Risk Spillovers among Financial Institutions*

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This Version: July 4, 2008
-Preliminary and Incomplete-

Abstract

This paper uses quantile regressions to document risk spillovers, the increase in financial institutions’ Value-at-Risk (VaR) when other institutions are under distress. We also find that distress in hedge fund sector predicts a higher VaR for investment banks in the subsequent month. We identify six common factors that explain the risk spillovers across institutions. This set of risk factors also explains a large part of financial institutions’ average returns.

Keywords: Hedge Funds, Tail Risk, Asset Pricing, Systemic Risk, Value-at-Risk
JEL classification: G10, G12

*The authors would like to thank René Carmona, Xavier Gabaix, Beverly Hirtle, Jon Danielson, John Kambhu, Burton Malkiel, Maureen O’Hara, Matt Pritsker, José Scheinkman, Kevin Stiroh and seminar participants at Columbia University, Princeton University, Cornell University, Rutgers University, the Bank for International Settlement, Mannheim University, Hong Kong University of Science and Technology, University of Arizona, Arizona State University, University of North Carolina, Duke University, and the Federal Reserve Bank of New York for helpful comments. We are grateful for support from the Institute for Quantitative Investment Research Europe (INQUIRE award). Brunnermeier also acknowledges financial support from the Alfred P. Sloan Foundation.


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1 Introduction

Our financial architecture underwent a dramatic transformation in the last three decades. Financial innovation and securitization of assets from loan portfolios, mortgages, corporate debt, to credit card payables led to the modern “originate and distribute” banking system. Assets are repackaged and tranched to transfer risk from commercial banks’ balance sheets to numerous financial players across the globe. Hedge funds have become important financial intermediaries, the distinction between commercial and investment banks has become blurred, and a new level of interconnectedness and interdependence across financial institutions emerged. While more interconnected and less segmented markets make the financial system more resistant to small and medium sized shocks, it may be more prone to a systemic crisis as more financial institutions are hit when an extreme tail event occurs.

In the last three decades at least three big risk spillover events threatened the integrity of the financial system. The 1987 stock market crash undermined the funding liquidity of many market makers leading to a sharp stock price drop. The Federal Reserve Bank of New York persuaded commercial banks to extend additional lines of credit to broker-dealers to slow down the liquidity spiral: initial losses in some asset class lead to higher margins, rapid asset sales, and reduction in mark-to-market wealth, which in turn leads to additional losses and potential spillovers into other asset classes (Brunnermeier and Pedersen (2007)). The collapse of Long Term Capital Management (LTCM) in 1998 made clear that the failure of a hedge fund can threaten the stability of the financial system. Investment banks and particularly prime brokers, who have credit risk exposure to hedge funds, suffer potentially large losses if many hedge funds experience distress at the same time. Therefore from a financial stability point of view,
it is important to understand which hedge fund styles tend to simultaneously experience large losses and to what extent the banking sector is shielded from hedge fund distress. Arguably, the financial system had to withstand the biggest stress during the ongoing 2007-08 liquidity and credit crunch. The correction following an unsustainable run-up in house prices and exceptionally low credit spreads, led to significant losses to banks and especially to bank-owned hedge funds and off-balance sheet vehicles like SIVs, which financed their long-term assets and structured products with on the short-term money markets. Several money market spreads and volatility measures reached unprecedented levels. Almost all major commercial banks and investment banks announced large write-downs and were forced to raise new equity capital. The adverse events were also felt among hedge funds, especially among quant funds.¹

The purpose of this paper is to analyze the risk spillovers of tail events within a sector, e.g. across different hedge fund styles, and across sectors (commercial banking, investment banking and hedge funds). Methodologically, we use quantile regressions which naturally yield our measure of tail risk – Value-at-Risk (VaR) – without requiring distributional assumptions. We present four main results: (i) our new measure of spillover risk, CoVaR – defined as financial institutions’ VaR conditional on the fact that some other institution is in distress – is significantly higher than the (unconditional) VaR. Spillover risk is pronounced within the investment, commercial banking or hedge fund sector but also across sectors. (ii) our predictive CoVaR analysis documents (delayed) spill-over effects to the banking sector. More specifically, we find that low returns of hedge funds predict a higher Value-at-Risk for investment banks in the subsequent months. Furthermore, (iii) we identify six risk factors that largely explain the tail risk spillovers across financial institutions and hedge fund styles and argue that

¹For a more detailed summary of the events on the 2007-08 crisis see Brunnermeier (2008).
(iv) these risk factors also explain a large part of financial institutions’ average returns.

Our method of using quantile regressions to study risk spillovers should appeal to a broad group of market participants. For example, fund-of-fund managers can use daily data from their constituent hedge funds to estimate risk spillovers across different hedge funds and use quantile factor loadings to off-load spillover risk. Similarly, banks’ risk managers can use intraday desk level P&Ls to manage risk spillovers across trading desks. Regulatory supervisors can make use of daily P&L data from supervised institutions to monitor the potential for spillover risk across institutions.

Our paper can be linked to several strands of literatures. First, our paper contributes to the growing literature that sheds light on the link between hedge funds and the risk of a systemic crisis. Boyson, Stahel, and Stulz (2006) also document contagion across hedge fund styles using logit regressions on daily and monthly returns. However, they do not find evidence of contagion between hedge fund returns and equity, fixed income and foreign exchange returns. In contrast, we show that our pricing factors explain the increase in comovement among hedge fund styles in times of stress. Chan, Getmansky, Haas, and Lo (2006) document an increase in correlation across hedge funds, especially prior to the LTCM crisis and after 2003. Adrian (2007) points out that the increase in correlation since 2003 is due to a reduction in volatility – a phenomenon that occurred across many financial assets – rather than an increase in covariance. Second, our work relates to the large literature in international finance that focus on cross-country spillovers. For example, King and Wadhwani (1990) document an increase in correlation across stock markets during the 1987 crash, which in itself – as Forbes and Rigobon (2002) argue – is only evidence for interdependence but not contagion, since estimates of correlation tends to go up when volatility is high. Claessens and Forbes (2001) and the articles therein provide a nice overview. In contrast to these
papers our analysis focuses on volatility spillovers. The most common method to test for volatility spillover is to estimate GARCH processes, as e.g. in Hamao, Masulis, and Ng (1990) do for international stock market returns. While GARCH processes allow for time-variation in conditional volatility, they assume that extreme returns follow the same return distribution as the rest of returns. Hartman, Straetmans, and de Vries (2004) avoid this criticism by developing a contagion measure that focuses on extreme events. Building on extreme value theory they estimate the expected number of market crashes given that at least one market crashes. However, extreme value theory works only best for very low quantiles (see Danielsson and de Vries (2000)) and implicitly assumes an i.i.d. framework. This motivated Engle and Manganelli (2004) to develop CAViaR that – like our approach – makes use of quantile regressions as initially proposed by Koenker and Bassett (1978) and Bassett and Koenker (1978). While Engle and Manganelli’s CAViaR focus on the evolution of quantiles over time, we study risk spillover effects across financial institutions as measured by our CoVaR. Data limitations on monthly hedge fund returns do not allow us to study time-variation of the risk spillover effects, but we can study spillover effects over long time horizons for portfolios of commercial and investment banks. Most recently, Rossi and Harvey (2007) estimate time-varying quantiles and expectiles using a state space signal extraction algorithm.

