# Technological Innovation, Resource Allocation, and Growth\*

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#### Abstract

We explore the role of technological innovation as a source of economic growth by constructing direct measures of innovation at the firm level. We combine patent data for US firms from 1926 to 2010 with the stock market response to news about patents to assess the economic importance of each innovation. Our innovation measure predicts productivity and output at the firm, industry and aggregate level. Furthermore, capital and labor flow away from non-innovating firms towards innovating firms within an industry. There exists a similar, though weaker, pattern across industries. Crossindustry differences in technological innovation are strongly related to subsequent differences in industry output growth.

JEL classifications: G14, E32, O3, O4

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# Introduction

Economists since Schumpeter have argued that technological innovation combined with resource reallocation is the driver of long-term economic growth. However, the impact of technical change on economic growth and business cycle fluctuations remains difficult to quantify mainly due to the scarcity of directly observable measures of innovation. Similarly, while technology shocks play a central role in macroeconomic real business cycle models, there is little consensus on whether the measured shocks represent actual technological improvements, or are reduced-form representations of other economic forces. The primary reason for these ambiguities is the difficulty in measuring technological innovation in the data. This paper aims to fill this gap.

We construct a novel economic measure of innovation that combines information from a patent dataset with stock market data over the period 1926 to 2010.<sup>2</sup> Patents provide useful direct information about technological innovation going as far back as the eighteenth century. However, since patents are highly heterogeneous in their economic value, an increase in the number of patents granted need not coincide with greater technological innovation. Thus, constructing an empirical measure of technological innovation using patent data poses a significant challenge.

Our central idea is to use the stock market reaction around the day each patent is granted to appropriately weigh its information content. We interpret the stock price reaction to patent grants using a model along the lines of Romer (1990), which models innovation as a shock embodied in new products.<sup>3</sup> In particular, we assume that patents are valuable because they restrict competition among producers of new products. On the day of an announcement of a successful patent application, the prior uncertainty about the applying firm's ability to extract monopoly rents going forward is resolved, resulting in the firm's stock price appreciation. Because patents on economically valuable new products or technologies have higher market value, they tend to result in a larger stock market reaction. We thus use this change in the stock market value to infer the economic value of the patent. We then aggregate these stock market responses to patent grants to construct measures of innovation at the firm, industry and economy level.

Our approach to measuring patent quality has several advantages over the existing approach that relies on patent citations. While citations are informative about the intrinsic quality of patents,<sup>4</sup> their use as a measure of innovation is subject to two significant limitations.

<sup>&</sup>lt;sup>1</sup>See, for instance, Cochrane (1994).

<sup>&</sup>lt;sup>2</sup>Several new studies exploit the same source of patent data (Google Patents) as we do in our paper. For instance, see Moser and Voena (2012), Moser, Voena, and Waldinger (2012) and Lampe and Moser (2011).

<sup>&</sup>lt;sup>3</sup>Not all innovation is patentable. However, innovation that is embodied in new products is more easily patentable (see for example Comin, 2008, for a discussion on patentable innovation). Hence, when we are measuring innovation through patents we are capturing technological change embodied in new products.

<sup>&</sup>lt;sup>4</sup>See, for example, Harhoff, Narin, Scherer, and Vopel (1999), Hall, Jaffe, and Trajtenberg (2005) and Moser, Ohmstedt, and Rhode (2011).

First, counting the number of future citations to each patent requires information over the entire sample. In many economic applications – such as exploring the short- and medium-run response of investment or hiring decisions to innovation – it is desirable to use a measure based on the contemporaneous assessment of the value of a patent, as is the case with our measure. Second, the patent citation data is reliably available only in the later part of our sample.<sup>5</sup> This lack of information creates problems in assessing the quality of earlier patents, since patents often tend to cite only the most recent ones (Caballero and Jaffe, 1993).<sup>6</sup> In contrast, our measure is reliably available over a long time period.

Despite these two drawbacks, patent citations provide a valuable independent measure of the *realized* value of a patent. We therefore use patent citations as a validation of our procedure. We find that the firm's stock market reaction to the patent grant is a strong predictor of the number of citations the patent receives in the future.

Our measure of technological innovation captures known periods of high technological progress as well as firms participating in these waves (e.g., technologically progressive 1960s and early 1970s, see Laitner and Stolyarov (2003)). In addition, the empirical distribution of our firm-level innovation measure is extremely fat-tailed, since a few large firms contribute disproportionately to the aggregate rate of innovation in the economy. The identity of these firms varies by decade. This finding is consistent with past research describing the nature of radical innovations (Harhoff, Scherer, and Vopel (1997)). Furthermore, we find that characteristics of innovating firms using our measure match those of innovators as described by Baumol (2002), Griliches (1990) and Scherer (1983).

In the second part of the paper we relate innovation to economic growth and resource allocation. One of the benefits of our measure is that it allows us to study the relation between innovation and subsequent changes in productivity, output and allocation of resources at the micro level. We show that our measure of innovation is strongly related to changes in productivity of capital and labor, both at the firm and at the industry level. Specifically, firms and industries that innovate experience a surge in productivity and output. Furthermore, we find that innovating firms and industries increase their use of capital and labor inputs. As a result, we find that innovation is strongly positively related to subsequent output growth both at the industry and firm level.

We observe several empirical patterns consistent with Schumpeter's notion of "creative destruction." First, innovation activity of competing firms is negatively related to firm productivity in the short run. Second, firms that do not innovate when their competitors do

<sup>&</sup>lt;sup>5</sup>Moser and Nicholas (2004) and Nicholas (2008) discuss issues in extracting citations data from patent documents before 1975. In addition, even in the post-1975 period citation outcomes are affected by the identity of the patent examiner (Cockburn, Kortum, and Stern, 2002).

<sup>&</sup>lt;sup>6</sup>The first year that patent citations are officially included on patent documents is 1947. Since patents are likely to cite only the latest patents, earlier patents will have lower citation counts. For instance, the telephone patent by Alexander Graham Bell (patent number 174,465) has only one citation in the Google Patent database.

reduce their use of capital and labor inputs. We find similar patterns of reallocation across industries. Last, an increase in industry innovation is associated with an increase in the rate of firm exit, consistent with the view that innovation leads to industry shakeouts.

Next, we relate our direct measure of technological change to medium-run fluctuations in aggregate variables. We find that aggregate innovation activity is strongly positively correlated with changes in aggregate total factor productivity (TFP) and output. In addition, we find that aggregate consumption has a U-shaped response to the innovation shocks. This property of our measure, and the fact that the innovation shock is associated with a decline in the aggregate Tobin's Q, are characteristic of embodied technology shocks (see e.g. Jovanovic and Rousseau, 2005).

Last, we show that our measure of innovation contains additional information relative to using the raw number of patents. We repeat our firm-level analysis measuring innovation by the number of patent grants. The results are qualitatively similar, but the economic magnitudes are smaller by a factor of two to three. At the aggregate level, we confirm the findings of Shea (1999) that the relation between the number of patents and aggregate variables is weak.

Our paper is connected to several strands of the literature. Our work is closely related to the literature in macroeconomics that aims to measure technological innovation. Broadly, there are three main approaches to identify technology shocks. First, researchers have measured technological change through Solow residuals, after accounting for non-technological effects such as imperfect competition and varying utilization (see e.g. Basu, Fernald, and Kimball, 2006). Second, researchers have imposed long-run restrictions on vector auto-regressions (VARs) to identify technology shocks. Both of these approaches measure technology indirectly. The resulting technology series are highly dependent on specific identification assumptions.

Our approach falls into the third category, which constructs direct measures of technological innovation using micro data. Shea (1999) constructs direct measures of technology innovation using patents and R&D spending and finds a weak relationship between TFP and technology shocks. Our contrasting results suggest that this weak link is likely the result of assuming that all patents are of equal value. Indeed, Kortum and Lerner (1998) show that there is wide heterogeneity in the economic value of patents. Furthermore, fluctuations in the number of patents granted are often the result of changes in patent regulation, or the quantity of resources available to the US patent office (see e.g. Griliches, 1990; Hall and Ziedonis, 2001). As a result, a larger number of patents does not necessarily imply greater technological innovation. Using R&D spending to measure innovation overcomes some of these issues, but doing so measures innovation indirectly. The link between inputs and output may vary as the efficiency of the research sector varies over time or due to other economic forces. For instance, Kortum (1993) documents that the patent-to-R&D ratio has shown a secular decline in the US. The measure proposed by Alexopoulos (2011) based on books published in the field of

technology overcomes many of these shortcomings. However, this measure is only available at the aggregate level, and does not directly capture the economic value of innovation. In contrast, our measure is available at the firm level, which allows us to evaluate reallocation and growth dynamics across firms and sectors.

Our paper is not the first to link firm patenting activity and stock market value (Pakes, 1985; Austin, 1993; Hall et al., 2005; Nicholas, 2008). In particular, Pakes (1985) examines the relation between patents and the stock market rate of return in a sample of 120 firms during the 1968–1975 period. His estimates imply that, on average, an unexpected arrival of one patent is associated with an increase in the firm's market value of \$810,000. The ultimate objective of these papers is to measure the economic value of patents; in contrast, we use the stock market reaction as a means to an end—to construct appropriate weights for an innovation measure which we employ to study reallocation and growth dynamics. Our paper is also related to work that examines whether technological innovation leads to positive knowledge spillovers or business stealing. Related to our paper is the work of Bloom, Schankerman, and Van Reenen (2010), who disentangle the externalities generated by R&D expenditures on firms competing in the product and technology space. We contribute to this literature by proposing a measure of patent quality based on stock market reaction and assessing within- as well as between-industry reallocation and growth dynamics after bursts of innovative activity.

Our work is also related to literature on endogenous growth and creative destruction (see Acemoglu, 2009, for a textbook treatment). We follow the spirit of the growth literature that emphasizes the role of technological progress in promoting growth at the aggregate level (see e.g. Aghion and Howitt, 1997) while abstracting away from the role of contracts and inner workings of the firms in developing innovation (e.g. Gorodnichenko and Schnitzer, 2010; Manso, 2011; Seru, 2012). Related to our work are the papers that explore the impact of innovation on firm productivity and growth (Caballero and Jaffe, 1993; Akcigit and Kerr, 2010; Acemoglu, Akcigit, Bloom, and William, 2011). Finally, our paper is related to work that explores the micro-foundations of aggregate economic shocks. In particular, Gabaix (2011) proposes that if the distribution of firm size is sufficiently fat-tailed, as is the case in the US and in most of the world, firm-specific shocks can have substantial effects on aggregate quantities due to the failure of the law of large numbers. Consistent with this view, the empirical distribution of firm-level innovation measure is fat-tailed, suggesting that the innovative activity of a few large firms can have a large aggregate impact.

The remainder of the paper is organized as follows. In Section I we describe the construction of our innovation measure. In Section II we provide external validation for our measure by relating stock market reaction to a patent to the number of subsequent citations it receives. Section III studies the response of individual firms and industries on our innovation measure

and documents patterns of reallocation. Section IV explores the response of aggregate variables on our innovation measure. Section V concludes.

## I Construction of our innovation measure

Here, we discuss the construction of our innovation measure. We start by developing a tractable general equilibrium model that links innovative activity of a firm to its stock market value. Using the model as a guide, we proceed to construct a measure of innovation that uses the stock market's response to news about patents to assess the economic importance of each innovation.

#### I.A The model

We represent innovation as expanding the variety of intermediate products, borrowing several key elements from models with endogenous growth (see e.g. Romer, 1990). To conserve space, we relegate all derivations to the Online Appendix.

#### Setup

There is a competitive representative firm producing a single consumption good (numeraire) from a variety of intermediate goods indexed by j according to the production function

$$Y_t = Z_t \left( L_t^F \right)^{1-\alpha} \int_0^{H_t} \theta_j^{1-\alpha} q_{jt}^{\alpha} dj, \tag{1}$$

where  $Z_t$  is a disembodied productivity shock;  $H_t$  is an embodied shock representing the current frontier state of technology;  $\theta_j$  represents the quality of intermediate good j;  $q_{jt}$  represents the produced quantity of intermediate good j, whose production has a unit labor cost; and  $L_t^F$  denotes the labor input used by the final-good producer. Here, note that Z affects the productivity of all intermediate goods equally. In contrast, innovation is embodied in new intermediate products, as it reduces the cost of producing them from infinity to one. Hence, an increase in H only benefits the producers of the new intermediate goods. We assume that the shocks  $\Delta \ln Z_t$  and  $\Delta \ln H_t \geq 0$  are IID over time and independent from each other.

There is a fixed set of firms  $f \in [0,1]$  that produce intermediate goods. Each new intermediate good created during period t is assigned a measure  $[(H_t - H_{t-1})/\chi] dj$  on the interval  $(H_{t-1}, H_t]$ . Thus, each firm is assigned a single new intermediate good with probability  $\chi$ . If a firm receives an intermediate good, it immediately files for patent protection. The probability that a patent is granted,  $p_j$ , is itself random with an IID distribution across the intermediate goods.

If the patent for good j is granted to the firm, the firm becomes a monopolist in good j in perpetuity.<sup>7</sup> It maximizes its intra-period profits

$$\max_{p_{jt}} (p_{jt} - w_t) q_{jt} (p_{jt}), \qquad (2)$$

where  $p_{jt}$  is the spot price of good j,  $w_t$  is the market wage, and  $q_{jt}(p_{jt})$  is the demand curve for good j. If the patent application for the intermediate good j is denied, all firms have access to this innovation. In this case, the market for good j is perfectly competitive,  $p_{jt} = w_t$ , and producing firms make zero profits from good j. After the outcome of the patent application is decided, period-t production takes place.

Last, there is an infinitely-lived representative household that supplies a unit of labor inelastically. The household faces a complete set of state-contingent securities and trades in financial markets to maximize life-time utility of consumption. The household's preferences are

$$E_0 \left[ \sum_{t=0}^{\infty} \rho^t \frac{c_t^{1-\gamma}}{1-\gamma} \right]. \tag{3}$$

#### **Equilibrium**

If a patent for good j is granted to a firm, the firm acts as a monopolist.<sup>8</sup> The equilibrium level of profits from producing good j at time t equals

$$\pi_{jt} = B_3 \chi^{-1} \left( H_{\tau(j)} - H_{\tau(j)-1} \right) \theta_j Z_t H_t^{-\alpha}, \tag{4}$$

where  $\tau(j)$  denotes the time good j is introduced and  $B_3$  is a constant defined in the Online Appendix. Hence, the stock market value of the firm increases by the present value of these profits (4), discounted using the equilibrium stochastic discount factor. Conversely, if the patent application is declined, production of this good is competitive, hence all firms make zero profits.

We focus on the stock market reaction to the following two information events. First, after the market learns that firm f has applied for a patent for good j in period t, but prior to the patent decision being made, the market value of the firm increases by

$$\Delta V_{ft} = p_j B_5 \chi^{-1} (H_t - H_{t-1}) \theta_j Z_t H_t^{-\alpha}$$
 (5)

<sup>&</sup>lt;sup>7</sup>We could generalize the model by allowing the patent protection to expire with a constant probability each period. Doing so has no qualitative impact on our results.

<sup>&</sup>lt;sup>8</sup>There is a continuum of intermediate products in this economy, and each firm produces only a finite number of such products. Hence, each firm takes prices of all intermediate goods it does not produce as given. Moreover, the firm's choice of the price for a particular good does not interact with its choices of prices for the rest of the goods it produces. As a result, each firm chooses the spot price for each intermediate good it produces to maximize the resulting profits, taking the demand curve for each good as given.

relative to the other firms. Second, if the patent application for good j is successful, the firm's market value increases by an additional amount

$$\Delta V_{ft} = (1 - p_j) B_5 \chi^{-1} (H_t - H_{t-1}) \theta_j Z_t H_t^{-\alpha},$$
(6)

where  $B_5$  is a constant defined in the Online Appendix.

Aggregating the gain in market value (6) across firms with successful patent applications in period t yields

$$\Delta V_t = B_5 \left( 1 - E[p_j \theta_j] \right) Z_t H_t^{1-\alpha} \left( 1 - e^{-\Delta \ln H_t} \right). \tag{7}$$

Normalizing (7) by the period-t aggregate market price  $P_t$  yields

$$\frac{\Delta V_t}{P_t} = B_7 \left( 1 - \operatorname{E} \left[ p_j \theta_j \right] \right) \left( 1 - e^{-\Delta \ln H_t} \right) 
\approx B_7 \left( 1 - \operatorname{E} \left[ p_j \theta_j \right] \right) \Delta \ln H_t,$$
(8)

where the approximation is valid for small values of  $\Delta \ln H$ , and  $B_7$  is a constant defined in the Online Appendix.

The growth rate of aggregate output is determined by the disembodied shock  $\Delta \ln Z_t$  and changes in the frontier level of technology  $\Delta \ln H_t$ 

$$\Delta \ln Y_t = (1 - \alpha) \Delta \ln H_t + \Delta \ln Z_t. \tag{9}$$

#### Discussion

The economy we consider features two aggregate shocks: the disembodied shock  $\Delta \ln Z$  and the embodied shock  $\Delta \ln H$ . Our model allows us to map the stock market reaction to successful patent grants to the innovation shock  $\Delta \ln H$ .<sup>9</sup> In the process, it provides a number of insights.

First, the market value reaction to a successful patent application (6) is increasing in the good-specific quality index  $\theta_j$  and the frontier level of technology  $H_t$ . This equation understates the total impact of the patent on the firm value because the information about the patent allocation is known to the market before the patent application is resolved. In particular, the total market value of a patent is given by the sum of (5) and (6).

Second, the change in the normalized aggregate market value observed upon patent awards (7) is increasing in the embodied technology shock  $\Delta \ln H_t$ . The aggregated market

<sup>&</sup>lt;sup>9</sup>In the remainder of our analysis we will use the terms innovation and embodied shock interchangeably. To be more precise, by innovation we are explicitly referring to patentable innovation, which is embodied in new goods or processes.

<sup>&</sup>lt;sup>10</sup>We have so far assumed that the value of the patent  $\theta_j$  is perfectly observable to market participants before the patent is granted. We show how relaxing this assumption affects our results in Section II.C.

reaction is informative about the average level of embodied technological progress because of patent protection. Even though patents serve only to restrict competition and limit output, in the absence of patent protection firms would make zero profits. Thus, the existence of patent protection allows us to infer the value of new innovations from stock market reactions.

Third, the aggregated change in stock market value around patent grants (8) is also a function of the contemporaneous disembodied shock  $\Delta \ln Z_t$ . Normalizing by the end-of-period market value (8) isolates the embodied technology shock  $\Delta \ln H_t$ .

Fourth, even though the firm-level market response to a successful patent grant (6) underestimates the value of a patent  $\theta_j$ , the effect of this bias at the aggregate level in (8) is a constant scaling factor. Hence, the total stock market reaction across patenting firms is increasing in the embodied shock  $\Delta \ln H$  regardless of the joint distribution of  $p_j$  and  $\theta_j$ .

