \text{if } \epsilon \neq 0 \\ \frac{\partial H}{\partial \epsilon} & \text{if } \epsilon = 0 \end{cases}$$

- $\frac{\partial \hat{H}}{\partial B} = 0$ when $\epsilon = 0$. Bifurcation point solves:

$$\frac{\partial \hat{H}}{\partial \epsilon} = 0$$

Approximating the solution

Theorem

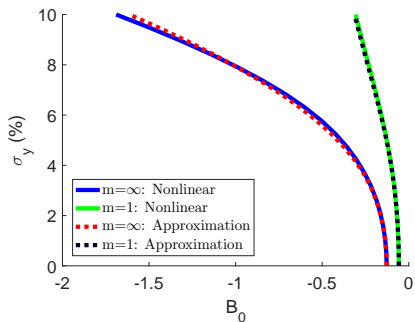
(Bifurcation Theorem). Suppose $H : \mathbb{R} \times \mathbb{R} \rightarrow \mathbb{R}$, H is analytic for (x, ϵ) in a neighborhood of $(x_0, 0)$, and $H(x, 0) = 0 \forall x \in \mathbb{R}$. Furthermore, suppose that

$$H_x(x_0, 0) = 0 = H_\epsilon(x_0, 0), H_{x\epsilon} \neq 0.$$

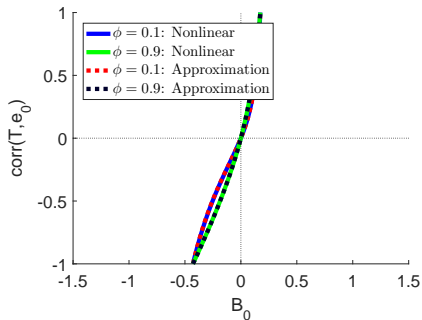
Then $(x_0, 0)$ is a bifurcation point and there is an open neighborhood \mathcal{N} of $(x_0, 0)$ and a function $h(\epsilon)$, $h(\epsilon) \neq 0$ for $\epsilon \neq 0$, such that h is analytic and $H(h(\epsilon), \epsilon) = 0$ for $(h(\epsilon), \epsilon) \in \mathcal{N}$.

▶ back

Example: portfolio



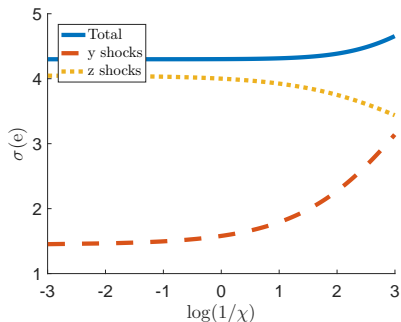
(k) Varying σ_y



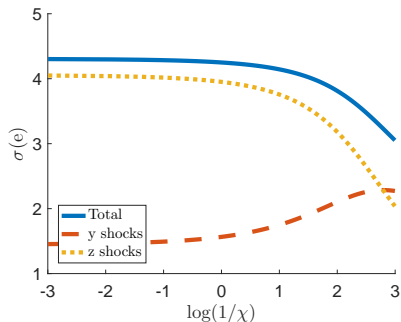
(l) Varying σ_{yz}

▶ back

Example: MP shifts the volatility



(m) Constrained B



(n) Unconstrained B

▶ back

Portfolio efficiency: Intuition

- FOC with respect to E yields, to first-order:

$$\hat{V}_E(s) = k_2 \hat{V}_{C_T} + O(\epsilon^2)$$

- *Intuition:* deviate from $\hat{V}_E = 0$ to provide insurance, i.e. to stabilize \hat{V}_{C_T}

- Portfolio optimality implies

$$\mathbb{E}e_s \hat{V}_{C_T} = O(\epsilon^3)$$

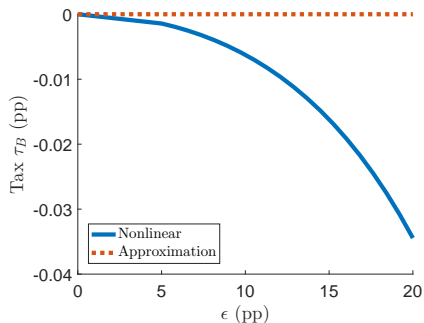
- Since AD is the only externality, we have

$$\hat{V}_{C_T} = \hat{U}_{C_T} + k_3 \hat{V}_E + O(\epsilon^2)$$

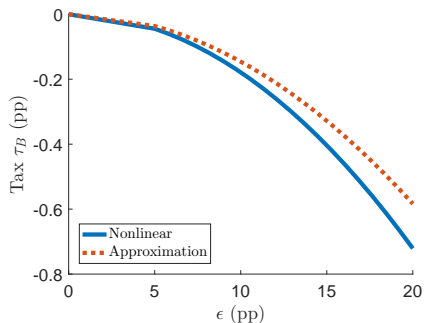
- Putting these together implies Home Euler holds to second-order.