Our finding that risk spillover effects in the tails can be off-loaded using “quantile regression factor loadings” squares well with Asness, Krail, and Liew (2001) and Agarwal and Naik (2004) findings that hedge funds load on various tail risks in order to boost their CAPM-α. Agarwal and Naik (2004) capture the tail exposure of equity hedge funds with non-linear market factors that take the shape of out-of-the-money put options. Patton (2007) develops several “neutrality tests” including a test for tail and VaR neutrality and finds that many so-called market neutral funds are in fact not
market neutral. Bali, Gokcan, and Liang (2007) and Liang and Park (2007) find that hedge funds that take on high left-tail risk outperform funds with less risk exposure. In addition, there is a large and growing number of papers that explain average returns of hedge funds using asset pricing factors (see e.g. Fung and Hsieh (2001, 2002, 2003), Hasanhodzic and Lo (2007)). Our approach is different in the sense that we study factors that explain the spillover risk across the tails of different hedge fund styles and financial institutions in general.

The remainder of paper is organized in four sections. In Section 2, we study the pairwise relationships between the returns to different hedge fund styles, and the relationships between hedge fund styles and other financial intermediaries. In Section 3, we estimate a risk factor model for the hedge fund returns. We document that six commonly traded risk factors that explain average returns well, and that also explain the increase of $CoVaR$ relative to unconditional VaR. We present robustness results in Section 4, and present conclusions in Section 5.

2 CoVaR

In this section, we first describe the data. We then introduce our risk spillover measure CoVaR and document that the Values-at-Risk of a commercial, investment bank or hedge fund is significantly higher when other financial institution are in distress. Subsequently, we outline the advantage of the quantile regression approach, namely that it captures heteroskedasticity. Finally, we introduce a predictive CoVaR which helps to forecast an increase in the Value-at-Risk one month in advance.
2.1 Financial Institution Return Data

We focus on three groups of financial institutions in this paper: commercial banks, investment banks and hedge funds. We use the equity returns of the five commercial banks with the largest size of total assets in recent years (Bank of America, Citibank, JPMorgan Chase, Wachovia, and Wells Fargo), as well as the equity returns of five large investment banks (Bear Stearns, Goldman Sachs, Lehman Brothers, Merrill Lynch, and Morgan Stanley). The equity return data is from CRSP. We start our sample of individual banks in April 1986, as only two of the five investment banks were public prior to that date.

In order to analyze a longer time series of banking data, we also use the banking and security broker dealer portfolios from the 49 industry portfolios by Kenneth French.\(^2\) These portfolios are constructed as value weighted averages from CRSP equity returns according to SIC codes, and are available since July 1926. Interestingly, the correlations between value weighted portfolios of the five commercial and five investment banks are, respectively, very highly correlated with the banking and security broker dealer industry factors (the correlation since April 1986 is over 90%).

In addition to commercial and investment banks, we also include hedge fund returns in our analysis. Hedge funds are private investment partnerships that are largely unregulated. Studying hedge funds is more challenging than the analysis of regulated financial institutions such as mutual funds, banks, or insurance companies, as only limited data on hedge funds is made available through regulatory filings. Consequently, most studies of hedge funds thus rely on self-reported return data.\(^3\) We follow this


\(^3\)A notable exception is a study by Brunnermeier and Nagel (2004) who use quarterly 13F filings to the SEC and show that hedge funds were riding the tech-bubble rather than acting as price-correcting force.
approach and use the hedge fund style indices by Credit Suisse/Tremont.

There are several papers that compare the self-reported returns of different vendors (see e.g. Agarwal and Naik (2005)), and some research compares the return characteristics of hedge fund indices with the returns of individual funds (Malkiel and Saha (2005)). The literature also investigates biases such as survivorship bias (Brown, Goetzmann, and Ibbotson (1999) and Liang (2000)), termination and self-selection bias (Ackermann, McEnally, and Ravenscraft (1999)), backfilling bias, and illiquidity bias (Asness, Krail, and Liew (2001) and Getmansky, Lo, and Makarov (2004)). We take from this literature that hedge fund return indices do not constitute ideal sources of data, but that their study is useful, and the best that is available. In addition, there is some evidence that the Credit Suisse/Tremont indices appear to be the least affected by various biases (Malkiel and Saha (2005)).

[Table 1]

Summary statistics for the value weighted portfolio of the five commercial banks and the five investment banks for April 1986 to March 2008 as well as for the ten hedge fund styles for January 1994 - May 2008 are given in Table 1 (Panel A). The summary statistics for the longer time series of the bank and security broker dealer industry portfolios since July 1926 to March 2008 are given Panel B. The hedge fund style indices have been extensively described in the literature (see Agarwal and Naik (2005) for a survey), and characterizations can also be found on the Credit Suisse/Tremont website (www.hedgeindex.com).

The Sharpe ratio of the hedge fund index (0.26 monthly) is nearly twice as high as the Sharpe ratio of either commercial or investment banks (both 0.15 monthly). The average CAPM $\alpha$'s of the two banking sectors and hedge funds are of comparable
magnitude (0.41, 0.43, and 0.38), but only the hedge fund \( \alpha \) is statistically significant. Over the longer period since 1926, commercial banks have a slightly smaller \( \alpha \) of 0.28 which is statistically significant, while security broker dealers have an \( \alpha \) close to zero over the longer period. Sharpe ratios are of comparable magnitude for the longer and shorter samples of Panels A and B.

Commercial and investment banks exhibit negatively skewed standardized returns, while the skewness of hedge funds is closer to 0. In the longer sample, the banking and trading portfolios exhibit positive skewness. All institutions exhibit excess kurtosis relative to a normal distribution.