#### I.B Patents and the stock market

Our model highlights the central idea in this paper, that is, to identify the value of a patent from the stock price reaction around the days when the market learns that a patent has been granted to the firm. In our analysis, we use patent data from Google Patents and financial data from CRSP. See the Online Appendix (Sections A-C) for details.

In order to examine stock market reactions, we need to define what constitutes an information event. The USPTO's publication, *Official Gazette*, which is published every Tuesday, lists patents that are granted that day and reports details of the patent. Prior to 2000, patent application filings were not publicized (see e.g. Austin (1993)). However, subsequent to the American Inventors Protection Act, which became effective on November 30, 2000, the USPTO began publishing applications 18 months after filing, even if the patents had not yet been granted. Publication of these applications occurs on Thursday of each week. Hence, when application publication dates are available, we combine the stock market reaction around both information events to construct our innovation measure.

To isolate market movements we focus on the firm's idiosyncratic return,  $r_{ft}$ , defined as the firm's return minus the return on the market portfolio. By using this 'market-adjusted-return model' (Campbell, Lo, and MacKinlay, 1997), we avoid the need to estimate the firm's stock market beta, therefore removing one source of measurement error. As a robustness check, we construct the idiosyncratic return as the firm's stock return minus the return on the beta-matched portfolio (CRSP: bxret). This has the advantage that it relaxes the assumption that all firms have the same amount of systematic risk, but is only available for a smaller sample of firms. Our results are quantitatively similar when using this alternative definition.

#### Information in stock-price responses

We start by assessing if information is revealed on patent grant dates by investigating whether stock prices behave differently on days patents are granted than when they are not. First, in Table 1, we document that trading volume increases around the days that patents are granted (or their applications are published). In particular, we regress a firm's share turnover x (trading volume divided by shares outstanding) on an announcement day dummy variable  $I_{fd}$ ,

$$x_{fd+k} = a_0 + a_{ft} + b_d + b(k) I_{fd} + u_{fd}, (10)$$

controlling for firm-year  $a_{ft}$  and day-of-week  $b_d$  fixed effects. The results show that, as we vary k from -1 to 5, there is a statistically significant increase in share turnover around the day that the firm is granted a patent or its application is publicized. Specifically, volume increases on the day of the announcement, and remains temporarily higher for the next two days. We find that the total turnover in the first three days after the announcement increases by 0.16%. Given that the daily median turnover rate is 1.29%, this is an economically significant increase in trading volume, and supports the view that patent issuance conveys important information to the market.<sup>11</sup> To conserve space, we report other variants of this specification in the Online Appendix (Table 1).

Second, we find that the distribution of stock returns for patenting firms differs on days when the firm is granted a patent relative to when the firm does not patent. In particular, we use the subsample of patenting firms and compare the distribution of idiosyncratic returns  $r_{ft}$  during the three day window [t, t+2] around patent-grant days with the distribution of three day returns on days that no patent is granted to the firm. A Kolmogorov Smirnov test rejects the hypothesis that the two distributions are the same at the 1 percent level.

## Some illustrative case-studies

Before turning to our main results, we provide some illustrative case studies to highlight the success of our method in identifying valuable patents. For these examples we performed an extensive search of online and print news sources to confirm that no other news events could account for the return around the patent dates.

The first example is patent 4,946,778, titled "Single Polypeptide Chain Binding Molecules", which was granted to Genex Corporation on August 7, 1990. As shown in Panel A of Figure 1, the stock price increased 67 percent (in excess of market returns) in the three days following the patent announcement. Investors clearly believed the patent was valuable, and news of the patent was reported in the media. For example, on August 8 Business Wire quoted the biotechnology head of a Washington-based patent law firm as saying "The claims issued to

<sup>&</sup>lt;sup>11</sup>Though prices can adjust to new information absent any trading, the fact that stock turnover increases following a patent grant or publication is consistent with the view that some information is released to the market, and not all agents share the same beliefs.

Genex will dominate the whole industry. Companies wishing to make, use or sell genetically engineered SCA proteins will have to negotiate with Genex for the rights to do so."

The patent has subsequently proved to be important on other dimensions as well. The research that developed the patent, Bird, Hardman, Jacobson, Johnson, Kaufman, Lee, Lee, Pope, Riordan, and Whitlow (1988), was published in *Science* and has since been cited over 1300 times, <sup>12</sup> while the patent itself has been subsequently cited by 775 patents. Genex was acquired in 1991 by another biotechnology firm, Enzon. News reports at the time indicate that the acquisition was made in particular to give Enzon access to Genex's protein technology.

Another example from the biotechnology industry is patent 5,585,089, granted to Protein Design Labs on December 17, 1996. The stock rose 22 percent in the next two days on especially high trading volume (Panel B of Figure 1). On December 20, the *New York Times* reported that the patent "could affect as much as a fourth of all biotechnology drugs currently in clinical trials."

Finally, consider the case of patent 6,317,722 granted to Amazon.com on November 13, 2001 for the "use of electronic shopping carts to generate personal recommendations". When Amazon filed this patent in September 1998, online commerce was in its infancy. Amazon alone has grown from a market capitalization of approximately \$6 billion to over \$100 billion today. The importance of a patent that staked out a claim on a key part of encouraging consumers to buy more – the now-pervasive "customers also bought" suggestions— was not missed by investors: the stock rose 34 percent in the two days after the announcement, adding \$900 million in market capitalization (see Panel C of Figure 1).

Other patents associated with large returns include an inkjet technology granted to Canon in 1982 (Panel D of Figure 1), and a digital storage device granted to Sperry Rand in 1959. These examples, and a number of others we carefully investigated, indicate that our method of identifying important patents by looking at stock returns appears to work well.

# I.C Measuring innovation

We now detail the construction of our measure of innovation. We use the stock market reaction around the day that a patent has been granted to the firm, or its application publicized, to infer the value of each patent. Since the stock price of innovating firms may fluctuate for reasons unrelated to innovation during the announcement window, we construct a measure of innovation that explicitly accounts for measurement error. <sup>13</sup> In particular, we decompose the idiosyncratic stock return r around the time that patent j is announced as

$$r_j^l = x_j + \varepsilon_{jl},\tag{11}$$

<sup>&</sup>lt;sup>12</sup>Google Scholar citation count.

<sup>&</sup>lt;sup>13</sup>We are grateful to John Cochrane for this suggestion.

where  $x_j$  denotes the value of patent j as a fraction of the firm's market capitalization; l denotes the length of the event window we use to compute returns and  $\varepsilon_{jl}$  denotes the component of the firm's stock return that is unrelated to the patent.

We construct the conditional expectation of the dollar value of patent j as

$$\widehat{A}_{j} = \frac{1}{N} E[x_{j} | r_{jd}^{l}] S_{jd-1}, \tag{12}$$

where  $S_{jd-1}$  is the market capitalization of the firm owning patent j on the day prior to the announcement. If multiple patents N are issued to the same firm on the same day, we assign each patent a fraction 1/N of the total value.

To recover the value of the patent, we need to make assumptions about the joint distribution of x and  $\varepsilon$ . Following our model (equations (5)-(6)), the value of the patent x is a positive random variable. Hence, we assume that x is distributed according to a Gaussian  $\mathcal{N}(0, \sigma_{vj}^2)$  truncated at zero. Further, we assume that the noise term is normally distributed,  $\varepsilon_{jl} \sim \mathcal{N}(0, \sigma_{\xi j}^2)$ . Last, there is strong evidence that idiosyncratic return volatility varies both in the time-series and the cross-section. Hence, we allow both  $\sigma_{\xi j}^2$  and  $\sigma_{vj}^2$  to vary across firms and across time, but in constant proportions. We do this in order to reduce the number of parameters we estimate.<sup>14</sup>

The filtered value of  $x_j$  as a function of the stock return is equal to

$$E[x_j|r_j^l] = \delta_j r_j^l + \sqrt{\delta_j} \,\sigma_{\xi j} \,\frac{\phi(R_j)}{1 - \Phi(R_j)},\tag{13}$$

where  $\phi$  and  $\Phi$  are the standard normal pdf and cdf, respectively, and R and  $\delta$  are the normalized return and the signal-to-noise ratio respectively,

$$R_j = -\sqrt{\delta_j} \frac{r_j^l}{\sigma_{\xi j}}, \qquad \delta_j = \frac{\sigma_{vj}^2}{\sigma_{vj}^2 + \sigma_{\xi j}^2}.$$
 (14)

The conditional value of a patent in equation (13) is an increasing and convex function of the daily firm return.

The next step is to choose the length of the announcement window, l. Varying the length of the window trades off potentially omitting useful information versus potentially adding noise to our estimates. We choose a three-day window (l = 2) and as a robustness test extend the window to five days (l = 4).

Our assumption that  $\sigma_{\xi j}^2$  and  $\sigma_{vj}^2$  vary in constant proportions implies that the signal-tonoise ratio is constant across firms and time,  $\delta_j = \delta$ . To estimate  $\delta$ , we compute the increase in the volatility of firm returns around patent announcement days. Specifically, we regress

<sup>&</sup>lt;sup>14</sup>Our specification of the distribution of  $x_j$  relaxes the assumption that  $\theta_j$  is identically distributed among intermediate goods we made in Section I.A. Doing so simplifies the empirical analysis but does not alter the main implications of the model.

log squared returns on a patent announcement-day dummy variable,  $I_{fd}$ ,

$$\ln \left(r_{fd}^{l}\right)^{2} = a_{0} + a_{ft} + b_{d} + \gamma I_{fd} + u_{fd},\tag{15}$$

where  $r_{fd}^l$  refers to the idiosyncratic return of firm f centered on day d with window of length l. We control for firm-year  $(a_{ft})$  and day-of-week  $(b_d)$  fixed effects. Taking into account the adjustment for the variance of the truncated normal, the signal-to-noise estimate can be recovered from our estimate  $\gamma$  by

$$\widehat{\delta} = 1 - \left(1 + \frac{1}{1 - \left(\frac{\phi(0)}{1 - \Phi(0)}\right)^2} \left(e^{\widehat{\gamma}} - 1\right)\right)^{-1}.$$
(16)

We estimate (15) using a three-day (l=2) and a five-day (l=4) return announcement window. Our estimates imply  $\hat{\delta} \approx 0.04$  in both cases, so we use this as our benchmark value.<sup>15</sup>

Last, we estimate the variance of the measurement error  $\sigma_{\xi j}^2$ . For every firm f and year t we estimate its idiosyncratic variance,  $\sigma_{ft}^2$ , from daily returns. This variance is estimated over both announcement and non-announcement days, so it is a mongrel of both  $\sigma_v^2$  and  $\sigma_\xi^2$ . Given the estimate of the daily variance  $\sigma_{ft}^2$ , the fraction of trading days that are announcement days,  $\mu$ , and our estimate  $\hat{\gamma}$ , we recover the measurement error by  $\sigma_{\xi ft}^2 = \sigma_{ft}^2 (1+l) \left(1 + \mu_{ft} (1+l) \frac{\hat{\gamma}}{1-\hat{\gamma}}\right)^{-1}$ .

In Table 2 we report the distribution of number of patents granted per day, idiosyncratic firm returns  $r_f$ , filtered values  $E[x_j|r_f]$  and dollar values A in 1982 dollars across our sample of 1,915,031 patents. To conserve space, we focus only on patent grant dates and a window of 3 days. We see that distribution of firm returns is rightly skewed, and positive roughly 55 percent of the time. Our measure implies that the median value of a patent is \$2.2 million, which is comparable to the findings of Harhoff, Scherer, and Vopel (2003) and Giuri et al. (2007) who report the distribution of valuations for small samples of European patents based on survey responses.

Equation (13) implies that negative returns are interpreted as small values for the patent, while positive returns are interpreted as larger positive values. This convex behavior stems from our assumption that the value of a patent  $x_j$  in equation (11) is non-negative, which follows from equations (5)-(6) in our model. One worry is that because  $\widehat{A}_j$  is a convex function of the idiosyncratic return  $r_{jd}^l$ , it is influenced by the firm's volatility. Hence, as a robustness check, we include the firm's idiosyncratic volatility as a control throughout our empirical analysis. Last, to assess the benefit of explicitly recognizing the non-negativity of  $x_j$  in our estimation of the patent value, we estimate an alternative measure where we assume that  $x_j \sim \mathcal{N}(0, \sigma_{vj}^2)$ , with no truncation at zero. We then follow equation (12) and construct a

<sup>&</sup>lt;sup>15</sup>As a robustness test, we estimate equation (15) allowing the signal-to-noise ratio  $\delta$  to vary across firm size or volatility quintiles. We find no meaningful differences in the estimates of  $\delta$  across quintiles.

second measure of patent values  $\overline{A}$ , which now is equal to the total dollar change in stock market value around the issue of patent j multiplied by our estimate of  $\gamma$ .

# II Evidence validating our innovation measure

Prior to using our measure for empirical work, we provide evidence that it is correlated with a measure of the *realized* value of a patent. In particular, we follow the literature studying innovation that concludes that the number of times that patents are cited in the future is correlated with the quality of the patent (Harhoff et al., 1999; Hall et al., 2005; Moser et al., 2011). Accordingly, this section uses the number of citations a patent receives in the future as a measure of its realized value.

#### II.A Patent citations

We examine whether the total number of citations the patent receives in the future  $N_j$  is related to our innovation measure  $\hat{A}_j$  using the specification

$$\ln(1+N_i) = a + b \ln \hat{A}_i + c Z_i + u_i. \tag{17}$$

We include a vector of controls Z that includes grant-year (or publication-year) fixed effects because older patents have had more time to accumulate citations; the firm's log idiosyncratic volatility to control for its possible effect on our innovation measure; the firm's log market capitalization, as larger firms may produce more influential patents; the log number of patents N granted on the same day, since it mechanically affects our measure; firm fixed effects to control for the presence of unobservable firm effects on citations and our innovation measure; and technology class-year fixed effects, since citation numbers may vary by industry. Since patent applications were only publicized after 2000, we analyze the information content of days when a patent is issued versus the firm's application publicized separately. Initially, we consider three-day (l=2) announcement day windows. We cluster the standard errors by grant or publication year and present the results with different versions of controls in Table 3.

Columns one to four of Panel I show the results of our benchmark specification – focusing on grant dates only – with different controls. We see that our innovation measure  $\widehat{A}$  is related to the number of future citations across specifications. The economic magnitudes are substantial. The median number of citations a patent receives is 5. Our point estimates imply that an increase from the median to the 90th percentile in terms of our innovation measure  $\widehat{A}$  – corresponding to an increase of approximately 23 million 1982 US dollars – is associated with a 9 to 54 percent proportional increase in the number of future citations. <sup>16</sup> Columns

<sup>&</sup>lt;sup>16</sup>Note that small changes in citations generated by a patent can be associated with large value implications for the firm producing the patent. For instance, Hall et al. (2005) show that 1 more citation per patent

five to eight of Panel I show the corresponding estimates when we focus *only* on dates that the patent application becomes public following the American Inventors Protection Act of 2000. We find that the economic magnitudes are smaller, ranging from 4 to 11 percent per 90th to 50th percentile change in  $\widehat{A}$  and not statistically significant if we include firm effects in the specification.

We perform several robustness tests to our specification (17). First, we estimate a semi-log specification, replacing  $\log(1+N)$  with N. As we see in Table 3, our point estimates are statistically significant across specifications. An increase in  $\widehat{A}$  from the median to the 90th percentile is associated with 1.3 to 6.1 (0.5 to 0.9) more citations focusing only on the grant-day (publication day). Second, we replace  $\log \widehat{A}$  with  $\widehat{A}$ . In this case, our results are similar using patent grant days, whereas there is no consistent pattern when using publication dates. In addition, the economic magnitudes are smaller, as an increase in  $\widehat{A}$  from the median to the 90th percentile is associated with 0.2 to 0.6 more citations. Given the skewness in our innovation measure  $\widehat{A}$ , we conclude that a log specification is preferable. Third, we repeat the exercise extending the announcement window to five-days (l=4). In this case our results are quantitatively similar, and we provide the details in the Online Appendix (Table 5).

Last, we document the relation between our measure of the raw change in stock market value  $\overline{A}$  and the future number of citations in Table 4. Regardless of whether we use a linear or a semi-log specification, even though the point estimates are positive, there is no statistically significant relation between the raw change in stock market value  $\overline{A}$  and the number of citations the patent receives in the future. We interpret this finding as evidence that the stock market reaction contains significant noise, and that our assumption that the value of a patent is weakly positive is crucial in disentangling the information contained in returns from components unrelated to the value of the patent.

## II.B Placebo tests

Our findings in Section II.A could be influenced by unobservable, time-varying effects at the firm level, that affect both the movements in the stock price of the firm as well as the number of citations that patents assigned to it receives. To address this concern, we perform a series of placebo tests to illustrate that the relation between stock market reaction to a particular patent and the number of citations received by that patent in the future is not spurious. In each placebo experiment, we randomly generate a different issue date for each patent within the same year the patent is granted to the firm. We reconstruct our measure using the placebo grant dates and estimate (17). We repeat this exercise 500 times. To conserve space, we report the results of placebo tests corresponding only to the specification in the first row, fourth column of Table 3.

(around the median cites per patent) is associated with 3 percent higher market value for the firm that produces the patent.

Figure 2 reports the distribution of estimate  $\hat{b}$  across the placebo tests. The coefficient  $\hat{b}$  ranges from -0.01 to 0.001 across replications, substantially different from our point estimate of 0.054. This analysis suggests that the relation between the stock market response to a patent being granted and the number of citations the patent receives in the future is unlikely to be spurious.

## II.C Effect of imperfect information about patents

Our operating assumption so far has been that the market does not revise its beliefs about the value of the patent at the time the patent is granted. This is because, in our model, the information content of the patent is perfectly anticipated by the market.<sup>17</sup> This assumption is valid post-2000, when the American Inventors Protection Act required that patent applications be publicly available before the patent is granted. In contrast, prior to 2000, patent applications were only disclosed to the public at the time the patent is granted to the firm. Hence, during this period, it is possible that the market did not know the full value of the patent prior to the patent being granted.

We now explore how the effect of imperfect information about patent quality impacts our empirical procedure. We introduce a small modification to the model in Section I.A, allowing for patent quality to be only imperfectly observable to the market prior to the patent being granted. Specifically, let

$$s = \theta + e, (18)$$

where e is a mean-zero random variable. The variable s is an imperfect but unbiased estimate of patent quality that is already incorporated into the firm's market value prior to the patent being granted. At the time of the patent grant, the true quality of the patent  $\theta$  is revealed to the market. In this case, following a successful patent grant, the stock price of the firm changes by

$$\Delta V_{ft} = (1 - p_j) B_5 \chi^{-1} (H_t - H_{t-1}) \theta_j Z_t H_t^{-\alpha} - p_j B_5 \chi^{-1} (H_t - H_{t-1}) Z_t H_t^{-\alpha} e_j.$$
 (19)

Examining equation (19), the stock market reaction to the patent grant contains two components. The first part is positive, reflects the true value of the patent, and is the same as in the baseline model. The second part is proportional to the mean-zero random variable e that reflects the revision of market beliefs about the value of the patent.