▶ back

Example: taxes



(o) Full integration ($m = \infty$)



(p) Limited participation ($m = 1$)

▶ back

Dynamic model: Savings taxes

Proposition

1. If wages are rigid ($\phi = 1$), savings taxes decay at rate $1 - \delta$

$$\tau_{B^*t} = -\bar{K}_0(\delta)(\delta\mu - \bar{K}_1 k_{ex}^{-1} k_{ux})(1 - \delta)^t \{(1 + \mu\bar{B})rr_0 - rr_0^{dm}(0)\} \quad (22)$$

where $\bar{K}_0 > 0$, $\bar{K}_1 > 0$ are constants, k_{ux} captures the reaction of private marginal utility to the output gap ($k_{ux} > 0$ implies agents overvalue tradable goods in booms). When $\delta = 0$, $\bar{K}_0(\delta) = 0$.

2. If bonds are short ($\delta = 1$), then saving taxes from $t \geq 1$ are given by

$$\tau_{B^*t} = k_{ux} R_{\pi}^{t-1} \pi_1$$

where R_{π} is the optimal decay rate of inflation after $t = 1$. At $t = 0$,

$$\tau_{B^*0} = k_0 \mu \{(1 + \beta^{-1}(1 - \beta)k_{ec})rr_0 - rr_0^{dm}(0)\} + k_{ux} \Delta x_1$$

where $\bar{k} > 0$. If $k_{ex} > 0$, then $\Delta x_1 > 0$ and $\pi_1 > 0$.

▶ back

Quantitative analysis: calibration

Parameter	Description	Value	Parameter	Description	Value
A. Structural parameters					
β	Discount factor	0.99	ϕ_W	Probability of not adjusting prices	0.75
γ	Home risk aversion	2	η	Elasticity of substitution (varieties)	6
γ^*	Foreign risk aversion	2	δ	Bond depreciation	0.042
α	Tradable share	0.55	m	Measure of foreigners	0.18
ν^{-1}	Frisch elasticity	0.5	ϕ_π	Reaction to CPI inflation	1.5
ρ	Elasticity of substitution (T/NT)	0.74	ρ_i	Smoothing coefficient	0.84
B. Shocks					
σ_z	Productivity s.d.	0.47%	ρ_ψ	Liquidity service persistence	0.79
σ_{p^*}	Terms-of-trade s.d.	0.2%	$\text{corr}(\epsilon_t^z, \epsilon_t^{p^*})$	Correlation: z and p^*	0.26
σ_{r^*}	World interest-rate s.d.	0.23%	$\text{corr}(\epsilon_t^z, \epsilon_t^{r^*})$	Correlation: z and r^*	-0.13
σ_{y^*}	Foreigners' output s.d.	0.53%	$\text{corr}(\epsilon_t^z, \epsilon_t^{y^*})$	Correlation: z and y^*	0.41
σ_ψ	Liquidity service s.d.	0.92%	$\text{corr}(\epsilon_t^{p^*}, \epsilon_t^{r^*})$	Correlation: p^* and r^*	-0.51
ρ_z	Productivity persistence	0.81	$\text{corr}(\epsilon_t^{p^*}, \epsilon_t^{y^*})$	Correlation: p^* and y^*	0.36
ρ_{p^*}	Terms-of-trade persistence	0.74	$\text{corr}(\epsilon_t^{r^*}, \epsilon_t^{y^*})$	Correlation: r^* and y^*	-0.15
ρ_{r^*}	World interest-rate persistence	0.87	$\text{corr}(\epsilon_t^\psi, \epsilon_t^x)$	Correlation: ψ and others	0
ρ_{y^*}	World output persistence	0.88			

▶ back

Quantitative analysis: results

	Taylor rule	Demand Management	Optimal	Optimal: fixed B	Optimal: Cooperation
A. Domestic-currency bond positions and excess returns					
\bar{B}	-15.0%	-16.0%	-22.7%	-15.0%	-57.9%
ω			7.72%	3.57%	22.0%
$\sigma(rr):total$	6.12%	3.79%	3.72%	3.82%	3.42%
$\sigma(rr) : r^*$	2.76%	1.58%	1.99%	1.91%	2.25%
$\sigma(rr) : \psi$	5.72%	3.44%	3.14%	3.32%	2.57%
$\sigma(rr) : y^*$	0%	0%	0.35%	0.35%	0.69%
B. Policy instruments					
$\tau_B / risk p.$		-80.5%	-103%		0%
$\sigma(\tau^*)$		0%	0.03%	0.02%	0.06%
$\sigma(e) : total$	3.59%	1.48%	1.60%	1.58%	1.70%
$\sigma(e) : r^*$	1.86%	1.48%	1.60%	1.59%	1.64%
$\sigma(e) : \psi$	3.35%	0.06%	0.19%	0.11%	0.48%
$\sigma(e) : y^*$	0%	0%	0.15%	0.10%	0.29%
C. Welfare gains (% of first-best)					
Gains		11.9%	16.9%	15.0%	41.3%

▶ back

No Portfolio Tax: Intuition

- Two observations
 - ① No reason to tax under complete markets
 - ② Cost of creating an excess return on the portfolio is the same across states to first-order
- 1 + 2 imply

inefficient wedges (i.e., output gap) \propto social marginal utility

- Disagreement between private agent and planner depends on wedge,

$$U_{C_T}(s) + \bar{k} \times \text{wedge}(s) \approx V_{C_T}(s)$$

- Putting both together,

private marginal utility \propto social marginal utility