### 2.2 Introducing CoVaR

We provide a short synopsis of quantile regressions in the context of linear factor models in the Appendix. Koenker (2005) provides a more detailed overview of many econometric issues. In this section, we use quantile regressions to analyze risk spillovers. Consider the prediction of quantile regression of style \( i \) on index return \( j \):

\[
\hat{R}_q^i = \hat{\alpha}_q^{ij} + \hat{\beta}_q^{ij} R_j^j
\]

where \( \hat{R}_q^i \) denotes the predicted value of excess return \( i \) for quantile \( q \) and \( R_j^j \) denotes the excess return of institution or portfolio \( j \) (a commercial bank, investment bank, or a hedge fund style index). Note that a median regression is the special case of a quantile regression where \( q = 50\% \). From the definition of Value-at-risk, it follows directly that:

\[
\text{VaR}_q^i | R_j^j = \hat{R}_q^i
\]
Note that the usual definition of VaR is the negative of our definition. Thus the predicted value from the quantile regression of returns of style $i$ on index $j$ gives the Value-at-Risk conditional on $R^j_i$. In principle, this regression could be extended to allow for nonlinearities by introducing higher order dependence of returns to style $i$ as a function of returns to index $j$.

**Definition 1** We denote the CoVaR$^{ij}$, the VaR of style $i$ conditional on the (unconditional) VaR of style $j$ by:

$$\text{CoVaR}_{ij}^q := \text{VaR}_i^q | \text{VaR}_j^q = \hat{\alpha}_{ij}^q + \hat{\beta}_{ij}^q \text{VaR}_j^q. \quad (3)$$

Thus CoVaR$^{ij}_q$ gives the VaR$_q$ of strategy $i$ conditional on the unconditional VaR$_q$ of strategy/index $j$.

We sometimes say that CoVaR$^{ij}$ is the VaR of style $i$ conditional on index $j$ being in distress. Our definition of CoVaR is a measure of comovement that reflects risk spillovers. It differs from the often used conditional VaR (CVaR), mean excess loss, expected/mean shortfall, or tail VaR, which are all defined for a single strategy as $E[R^i | R^i \leq \text{VaR}_i]$.

Rather than reporting the CoVaRs directly we report the relative to increase relative to the unconditional VaRs

$$100 \cdot \frac{\text{CoVaR}^{ij} - \text{VaR}^i}{\text{VaR}^i}.$$

---

4While quantile regressions are regularly used in many applied fields of economics, their applications to financial economics are limited. Notable exceptions are econometric papers like Bassett and Chen (2001), Chernozhukov and Umantsev (2001), and Engle and Manganelli (2004) as well as the working papers by Barnes and Hughes (2002) and Ma and Pohlman (2005). This is surprising to us, since the quantile of the return directly provides an estimate of the (negative of) Value-at-Risk, a widely used risk-measure.
This has the advantage that it normalizes data across strategies with different unconditional VaRs.

For our baseline results, we report the value weighted average the CoVaR for the institutions within one group $i$ (for example investment banks), conditional on the VaR of the overall index of other institutions $j$ (or conditional on the own group $i$). For example, after quantile regressing each of five investments banks on the hedge fund index we obtain five CoVaR measures. We value-weight the five CoVaRs and report the weighted average.

Table 2 reports in the first column the unconditional VaRs which corresponds to the 5th percentile of the return distribution. Panel A gives the VaRs and CoVaRs for individual institutions, Panel B for the portfolios since 1926. In Panel A, the average unconditional 5%-VaR is $-12.23\%$ for commercial banks (since 1986), $-13.69\%$ for investment banks (since 1986), and $-2.40\%$ for the ten hedge fund styles (since 1994). The unconditional VaR in the longer data set is $-10.13\%$ for the commercial banks, and $-11.83\%$ for the security broker dealers.

[Table 2]

Columns 2-4 of Table 2 give the CoVaRs, and columns 5-8 the t-statistic. Consider column (2)/row (2) of Table 2. This gives the CoVaR of investment banks conditional on commercial bank distress. We run a 5% quantile regression of each investment bank on the value weighted commercial bank index and compute the conditional VaR of the investment banks conditional on commercial banks being at the worst 5%. We then compute the percent increase of this conditional VaR for each of the investment banks relative to the unconditional VaR, take the value weighted average across investment banks, and report it in the Table. The 45% CoVaR-increase of investment banks
conditional on commercial banks means that the investment bank $CoVaR$ is $(1 + 45\%) \cdot (-13.69\%) = -19.86\%$. In column (2)/row (3) we report the average percentage $CoVaR$ increase of individual investment banks relative to the investment bank index (where the average is again value weighted). The percentage $CoVaR$-increase of 24\% indicates that individual investment bank $VaR$s increase on average from $-13.69\%$ to $(1 + 24\%) \cdot (-13.69\%) = -16.99\%$.

We find that investment bank tail risk significantly increases conditional on distress of other investment banks, conditional on distress of commercial banks, and conditional on hedge fund distress. Commercial bank $VaR$s significantly increase after conditioning on investment bank distress, but not after conditioning on hedge fund distress. Distress of the hedge fund universe increases the tail risk of the individual hedge fund strategies, but investment and commercial bank distress does not lead to an increased hedge fund $VaR$.

In Panel B of Table 2 we report the $CoVaR$ of commercial banks conditional on security broker dealer distress (column (3)/row (4)), and vice versa (column (2)/row (5)) for the longer time period 1926 – 2008. As in the shorter sample of Panel A, we find significant $CoVaR$ increases of similar orders of magnitude.

Note that the $CoVaR$ matrix unlike a correlation coefficient matrix is not symmetric. This makes sense that distress of one sector might cause distress in another sector but not vice versa.

### 2.3 Reasons for $CoVaR$ Increase

The Value-at-Risk after conditioning on an adverse event for the index changes for at least three reasons. If the returns of a particular hedge fund strategy, investment/commercial bank is positively correlated with the index, the conditional mean
return is naturally lower than the unconditional one. This leads to a higher \textit{CoVaR}. Conditioning in general also lowers uncertainty since conditional variance is typically lower the variance of an unconditional return. This should lower the \textit{CoVaR}. However, with heteroskedasticity, it can be the case that for low index returns, the return distribution of a particular hedge fund style or investment/commercial bank is more volatile. This leads to a higher \textit{CoVaR}. Our quantile regression approach picks up the heteroskedasticity aspect (see Appendix), while a simple OLS approach under the homoskedasticity assumption does not. To see whether our \textit{CoVaR} results are purely driven by the mean-effect, we also calculate the \textit{CoVaR} that would arise if we assume that returns are normally distribution with homoskedasticity. More specifically we compute the OLS-\textit{CoVaR} using the sensitivity from an OLS regression, assume that shocks have a normal distribution, and condition on the fifth percentile of the right hand side portfolio. In Table 3, we report the percent increase of the \textit{CoVaR} estimated from the quantile regression (as in Table 2) minus the percentage \textit{CoVaR} increase estimated from an OLS regression.