The problem of extracting the value of the patent with imperfect information fits into the framework of equation (11) with one modification. Specifically, the noise term  $\varepsilon$  in equation (11) now includes movements in stock returns unrelated to the value of the patent plus the revision in market expectations e. Hence, we might need to revisit our estimation

<sup>&</sup>lt;sup>17</sup>Alternatively, the assumption is consistent with information about the patent being fully unanticipated.

of the signal-to-noise ratio  $\delta$ , since we may no longer be able to use the difference in the volatility of firm returns on patenting versus non-patenting days to infer the variance of noise.

We address this issue by assessing the nature of information about the quality of the patent released on grant days. Specifically, we exploit the change in information disclosure policy by the American Inventors Protection Act (AIPA) that applied to all patents filed after November 30th. For the patents that were filed after November 30th 2000, the market had full knowledge of their quality at the time these patents were granted. On the other hand, for the patents filed before November 30th, it is possible that on the grant day the stock market reaction indeed contains news about  $\theta_j$ . We thus compare estimates of the signal-to-noise ratio across the two sets of patents: patents that were filed just before the act, that is in the month of November 2000; and patents that were filed immediately after the act, that is in December 2000.

We first establish that these patents are similar in terms of quality, by comparing the distribution of patent citations across the two groups. The Kolmogorov-Smirnov test fails to reject the null that the two distributions are the same at the 10 percent level. Next, we estimate the signal-to-noise ratio  $\delta$  across these two sets of patents, allowing the coefficient on the grant in equation (15) to vary across the two groups. Even though the point estimate is 0.005 smaller for the patents filed in December 2000, the difference is not statistically significant (p-value is 0.29). As further supporting evidence that the market was already informed about the quality of the patents prior to the AIPA, we estimate equation (10) separately for each group of patents, and find no evidence that the response of trading volume on grant dates is systematically different across the two groups.

Overall, our results suggest that, prior to the enactment of AIPA, the market was as well informed about the value of the patent before the grant date as post-2000, when the patent document was in the public domain. These findings suggests that the variance of e may be small and as a result we do not have to alter the estimation of the signal-to-noise ratio from equation (11).<sup>18</sup>

# III Innovation, productivity and reallocation

In this section, we study the general relation between our measure of innovation and economic activity. We focus on the idea that resources in an economy need to be allocated to the most productive firms and industries to maximize its overall level of production – a cornerstone of

<sup>&</sup>lt;sup>18</sup>Nevertheless, we also investigate the robustness of our results to different values of  $\delta$ . In particular, in the presence of imperfect information about the patent, equation (19) shows that our estimate of the signal-to-noise ratio  $\delta$  based on patenting versus non-patenting days might *underestimate* the amount of noise. We repeat our analysis relating patent citations to our innovation measure constructed using smaller estimates of  $\delta$  ( $\delta = 0.03$  and  $\delta = 0.015$ ). Our results relating our measure of innovation to the number of citations a patent receives in the future remain very similar.

many models of economic growth.<sup>19</sup> In particular, we analyze this mechanism on two broad fronts. First, we document the link between innovation and productivity. Second, we show that, consistent with economic optimization, productive resources flow into the innovating firm away from firms that do not innovate.<sup>20</sup> We perform our analysis both within and across industries.

Before we conduct our analysis, a caveat is in order. When constructing our innovation measure, we only use information on patents by publicly-traded firms. Hence, one worry is that we do not include private companies, several of which might be responsible for large and more important technology shocks.<sup>21</sup> This omission is likely to bias our findings toward zero. The magnitude of any bias, however, is likely to be small for two reasons. First, Bloom et al. (2010) show that public firms in Compustat account for most of the R&D expenditures in the United States. Second, Baumol (2002) notes that while several independent and private firms might provide initial innovation, large publicly traded firms conduct most of the refinements that lead to large improvements in welfare.

#### III.A Firm-level evidence

We start by describing how we construct our firm-level measure of innovation. We then document the relation between our measure of innovation and capital and labor productivity, reallocation of inputs across firms within an industry and output growth. We also discuss these results when using other measures of innovation.

#### Construction of firm-level measure

We construct our dollar measure of innovation at the firm level by aggregating the dollar values across all patents granted, or its application published (after 2000), to firm f in year t,

$$A_{ft}^v = \sum_{j \in P_{ft}^g} \widehat{A}_j^g + \sum_{j \in P_{ft}^p} \widehat{A}_j^p, \tag{20}$$

where  $P_{ft}^g$  and  $P_{ft}^p$  denote the sets of patents granted and published applications, respectively, to firm f in year t. For most of our sample period, patent applications were kept secret until the patent was granted, hence when constructing our firm measure we only use the stock market reaction on the grant date. After 2000, patent applications where publicized, hence

<sup>&</sup>lt;sup>19</sup>There exists a large literature on the importance of resource allocation for economic growth (see, e.g. Restuccia and Rogerson (2008); Hsieh and Klenow (2009); Jones (2011); Acemoglu et al. (2011)).

<sup>&</sup>lt;sup>20</sup>Some of the economic variables we consider in this analysis are not an explicit part of our basic model. For instance, we do not introduce physical capital in our model, hence reallocation is explicitly defined only in terms of labor inputs. However, it is natural to consider physical capital in our empirical analysis.

<sup>&</sup>lt;sup>21</sup>Kortum and Lerner (2000) find that venture capital, which accounts for 3 percent of total R%D expenditures, is responsible of 15 percent of industrial innovations.

following equations (5)-(6) we add the filtered dollar reaction during the patent publication window  $\widehat{A}_{i}^{p}$  to the dollar reaction during the grant window  $\widehat{A}_{i}^{g}$ .

To avoid scale effects, we divide the dollar value of innovation  $A^v$  by the end-of-year firm market capitalization, S, in year t:

$$A_{ft} = \frac{A_{ft}^v}{S_{ft}}. (21)$$

Hence, our firm-level innovation measures can be interpreted as the fraction of firm f's value that can be attributed to innovation in year t.

As we see in Table 5, the distribution of our firm-level measure  $A_{ft}$  is skewed to the right, similarly to the distribution of number of patents or patent citations at the firm level. In addition, the distribution of our firm-level measures of innovation  $A_f$  has fat tails. In particular, restricting attention to the top 10 percent of the distribution, the relation between the log complementary empirical cdf,  $\log(1 - F(A))$ , and the log innovation measure,  $\log A$  is close to linear, with a slope coefficient of -1.9 (see Figure 2 in Online Appendix). Hence, the tail behavior of A can be well approximated by a power law.

Next, we relate our firm-level measure of innovation to firm characteristics, in particular Tobin's Q, firm size, K, and R&D expenditures to total assets

$$A_{ft} = a_0 + a_1 \log Q_{t-1} + a_2 \log K_{t-1} + a_3 \log RD_{t-1} + \rho A_{ft-1} + u_{ft}. \tag{22}$$

We estimate equation (22) using the entire sample of Compustat firms from 1950 to 2010 using a Tobit model.<sup>22</sup> We include industry dummies to account for industry-level time invariant characteristics; and time dummies to account for changing state of the business cycle as well as changes in patent law or changes in the efficiency and resources of the USPTO (see e.g. Griliches (1989)) during our sample period. We cluster the errors by firm.

We find that firms that are large, have higher Tobin's Q, and have higher R&D expenditures are more likely to innovate. These findings are similar to those discussed in Baumol (2002), Griliches (1990), Scherer (1965) and Scherer (1983) on the characteristics of firms that have conducted radical innovation and have been responsible for technical change in the U.S. See the Online Appendix (Table 4) for the full set of results.

#### Methodology

We begin by exploring the productivity and reallocation dynamics subsequent to innovative activity within an industry. In particular, we examine the response of productivity, Tobin's Q and factor demand to a firm's own innovation activity,  $A_f$ , and also to the innovation output of its competitors. We construct our measure of innovation of a firm's competitors,  $A_{If}$ , as the average innovative activity of all firms in the same industry excluding firm f,

<sup>&</sup>lt;sup>22</sup>Note that information on R&D expenditure is reliably reported in Compustat only from 1975 onwards. As a result our sample period for regressions that use R&D spending is restricted to 1975–2010.

weighted by market capitalization S:

$$A_{Ift} = \sum_{h \in J_{It} \setminus \{f\}} A_{ht}^v / \sum_{h \in J_{It} \setminus \{f\}} S_{ht}, \tag{23}$$

where  $J_{It}$  denotes the set of firms in industry I, defined according to 3-digit SIC codes.<sup>23</sup> We explore the effect of innovation of a firm and its competitors on various firm outcome variables, x, by estimating the regression

$$x_{ft+1} = a_0 + a_1 A_{ft} + a_2 A_{Ift} + b Z_{ft} + u_{ft+1}. (24)$$

We include a vector of controls Z that includes lags of the dependent variable; industry fixed effects; year fixed effects; firm idiosyncratic volatility  $\sigma_{ft}$  to account for its possible effect on our innovation measure; and firm and industry stock returns, to control for the possibility that our innovation measure is inadvertently capturing changes in valuations unrelated to innovation. In addition, we control for a number of firm characteristics that may cause the dependent variable while being correlated with our innovation measure. Hence, we include controls for firm size and Tobin's Q, since large firms and growth firms innovate more; and firm profitability, since firms experiencing a shock to profitability – for instance due to a positive demand shock to their product – may have higher propensity to innovate. We present results with and without these controls, and cluster the standard errors by firm.

We are interested in the estimates of  $a_1$  and  $a_2$ , which capture the impact of innovation by the firm and its competitors. A firm's innovative output,  $A_f$ , is highly skewed so we focus on inter-decile movements in firm-level innovation to explore the economic magnitude of  $a_1$ . Our prior is that the coefficient  $a_1$  is positive, since increased innovation should have a positive effect on firm outcomes. In contrast, the coefficient  $a_2$  can be either positive or negative, depending on whether the innovation of other firms has a positive or a negative effect on a firm's outcome variables. An increase in the innovative output of competing firms can have a positive effect on the firm because of knowledge spill-overs. However, innovation of competitors can also have a negative effect due to business stealing or an increase in factor prices. We should note that the presence of unobserved variables that drive the common propensity of firms to innovate are likely to bias our estimate  $a_2$  upwards. For instance, common productivity shocks could impact many firms in the same industry – thereby creating a positive correlation between innovative activity of a firm's competitors and a firm's own productivity.

 $<sup>^{23}</sup>$ We obtain quantitatively similar results when we define industries according to their 4-digit SIC.

#### **Productivity**

First, we examine whether firms have higher productivity subsequent to innovative activity. We consider both capital- and labor-productivity ( $z_{ft}^k$  and  $z_{ft}^l$ ), defined as the log ratio of firm output – total sales plus change in inventories – divided by capital or number of employees, respectively.<sup>24</sup> We evaluate the relation between subsequent productivity of capital and labor and innovation by a firm  $A_f$  or its competitors  $A_I$  by estimating (24) with  $x_{ft} = [z_{ft}^k, z_{ft}^l]$ . Depending on whether we focus on the productivity of capital or labor, we measure firm size as the stock of physical capital or number of employees respectively to ensure that our effects are not driven by differences in the denominator of the dependent variable.

We report the results in Panel A of Table 6. We find a substantial increase in firmlevel productivity subsequent to an innovation. Our estimates of  $a_1$  imply that an increase in innovation by the firm from the 50th to the 90th percentile leads to an 0.7% to 1.3% increase in the productivity of capital and a 1.7% to 2.1% increase in the productivity of labor. Furthermore, we find some evidence that the business-stealing effect dominates, as the estimated coefficient  $a_2$  is negative and statistically significant across specifications. In particular, a one-standard deviation increase in the amount of innovation by the firm's competitors is associated with a 1% to 1.7% decline in the productivity of capital and a 1.1-1.7% decline in the productivity of labor.<sup>25</sup>

Our estimates imply that the business-stealing effect is substantial. However, this finding may be an artifact of the short horizon considered in our analysis if the business-stealing effect and positive spillovers operate at different frequencies. In particular, positive spillovers may affect firms with a lag, so in the medium run, the response of productivity may be different. To explore this possibility, we estimate a dynamic version of equation (24) with k-year ahead productivity  $x_{ft+k}$  as the regressand. We consider horizons of one to five years k = [1..5]. To conserve space, we present results with only size, lagged productivity and volatility controls. Including additional controls leads to quantitatively similar findings.

As we see in Figure 4, the negative effect of competitor innovation,  $A_{If}$ , on productivity is stronger in the short run. As we increase the horizon k, the estimated coefficients  $a_2(k)$  increase, becoming zero or positive after 5 years. In contrast, the positive effect of firm innovation on productivity increases with the horizon k. After 5 years, the response of productivity of capital is between 37 to 50 percent higher than on impact. Labor productivity displays a similar, though quantitatively stronger response. The positive effect of firm innovation on labor productivity increases with the horizon by 65 percent.

In summary, our findings are consistent with the view that positive spillovers and business stealing operate at different horizons. In the short run, firms that do not innovate when

<sup>&</sup>lt;sup>24</sup>As is often the case, our measures of firm productivity may partly reflect changes in output prices.

<sup>&</sup>lt;sup>25</sup>We also explore the additional information contained in our innovation measure relative to using the number of patents that were granted to the firm in year t; the number of citation-weighted patents; and our raw stock market reaction  $\overline{A}$  in the Online Appendix (Table 9).

their competitors do experience a decline in their productivity. However, in the medium run, the innovation of other competitors has either a zero or a positive effect. This positive effect can arise because competitor innovations affect the firm either directly, for instance through knowledge spillovers, or indirectly, by spurring future firm innovation. Last, another possibility, which we explore below, is that the firm scales down operations in response to innovation by competitors and therefore operates at a higher marginal product of capital and labor.

#### Tobin's Q

Next, we explore the effect of innovation on the firm's average Tobin's Q. We estimate equation (24) with  $x_{ft+1} = [\log Q_{ft}]$ , so that Tobin's Q enters contemporaneously with our innovation measure. We present the results in Panel B of Table 6.

We find that Tobin's Q is positively related to the firm's own innovation activity, provided we control for its own stock return during the period. Our estimate of  $a_1$  implies that an increase in innovation by the firm from the 50th to the 90th percentile leads to an 0.7% increase in the firm's Tobin's Q. These magnitudes are in line with those reported in Hall et al. (2005). In addition, a one standard deviation increase in the innovation activity of other firms in the industry is associated with a 0.7% to 2.1% decline in Tobin's Q, again consistent with business stealing.

#### Reallocation

In this section we explore the reallocation dynamics subsequent to innovation by a firm. In particular, we explore how our innovation measures are related to reallocation of physical capital and labor. We focus on the firm's investment and hiring rate. In addition, since adjusting a firm's capital and labor input often involves upfront costs, we explore the allocation of financial resources. We focus on the net financial inflows to the firm, defined as new issuance of equity and debt minus payouts to stock- and bond-holders.

We estimate equation (24), using firm investment, i, net hiring rate, h, and net financial inflows, b, as outcome variables  $x_{ft} = [i_{ft}, h_{ft}, b_{ft}]$ . As before, our main estimates of interest are  $a_1$  and  $a_2$ , which capture the change in factor inputs and financial inflows following innovation by the firm and its competitors, respectively.

In Panel A of Table 7 we examine how physical capital gets reallocated subsequent to innovation by a firm or by its competitors. Subsequent to an innovation by a firm, there is a substantial increase in its investment rate – defined as capital expenditures divided by physical capital. In particular, our estimates imply that an increase in innovation by the firm from the 50th to the 90th percentile leads to an increase in the firm's investment rate by 0.5% to 0.7%. This increase is statistically but also economically significant given that the median firm investment rate is 11 percent in our sample. Furthermore, we find evidence

that new capital flows more towards firms that innovate than towards those that do not. Specifically, if the firm does not innovate but its competitors do, then its investment rate is substantially lower. A one-standard deviation increase in the level of innovation by the firm's competitors leads to a decline in the firm's investment rate of 0.8-1.4%.

Next, we examine the reallocation of labor. Panel B of Table 7 shows that subsequent to an innovation by a firm, there is a substantial increase in its employment. As before, the economic magnitudes are significant. Our estimates imply that an increase in innovation by the firm from the 50th to the 90th percentile leads to an increase in employment by 0.2% to 0.5%, compared to the median firm-level hiring rate of 2.7%. In addition, labor declines when a firm does not innovate but its competitors in the same industry do. A one-standard deviation increase in the average innovation of the firm's competitors leads to a reduction of 0.7% to 1.2% in the firm's hiring rate.

Last, we examine the reallocation of net financial inflows – defined as net security issuance minus net payout divided by book assets – subsequent to innovation by a firm. We present the results in Panel C of Table 7. Following an innovation by a firm, there is a substantial increase in its financial inflows. Our estimates imply that an increase in innovation by a firm from the 50th to the 90th percentile leads to an increase of capital inflows to book assets of 0.3% to 0.6%, compared to the median level of zero capital flows. We also find that a firm is more likely to increase payout and decrease new issuance when it does not innovate but its competitors do. In particular, a one-standard deviation increase in the average innovation of the firm's competitors is associated with a reduction of up to 0.3% in net financial capital flows to the firm, though the effect is not statistically significant across specifications.

In summary, our results in this section suggest that, consistent with economic optimization, resources are reallocated to innovating firms and away from firms that fail to innovate when their competitors do. In addition, we find that relative to their median value, new hiring exhibits a quantitatively stronger response than capital, both in terms of inflow and outflow. This increased reallocation response of labor relative to firm capital within industries is consistent with the view that capital is more firm-specific than labor.

#### Output growth

The results of the previous sections imply that innovation is followed by increased productivity of capital and labor, as well as reallocation of resources towards innovating firms. These findings suggest that own innovation should be followed by increased output growth. In contrast, the long-run response of output to innovation by other firms is ambiguous. It depends on whether productivity increases in the long run, as well as whether the patterns of reallocation we document are reversed in the long run. To answer these questions, we estimate the dynamic response of output – measured as firm sales plus change in inventories –

to the firm's own innovation  $A_f$  and innovation by its competitors  $A_{If}$ 

$$\log y_{ft+k} = a_0 + a_1 A_{ft} + a_2 A_{Ift} + b Z_{ft} + u_{ft+k}. \tag{25}$$

Our vector of controls includes firm and industry stock returns; firm idiosyncratic volatility; firm size (capital); two lags of the dependent variable; industry and time fixed effects. We cluster the standard errors by firm. We again examine horizons of k = 1 to k = 5 years. We plot the estimated coefficients  $a_1(k)$  and  $a_2(k)$  in Panels (a) and (b) of Figure 5, along with 90 percent confidence intervals.