\begin{table}[h]
\centering
\begin{tabular}{|c|c|}
\hline
\textbf{Institution} & \textbf{Percent Increase} \\
\hline
Investment Banks & 1.23 \% \\
Commercial Banks & 2.34 \% \\
Hedge Funds & 3.45 \% \\
\hline
\end{tabular}
\caption{Percent Increase of \textit{CoVaR} Estimated from Quantile Regression Minus OLS-\textit{CoVaR} Increase}
\end{table}

We can see from Table 3 that the quantile regression based estimates of the \textit{CoVaR} are generally higher than the OLS-\textit{CoVaR}, indicating that the quantile regression captures the increased heteroskedasticity of returns in the left tail. Column (2) indicates that the quantile \textit{CoVaR} is significantly higher than the OLS-\textit{CoVaR} for investment banks, conditional on any of the other institutions being in distress. For commercial banks and hedge funds, only distress within their own industry is associated with higher quantile \textit{CoVaRs} relative to the OLS-\textit{CoVaRs}. Our interpretation of these findings is that the \textit{CoVaR} is a better method to estimate conditional tail risk, as it takes
time variation of conditional heteroskedasticity into account. An alternative test for heteroskedasticity that follows steps outlined in the appendix would lead to a similar conclusion.

2.4 Predictive CoVaRs

So far we focused on contemporaneous relationship between returns. Next, we incorporate quantile regressions into a Granger causality test to determine whether certain index returns predict distress in other financial intermediaries (in the sense of an increased Value-at-Risk), and vice versa. More specifically, we run two quantile regressions:

\[
R^i_t = \alpha^{ij}_q + \gamma_q R^i_{t-1} + u^i_t
\]

\[
R^i_t = \alpha^{ij}_q + \beta^{ij}_q R^j_{t-1} + \gamma_q R^i_{t-1} + u^{ij}_{it}
\]

We first compute the \(VaR^i\) from equation (4) conditional on \(R^i_{t-1}\) being at the unconditional \(VaR\) of \(i\). This is the \(VaR\) conditional on an institution/index having experienced a bad shock in the previous month. We then compute the “predictive 5%-CoVaR” as percent increase over the latter \(VaR\), conditional on institution/index \(j\) having also experienced a tail event in the previous month. We report the results in Table 4.

[Table 4]

Our findings, presented in Table 4, show that hedge fund distress predicts a statistically significantly higher Value-at-Risk in the investment banking sector. The converse and a link to the commercial banking sector is not statistically significant, which is most likely due the fact that at the beginning of our data sample 1994, the interdependence between hedge funds and commercial banks was weaker than it is today. As
commercial banks are entering more and more into the investment banking business (whose trading resembles to a large extent that of hedge funds), we would expect that the predictable risk spillovers from hedge funds to investment banks that we document might also show up for commercial banks.

By comparing column (1) of Tables 2 and 4 we can see that distress within institutional classes do predict higher tail risk within that class in the following month. For example, the predictive VaR for investment banks is $-15.09\%$ (Table 4, column 1, row 2), compared to an unconditional VaR of $-13.69\%$ (Table 4, column 1, row 2), representing an $15.09/13.60 - 1 = 11\%$ increase.

3 Tail Spillover Risk Factors

Having established that Value-at-Risk of institution $i$ increases when the index return $j$ is in distress, in this section we identify factors that explain this risk spillover effects. We argue that a factor structure explains this risk spillover, if the $CoVaR$ after off-loading the risk associated with these factors roughly coincides with the unconditional off-loaded $VaR$. That is, if the risk spillover for residuals of the quantile regression is much lower compared to the dependence of the raw returns. We first introduce our six factors, before creating offloaded returns.

3.1 Description and Data

We select six factors that capture the increase in comovement across hedge fund styles’ VaRs. All of them have solid theoretical foundations, capturing certain aspects of risks and hence, are not simply due to data mining. They are also liquid and easily tradable. We restrict ourselves to a small set of seven risk factors to avoid overfitting the data.
All data are monthly from 04:1986 to 05:2008. Our factors are:

(i) CRSP market return in excess to the 3-month bill rate reflecting the equity market risk. The Center for Research in Security Prices (CRSP) market index is a broad benchmark reflecting the value weighted of all publicly traded securities;

(ii) VIX straddle excess return to capture the implied future volatility in the stock market. This implied volatility index is available on Chicago Board Options Exchange’s website. To get a tradable excess return series we calculate the straddle return of a hypothetical at-the-money straddle position that is based on the VIX implied volatility and substract the 3-month bill rate.

(iii) the variance swap return to capture the associated risk premium for risky shifts in volatility. The variance swap contract pays off the difference between the realized variance over the coming months and its delivery price at the beginning of the month. Since the delivery price is not commonly observable over our whole sample period, we use – as is common practice – the VIX squared normalized to 21 trading days, i.e. \((VIX^*21/360)^2\). The realization of the index variance is computed from daily S&P 500 index data for each month. Note also since the initial price of the swap contract is zero, returns are automatically excess returns.

(iv) a short term “liquidity spread”, defined as the difference between the 3-month repo rate and the 3-month bill rate measures the short-term counterparty liquidity risk. We use the 3-month general collateral repo rate that is available on Bloomberg, and obtain the 3-month Treasury rate from the Federal Reserve Bank of New York.

In addition we consider the following two fixed-income factors that are known to be indicators in forecasting the business cycle and also predict excess stock returns (Estrella and Hardouvelis (1991), Campbell (1987), and Fama and French (1989)).

(v) the return to the slope of the yield curve, measured by the yield-spread between
the 10-year Treasury rate and the 3-months bill rate.

(vi) the return to the credit spread between BAA rated bonds and the Treasury rate (with same maturity of 10 years).

The last two factors are from the Federal Reserve Board’s H.15 release. Table 5 gives the summary statistics for the risk factors.

[Table 5]

The literature has studied related factors. Boyson, Stahel, and Stulz (2006) use the S&P500, Russell 3000, change in VIX, FRB dollar index, Lehman US bond index and the 3-Month Bill return as factors, but — unlike our study — they do not find a link between these factors and contagion. Agarwal and Naik (2004) also focus on tail risk. In addition to out of the money put and call market factors they use the Russell 3000, MSCI excluding US (bonds), MSCI emerging markets, HML, SMB, MOM, Salomon Government and corporate bonds, Salomon world government bonds, Lehman high yield, Federal Reserve trade weighted dollar index, GS commodity index and change in default spread. Factors used in Fung and Hsieh (1997, 2001, 2002, 2003) differ depending on the hedge fund style they analyze. An innovative feature of their factor structure is to incorporate lookback options factors that are intended to capture momentum effects. We opted not to include this factor since restricted ourselves only to highly liquid factors. Fung, Hsieh, Naik, and Ramadorai (2008) try to understand performance of fund of fund managers. They employ the S&P 500 index as factor; a small minus big factor; the excess returns on portfolios of lookback straddle options on currencies, commodities and bonds; the yield spread – our factor (v) – and the credit spread – our factor (vi). Finally, Chan, Getmansky, Haas, and Lo (2006) use the S&P 500 total return, bank equity return index, the first difference in the 6-months LIBOR,
the return on the U.S. Dollar spot rate, the return to a gold spot price index, the Dow Jones / Lehman Brothers bond index, Dow-Jones large cap - small cap index, Dow Jones value minus growth index, the KDP high yield minus U.S. 1-year Treasury yield, the 10-year Swap / 6-month Libor spread, and the change in CBOE's VIX implied volatility index. Bondarenko (2004) introduced the Variance swap contract as a new factor.

3.2 Off-loaded Returns

After having specified our factors, we study next how offloading the tail risk that is associated with the six risk factors affects risk spillovers as measured by the $CoVaRs$. We construct “5%-quantile offloaded returns” in the following way. We 5%-quantile-regress the excess return of each bank or hedge fund style on the risk factors, and call the constant plus the residual of that regression the offloaded return. This residual is a return as all of the factors are excess returns, i.e. zero investment portfolios, and the regression slopes can be interpreted as portfolio weights of a tail risk offloading strategy and $VaR$ of the offloaded returns stays constant as one varies the factors.

Table 6 gives the summary statistics for the offloaded returns of different institutions and styles. Unfortunately, we cannot offload over the longer time period since 1926 as the volatility risk factors and the repo spread are not available for a longer history.

[Table 6]

The following differences between Tables 1 and 6 stand out: First, offloading the risk associated with our factors markedly reduces average returns and Sharpe ratios for commercial banks and hedge funds. The CAPM-α of hedge funds drops notably after offloading the risk associated with our factors. The average CAPM for hedge funds
declines from a statistically significant .38% to -.15%. The kernel densities of Figure 1 reveal that offloading reduces the fat left tail, but does not affect the right tail much. Figure 1 also shows that the average of the return distribution is shifted to the left, indicating that there is a tail risk-average return tradeoff: institutions can reduce tail risk, but have to give up average return.

[Figure 1]

3.3 CoVaRs of Off-loaded Returns

The percentage increase in CoVaR over the unconditional VaR for offloaded returns is given in Table 6. We can see that tail risk offloading eliminates the risk spillovers to investment banks (from both commercial banks and hedge funds) that is documented in Table 2. For total returns we find that the CoVaR increase of investment banks is 45% and 61% conditional on commercial bank and hedge fund distress, respectively. For offloaded returns, we do not find such a risk spillover to investment banks (Table 7). We also find that tail risk offloading with the systematic risk factors eliminates the risk spillover from investment banks to commercial banks.

[Table 7]

Among hedge fund styles, tail risk offloading also makes risk spillovers among hedge fund styles statistically insignificant. For excess returns, Table 2 shows an average CoVaR percent increase of 48% which is statistically significant with a t-statistic of 2.84. After tail risk offloading, the risk spillovers among styles decline to an insignificant 10%.

Tail risk offloading reduces the risk spillovers among commercial and investment banks, but does not eliminate them. In particular, by again comparing Tables 2 and 7s,
we can see that risk spillovers are reduced from 43% to 30% for commercial banks and from 24% to 14% for investment banks. However, these spillovers are still statistically significant. We are thus missing a risk factor that allows the offloading of banking risk. We tried a number of commonly used additional risk factors (such as Fama-French, momentum, and reversal factors, other credit and liquidity spreads, foreign exchange returns, and additional option factors but have not been able to identify factors that can be useful in offloading the risk spillovers among banks).

We report the quantile CoVaRs relative to the OLS-CoVaRs in Table 8 and find that the quantile based measure of spillover risk is generally lower for the offloaded returns. This is the opposite of the result that we presented in Table 3. We find this result as offloading is asymmetric, and primarily reduces the left tail. The OLS based spillover measure overestimates the left tail, as it does not take into account that offloaded returns are more positively skewed.

[Table 8]

### 3.4 Incentives to Load on Tail Risk

Section 2 documents tail risk spillovers among financial institutions during times of distress. Section 3 identifies tradable factors that explain a large part of these risk spillovers. Do financial institutions have incentive to offload their tail risk, thus reducing the potential for spillover?

Hedge fund managers, investors, banks, or fund of fund managers can offload some of their tail risk with tradable risk factors without incurring large trading costs since our factors tradable and highly liquid. Furthermore, our offloading strategy is $\alpha$-neutral. However, comparing Tables 1 and 6 shows that offloading markedly reduces
the average monthly return for some institutions, particularly hedge funds. Stated differently, trading out of tail risk, and consequently out of spillover risk is costly in terms of expected returns. There appears to be a risk-return trade-off between returns and conditional Value-at-Risk in hedge fund returns.

4 Robustness

4.1 Alternative measures of risk spillovers

The comparison of $q$-sensitivities (quantile regression coefficients) across different quantiles $q$ can be interpreted as a comparison of dependence across states of the world. In Figure 2, we plot the average sensitivities among hedge fund styles for all quantiles between 5% and 95% for total returns, OLS offloaded returns, and 5% offloaded returns. The OLS offloaded returns are constructed as the OLS alpha plus the residual relative to the six risk factors. The plot shows that the sensitivities across quantiles is relatively flat for the 5%-offloaded returns. In contrast, average sensitivities are sharply decreasing along the quantiles for the total returns, and are also decreasing for the OLS offloaded returns.

[Figure 2]

Instead of looking at sensitivities across states of the world, we can also investigate the evolution of dependence over time. To do so, we estimate a multivariate BEKK-ARCH(12) model, and extract the evolution of covariances across hedge fund strategies over time. We plot the average of the covariances across the ten strategies in Figure 3.

[Figure 3]
The covariances for the 5%-offloaded returns are clearly less volatile than for the total returns. In particular, estimated average covariances spiked during the LTCM crisis in the third quarter of 1998, and in January 2000. In contrast, the average covariances of 5%-offloaded returns increased much less during those volatile times.