We find that firm output displays a positive and statistically significant response to an own-innovation shock. A firm that experiences an innovation shock from the median to the 90th percentile experiences a 1.5% increase in output over a period of 5 years. In contrast, a positive one-standard-deviation shock to innovation by other firms in the same industry is associated with a decline in output by 2.5% to 3.5%. Here, we should note that since we do not have access to firm-level price data, we cannot distinguish an increase in market share from an increase in the quantity of output.

#### Comparison to other measures

Here, we explore the additional information contained in our innovation measure relative to using the number of patents that were granted to the firm in year t; the number of citation-weighted patents; and our raw stock market reaction  $\overline{A}$ . For brevity, we summarize the results here and refer the reader to the Online Appendix (Tables 6-8) for more details.

First, we measure innovation  $A_{ft}$  as the number of patents granted to firm f in year t, and construct  $A_{Ift}$  as the average number of patents granted to the firm's competitors in the same year. We estimate equation (24) for capital and labor productivity; investment; labor hiring; and financial flows. We find qualitatively similar results as our innovation measure, but the magnitudes are smaller by a factor of 2 to 3. Second, we repeat the same exercise replacing patent counts with citation-weighted counts. In contrast to our measure, citations contain information not available to economic actors at the time that production and allocation decisions are made. In this case, our results are qualitatively similar, slightly stronger than using patents alone but smaller in magnitude by a factor of 2 compared to our benchmark measure. Third, we repeat this exercise using the raw stock market reaction A. In this case our results are mostly qualitatively similar, though not always statistically significant across specifications. Furthermore, the economic magnitudes are smaller than our baseline results by a factor of 5. This provides further evidence that the raw stock market reaction contains significant noise and that our identification assumption in equation (11) - that the value of a patent x is positive - improves upon the raw measure by parsing out information contained in returns that are unrelated to the value of the patent.

## III.B Industry-level evidence

So far we have focused on the dynamics of productivity and reallocation within an industry. We now conduct a similar exercise examining the response of productivity and reallocation of inputs at the sector level. To do so, we use the KLEMS industry-level output data provided by Dale Jorgenson. First, we document the dynamic response of capital and labor productivity, defined as the ratio of the quantity of output to the quantity of capital and labor services, respectively. Second, we focus on the reallocation of inputs, namely the growth rate in the quantity of capital and labor services. Last, we relate the rate of establishment exit to our innovation measures, using information on establishment exit rates at the industry level from the US Census tables on Business Dynamics Statistics (BDS).

#### Construction of industry measures of innovation

We construct industry-level measures of innovation by aggregating our firm-level dollar measures of innovation across the set  $J_{It}$  of firms in industry I

$$A_{It}^{v} = \sum_{f \in J_{It}} A_{ft}^{v}.$$
 (26)

Our dollar measure  $A^v$  will be mechanically affected by economic forces that affect the level of stock prices but are likely to be unrelated to innovation, such as disembodied productivity shocks or changes in discount rates. Hence, following equation (8), we scale our dollar measure  $A_I^v$  by the total market capitalization of the industry  $S_I$ 

$$A_{It} = \frac{A_{It}^v}{S_{It}},\tag{27}$$

where  $S_t = \sum_{f \in J_{It}} S_{ft}$ . Thus, our industry-level measure,  $A_{It}$ , is the value-weighted average of our firm-level innovation measure  $A_{ft}$  across all firms in the industry.

#### Methodology

We estimate specifications similar to (24), but at the industry level:

$$x_{It+1} = a_0 + a_1 A_{It} + a_2 A_{MIt} + b Z_t + u_{It+1}. (28)$$

Here,  $A_I$  is our measure of innovation at the industry, and  $A_{MI}$  is the average level of innovation in the economy, excluding industry I constructed in a manner similar to (23). In analogy to the firm-level regressions, we include a vector of controls Z which includes: industry stock returns; the average idiosyncratic volatility in the industry; time effects; and lagged values of the dependent variable. In the presence of time dummies, the interpretation

of the coefficient  $a_2$  is unclear, so we only include one of the two. We cluster the standard errors by industry.

## **Productivity**

First, we explore the dynamic response of industry productivity to its own innovation  $A_I$  and the innovation of the other industries  $A_{MI}$ . We are interested in the coefficients  $a_1$  and  $a_2$ , which measure the response of productivity to an industry and economy-wide (excluding the given industry) innovation shock respectively. The coefficient  $a_1$  is informative as to whether innovation creates net value or is a zero-sum game that merely affects the distribution of rents within an industry. We estimate (28) with k-period ahead productivity as the regressand,  $x_{ft+1} = [\log z_{ft+k}^k, \log z_{ft+k}^l]$ . We consider horizons of one to five years k = [1..5]. We plot the results in Figure 6, controlling for lagged productivity and volatility. Controlling for firm- or industry-level stock returns leads to similar results.

We find that both labor and capital productivity increase in response to own industry innovation. A one-standard-deviation  $A_I$  shock is associated with a 2.5% increase in the productivity of capital and labor, after a period of 5 years. By contrast, capital and labor productivity show no statistically significant response to the innovation activity of other industries.

#### Reallocation and creative destruction

Next, we examine the response of capital and labor to an industry innovation shock, as well as to the innovation of other industries. We estimate equation (28), using as the outcome variable the growth rate in the quantity of capital and labor services  $x_{It} = [i_{It}, h_{It}]$ . As before, the main estimates of interest in this specification are  $a_1$  and  $a_2$ , which capture the change in the quantity of factor inputs in response to innovation in the industry and the rest of the economy respectively. We show our results in Table 8.

We find that an increase in the amount of industry innovation increases the quantity of capital and labor services used by the industry, though in some specifications the effect is not statistically different from zero. As before, we find that the response of labor is greater than the response of capital. An increase in industry innovation is associated with a 0.2% to 0.4% increase in capital services and a 0.3% to 0.7% increase in labor services. These magnitudes are economically significant, given that the median annual growth rate in capital and labor services equals 3.1% and 0.7% respectively.

Our results suggest that increases in economy-wide innovation lead to cross-industry reallocation of labor and capital. In particular, a one-standard-deviation increase in the economy-wide innovation measure is associated with a 0.5% to 1.0% decline in the growth of capital services and a 1.4% to 2.2% decline in the growth of labor services.

Next, we examine patterns of firm turnover at the industry level. Our measure captures the innovation of existing firms, since we do not observe the firm's innovation activity prior to entry. Hence, we relate firm exit to innovation by incumbent firms. If industry innovation spurs creative destruction, we expect to find a positive relation between the rate of firm exit and the level of industry innovation. We estimate specifications similar to (28), but we replace the outcome variable with the rate of firm exit and examine the response of this variable to own industry innovation  $A_I$  and innovation of other industries  $A_{MI}$ . Table 9 presents the results.

Industry innovation is accompanied by an increase in firm exit. The estimated coefficient  $a_1$  is positive and statistically significant across specifications. Innovation accounts for an economically significant fraction of the variation in firm exit rates. A one standard deviation increase in industry innovation is associated with an increase in the firm exit rate by 0.2% to 0.4%, while the unconditional volatility of exit rates is equal to 2.1%. Economy-wide innovation  $A_{MI}$  has no statistically significant effect on firm exit.

#### Output growth

Last, we explore the dynamic response of the quantity of industry output to industry innovation  $A_I$  and innovation of other industries  $A_{IM}$ , by estimating a specification similar to (25)

$$\log y_{It+k} = a_0 + a_1 A_{It} + a_2 A_{MIt} + b Z_{It} + u_{It+k}, \tag{29}$$

where our vector of controls Z includes industry stock returns; the cross-sectional average idiosyncratic volatility; and two lags of the dependent variable. We again examine horizons of k = 1 to k = 5 years. We plot the estimated coefficients  $a_1(k)$  and  $a_2(k)$  in Panels (c) and (d) of Figure 7, along with 90 percent confidence intervals.

Innovation is associated with substantial subsequent increases in output. In particular, the response of output at the industry level is qualitatively similar to the firm-level responses, though the magnitudes are stronger. A one standard deviation shock to industry innovation is associated with a 5 percent output growth over a period of 5 years. In contrast, a positive innovation by other industries, is associated with a 3.5% to 6.8% decline in output. In contrast to our firm-level output results, industry output is deflated by price, hence our results correspond to real increases in output rather than market share.

The results of this section can be summarized by examining the relation between industry innovation in the first half of the sample (1960–1982) and subsequent output growth in the second half of the sample (1983–2006). In Figure 8 we plot the industry innovation measure  $A_I$  averaged over the first half of the sample (1960–1982) on the X axis and the corresponding output growth of the industry in the second half of the sample (1983–2006) on the Y axis.

The correlation between the two series is 41 percent with a robust t-statistic of 2.6. Industries which experienced high technological innovation in the first half of the sample were also the ones whose growth rate was subsequently higher in the second half of the sample. For example, industries such as Electrical Machinery, Automotive and Communication, which are in the highest quartile of innovation during the first half of the sample, had an annualized growth rate of more than 4 percent over the second part of the sample. Similar correlation is found for low-innovative industries such as Textile and Utilities.<sup>26</sup>

# IV Innovation and aggregate dynamics

Our results in the previous section show that innovation is positively related to subsequent changes in industry-level productivity and output growth, especially in the medium term. In this section, we analyze the effect of innovation at the level of the U.S. economy.

# IV.A Construction of aggregate measures of innovation

We construct economy-wide measures of innovation by aggregating our firm-level measure across the set  $J_t$  of firms across the entire economy

$$A_t^v = \sum_{f \in J_t} A_{ft}^v. \tag{30}$$

As before, we scale our dollar measure  $A^{v}$  by the total market capitalization

$$A_t = \frac{A_t^v}{S_t},\tag{31}$$

where  $S_t = \sum_{f \in J_t} S_{ft}$  is the total market capitalization of all firms in our sample.

Examining the composition of our aggregate innovation measure A, we find that a few large firms account for a significant fraction of the aggregate rate of innovation in the economy. The identity of these firms varies by decade. In the 1930s and 1940s, AT&T and GM are responsible for a large share of innovative activity. In the 1950s and 1960s, du Pont and Kodak take a leading role. In 1970s and 1980s, a large share of innovation takes place in Exxon, GE, 3M and IBM. Finally, in the 1990s and 2000s, "new economy" firms are responsible for a large share of innovation, namely Sun, Oracle, Microsoft, Intel, Cisco, Dell, and Apple.

 $<sup>^{26}</sup>$ One source of concern with our analysis could be that the relation between innovation and output growth is driven by omitted variables. To alleviate these concerns we generate exogenous changes in R&D activity across industries by employing the Bloom et al. (2010) instrument for firm-level R&D activity. As discussed in Bloom et al. (2010), the firm-level tax price of R&D can be decomposed into a component that is relatively exogenous since it is based solely on federal rules. In unreported tests we use the Bloom et al. (2010) firm-level R&D instrument and construct its industry counterpart by taking the average of this tax price across firms in a given industry. We find qualitatively similar results to those reported in the table when we instrument the endogenous innovation variable (A).

We compare our measure of aggregate innovation with three aggregate measures proposed in the literature: the log number of total patents granted; the log R&D expenditures from the BEA; and the log number of technology books published from Alexopoulos (2011). Some of these measures show a secular time trend, so we remove a deterministic time-trend from all measures. We plot these series in Figure 3.

Our measure of innovative activity lines up well with the three major waves of technological innovation in the U.S. First, our measure suggests high values of technological innovation in the 1930s, consistent with the views expressed in Field (2003). When we dissect our measures we find that firms that primarily contribute to technological developments during the thirties are in the automobiles (such as General Motors) and telecommunication (such as AT&T) sectors. This description is consistent with studies that have examined which sectors and firms led to technological developments and progress in the 1930s (Smiley, 1994).

Second, our measure suggests higher innovative activity during 1960s and early 1970s – a period commonly recognized as a period of high innovation in the U.S (see Laitner and Stolyarov (2003)). As has been noted, this was a period that saw development in chemicals, oil and computing/electronics – the same sectors we find to be contributing the most to our measure with major innovators being firms such as IBM, GE, 3M, Exxon, Eastman Kodak, du Pont and Xerox.

Third, developments in computing and telecommunication have brought about the latest wave of technological progress in the 1990s and 2000s, which coincides with the high values of our measure. In particular, it is argued that this is a period when innovations in telecommunications and computer networking spawned a vast computer hardware and software industry and revolutionized the way many industries operate. We find that firms that are main contributors to our measure belong to these sectors with firms such as Sun Microsystems, Oracle, EMC, Dell, Intel, IBM, AT&T, Cisco, Microsoft and Apple being the leaders of the pack. We next turn to providing firm level evidence that lends additional support to validity of our measures.

Comparing the aggregate innovation series, we note three important points. First, our measure displays different behavior than the total number of patents, especially in the beginning and towards the end of the sample. The correlation between  $A_t$  and the log number of patents is equal to 0.42 in levels and 0.11 in first differences. Second, our innovation measure captures similar low-frequency movements to R&D spending and the number of technology books published in the Library of Congress, in particular the rise in innovative activity during the 1960s and early 1970s. Finally, our innovation measure displays substantial high-frequency variability relative to either the stock of R&D or the number of technology books. Some of this variability comes from variation in the number of patents granted, but a significant part comes from changes in the average response of the stock market on these

patent grant dates. In contrast, the stock of R&D capital and the number of technology books display mostly low-frequency variation.

#### IV.B Evidence

In this section, we examine the extent to which our innovation measures account for shortand medium-run fluctuations in aggregate economic quantities. We start by exploring the relation between measures of innovation and quantities of interest using VARs and VECMs. Then, we explore whether our results are sensitive to the details of the specification.

#### Methodology

We estimate bivariate VARs of the form  $Z = [\log X, \log A]'$ , where X is our variable of interest and A is our measure of innovation. In addition, we also compute responses using a vector-error-correction model (VECM), including a deterministic trend. The number of cointegrating relations are selected using the Johansen test, which suggests the presence of one cointegrating relation in all systems. The number of lags are selected using the Akaike-Information Criterion, which advocates a lag length of one to two years for each of the systems. We plot the impulse-response functions in Figures 9 and 10, along with 90 percent confidence intervals. Standard errors are computed by a bootstrap simulation of 500 samples. The impulse responses are computed by ordering the innovation shock A last, so the technology shock affects the variables of interest only with a lag.

#### Total Factor Productivity and Output

First, we focus on aggregate productivity and output, with productivity measured using utilization-adjusted TFP from Basu et al. (2006) and output measured as the real per capita gross domestic product. We find that TFP increases by 1 to 2 percent over 8 years following a one-standard deviation increase in innovation output, depending on whether we use the VAR or the VECM specification. The forecast error variance attributed to our innovation measure ranges from 36 to 70 percent at the 8-year horizon, depending on the specification. Our findings are comparable to the results in Alexopoulos (2011), but in contrast to Shea (1999) who uses only information on patents and finds a negative relation.

Aggregate output displays a delayed positive response. In the first two years, the response of output to a one-standard deviation shock is slightly negative at -0.2% but statistically insignificant. However, output increases in the long run by a substantial amount: a one-standard deviation innovation shock results in a net 2.5% to 4.2% increase in aggregate output after 8 years. The share of 8-year forecast-error variance attributed to our innovation measure ranges from 5 to 13 percent .

We perform several robustness tests. For brevity, we summarize the results here and refer the reader to the Online Appendix for the full set of results. First, we include the cross-sectional average of idiosyncratic volatility  $\bar{\sigma}$  to ensure that our innovation measure does not pick up movements in firm-level volatility. We order volatility second, so now  $Z = [\log X, \log \sigma, \log A]'$ . The magnitudes of the impulse responses are similar in this specification (see Figure 3 in the Online Appendix).

Second, we explore whether our measure of innovation contains incremental information to stock prices. Following Beaudry and Portier (2006), we include the level of the stock market in our VAR, scaled by the consumption deflator and population.<sup>27</sup> This helps us evaluate the extent to which our results are driven by variation in the denominator of A (the stock market capitalization). We order the level of stock prices second, so now  $Z = [\log X, \log M, \log A]'$ . Our results are qualitatively similar in terms of statistical significance, but the economic magnitudes are somewhat smaller for TFP (see Figure 4 in the Online Appendix). Productivity and output increase by 0.5 and 2.6% respectively at the peak following a one-standard deviation shock in our technological innovation measure. In contrast, the response of output to a one-standard deviation shock in  $\log M$  is not statistically significant beyond the one-year horizon. Furthermore, the innovation shock accounts for a comparable fraction of the variance of productivity (13.9%) and output (10.5%) relative to the stock market shock (13.4% and 4%, respectively). Hence, our innovation shock contains incremental information about future productivity and output to the level of the stock market.

Last, we repeat the analysis using k-period OLS regressions of T-period ahead growth rates of output and TFP on first differences in our innovation measure. Doing so verifies that our findings are not driven by specification of the VAR/VECM. We find similar results: an increase in innovation has a permanent positive effect on the level of TFP. In the short run, output exhibits slightly negative response, and it increases in the long run (see Table 10 in the Online Appendix).

#### Comparison to number of patents and R&D spending

We also explore whether our measure of innovation contributes information relative to other commonly employed measures of technological innovation: R&D spending, and the log number of patents. We estimate bivariate VARs for productivity and output, with the log number of patents or R&D spending series ordered last. The number of patents has some ability to predict TFP, but the results are quantitatively weaker. A one-standard deviation shock to the log number of patents is associated with a 0.4% increase in TFP, and the patent shock accounts for 13.1% of the forecast error variance. Output shows no statistically significant response to number of patents. In contrast, R&D Expenditure has some ability to predict

<sup>&</sup>lt;sup>27</sup>We depart from Beaudry and Portier (2006) in that we include the level of the CRSP value-weighted rather the level of the S&P 500 index, since the former includes all stocks traded on the three major exchanges.

output, but not productivity. Output drops in the short run by 0.4%. At the eight-year horizon output displays a statistically significant increase of 0.3%.<sup>28</sup>

## Consumption

Next, we analyze the impulse response of aggregate consumption to our innovation measure. The response of consumption is informative about whether our innovation measure is an example of an embodied or disembodied shock. If technological innovation represents a disembodied shock, we expect that consumption should increase immediately. Due to the positive wealth effect, agents anticipating an increase in future consumption would like to increase their consumption today. In contrast, if innovation is embodied in new vintages of capital, then consumption may only increase in the long run. In the short run, agents will divert resources away from consumption towards adopting new innovations.

We analyze the response of real per capita consumption of non-durables and services using VARs and VECMs, as in Section IV.B. We plot the impulse-response functions in Figure 11, along with 90 percent confidence intervals. We find that consumption displays a U-shaped response to innovation. In the first two years consumption displays a statistically significant drop of 0.5% to 0.6%. Subsequently, consumption increases, leading to a 0.3% to 0.6% net increase after 8 years. The innovation shock accounts for 5 to 7 percent of the forecast-error variance of consumption growth after 8 years.