4.2 Alternative risk measures

Our main results were derived for 5%-VaRs and 5%-CoVaRs. We chose the 5-th percentile for data reasons: for hedge funds, only data since 1994 is available. However, for commercial and investment banks, we can analyze spillover risk since 1926, so that we can estimate VaRs and CoVaRs for lower percentiles. In Table 9, we re-estimate Panel B of Table 2 for 1%-VaRs and 1%-CoVaRs. We find significant risk spillovers between commercial banks and security broker dealers for the first percentile. The CoVaR percent increase is smaller in magnitude for the first compared to the fifth percentile. However, it is highly significant for the spillover from commercial to investment banks, and significant at the 7% for the reverse (with a t-stat of 1.89).

[Table 9]

Value-at-Risk – our main measure of tail risk – is only one possible characterization of tail risk. Many alternative measures have been proposed. A particularly appealing measure of tail risk that has been proposed in the literature Artzner, Delbaen, Eber, and Heath (1999) is expected shortfall. It is defined as the average loss below the VaR. As robustness check, we calculate an expected shortfall spillover measure as the average CoVaR for 1%, 2%, 3%, 4%, and 5%. Panel B in Table 9 shows that we also find significant risk spillovers using the expected shortfall measure.
5 Conclusion

During financial crisis or periods of financial intermediary distress, tail events tend to spill over across financial institutions. Such risk spillovers are important to understand for portfolio managers, risk managers, and supervisors the supervisors of financial institutions. The ability to monitor and potentially hedge risk spillovers can help to optimize portfolio performance, to set risk limits and margins, and to adequately regulate institutions.

We find statistically and economically significant risk spillovers across institutions. We document that the spillover risk across institutions and across hedge fund styles can be hedged by offloading tail risk via tradable risk factors. However, the offloading comes at the cost of lower average returns for some financial institutions, particularly for hedge funds.
A Appendix

This appendix is a short introduction to quantile regressions in the context of a linear factor model. Suppose that excess returns $R_t$ have the following (linear) factor structure:

$$R_t = \gamma_0 + X_t \gamma_1 + (\gamma_2 + X_t \gamma_3) \varepsilon_t$$

(6)

where $X_t$ is a vector of risk factors. Factors are assumed to be excess returns. The error term $\varepsilon_t$ is assumed to be i.i.d. with zero mean and unit variance and is independent of $X_t$ so that $E[\varepsilon_t | X_t] = 0$. Our returns are generated by a process of the “location-scale” family, so that both the conditional expected return $E[R_t | X_t] = \gamma_0 + X_t \gamma_1$ and the conditional volatility $Vol_{t-1} [R_t | X_t] = (\gamma_2 + X_t \gamma_3)$ depend on a set of factors. The coefficients $\gamma_0$ and $\gamma_1$ can be estimated consistently via OLS:

$$\hat{\gamma}_0 = \alpha_{OLS}$$

(7)

$$\hat{\gamma}_1 = \beta_{OLS}$$

(8)

We denote the cumulative distribution function (cdf) of $\varepsilon$ by $F_\varepsilon(\varepsilon)$, and the inverse cdf by $F_{\varepsilon}^{-1}(q)$ for percentile $q$. It follows immediately that the inverse cdf of $R_t$ is:

$$F_{R_t}^{-1} (q|X_t) = \gamma_0 + X_t \gamma_1 + (\gamma_2 + X_t \gamma_3) F_{\varepsilon}^{-1} (q)$$

(9)

$$= \alpha(q) + X_t \beta(q)$$

$^5$The volatility coefficients $\gamma_2$ and $\gamma_3$ can be estimated using a stochastic volatility or GARCH model if distributional assumptions about $\varepsilon$ are made, or via GMM. Below, we will describe how to estimate $\gamma_2$ and $\gamma_3$ using quantile regressions, which do not rely on a specific distribution function of $\varepsilon$. 

24
where

\[ \alpha(q) = \gamma_0 + \gamma_2 F_\varepsilon^{-1}(q) \]  
\[ \beta(q) = \gamma_1 + \gamma_3 F_\varepsilon^{-1}(q) \]

with quantiles \( q \in (0, 1) \). We also call \( F_{R_t}^{-1}(q|X_t) \) the conditional quantile function and denote it by \( Q_{R_t}(q|X_t) \). From the definition of VaR:

\[
VaR_{q|X_t} = \inf_{VaR_q} \{ \Pr(R_t \leq VaR_{q|X_t}) \geq q \}
\]

(12)

follows directly that

\[
VaR_{q|X_t} = Q_{R_t}(q|X_t)
\]

(13)

the \( q \)-VaR in returns conditional on \( X_t \) coincides with conditional quantile function \( Q_{R_t}(q|X_t) \). Typically, we are interested in values of \( q \) close to 0, or particularly \( q = 1\% \).

Note that by multiplying the (absolute value of the) VaR in return space the by hedge fund capitalization gives the VaR in terms of dollars.

We can estimate the quantile function via quantile regressions:

\[
[\alpha_q, \beta_q] = \arg \min_{\alpha_q, \beta_q} \sum_t \theta_q(R_t - \alpha_q - X_t \beta_q) \text{ with } \theta_q(u) = (q - I_{u \leq 0}) u
\]

(14)

References


Figure 1: Kernel Densities of Total and 5%-Offloaded Returns

Commercial Banks

Investment Banks

CS/Tremont Hedge Fund Index
Figure 2: Average q-Sensitivities by Quantiles

- Average Sensitivities of Total Returns
- Average Sensitivities of OLS Offloaded Returns
- Average Sensitivities of 5% Offloaded Returns
Figure 3: Average GARCH Covariances over Time

- Total Returns
- 5% Offloaded Returns
Table 1: Summary Statistics of Monthly Excess Returns

Panel A reports summary statistics for five commercial banks (Bank of America, Citibank, J. P. Morgan Chase, Wachovia, and Wells Fargo), five investment banks (Bear Stearns, Goldman Sachs, Lehman Brothers, Merrill Lynch, and Morgan Stanley), and the ten hedge fund style indices from Credit Suisse / Tremont. Panel B reports summary statistics for the commercial bank portfolio and the security broker dealer portfolio of Ken French's 49 industry portfolios. The return data for commercial and investment banks / security broker dealers are from CRSP. All returns are monthly, in excess of the three month Treasury bill rate. The Sharpe ratio is the ratio of mean excess returns to the standard deviation of excess returns. The skewness (skew), kurtosis (kurt), and first and fifth percentiles (1% and 5%).

<table>
<thead>
<tr>
<th>Panel A: Institutions</th>
<th>Data range</th>
<th>Obs</th>
<th>Sharpe</th>
<th>Mean</th>
<th>Std Dev</th>
<th>CAPM α</th>
<th>Skew</th>
<th>Kurt</th>
<th>1%</th>
<th>5%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Five Large Commercial Banks</td>
<td>04/1986-03/2008</td>
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<td>0.15</td>
<td>1.04</td>
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<td>0.41</td>
<td>-0.36</td>
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<td>-22.43</td>
<td>-9.87</td>
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<td>Five Investment Banks</td>
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<td>-0.14</td>
<td>4.80</td>
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<td>-12.33</td>
</tr>
<tr>
<td>Ten CSFB/Tremont Hedge Fund Styles</td>
<td>01/1994-05/2008</td>
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<td>0.55</td>
<td>2.14</td>
<td>0.38</td>
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<td>-5.12</td>
<td>-2.61</td>
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<table>
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<th>Panel B: Portfolios</th>
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<th>Mean</th>
<th>Std Dev</th>
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<th>Skew</th>
<th>Kurt</th>
<th>Min</th>
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<td>0.24</td>
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<td>0.11</td>
<td>0.84</td>
<td>7.82</td>
<td>0.02</td>
<td>0.57</td>
<td>12.58</td>
<td>-21.67</td>
<td>-11.34</td>
</tr>
</tbody>
</table>
Table 2: 5%-CoVaRs

This table reports the percentage increase of the five percent Value-at-Risk for the returns of the left column conditional on the fifth percentile of the returns of the top row, relative to the unconditional 5% Value-at-Risk (reported in the first column). The t-stats test the null hypothesis that the percentage CoVaRs increase relative to the unconditional VaRs are zero. Standard errors are generated via bootstrap with 200 draws.

| Panel A: Institutions |  \(5\%-\text{VaR}\) |  \(5\%-\text{CoVaR} / 5\%-\text{VaR}\) | \(\text{percent increase}\) |  |  |  |  |  |
|-----------------------|-------------------|-------------------------------|-----------------|---|---|---|---|
|                       | CB | IB | HF | CB | IB | HF | t-stats | CB | IB | HF |
| (1) Commercial Banks (CB) | -12.23 | 43 | 29 | 18 |  |  |  | -12.85 | 5.01 | 3.73 | 0.94 |
| (2) Investment Banks (IB) | -13.69 | 45 | 24 | 61 |  |  |  | -7.86 | 5.03 | 3.14 | 4.13 |
| (3) CSFB/Tremont Hedge Fund Styles (HF) | -2.40 | 27 | 23 | 48 |  |  |  | -9.24 | 1.40 | 1.13 | 2.84 |

| Panel B: Portfolios 1926-2008 |  \(5\%-\text{VaR}\) |  \(5\%-\text{CoVaR} / 5\%-\text{VaR}\) | \(\text{percent increase}\) |  |  |  |  |  |
|-----------------------------|-------------------|-------------------------------|-----------------|---|---|---|---|
|                             | CB | IB | HF | CB | IB | HF | t-stats | CB | IB | HF |
| (4) Commercial Bank Portfolio (CB) | -10.13 | . | 43 | . |  |  |  | -17.84 | . | 6.15 | . |
| (5) Security Broker Dealer Portfolio (IB) | -11.83 | 37 | . | . |  |  |  | -17.37 | 5.06 | . | . |
### Table 3: 5%-CoVaRs versus OLS-CoVaRs

This table reports the percentage increase of the 5%-quantile CoVaR relative to the 5%-OLS CoVaR. The t-statistic tests the null hypothesis that the percent increase of quantile CoVaRs relative OLS CoVaRs is zero. Standard errors are generated via bootstrap with 200 draws.

<table>
<thead>
<tr>
<th>Panel A: Institutions</th>
<th>5%-CoVaR / OLS-CoVaR</th>
<th>t-stats</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>percent increase</td>
<td></td>
</tr>
<tr>
<td>CB</td>
<td>IB</td>
<td>HF</td>
</tr>
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<td>Commercial Banks (CB)</td>
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</tr>
<tr>
<td>Investment Banks (IB)</td>
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<td>12</td>
</tr>
<tr>
<td>CSFB/Tremont Hedge Fund Styles (HF)</td>
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<td>17</td>
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<table>
<thead>
<tr>
<th>Panel B: Portfolios 1926-2008</th>
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<th>t-stats</th>
</tr>
</thead>
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<tr>
<td></td>
<td>percent increase</td>
<td></td>
</tr>
<tr>
<td>CB</td>
<td>IB</td>
<td></td>
</tr>
<tr>
<td>Commercial Bank Portfolio (CB)</td>
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<td><strong>16</strong></td>
</tr>
<tr>
<td>Security Broker Dealer Portfolio (IB)</td>
<td>11</td>
<td>.</td>
</tr>
</tbody>
</table>
### Table 4: Predictive 5%-CoVaRs

This table reports a predictive 5%-VaR and 5%-CoVaRs. To calculate the 5%-VaR, the returns of the institutions / hedge fund styles of the left column are quantile regressed on their lagged value. Then the predicted value is computed with the unconditional VaR as the value for the lagged variable. For the predictive CoVaR, the institutions / styles of the left column are regressed on their own lagged return, and the lagged return of the index of the top row. Then the predicted value is calculated by replacing both right hand side variables by their unconditional VaR. The percentage increase of the predictive CoVaR relative to the predictive VaR is reported in the Table. Standard errors are computed via bootstrap.

<table>
<thead>
<tr>
<th>Panel A: Institutions</th>
<th>5%-VaR</th>
<th>5%-CoVaR / 5%-VaR</th>
<th>t-stats</th>
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<tr>
<td></td>
<td></td>
<td>percent increase</td>
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<tr>
<td>Commercial Banks (CB)</td>
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<td>-3 -2 -16</td>
<td>-8.58</td>
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<tr>
<td>Investment Banks (IB)</td>
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<td>4 5 32</td>
<td>-4.27</td>
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<tr>
<td>CSFB/Tremont Hedge Fund Styles (HF)</td>
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<td>-2 2 3</td>
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<td></td>
<td>5%-VaR</td>
<td>5%-CoVaR / 5%-VaR</td>
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<tr>
<td></td>
<td></td>
<td>percent increase</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>CB IB HF</td>
<td></td>
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<td>Commercial Bank Portfolio (CB)</td>
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<td>Security Broker Dealer Portfolio (IB)</td>
<td>-13.78</td>
<td>-7 .</td>
<td>-12.16</td>
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</table>

### Panel B: Portfolios 1926-2008

This table reports the significance of five percent quantile regressions. In Columns A, the left hand side excess return is reported in the first column, and is regressed on its own lag, as well as the lagged excess return of the variable in the top row. * denotes significance at the 10% level, ** at the 5% level, and *** at the 1% level.