The short-run decline in consumption is consistent with the delayed response of output in Section IV.B. Innovation affects output with a lag, so the positive response of consumption is necessarily delayed. This evidence suggests that our innovation measure at least partially captures an embodied – rather than a disembodied – technology shock.

#### Innovation and Tobin's Q

We conclude our analysis by examining the relationship between our measures of innovation and Tobin's Q at the aggregate level. The theoretical relation between innovation and Tobin's Q is ambiguous. If innovation represents an increase in TFP that costlessly affects all firms – a disembodied shock – then standard models will imply that average Tobin's Q should rise (see, e.g. Hayashi (1982)). However, it is also possible that innovation renders part of the capital stock obsolete (see e.g. Laitner and Stolyarov (2003)) or a reduction in profits for incumbent firms (e.g. Greenwood and Jovanovic (1999); Hobijn and Jovanovic (2001); Garleanu, Kogan, and Panageas (2012)). In these cases technological innovation represents

<sup>&</sup>lt;sup>28</sup>We also explore if our measure of innovation is predictable by output or productivity. If the measure captures fundamental shocks we expect to find limited evidence of predictability. In addition, we explore whether our measure of innovation is predictable by other measures of technological growth in the literature, for instance the book-based measures of Alexopoulos (2011) and the stock of R&D capital. In unreported tests we find that output and TFP do not Granger-cause our measure of innovation. Further, our measure of innovation is distinct from the measures of Alexopoulos (2011), in that neither causes the other. Finally, our measure is also not Granger-caused by either the number of patents or R&D spending.

an embodied shock, and thus the relationship between innovation and average Tobin's Q could be negative.

We estimate the contemporaneous response of Tobin's Q to our innovation measures

$$\Delta \log Q_t = a + b \Delta \log A_t + c Z_t + u_t, \tag{32}$$

where the vector of controls includes lagged values of Q, our innovation measure A and changes in the cross-sectional average of idiosyncratic volatility,  $\Delta \log \overline{\sigma}$ .

We show the results in Panel A of Table 10. We find that our innovation measure is negatively correlated with average Q. This negative correlation is statistically and economically significant. A one standard deviation increase in innovation is associated with a 8.1% to 12% contemporaneous drop in aggregate Tobin's Q. Our findings echo the stylized facts reported in Greenwood and Jovanovic (1999), Hobijn and Jovanovic (2001) and Laitner and Stolyarov (2003), who argue that Tobin's Q was too low in the 1960s and 1970s, despite the technological advances taking place.

One source of concern is that our aggregate innovation measure A may be mechanically negatively related to average Q due to our choice of scaling by the market capitalization of all firms S. As a robustness test, we scale our aggregate innovation measure by the market capitalization of innovating firms,  $S_{It} = \sum_{f \in N_t} S_{ft} 1_{A_{ft} > 0}$ . Thus, this alternative normalization ameliorates somewhat the concern that this finding is mechanical. As we show in Panel B of Table 10, we obtain similar results using this alternative normalization.

# V Conclusion

We explore the role of technological innovation as a source of economic growth by constructing direct measures of innovation at the micro level. We combine patent data for US firms from 1926 to 2010 with the stock market response to news about patents to identify the economic importance of each innovation. Our measure allows us to uniquely identify the reallocation and growth dynamics within- and across industry after bursts of innovative activity.

We document a strong link between innovation and productivity at the firm and industry level. Our evidence suggests that innovation is accompanied by creative destruction in the form of resource reallocation – both within and between sectors – as well as firm exit. Resources flow to innovating firms and sectors, away from firms and sectors that do not innovate. There are stronger patterns of reallocation for labor than for capital, consistent with the view that capital is more specific than labor (Ramey and Shapiro, 2001).

Technological innovation is significantly related to movements in aggregate measured TFP. In addition, several of the relations between our innovation measure and aggregate variables are consistent with this innovation measure representing an embodied technological shock. In particular, our innovation measure has a delayed positive effect on aggregate output and a

U-shaped effect on consumption growth. This pattern is typical of models with embodied technology shocks (see, e.g. Papanikolaou, 2011), as resources get reallocated away from consumption in the short run towards the implementation of innovation. Finally, we find that an increase in innovative activity leads to a fall in aggregate Tobin's Q, as in the models of Greenwood and Jovanovic (1999), Laitner and Stolyarov (2003), and Garleanu et al. (2012).

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## **Tables**

Table 1: Stock turnover around patent announcement days

Event	k = -1	k = 0	k = 1	k = 2	k = 3	k=4				
		I. Turnover								
A. Patent grant	-0.147	-0.008	0.0502	0.0588	0.0487	-0.074				
	(-5.27)	(-0.68)	(3.63)	(3.22)	(1.78)	(-4.65)				
B. Patent publication	0.152	0.255	-0.194	-0.385	0.114	-0.205				
	(4.02)	(5.51)	(-3.03)	(-4.17)	(3.08)	(-3.07)				
		II	. Relative	e turnove	r					
A. Patent grant	-0.156	-0.006	0.055	0.061	0.047	-0.091				
	(-6.74)	(-0.57)	(5.19)	(4.24)	(3.76)	(-6.71)				
B. Patent publication	0.130	0.182	-0.015	-0.335	0.085	-0.191				
	(4.33)	(7.25)	(-0.37)	(-8.41)	(2.73)	(-5.75)				

Table shows the output of the regression of share turnover  $(x_{t+k} = vol_t/shrout_t)$  in Section I and share turnover relative to the market average  $(vol/shrout - \overline{vol/shrout})$  in Section II on a dummy variable taking the value 1 if a patent was granted to the firm on day t (Panel A), or the USPTO publicized the grant application of the firm on day t (Panel B). Each column in the two panels represents a regression. We include firm-year and day-of-week fixed effects. We cluster standard errors by year and report t-statistics in parenthesis. We restrict the sample to firms that have been granted at least one patent.

Table 2: Distributions of event returns (3-day) and innovation measure

Moment	P	N	$r_f$	$E[x_j r_f]$	Â
					(\$m, 1982)
Mean	12.6	10.2	0.15	0.46	7.9
Std. Dev.	18.8	20.1	5.41	0.28	23.0
Percentiles					
1%	1	0	-9.60	0.17	0.01
5%	1	0	-5.05	0.22	0.03
10%	1	0	-3.51	0.26	0.08
25%	2	1	-1.65	0.31	0.50
50%	6	5	0.07	0.39	2.20
75%	15	11	1.67	0.59	7.23
90%	33	24	3.92	0.73	17.07
95%	50	38	5.89	1.11	29.31
99%	88	90	12.05	1.71	89.47

Table reports the distribution at the patent level of the following variables: the number of patents granted to the same firm per day P; the number of citations N; the market-adjusted firm returns  $r_f$  on the 3-day window of patent grant dates; the filtered component of returns  $E[x_j|r_f]$  related to innovation, using equation (13); and the filtered value of innovation  $A_j$  using equation (12).

Table 3: Number of future citations and filtered value of patent

		Gran	t Day		Publication Day			
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
$\log(1+N)$			I. Log nu	mber of cit	ations pl	us one		
$\log \hat{A}$	0.037	0.193	0.104	0.054	0.030	0.047	0.036	0.014
	(8.99)	(5.76)	(5.70)	(5.34)	(5.74)	(5.75)	(4.39)	(1.26)
$R^2$	0.289	0.296	0.401	0.426	0.245	0.250	0.318	0.355
Â	1.568	0.449	0.110	0.358	0.274	-0.632	-0.423	-0.195
	(8.49)	(2.12)	(1.85)	(4.42)	(1.74)	(-3.99)	(-2.01)	(-1.14)
$R^2$	0.285	0.293	0.400	0.426	0.240	0.249	0.318	0.355
$\overline{N}$			II.	Number of	citations			
$\log \hat{A}$	0.675	3.176	1.768	1.069	0.249	0.384	0.280	0.221
	(7.74)	(4.49)	(4.66)	(4.18)	(3.94)	(4.40)	(4.35)	(2.27)
$R^2$	0.097	0.104	0.221	0.262	0.105	0.109	0.186	0.233
Â	45.875	25.104	11.780	17.810	6.068	0.472	2.096	2.220
	(6.47)	(3.74)	(2.68)	(4.04)	(1.99)	(0.25)	(1.18)	(1.11)
$R^2$	0.095	0.103	0.221	0.26	0.100	0.107	0.184	0.232
Observations	1776458	1776458	1776458	1776458	405691	405691	405691	405691
Controls								
Volatility	_	Y	Y	Y	_	Y	Y	Y
Firm Size	_	Y	Y	Y	_	Y	Y	Y
# patents	_	Y	Y	Y	_	Y	Y	Y
granted same day								
Fixed Effects	Т	Т	TxC	TxC,F	T	Т	TxC	TxC,F

Table shows output of the regressions of number of future citations N on the filtered value of innovation A (see equation (12) in text), using the three day (t, t + 2) stock market reaction around the patent grant day (columns 1-4) or the day the application is publicized by the USPTO (columns 5-8). We construct the filtered dollar value of innovation A using equation (12), expressed in 1982 US dollars (billion). We report log-log, semi-log and linear specifications. Depending on the specification we include grant- or publication-year T fixed effects; firm F fixed effects; USPTO 3-digit technology classification C interacted with year T fixed effects; firm idiosyncratic volatility; firm size, measured as market capitalization; and the number of patents granted in the same day. We cluster standard errors by announcement year and report t-statistics in parenthesis.

Table 4: Number of future citations and announcement day return, raw dollar reaction

		Gran	t Day		Publication Day			
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
$\log(1+N)$			I. Log nu	mber of cit	ations pl	us one		
Ā	0.003	0.005	0.001	-0.002	0.003	0.008	0.005	0.003
	(0.17)	(0.30)	(0.13)	(-0.50)	(0.44)	(1.03)	(0.77)	(0.43)
$R^2$	0.284	0.293	0.400	0.426	0.242	0.248	0.318	0.356
$\overline{N}$			II.	Number of	citations			
Ā	0.129	0.165	0.090	0.085	0.068	0.103	0.098	0.082
	(0.32)	(0.44)	(0.38)	(0.43)	(0.33)	(0.49)	(0.47)	(0.39)
$R^2$	0.092	0.103	0.221	0.265	0.101	0.108	0.185	0.233
Observations	1776458	1776458	1776458	1776458	405691	405691	405691	405691
Controls								
Volatility	_	Y	Y	Y	_	Y	Y	Y
Size	_	Y	Y	Y	_	Y	Y	Y
# patents	_	Y	Y	Y	_	Y	Y	Y
granted same day								
Fixed Effects	$\Gamma$	${ m T}$	TxC	$_{\rm TxC,F}$	$\Gamma$	${ m T}$	TxC	$_{\rm TxC,F}$

Table shows output of the regressions of number of future citations N on the raw three day (t, t+2) stock market reaction around the patent grant day (columns 1-4) or the day the application is publicized by the USPTO (columns 5-8). We construct the dollar value of innovation  $\bar{A}$  using the raw stock market reaction multiplied by our estimate of  $\gamma$ , expressed in 1982 US dollars (billion). Since this measure takes negative values, we cannot run the log-log specification. We report the results from a linear specification. Depending on the specification we include grant- or publication-year T fixed effects; firm F fixed effects; USPTO 3-digit technology classification C interacted with year T fixed effects; firm idiosyncratic volatility; firm size, measured as market capitalization; and the number of patents granted in the same day. We cluster standard errors by announcement year and report t-statistics in parenthesis.

Table 5: Descriptive statistics on firm-level innovation variables

statistic	$\hat{A}_{ft}$	$\bar{A}_{ft}$	# Patents	# Cites
			(1000's)	(1000's)
Mean	0.044	0.000	0.007	0.072
St. Dev.	0.129	0.003	0.028	0.303
Percentiles				
5	0.000	-0.003	0.000	0.000
10	0.000	-0.001	0.000	0.000
25	0.000	0.000	0.000	0.000
50	0.000	0.000	0.000	0.000
75	0.027	0.000	0.001	0.009
90	0.149	0.001	0.010	0.109
95	0.289	0.003	0.031	0.327

Table presents descriptive statistics for our firm-level annual innovation measures  $\hat{A}$ ; the raw stock market reaction to patent grants  $\bar{A}$ , aggregated at the firm level, scaled by firm market capitalization; the number of patents granted to the firm that year; and the number of citations received by patents granted to the firm that year.

**Table 6:** Firm-level productivity and Tobin's Q

		I. Prod	uctivity			II. Tobin's Q		
$z_{t+1}^k, z_{t+1}^l$	1. Ca	apital	2. L	abor	$\mid q_t \mid$	11. 100m s Q		
	(1)	(2)	(3)	(4)		(5)	(6)	
$\hat{A}_{It}$	-0.087	-0.049	-0.084	-0.056	$\hat{A}_{It}$	-0.106	-0.037	
	(-6.27)	(-3.56)	(-6.72)	(-6.47)		(-8.83)	(-3.76)	
$\hat{A}_{ft}$	0.053	0.102	0.132	0.163	$\hat{A}_{ft}$	-0.014	0.057	
•	(3.70)	(7.02)	(10.41)	(12.58)		(-0.99)	(4.81)	
$R^2$	0.844	0.847	0.847	0.850	$R^2$	0.693	0.797	
Observations	125678	125678	120020	120020	Observations	123540	123540	
Controls					Controls			
Size, Lag	Y	Y	Y	Y	Size, Lag	Y	Y	
$R_f, R_I, q, \sigma$	_	Y	_	Y	$R, R_I, y/k, \sigma$	-	Y	
Fixed Effects	I,T	I,T	I,T	$_{\mathrm{I,T}}$	Fixed Effects	I,T	I,T	

Table shows output of regressing firm output-capital ratio  $z^k$  (Panel I.1), output-labor ratio  $z^l$  (Panel I.2) and Tobin's Q q (Panel II) on our firm-level measure of innovation  $A_f$  (see equation (21) in text) and the average level of innovation of other firms in the same 3-digit SIC industry  $A_{If}$  (see equation (23) in text). Depending on the specification, we control for lagged values of the dependent variable (Lag); firm size (log capital or number of employees); firm  $(R_f)$  and industry  $(R_I)$  stock returns; firm volatility  $(\sigma)$ ; and industry (I) or time (T) fixed effects. Standard errors are clustered by firm. All variables are winsorized by year at the 1% level.

Table 7: Firm-level reallocation

$\overline{i_{t+1}}$		I.	Investmen	nt	
	(1)	(2)	(3)	(4)	(5)
$\hat{A}_{It}$	-0.061	-0.060	-0.051	-0.036	-0.035
	(-12.27)	(-12.24)	(-13.52)	(-9.84)	(-9.48)
$\hat{A}_{ft}$	0.035	0.044	0.038	0.044	0.045
	(7.10)	(8.91)	(10.31)	(11.88)	(12.33)
$R^2$	0.085	0.093	0.221	0.260	0.261
$n_{t+1}$		II.	Labor hiri	ing	
	(1)	(2)	(3)	(4)	(5)
$\hat{A}_{It}$	-0.054	-0.054	-0.055	-0.035	-0.031
	(-7.65)	(-7.78)	(-8.18)	(-5.23)	(-4.78)
$\hat{A}_{ft}$	-0.007	0.002	0.012	0.018	0.021
	(-0.96)	(0.26)	(1.83)	(2.71)	(3.22)
$R^2$	0.039	0.044	0.053	0.086	0.088
$e_{t+1}$			nancial ir	nflows	
	(1)	(2)	(3)	(4)	(5)
$\hat{A}_{It}$	-0.015	-0.015	-0.015	-0.005	-0.015
	(-2.32)	(-2.36)	(-2.71)	(-0.86)	(-2.85)
$\hat{A}_{ft}$	0.045	0.038	0.035	0.033	0.019
	(6.03)	(5.21)	(5.53)	(5.03)	(3.09)
$R^2$	0.114	0.117	0.155	0.185	0.219
Observations	126727	126727	126727	126727	126727
Controls					
Size	Y	Y	Y	Y	Y
$\sigma_t$	-	Y	Y	Y	Y
$i_t/n_t/e_t$	-	-	Y	Y	Y
$R_{ft}, R_{It}, Q_t$	-	-	-	Y	Y
$ROA_t$	- T (T)	- T. (T)	- T. (T)	- T. (T)	Y
Fixed Effects	I,T	I,T	I,T	I,T	I,T

Table shows output of regressing firm investment (Panel I), change in number of employees (Panel II) and financial inflows (Panel III) on our firm-level measure of innovation  $A_f$  (see equation (21) in text) and the average level of innovation of other firms in the same 3-digit SIC industry  $A_{If}$  (see equation (23) in text). Depending on the specification, we control for lagged values of log Tobin's Q; firm size (log capital or number of employees); earnings to assets (ROA); firm  $(R_f)$  and industry  $(R_I)$  stock returns; firm volatility  $(\sigma)$ ; lagged values of the dependent variable; and industry (I) or time (T) fixed effects. Standard errors are clustered by firm. All variables are winsorized by year at the 1% level.

Table 8: Industry reallocation

$\overline{x_{t+1}}$	I. Quantity of capital services				II. Quantity of labor services			
$\hat{A}_{It}$	0.023	0.015	0.032	0.027	0.021	0.036	0.029	0.043
	(1.99)	(1.39)	(2.83)	(2.24)	(0.94)	(1.73)	(1.34)	(2.09)
$\hat{A}_{MIt}$	-0.153	-0.126			-0.263	-0.239		
	(-8.77)	(-4.31)			(-6.35)	(-5.49)		
$R^2$	0.048	0.094	0.164	0.184	0.033	0.072	0.163	0.183
Observations	1395	1395	1395	1395	1395	1395	1395	1395
Controls								
$R, \sigma, x_t$	_	Y	-	Y	_	Y	-	Y
Time Effects	_	-	Y	Y	-	-	Y	Y

Table reports results from a regression of the quantity [k,n] of capital and labor services on the amount of innovation at the industry level  $[A_I]$  – see equation 27 in the text – and on the amount of innovation of all other industries  $[A_{MI}]$ . We control for time effects (T); industry stock return  $R^I$ ; industry volatility  $\sigma^I$ ; and one lag of the dependent variable. Data is from Dale Jorgenson's 35-sector KLEM, described in Jorgenson and Stiroh (2000). Sample is 1960-2005 and covers 31 industries after excluding the finance, utilities and government enterprises sector. We report t-statistics in parenthesis, with standard errors clustered by industry.

Table 9: Innovation and Firm Exit

$\overline{x_{t+1}}$	Rate of establishment exit								
$\hat{A}_{It}$	1.313	1.322	2.227	2.171					
	(2.14)	(2.20)	(3.31)	(2.94)					
$\hat{A}_{MIt}$	-4.691	-4.745							
	(-1.32)	(-1.38)							
$R^2$	0.509	0.510	0.732	0.735					
Observations	231	231	231	231					
Controls									
$R, \sigma$	_	Y	-	Y					
Time Effects	-	-	Y	Y					

Table reports results from a regression of the rate of establishment exit on the amount of innovation at the industry level  $[A_I]$  – see equation 27 in the text – and on the amount of innovation of all other industries  $[A_{MI}]$ . We include industry fixed effects throughout. Depending on the specification, we include time effects (T); industry stock return  $R^I$ ; and industry volatility  $\sigma^I$ . Data is from the tables of Business Dynamics Statistics at the US Census, and cover 7 industries, after dropping the finance sector and utilities, over the period 1977 to 2009. Industries correspond to the one-digit SIC code level. We report t-statistics in parenthesis, with standard errors clustered by year.

Table 10: Innovation and Tobin's Q

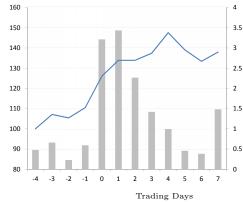
$\Delta \log Q_t$	I. Bend	chmark N	Ieasure	II. Alt. Normalization		
$\Delta \log \hat{A}_t$	-0.185	-0.223 -0.218		-0.196	-0.188	-0.143
	(-3.87)	(-4.17)	(-3.91)	(-3.83)	(-3.67)	(-2.66)
$R^2$	0.188	0.266	0.268	0.186	0.223	0.225
Observations	58	58	58	58	58	58
Controls						
$\log A_{t-1}$	_	Y	Y	_	Y	Y
$\log Q_{t-1}$	-	Y Y		-	Y	Y
$\Delta \log \bar{\sigma}_t$	-	Y			-	Y

Table shows output of a regression of changes in log Tobin's Q at the aggregate level on our aggregate measure of innovation – see equation (31) in text. Depending on the specification, we control for changes in the cross-sectional average of idiosyncratic volatility  $\bar{\sigma}$ ; lagged value of Q; and one lag of our innovation measure. Sample is 1952-2008. The aggregate measure of Tobin's Q is constructed using data from the flow of funds. Standard errors are computed using Newey-West.

Figure 1: Some illustrative examples



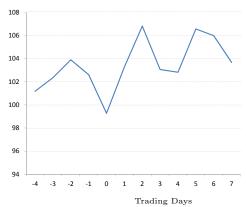
(a) Patent 4,946,778 granted to Genex on Aug, 7 1990, "Single Polypeptide Chain Binding Molecules."



(b) Patent 5,585,089 granted to Protein Design on Dec  $17,\,1996,$  "Humanized Immunoglobulins."



(c) Patent 6,317,722 granted to Amazon.com on Nov 13, 2001, "Use Of Electronic Shopping Carts To Generate Personal Recommendations."



(d) Patent 4,345,262 granted to Canon on Aug 17, 1982, "Ink Jet Recording Method."

Figure plots cumulative abnormal returns (left axis) and turnover (right axis) around the date the patent is granted for illustrative examples discussed in the text. Volume data is not available for Canon. Note that Canon reported a 6% fall in pre-tax profits on Aug 19 (two days subsequent to the patent grant).

Figure 2: Relation between stock market reaction and number of citations across placebo experiments

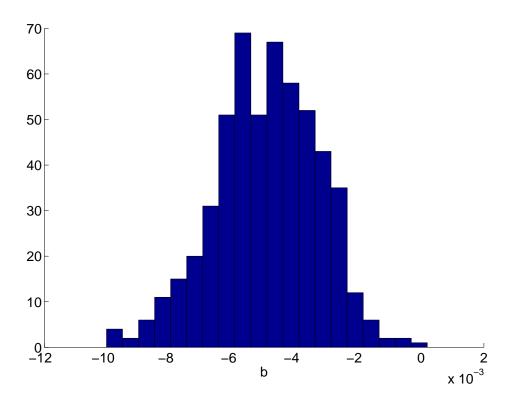


Figure plots distribution of estimated coefficients  $\hat{b}$  across 500 placebo experiments, corresponding to the specification in column (4), row (1) of Table 3.

Figure 3: Aggregate measures of innovation

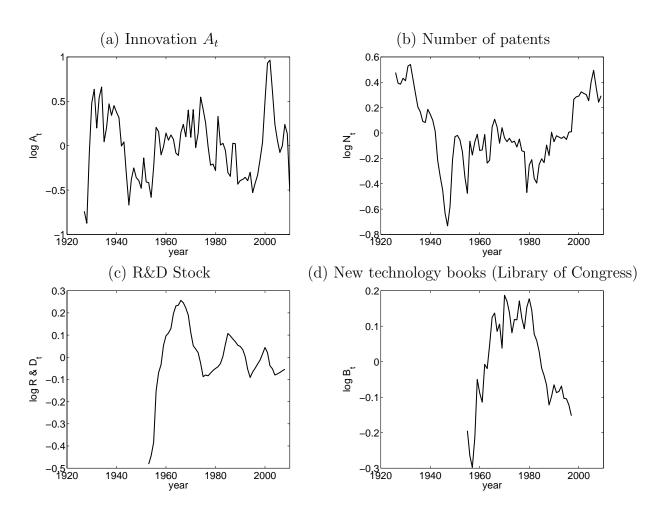


Figure plots log values of a) our measure of innovation A; b) total number of patents granted; c) R&D Capital stock (from BEA); d) number of new technology books in the Library of Congress (from Alexopoulos (2011)).

Figure 4: Firm productivity – Dynamic response

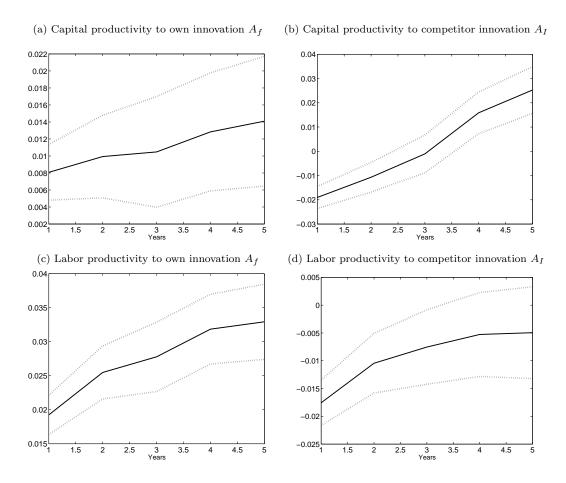
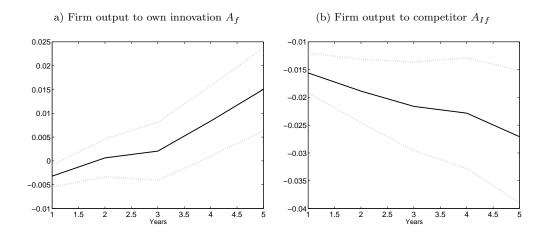


Figure plots coefficients  $a_1(k)$  and  $a_2(k)$  (and 90% confidence intervals) of a regression of k-period ahead capital (Panels a and b) or labor (Panels c and d) firm-level productivity on innovation of firm  $(A_f)$  and competitors  $(A_I)$ , using the specification (24) in main text. We control for lagged values of firm size (log capital or number of employees); log Tobin's Q; firm stock return (R); firm volatility  $(\sigma)$ ; one lag of the dependent variable; and industry (I) and time (T) fixed effects. We cluster the standard errors at the firm level.

Figure 5: Firm output – Dynamic response



Panels (a) and (b) of Figure plot coefficients  $a_1(k)$  and  $a_2(k)$  (and 90% confidence intervals) of a regression of k-period ahead log firm output on innovation of firm  $(A_f)$  and competitors  $(A_I)$  using the specification (25) in main text. We control for lagged values of firm size (log capital); log Tobin's Q; firm stock return (R); firm volatility  $(\sigma)$ ; two lags of the dependent variable; and industry (I) and time (T) fixed effects. We cluster the standard errors at the firm level.

Figure 6: Industry productivity – Dynamic response

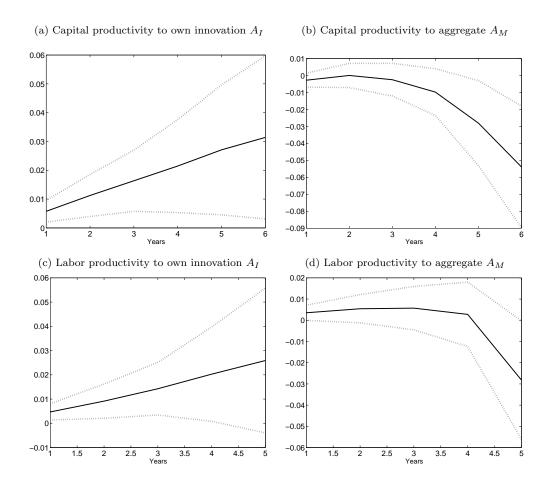


Figure plots coefficients  $a_1(k)$  and  $a_2(k)$  (and 90% confidence intervals) from a regression of k-period log capital (panels a and b) and labor productivity (panels c and d) on amount of innovation  $A_I$  at the industry level, and the aggregate amount of innovation excluding that industry  $A_M$ , using the specification (28) in main text. We control for industry stock returns; the cross-sectional average of idiosyncratic volatility  $\bar{\sigma}$  at the industry level; and one lag of the dependent variable. Data is from Dale Jorgenson's 35-sector KLEM. We compute standard errors clustered by industry.

Figure 7: Industry output – Dynamic response

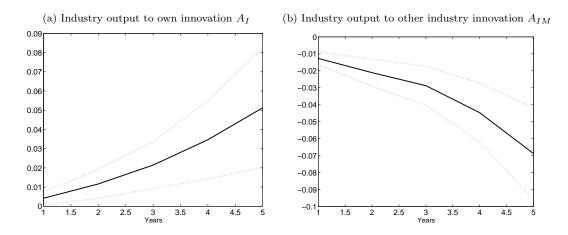


Figure plots coefficients  $a_1(k)$  and  $a_2(k)$  (and 90% confidence intervals) of a regression of k-period ahead log firm output on innovation of industry  $(A_I)$  and innovation of other industries  $(A_{MI})$  using the specification in equation 29. We control for industry stock return; the cross-sectional average of idiosyncratic volatility  $\bar{\sigma}$  at the industry level; and two lags of the dependent variable. Data is from Dale Jorgenson's 35-sector KLEM. Output is measured as value added in constant prices. We compute standard errors clustered by industry.

Figure 8: Innovation and Industry Growth

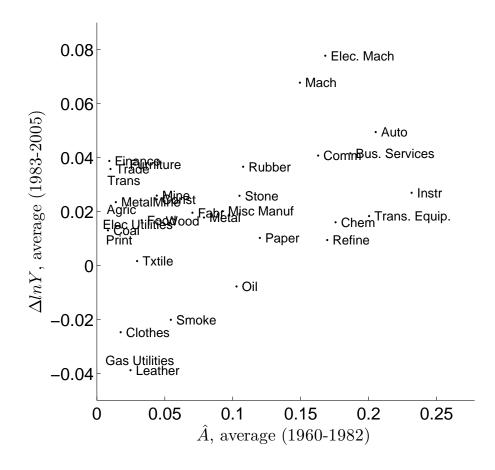


Figure plots the average output growth rate of 34 industries during the 1983-2006 period, versus the amount of innovation in 1960-1982. We use our innovation measure adjusted for measurement error  $\hat{A}$ . Data is from Dale Jorgenson's website. Output is measured as value added in constant prices.

Figure 9: Impulse responses, Productivity

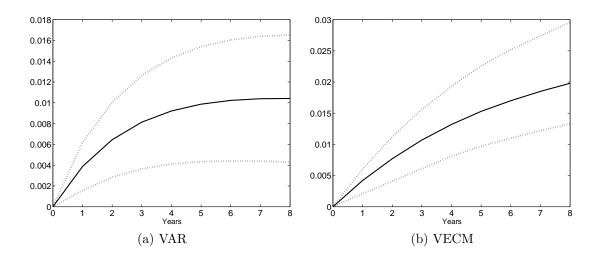


Figure shows impulse response of productivity from a bi-variate VAR (left) or VECM (right) containing total factor productivity and our aggregate innovation measure constructed using equation (31) in the main text. We obtain impulse responses by ordering our innovation measure last. We include a deterministic trend in the VECM. We select lag length based on the AIC criterion. Dotted lines represent 90% confidence intervals using standard errors are computed using 500 bootstrap simulations.

Figure 10: Impulse responses, Output

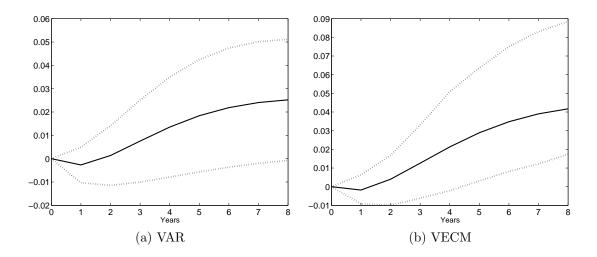


Figure shows impulse response of aggregate output from a bi-variate VAR (left) or VECM (right) containing output and our aggregate innovation measure constructed using equation (31) in the main text. We obtain impulse responses by ordering our innovation measure last. We include a deterministic trend in the VECM. We select lag length based on the AIC criterion. Dotted lines represent 90% confidence intervals using standard errors are computed using 500 bootstrap simulations.

Figure 11: Impulse responses, Consumption

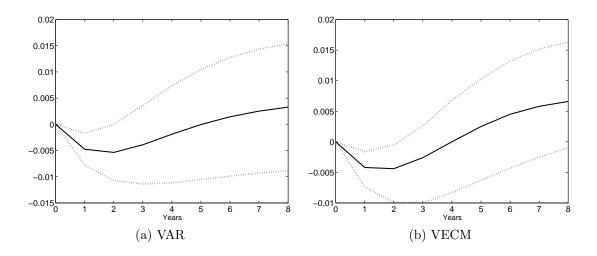


Figure shows impulse response of consumption from a bi-variate VAR (left) or VECM (right) containing consumption and our aggregate innovation measure constructed using equation (31) in the main text. We obtain impulse responses by ordering our innovation measure last. We include a deterministic trend in the VECM. We select lag length based on the AIC criterion. Dotted lines represent 90% confidence intervals using standard errors are computed using 500 bootstrap simulations.

## Data Appendix

#### Patent Data

We download the entire history of U.S. patent documents from Google Patents. Using text analysis algorithms, we match all patents in the Google data to corporations whose returns are in the CRSP database. In addition, we extract the USPTO technology classes and number of forward citations from the document. We merge our extracted citations data to data provided by Tom Nicholas. See the Online Appendix for more details.

#### Stock Market and Financial Data

The return data used to assess the stock market response to news about patents are from CRSP over the period 1926–2010. In several of our analyses we use financial and accounting data that are from Compustat. The sample in these cases is determined by the availability of Compustat data (available from 1951 onwards). As is standard, we omit financial firms and utilities from our analysis.

#### Business-cycle data

Productivity is utilization-adjusted TFP from Basu et al. (2006). Populations is from the U.S. Census Bureau (http://www.census.gov/popest/national/national.html). Output and consumption are from the Bureau of Economic Analysis. Output is gross domestic product (NIPA Table 1.1.5) divided by the consumption price index (St Louis Fed, CPIAUCNS). Consumption is consumption of non-durables plus services, deflated by the price index of non-durables and services respectively (NIPA Tables 1.1.5, 2.3.4). To get hours worked, we merge series CEU0500000007 and EEU00500005 from the BLS, times total private employment(BLS, CEU0500000001) divided by population. The aggregate Tobin's Q is computed using NIPA and FRB Flow of Funds Data as in Laitner and Stolyarov (2003). Finally, the time series information on R&D expenditure spending in the US is obtained from the NSF website.

### **Industry Data**

The industry-level data is from the KLEMS dataset of Dale Jorgenson. We use industry value added (constant prices) as measure of industry output.

#### Firm-level data

We define the investment rate as capital expenditures (Compustat: capx) divided by lagged gross property, plant and equipment (ppegt); labor hiring as the percentage change in the number of employees (emp); financial capital inflows as debt issuance plus equity issuance minus payout (Compustat sstk + dltis - prstkc-dv-dltr) normalized by assets (at); return on assets as operating income (ib) plus depreciation divided by lagged gross property, plant and equipment; Tobin's Q as the sum of the market value of common equity (CRSP December market capitalization), the book value of debt (dltt), the book value of preferred stock (pstkrv), minus the book value of inventories (invt) and deferred taxes (txdb), divided by gross property, plant and equipment (ppegt); productivity of capital as sales (sale) plus change in inventories (invt) over number of employees (emp).

# Online Appendix to "Technological Innovation, Resource Allocation and Growth"

Leonid Kogan, Dimitris Papanikolaou, Amit Seru and Noah Stoffman

### A Patent Data

Our measure of innovation relies on using information on patents that a firm creates and the stock market response to news about these patents. We now discuss the data that we employ in our analysis.

Patents in the United States are granted by the United States Patent and Trademark Office (USPTO). We download the entire history of U.S. patent documents from Google Patents.<sup>1</sup> Each of about 7.8 million patent files was downloaded using an automation script.<sup>2</sup>

To construct our measure of innovation, we match all patents in the Google data to corporations whose returns are in the CRSP database. Patent regulations require that only an individual, not a corporation, can be an inventor. However, the inventor can assign the granted property rights to a corporation or another person. Therefore, when patents are granted they always have an inventor, and sometimes an "assignee", that is, one or more corporations or persons.

For most patents, Google provides a text version of the patent document, created using OCR software. We use this text version of the document to extract the names of corporations to which patents are assigned. However, OCR technology is imperfect, and many of the downloaded documents include a great deal of garbled text. We therefore make use of a number of text analysis algorithms to extract relevant information from the documents.

Our sample covers patents granted between 1926 and 2010 matched to firms with returns in CRSP database. Since we merge our patent data with data on stock returns, we are limited to the period after 1926, when the CRSP database begins.

<sup>1</sup>http://www.google.com/patents

<sup>&</sup>lt;sup>2</sup>Google also makes available for downloading bulk patent data files from the USPTO. The bulk data does not have all of the additional "meta" information including classification codes and citation information that Google includes in the individual patent files. Moreover, the quality of the text generated from Optical Character Recognition (OCR) procedures implemented by Google is better in the individual files than in the bulk files provided by the USPTO. As explained below, this is crucial for identifying patent assignees.

#### Matching patents to firms

Here, we briefly discuss the steps our matching procedure followed, and provide extensive details Section C. We search the document for the words "assignee" or "assigned" and extract the text that immediately follows. This text is either a company name, or the name of an individual to whom the patent is assigned. We then count the number of times each assignee name appears across all patent documents. We compare each assignee name to more common names, and if a given name is "close", in the sense of the Levenshtein distance, to a much more common name, we substitute the common name for the uncommon name.<sup>3</sup> For example, one of the most common names is "General Electric Company", which is associated with over 43,000 patents. We substitute this name for the far less common, but quite similar, names "General Electbic Oohpany", "General Electbic Cqhpany", and "Genebal Electbic Compakt".