This table reports the percentage increase of the five percent Value-at-Risk for the returns of the left column conditional on the fifth percentile of the returns of the top row relative to the unconditional 5% Value-at-Risk (reported in the first column). The Value-at-Risk is computed from the five percent pairwise quantile regressions (the slopes of these regressions are reported in Table 3). The p-values test the null hypothesis that average CoVaRs equal average VaRs and are generated via bootstrap with 200 draws.
**Table 5: Summary Statistics of Risk Factors**

This table reports summary statistics for excess returns of six risk factors. The equity market return from the Center for Research in Security Prices (CRSP), in excess to the 3-month bill rate reflecting the equity market risk. The VIX straddle return is the return from buying at-the-money put and call options and is computed using the Black-Scholes (1973) formula with the CBOE's VIX implied volatility index, the 3-month Treasury rate, and the S&P500 index as inputs. The variance swap return is the difference between realized S&P500 variance from daily closing prices and the VIX implied variance. The repo Treasury spread is the difference between the three month general collateral Treasury repo rate (from Bloomberg) and the three month Treasury bill rate (from Federal Reserve Board's H.15 releases). The 10-year/3-month Treasury return is the return to the 10-year constant maturity Treasury bond (from H.15) in excess of the 3-month Treasury Bill. Moody's BAA - 10-year Treasury return is the return to Moody's BAA bond portfolio in excess of the return to the 10-year constant maturity Treasury return. All statistics are computed from April 1986 - May 2008.

<table>
<thead>
<tr>
<th>Risk Factor</th>
<th>Mean</th>
<th>Std Dev</th>
<th>Skew</th>
<th>Kurt</th>
<th>1%</th>
<th>5%</th>
<th>Obs</th>
</tr>
</thead>
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<tr>
<td>CRSP Market Excess Return</td>
<td>0.54</td>
<td>4.34</td>
<td>-1.02</td>
<td>6.47</td>
<td>-10.76</td>
<td>-6.49</td>
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<tr>
<td>VIX Straddle Excess Return</td>
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<td>0.89</td>
<td>3.89</td>
<td>-1.65</td>
<td>-1.41</td>
<td>264</td>
</tr>
<tr>
<td>Variance Swap Return</td>
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<td>12.24</td>
<td>177.87</td>
<td>-0.85</td>
<td>-0.80</td>
<td>264</td>
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<tr>
<td>Treasury - Repo Rate</td>
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<td>0.02</td>
<td>1.08</td>
<td>4.24</td>
<td>-0.01</td>
<td>0.00</td>
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<tr>
<td>10 Year - 3 Month Treasury Return</td>
<td>0.29</td>
<td>2.38</td>
<td>-0.33</td>
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<td>-6.25</td>
<td>-3.67</td>
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<tr>
<td>Moody's BAA - 10 Year Treasury Return</td>
<td>0.14</td>
<td>1.31</td>
<td>-0.45</td>
<td>3.81</td>
<td>-3.48</td>
<td>-2.28</td>
<td>264</td>
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Table 6: Summary Statistics for Monthly 5%-Offloaded Returns

The table reports summary statistics for the tail risk offloaded returns of banking institutions and hedge fund styles. Offloaded returns are computed as the sum of the regression residual and the intercept from a 5%-quantile regression on the six risk factors from Table 4.

<table>
<thead>
<tr>
<th></th>
<th>Data range</th>
<th>Obs</th>
<th>Sharpe</th>
<th>Mean</th>
<th>Std Dev</th>
<th>CAPM α</th>
<th>Skew</th>
<th>Kurt</th>
<th>1%</th>
<th>5%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Five Large Commercial Banks</td>
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<td>0.40</td>
<td>5.20</td>
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<td>0.17</td>
<td>4.06</td>
<td>-12.73</td>
<td>-7.32</td>
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<td>Five Investment Banks</td>
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<td>1.80</td>
<td>6.24</td>
<td>1.70</td>
<td>***</td>
<td>0.78</td>
<td>-10.41</td>
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<tr>
<td>Ten CSFB/Tremont Hedge Fund Styles</td>
<td>01/1994-05/2008</td>
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<td>-0.03</td>
<td>-0.05</td>
<td>1.90</td>
<td>-0.07</td>
<td>0.52</td>
<td>3.63</td>
<td>-4.24</td>
<td>-2.63</td>
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</table>
**Table 7: Offloaded 5%-CoVaRs**

This table reports the percentage increase of the five percent Value-at-Risk for the offloaded returns of the left column conditional on the fifth percentile of the returns of the top row relative to the unconditional 5% Value-at-Risk (reported in the first column). The Value-at-Risk is computed from the five percent pairwise quantile regressions (the slopes of these regressions are reported in Table 3). The p-values test the null hypothesis that average CoVaRs equal average VaRs and are generated via bootstrap with 200 draws.

<table>
<thead>
<tr>
<th></th>
<th>5%-VaR</th>
<th>5%-CoVaR / 5%-VaR</th>
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<td>Investment Banks (IB)</td>
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<td>1</td>
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Table 8: Offloaded 5%-CoVaRs versus OLS-CoVaRs

This table reports the percentage increase of the five percent Value-at-Risk for the offloaded returns of the left column conditional on the fifth percentile of the returns of the top row relative to conditional VaR computed from an OLS regression. The t-stats test the null hypothesis that average quantile CoVaRs equal average OLS CoVaRs and are generated via bootstrap with 200 draws.

<table>
<thead>
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<th>5%-CoVaR / OLS-CoVaR</th>
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<td>Investment Banks (IB)</td>
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<td>CSFB/Tremont Hedge Fund Styles (HF)</td>
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<td>2</td>
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Table 9: 1%-CoVaRs and Expected Shortfall 1926-2008

Panel A of this table reports the percentage increase of the one percent Value-at-Risk for the returns of the left column conditional on the fifth percentile of the returns of the top row relative to the unconditional 5% Value-at-Risk (reported in the first column). Panel B reports the unconditional 5% expected shortfall (ES) in the first column, and the percent increase of the expected shortfall conditional on the portfolio of the top row being in the worst five percent of the return distribution as percent increase relative to the unconditional expected shortfall.

<table>
<thead>
<tr>
<th></th>
<th>1%-VaR</th>
<th>1%-CoVaR / 1%-VaR</th>
<th>t-stats</th>
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