At this point, we have an assignee name for each patent. These names must be matched to a company identifier such as the CRSP permoon. This is accomplished in two steps. We begin by looking only at patents that are also in the NBER database. For each assignee name identified in the steps above, we count how many different permoons are matched to patents in the NBER database. For example, all of the patents with an assignee name "General Electric Company" are matched to one permoon in the NBER database. We can therefore safely assume that all of the patents assigned to the General Electric Company can be matched to that permoon, even for patents not included in the NBER data. Remaining assignee names are matched to CRSP firm names using a name matching algorithm. The algorithm uses a score based on the inverse word frequency to match assignee names to possible company names. For example, the word "American" is quite common in company names, and so contributes little to name matching; the word "Bausch" is quite uncommon, so it is given much more weight. Visual inspection of the matched names confirms very few mistakes in the matching.

#### Extracting patent citations

We extract patent citations from three sources. First, all citations for patents granted between 1976 and 2011 are contained in text files available for bulk downloading from Google. These citations are simple to extract and likely to be free of errors, as they are official USPTO data. Second, for patents granted before 1976, we extract citations from the OCR text generated from the patent files. We search the text of each patent for any 6- or 7-digit numbers, which could be patent numbers. We then check if these potential patent numbers are followed closely by the corresponding grant date for that patent; if the correct date appears, then we can be certain that we have identified a patent citation. Since we require the date to appear near any potential patent number, it is

<sup>&</sup>lt;sup>3</sup>The Levenshtein distance is the number of edits required to make one string match another string, where an edit is inserting, deleting, or substituting one character.

<sup>&</sup>lt;sup>4</sup>The algorithm is based on code written by Jim Bessen, available at http://goo.gl/m4AdZ.

unlikely that we would incorrectly record a patent citation – it is far more likely that we would fail to record a citation than record one that isn't there. Third, we complement our citation data with the hand-collected reference data of Nicholas (2008). See Section C of this Appendix for a detailed explanation of this process.

#### Summary statistics

We now provide some statistics that lend credence to our method for extracting patent information. Table 1 shows the number of patents we match to companies. Of the 6.2 million patents granted in or after 1926, we find the presence of an assignee in 4.4 million. The matching procedure provides us with a database of 1.9 million matched patents, of which 523,301 (27%) are not included in the NBER data. Figure 1 graphs the total number of patents matched by the year the patent was granted. Patents included in the NBER data, which is the most comprehensive database previously available, are shown in light shading. Patents unique to our database are presented in dark shading. Note that the two sets of data appear to fit together fairly smoothly, and that even during the period covered by the NBER data, our database adds an average of 2,187 patents to the NBER data.<sup>5</sup>

Table 2 provides additional summary statistics. Overall, our data provides a matched permoo for 66% of all patents with an assignee, or 31% of all granted patents. By comparison, the NBER patent project provides a match for 32% of all patents from 1976–2006, so our matching technique works quite well, even using only data extracted from OCR documents for the period before the NBER data. Another point of comparison is Nicholas (2008), who uses hand-collected patent data covering 1910 to 1939. From 1926–1929, he matches 9,707 patents, while our database includes 8,858 patents; from 1930–1939 he has 32,778 patents while our database includes 47,036 matches during this period.

### B Other Data

#### Stock Market and Financial Data

The return data used to assess the stock market response to news about patents are from CRSP over the period 1926–2010. In several of our analyses we use financial and accounting data that are from Compustat. The sample in these cases is determined by the availability of Compustat data (available from 1951 onwards). As is standard, we omit financial firms and utilities from our analysis.

<sup>&</sup>lt;sup>5</sup>We use information on the patent-assignee match in the NBER data to assist with our matching, so the match during the overlapping period is mostly the same, by construction. An exception is for cases where there is apparently a mistake in the NBER match and our patent-assignee frequency-based matching system corrects an error.

#### Business-cycle data

Productivity is utilization-adjusted TFP from Basu, Fernald, and Kimball (2006). Populations is from the U.S. Census Bureau (http://www.census.gov/popest/national/national.html). Output and consumption are from the Bureau of Economic Analysis. Output is gross domestic product (NIPA Table 1.1.5) divided by the consumption price index (St Louis Fed, CPIAUCNS). Consumption is consumption of non-durables plus services, deflated by the price index of non-durables and services respectively (NIPA Tables 1.1.5, 2.3.4). To get hours worked, we merge series CEU0500000007 and EEU00500005 from the BLS, times total private employment(BLS, CEU0500000001) divided by population. The aggregate Tobin's Q is computed using NIPA and FRB Flow of Funds Data as in Laitner and Stolyarov (2003). Finally, the time series information on R&D expenditure spending in the US is obtained from the NSF website.

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### C Patent Data Construction – Details

In this section we explain in detail how we constructed our new patent data set. The raw data are very large and not very well structured, and thus required a great deal of effort to clean. We used a number of techniques to extract, clean, and match assignees from patents. As with any such project there is a trade-off between type-I and type-II errors (in this case, failing to match an assignee to CRSP or incorrectly matching an assignee to CRSP). Our approach was to be as conservative as possible, attempting to minimize mismatches while at the same time extracting as many correct matches as possible.

#### C.1 Data sources

We use three sources of data to construct the new patent database:

- 1. Details of patents granted from 1976–2010 is available in high-quality text files available for bulk downloading from Google, through a special data-hosting arrangement with the United States Patent and Trademark Office (USPTO). The text files use one of two data structures that allows relatively straightforward data extraction: files for 2001–present use XML, while files for 1976–2000 use a fixed-width data structure with labeled fields.
- 2. Patents granted prior to 1976 are also stored on Google, but only in individual web pages (one per patent). Information during this period is drawn from Optical Character Recognition (OCR) of original patent documents, and is of highly-variable quality. There is very limited, if any, structure to these files.
- 3. We use the NBER patent data (Hall and Trajtenberg, 2001), which covers the period 1976–2006, to help with the matching and to validate our other data extraction methods.

Due to varying data sources and quality over time, it worth stressing that from 1976–2010 we use the *official records* of the USPTO. As we discuss below, we are able to provide some additions and corrections to the NBER data during the period of overlap with our data. Prior to 1976 the data are more difficult to work with, but we have implemented a number of sophisticated text analysis algorithms to create a very high-quality database.

#### Downloading individual patent files

We downloaded individual patent data from Google. The URL for each patent's summary page is of the form http://www.google.com/patents/?id=RDOyAAAAEBAJ, where RDOy is a 4-character code used by Google to identify each patent. The IDs use any of the characters  $\{a, \ldots, z, A, \ldots, Z, 0, \ldots, 9, -, -\}$ . There are  $64^4 = 16.8$  million possible IDs, but only about 8 million patents. However,

all 16.8 million URLs must be checked, because there is no publicly-available mapping of patent numbers to the Google ID.

A screen shot of the summary page for the patent with id RD0y, which is patent 4,345,262, is shown in Figure 1. The main page includes—when available—the title of the patent, the filing and grant dates, the abstract, inventor(s), original assignee(s), current classifications, and a record of citations (out-cites) and references (in-cites). The information reported on this page by Google was gleaned from the OCR analysis of the original patent document, and consequently less information is reported for older documents, especially patents granted before 1976.

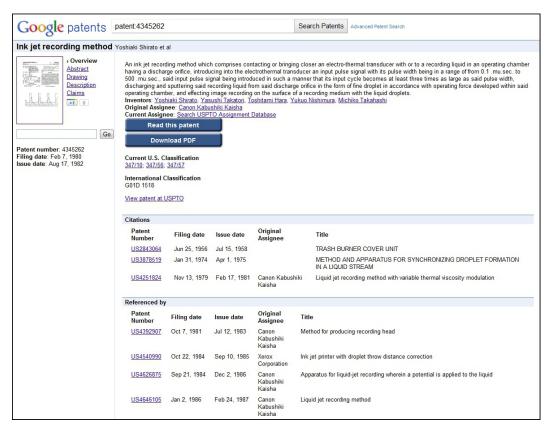


Figure 1: Google summary page for U.S. patent 4,345,262

Using a Perl automation script, we sequentially navigated to each of the 16.8 million patent summary pages.<sup>6</sup> From this page, we stored all available information. The script then loaded the "Read this patent" link, which loads a PDF version of the patent document. From here, we loaded the "plain text" version of the document, which is simply the text derived from OCR of the PDF document. Examples of these pages are shown in Figures 2 and 3. We saved the complete text of the plain text version of each patent. After compression, the complete archive of text requires

<sup>&</sup>lt;sup>6</sup>Google generally blocks users from downloading so many web pages. We are grateful to Hal Varian for his assistance with arranging permission to access these pages.

approximately 56 gigabytes of disk space.

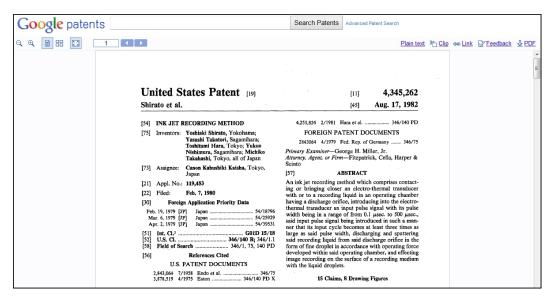


Figure 2: PDF view

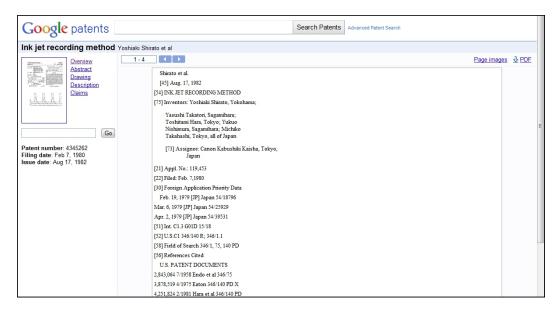


Figure 3: Plain text view

#### Download bulk patent files

As part of a special arrangement with the USPTO, Google also makes available for downloading bulk patent data files. The bulk data does not have all of the additional "meta" information including classification codes and citation information that Google includes in the individual patent files.

Moreover, the quality of the text generated from OCR procedures implemented by Google is better in the individual files than in the bulk files provided by the USPTO. We therefore do not use the bulk download files for data in the pre-NBER period.

For the post-NBER period, however, the bulk data files are of extremely high quality because they are based on digital patent records as opposed to OCR data drawn from images of patent documents. These data files are provided either in XML format or in a fixed-width record format. In both cases, all fields (inventor name, grant date, etc.) are clearly identified. We rely on these files to construct the database during the post-NBER period (2006–2009) and to make additions and corrections to the NBER data.

#### C.2Identifying assignees

#### Extracting assignee names

For data during the post-1976 period, we can use the XML files available for bulk download to identify the assignee with virtually no errors.

During the pre-1976 period, we cannot rely solely on Google's extraction of the filing and grant dates or the assignee name because the OCR for patents frequently has errors. As an example, consider patent 1,131,249, shown in Figure 4.

## UNITED STATES PATENT OFFICE.

EARLE R. KNIGHT, OF NORWOOD, OHIO, ASSIGNOR, BY MESNE ASSIGNMENTS, TO ALLIS-CHALMERS MANUFACTURING COMPANY, A CORPORATION OF DELAWARE,

RETAINING-BING FOR DYNAMO-ELECTRIC MACHINES.

1,131,249.

Specification of Letters Patent.

Patented Mar. 9, 1915.

Application filed May 1, 1909. Serial No. 492,399.

To all whom it may concern: Be it known that I, EARLE R. KNIGHT, a citizen of the United States, residing at Norwood, in the county of Hamilton and State of Ohio, have invented certain new and use-

ring is shown in perspective in Fig. 3. It 55 comprises two segmental duplicate interchangeable parts each part of which has two male portions 16 and two female portions 17. The male and female portions of one part ful Improvements in Retaining-Rings for of the split retaining rings are respectively 60

Figure 4: Title page of patent 1,131,249

It is clear to a human reader that this patent was assigned to the Allis-Chalmers Manufacturing Company, but the OCR for this patent reads

EASLS B. KNIGHT, OF NORWOOD, OHIO, ASSIGNOR,, BY MESH'S ASSIGN1IBNTS, TO ALUSCHALME&S MANOTAC/rURING- COMPANY, A COBPOBAT'10H OF DELAY/ABE.

Consequently, Google records the assignee as "BY MESH S ASSIGNIIBNTS", which is clearly not accurate.

We therefore rely on a number of textual analysis algorithms to extract the assignee name from the full text files we saved for each patent. In general, our approach to performing a "fuzzy" match on a text string is to use the maximum likelihood *n*-gram approach described by Norvig (2009).

We begin by identifying the text where the assignee, if there is one, will be named. We do this by searching for words that appear similar to "assign", "assignor", or "assignee". When found near the beginning of the patent document, this word is typically followed closely by the name of the assignee, so we extract a text string of 200 characters for further processing. The assignee may be a person, or a corporation, in which case the name will include a word like "company", "corporation" or "incorporated". If the word "assign" and its variants are not found, we assume the inventor did not assign the patent to another entity.

#### Cleaning assignee names

After extracting the string that is likely to contain the assignee name, additional cleaning is necessary. Because of OCR errors, company names may be garbled. For example, the General Electric Company, which has more than 43,000 patents in our data, appears as "General Electric Cohpany", "General Electric Cohpany", and "Genebal Electric Compakt", among hundreds of other misspellings. To fix these, we first count how many patents have been granted to each assignee name, regardless of how the assignee name is spelled. In this example, General Electric Company appears in 42,693 patents, while each of the misspelled variants appears fewer than 5 times.

We then calculate the Levenshtein edit distance<sup>7</sup> between each assignee name and all other names that have more patents. If any assignee name is close to another assignee name that is associated with many more patents, then the more common assignee name is substituted for the less common name. This algorithm correctly identifies all of the misspellings noted above as being General Electric.

After cleaning assignee names, we manually checked which misspelled names were matched to the 500 assignees with the most patents to confirm that no significant errors were introduced in this step.

<sup>&</sup>lt;sup>7</sup>The Levenshtein distance is the number of edits required to transform one string into another string, where allowed edits are inserting, deleting, or substituting one character. For example, the Levenshtein distance between "patent" and "parent" is 1, while the distance between "patent" and "apparent" is 3.

#### Matching to CRSP

Having extract a list of assignee names, the next step is to match company names to the CRSP permonent permonent identifier. This is accomplished in three steps.

We begin by looking only at those patents that are included in the NBER patent database. For each assignee name identified in the steps above, we count how many different permos are matched to patents in the NBER database. For example, all of the patents with an assignee name "General Electric Company" are matched to one permon in the NBER database. We can therefore safely assume that all of the patents assigned to the General Electric Company can be matched to that permon, even for patents not included in the NBER data. This step allows us to draw on the extensive data cleaning and matching project undertaken by Hall and Trajtenberg (2001) while at the same time identifying some errors in the NBER database. For example, patent 4,994,660 was assigned to General Electric but is identified in the NBER data as being assigned to Hitachi, Ltd. Because our algorithm relies on name matching, and the assignee name in that patent is General Electric, the patent is correctly identified in our data.

The first step only helps us match assignees with patenting activity during the period covered by the NBER database. We therefore proceed with a second step to match remaining assignee names. We do this with a name matching algorithm based on code written by Jim Bessen, available at <a href="http://goo.gl/m4AdZ">http://goo.gl/m4AdZ</a>. The algorithm uses a score based on the inverse word frequency to match assignee names to possible company names. For example, the word "American" is quite common in company names, and so contributes little to name matching; the word "Bausch" is quite uncommon, so it is given much more weight. Visual inspection of the matched names confirms very few mistakes in the matching.

Finally, we identify the top 250 assignees (by patents) with no CRSP matches. We manually matched these to CRSP whenever possible. Examples of firms requiring manual matching include research subsidiaries such as 3M Innovative Properties Company, which was not successfully matched to CRSP because its name differs substantially from its parent. Although we only checked 250 assignees, this manual check allowed us to match an additional 64,000 patents. Firms with high patenting activity but not matched to CRSP are either private companies or foreign firms that are not listed on U.S. exchanges, an example of which is Hoffmann-La Roche, the large Swiss drug company.

#### C.3 Correcting grant dates

The filing and grant dates of the patents are subject to the same sort of OCR errors as the assignee information. The grant dates are particularly important for our purposes because we use them to calculate the return around the grant date. Since patent numbers are sequential by grant dates, it is easy to infer missing or incorrect grant dates by comparing patent dates to the grant dates of adjacent patents. The same is not true of filing dates, but do not use filing dates in our current work.

To populate missing patent dates and correct mistakes we identify the 3 non-missing grant dates immediately preceding and following each patent. For example, if patent k's grant date is missing but patents  $(k-3,\ldots,k-1,k+1,\ldots,k+3)$  have grant date D, then we set patent k's grant date to D. By applying this procedure iteratively we are able to correct most grant dates, with the exception of patents whose grant dates are missing and lie at a boundary between two grant dates. We fill in these missing boundary dates by manually checking their grant dates on the USPTO's web site.

While we don't rely on filing dates in the paper, it is possible to correct large errors in filing dates by identifying cases where filing dates occur after the grant date, or much earlier than the filing dates of adjacent patents. These errors often occur only in the year, so we can keep the recorded month and day the same while setting the year of the patent filing to the median filing year of a 20-patent window centered on a patent with an apparent error.

#### C.4 Extracting citations

Extracting patent citations from the patent text documents presents another challenge. The format of a patent document has changed several times, as has the location and formatting of citations within the document. For example, Figure 5 shows the references section of patent 2,423,030, granted in 1947. The format seen here is the first format used after patent citation began in February, 1947.

A human reader has no problem identifying the citations in this patent. But to understand the considerable challenge faced in automating this identification, consider the OCR for this part of the patent:

other side. 35 REFERENCES CITED

By this invention I am able satisfactorily and The following references are of record in the conveniently to effect the drying of'Shaped pot-jjle of tllis patent:

tery or other ceramic articles either in their

other side.  By this invention I am able satisfactorily and conveniently to effect the drying of snaped pot-	35		REFERENCES CIT ving references are opatent:	
tery or other ceramic articles either in their moulds or otherwise, in a manner which min- imises risk of injury by excessively rapid heating		UN	NAME	TENTS Date
or moisture extraction. The invention is not, however, restricted to the example described as subordinate details may be modified to suit dif-	40	1,767,872 1,934,904	FoxBarnett et al	June 24, 1930 Nov. 14, 1933
ferent requirements.  Having thus described my invention what I claim as new and desire to secure by Letters Pat-	45	2,257,180 1,893,963	Russ	Jan. 10, 1933
ent is:  1. Means for drying ceramic ware, comprising		Number 439,577	Country Great Britain	Date

Figure 5: A patent citation section

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moulds or otherwise, in a manner which min- UNITED STATES PATENTS imises risk of injury by excessively rapid heating 40 Number Name Date or moisture extraction. The invention is not, 1,767,872 Pox June 24, 1930 however, restricted to the example described as 1^934,904 Barnett et al Nov. 14', 1933 subordinate details may be modified to suit dif- 2,257,180 Mayer Sept. 30, 1941 ferent requirements. 1,893,963 Russ Jan. 10,1933 Having thus described my invention what I 45 claim as new and desire to secure by Letters Pat- * ("uu-^ f A 1 Jun 11> entis: Number Country Date

1. Means for drying ceramic ware, comprising 439,577 Great Britain Dec. 10,1935
```

Our approach is to identify any text that could be a patent number (a 6- or 7-digit number, perhaps separated by commas, spaces, or other "noise" characters) and is closely followed by the correct grant date for the cited patent. In particular, for every potential patent number we identify, we determine its grant date and then search near the possible citation for that date. If the date appears, we can be very confident that we have correctly identified a citation. For example, for the patent shown in Figure 5 we extract the patent number 1,767,872 and then confirm that its grant date—June 24, 1930—appears somewhere nearby in the text. By using this two-step process to identify citations, our citation extraction is of very high quality—the probability that some random 7-digit number will be followed closely by the correct date is clearly extremely small.

Our citation extraction method provides more citations than what is available on the Google summary page. For example, the Google summary page for the patent shown in the previous example provides no citations at all, while our algorithm correctly extracted all four citations. (We exclude citations to foreign patents, as these patents are not in our database.) In general, Google does not currently report out-cites from patents granted before 1976, so we use this extraction method on all patents granted between 1926 and 1975.

## C.5 Data validation

As previously mentioned, any data extraction project such as this can lead to two types of errors: matching a patent to a firm that is not the assignee, or failing to match a patent to a any firm when it does have an assignee. Our strategy makes the first error very unlikely, as a match occurs only when a name closely resembling a CRSP company name appears around the word "assignee" at the beginning of patent document. We cannot be sure how many errors of the second type we made, but we have taken care to ensure that our algorithms allow as flexible matching as possible.

We also did two final checks to check the quality of our matching strategy. First, we visually inspected a random sample of 500 patents granted between 1926 and 1975 and confirmed that assignees had been correctly extracted, and correctly matched if the assignee appeared in CRSP. This is obviously a very small sample of patents, but this careful check confirmed that no serious errors existed.

Second, we applied the extraction and matching algorithms we used in the pre-1976 period to a random sample of 25,000 patents granted between 1976 and 1999. We then compared our matches to the matches in the NBER data. None of our matches was incorrect, and only 3 patents were incorrectly not matched to an assignee. In other words, applying the techniques we used on pre-1976 data to data from the NBER period yields results that are virtually identical to those in the NBER database.

## D Analytical Appendix

Here, we provide the derivation of the theoretical results in Section 2.1. The final-good producer solves the intra-period profit maximization problem

$$\max_{L_{t}^{F}, \{q_{jt}\}} Z_{t} \left(L_{t}^{F}\right)^{1-\alpha} \int_{0}^{H_{t}} (\theta_{j})^{1-\alpha} (q_{jt})^{\alpha} dj - \int_{0}^{H_{t}} p_{jt} q_{jt} dj - w_{t} L_{t}^{F}.$$

The associated optimality conditions for intermediate good inputs dictate that the price of intermediate goods  $p_j$  is equal to

$$Z_t \left( L_t^F \right)^{1-\alpha} \left( \theta_j \right)^{1-\alpha} \alpha \left( q_{jt} \right)^{\alpha-1} = p_{jt}$$

and therefore

$$q_{jt} = L_t^F \theta_j \left(\frac{p_{jt}}{\alpha Z_t}\right)^{\frac{1}{\alpha - 1}}.$$

If a good is covered by a patent, the monopolist producer maximizes intra-period profits, taking production plans for all other goods as given:

$$\max_{p_{jt}} (p_{jt} - w_t) L_t^F \theta_j \left( \frac{p_{jt}}{\alpha Z_t} \right)^{\frac{1}{\alpha - 1}},$$

which implies the equilibrium spot price

$$p_{jt} = \frac{w_t}{\alpha}$$
.

and hence the equilibrium output of an intermediate good covered by a patent is

$$q_{jt} = L_t^F \theta_j \left(\frac{w_t}{\alpha^2 Z_t}\right)^{\frac{1}{\alpha - 1}}.$$

The equilibrium output of an intermediate good not covered by a patent is

$$q_{jt} = L_t^F \theta_j \left(\frac{w_t}{\alpha Z_t}\right)^{\frac{1}{\alpha - 1}}.$$

The optimality condition with respect to the labor input in the final-good firm's problem is

$$(1 - \alpha) Y_t = w_t L_t^F.$$

Substituting into this relation the equilibrium output of intermediate goods, we find

$$\begin{split} w_t L_t^F &= (1-\alpha) \left(L_t^F\right)^{1-\alpha} Z_t \left\{ \begin{array}{l} \int_0^{H_t} p_j \theta_j \left(L_t^F \left(\frac{w_t}{\alpha^2 Z_t}\right)^{\frac{1}{\alpha-1}}\right)^{\alpha} dj + \\ \int_0^{H_t} \left(1-p_j\right) \theta_j \left(L_t^F \left(\frac{w_t}{\alpha Z_t}\right)^{\frac{1}{\alpha-1}}\right)^{\alpha} dj \end{array} \right\} \\ &= (1-\alpha) L_t^F Z_t \left\{ \begin{array}{l} H_t \mathbf{E} \left[p_j \theta_j\right] \left(\left(\frac{w_t}{\alpha^2 Z_t}\right)^{\frac{1}{\alpha-1}}\right)^{\alpha} + \\ H_t \left(1-\mathbf{E} \left[p_j \theta_j\right]\right) \left(\left(\frac{w_t}{\alpha Z_t}\right)^{\frac{1}{\alpha-1}}\right)^{\alpha} \end{array} \right\} \end{split}$$

and therefore the equilibrium wage is given by

$$w_{t} = (1 - \alpha)^{1 - \alpha} Z_{t} \left\{ \int_{0}^{H_{t}} p_{j} \theta_{j} \alpha^{\frac{2\alpha}{1 - \alpha}} dj + \int_{0}^{H_{t}} (1 - p_{j} \theta_{j}) \alpha^{\frac{\alpha}{1 - \alpha}} dj \right\}^{1 - \alpha}$$
$$= B_{0} Z_{t} (H_{t})^{1 - \alpha},$$

where

$$B_0 = (1 - \alpha)^{1 - \alpha} \left\{ \operatorname{E}\left[p_j \theta_j\right] \alpha^{\frac{-2\alpha}{\alpha - 1}} + (1 - \operatorname{E}\left[p_j \theta_j\right]) \alpha^{\frac{-\alpha}{\alpha - 1}} \right\}^{1 - \alpha}.$$

The market clearing condition in the labor market that determines the equilibrium allocation of labor between production of the final good and production of the intermediate goods is

$$L_t^F + \int_0^{H_t} q_{jt} dj = 1,$$

hence

$$L_{t}^{F} \left\{ 1 + \left( \operatorname{E}\left[p_{j}\theta_{j}\right] \alpha^{\frac{2}{1-\alpha}} B_{0}^{\frac{1}{\alpha-1}} + \left(1 - \operatorname{E}\left[p_{j}\theta_{j}\right]\right) \alpha^{\frac{1}{1-\alpha}} B_{0}^{\frac{1}{\alpha-1}} \right) \right\} = 1$$

and

$$L_{t}^{F} = B_{1} \equiv \left\{ 1 + \left( \operatorname{E}\left[p_{j}\theta_{j}\right] \alpha^{\frac{2}{1-\alpha}} B_{0}^{\frac{1}{\alpha-1}} + \left(1 - \operatorname{E}\left[p_{j}\theta_{j}\right]\right) \alpha^{\frac{1}{1-\alpha}} B_{0}^{\frac{1}{\alpha-1}} \right) \right\}^{-1}$$

In summary, the equilibrium output of an intermediate good covered by a patent is

$$q_{jt} = B_1 \left( B_0 \alpha^{-2} \right)^{\frac{1}{\alpha - 1}} \left( \theta_j H_t^{-1} \right).$$

and the equilibrium output of an intermediate good not covered by a patent is

$$q_{jt} = B_1 \left( B_0 \alpha^{-1} \right)^{\frac{1}{\alpha - 1}} \left( \theta_j H_t^{-1} \right).$$

The equilibrium output of the final consumption good is

$$Y_t = (1 - \alpha)^{-1} w_t B_1 = (1 - \alpha)^{-1} B_0 B_1 Z_t (H_t)^{1 - \alpha} = B_2 Z_t (H_t)^{1 - \alpha}$$

where

$$B_2 = (1 - \alpha)^{-1} B_0 B_1.$$

Next, we determine the stock market reaction to a successful patent application. A monopolistic producer of an intermediate good j generates equilibrium profits equal to

$$\frac{H_{\tau(j)} - H_{\tau(j)-1}}{\delta} (p_{jt} - w_t) q_{jt} = \frac{H_{\tau(j)} - H_{\tau(j)-1}}{\delta} w_t (\alpha^{-1} - 1) q_{jt} 
= \frac{H_{\tau(j)} - H_{\tau(j)-1}}{\delta} B_0 Z_t (H_t)^{1-\alpha} (\alpha^{-1} - 1) B_1 (B_0 \alpha^{-2})^{\frac{1}{\alpha-1}} (\theta_j (H_t)^{-1}) 
= \frac{H_{\tau(j)} - H_{\tau(j)-1}}{\delta} B_3 \theta_j Z_t (H_t)^{-\alpha},$$

where

$$B_3 = B_0^{\frac{\alpha}{\alpha - 1}} B_1 (\alpha^{-1} - 1) \alpha^{\frac{2}{1 - \alpha}}$$

The equilibrium stochastic discount factor, based on the household's optimality conditions, is

$$M_t = \rho^{-t} (Y_t)^{-\gamma} = \rho^{-t} \left( B_2 Z_t (H_t)^{1-\alpha} \right)^{-\gamma}$$

Therefore, the time-t present value of profits generated by the patent-protected good j (including the current period) is

$$B_{3} \frac{H_{\tau(j)} - H_{\tau(j)-1}}{\delta} \theta_{j} \mathcal{E}_{t} \left[ \sum_{s=0}^{\infty} Z_{t+s} \left( H_{t+s} \right)^{-\alpha} \rho^{-s} \left( \frac{Z_{t+s}}{Z_{t}} \right)^{-\gamma} \left( \frac{H_{t+s}}{H_{t}} \right)^{-\gamma(1-\alpha)} \right]$$

$$= B_{3} \frac{H_{\tau(j)} - H_{\tau(j)-1}}{\delta} \theta_{j} Z_{t} \left( H_{t} \right)^{-\alpha} \mathcal{E}_{t} \left[ 1 + \sum_{s=1}^{\infty} \rho^{-s} \left( \frac{H_{t+s}}{H_{t}} \right)^{-\gamma(1-\alpha)-\alpha} \left( \frac{Z_{t+s}}{Z_{t}} \right)^{1-\gamma} \right]$$

$$= (B_{3} + B_{4}) \frac{H_{\tau(j)} - H_{\tau(j)-1}}{\delta} \theta_{j} Z_{t} \left( H_{t} \right)^{-\alpha},$$

where

$$B_4 = B_3 \mathcal{E}_t \left[ \sum_{s=1}^{\infty} \rho^{-s} e^{-(\gamma(1-\alpha)+\alpha)\left(\sum_{n=1}^s \Delta \ln H_n\right) - (\gamma-1)\left(\sum_{n=1}^s \Delta \ln Z_n\right)} \right].$$

We conclude that the cumulative stock market gain in response to successful patent applications in period t – the sum of the individual stock firm responses  $\Delta V_{ft}$ ,

$$\Delta V_{ft} = (1 - p_j) (B_3 + B_4) \chi^{-1} (H_t - H_{t-1}) \theta_j Z_t H_t^{-\alpha},$$

is

$$\Delta V_{t} = \int_{H_{t-1}}^{H_{t}} (1 - p_{j}) (B_{3} + B_{4}) \theta_{j} Z_{t} (H_{t})^{-\alpha} dj = (B_{3} + B_{4}) (1 - \mathbb{E}[p_{j}\theta_{j}]) Z_{t} (H_{t})^{-\alpha} (H_{t} - H_{t-1})$$

$$= B_{5} (1 - \mathbb{E}[p_{j}\theta_{j}]) Z_{t} (H_{t})^{1-\alpha} \left(1 - e^{-\Delta \ln H_{t}}\right),$$

where  $B_5 = (B_3 + B_4)$ .

We normalize the aggregate market reaction by the total (ex-dividend) stock market value at the end of period t to eliminate the effect of the aggregate disembodied productivity process  $Z_t$  on the stock market reaction to patent grants. The time-t stock market value is

$$P_{t} = E_{t} \left[ \sum_{s=1}^{\infty} \int_{0}^{H_{t+s}} \underbrace{\left(B_{3}\theta_{j}Z_{t+s}\left(H_{t+s}\right)^{-\alpha}\right)}_{\text{Cash flow}} \underbrace{\left[\rho^{-s}\left(\frac{Z_{t+s}}{Z_{t}}\right)^{-\gamma}\left(\frac{H_{t+s}}{H_{t}}\right)^{-\gamma(1-\alpha)}\right]}_{\text{Discount factor}} dj \right]$$

$$= B_{3}Z_{t}\left(H_{t}\right)^{1-\alpha} E_{t} \left[ \sum_{s=1}^{\infty} \rho^{-s}\left(\frac{H_{t+s}}{H_{t}}\right)^{(1-\gamma)(1-\alpha)}\left(\frac{Z_{t+s}}{Z_{t}}\right)^{1-\gamma} \right]$$

$$= B_{6}Z_{t}\left(H_{t}\right)^{1-\alpha},$$

where

$$B_6 = B_3 E_t \left[ \sum_{s=1}^{\infty} \rho^{-s} e^{(1-\gamma)(1-\alpha) \left( \sum_{n=1}^{s} \Delta \ln H_n \right) - (\gamma - 1) \left( \sum_{n=1}^{s} \Delta Z_n \right)} \right]$$

Therefore, the normalized aggregate stock market reaction to patent grants is

$$\frac{\Delta V_t}{P_t} = \frac{B_5 (1 - \mathrm{E} [p_j \theta_j]) Z_t (H_{t-1})^{1-\alpha} e^{-\alpha \Delta \ln H_t} (e^{\Delta \ln H_t} - 1)}{B_6 Z_t (H_t)^{1-\alpha}}$$

$$= B_7 (1 - \mathrm{E} [p_j \theta_j]) (1 - e^{-\Delta \ln H_t}),$$
where  $B_7 = B_5 / B_6$ .

For small values of  $\Delta \ln H_t$ , the term  $(1 - e^{-\Delta \ln H_t})$  is approximately equal to  $\Delta \ln H_t$ .

The log growth of aggregate output during the same period is

$$\ln Y_t - \ln Y_{t-1} = (1 - \alpha) \Delta \ln H_t + \Delta \ln Z_t.$$

## E Additional results and descriptive statistics

Table 1: Number of patents

Data step	Number of patents
Total downloaded patents	7,797,506
Granted in 1926 or later	6,272,428
Identified as having an assignee	4,374,524
Matched to CRSP	1,928,123
Of which:	
Present in NBER data	1,404,822
New to this paper	523,301

The table provides details on patents in our sample. We begin with all patents downloaded from Google Patents, and restrict the sample to post-1926. Not all patents have assignees, and among those that do, not all are companies in CRSP. We are able to match 1,928,123 patents to CRSP firms, of which 523,301 (27%) are new to this study. Further details are reported in Table 2 and Figure 1.

Table 2: Assignee matching by Decade

		Number of pa	Number o	f unique	
Years	Total	With assignee	Matched to CRSP	Matched firms	CRSP firms
1926–1929	174,022	48,433	8,858	182	786
1930–1939	442,700	172,925	47,029	355	951
1940–1949	307,499	141,345	60,616	451	1,042
1950-1959	$425,\!953$	171,157	82,255	587	1,246
1960-1969	567,599	$265,\!524$	165,409	1,175	3,177
1970–1979	690,459	393,661	247,102	2,086	7,204
1980–1989	708,735	579,518	$235,\!525$	2,756	11,715
1990 - 1999	1,109,398	933,705	352,005	3,664	14,882
2000-2010	1,846,063	1,668,256	729,324	4,415	11,900
All years	6,272,428	4,374,524	1,928,123	7,864	26,660

The shows summary statistics for patents in our sample by decade. Column 2 shows the total number of patents, and column 3 shows how many patents are identified as having an assignee. Column 4 shows how many of those patents with assignees are matched to a company in CRSP. (The remaining assignees are either individuals, private companies, or the matching process was unable to identify the correct company.) Columns 5 and 6 show how many unique firms there are matched to patents or in CRSP.

Table 3: Stock turnover around patent announcement days

Event	k = -1	k = 0	k = 1	k = 2	k = 3	k = 4
vol/shrout			I. Tu	rnover		
A. Patent grant	-0.147	-0.008	0.0502	0.0588	0.0487	-0.074
	(-5.27)	(-0.68)	(3.63)	(3.22)	(1.78)	(-4.65)
B. Patent publication	0.152	0.255	-0.194	-0.385	0.114	-0.205
	(4.02)	(5.51)	(-3.03)	(-4.17)	(3.08)	(-3.07)
$vol/shrout - \overline{vol/shrout}$		]	II. Relati	ve turnove	r	
A. Patent grant	-0.156	-0.006	0.055	0.061	0.047	-0.091
	(-6.74)	(-0.57)	(5.19)	(4.24)	(3.76)	(-6.71)
B. Patent publication	0.130	0.182	-0.015	-0.335	0.085	-0.191
	(4.33)	(7.25)	(-0.37)	(-8.41)	(2.73)	(-5.75)
$\log(a + vol/shrout)$			III. Log	turnover		
A. Patent grant	-0.035	-0.004	0.013	0.016	0.021	-0.017
	(-12.44)	(-1.76)	(6.45)	(6.57)	(7.35)	(-7.00)
B. Patent publication	0.001	0.018	-0.019	-0.012	-0.009	-0.002
	(0.13)	(3.82)	(-2.29)	(-1.20)	(-1.76)	(-0.36)
$\log\left(\frac{a+vol/shrout}{a+vol/shrout}\right)$		IV	. Log rela	tive turno	ver	
A. Patent grant	-0.037	-0.005	0.013	0.016	0.020	-0.023
	(-16.14)	(-2.59)	(8.23)	(8.12)	(8.23)	(-12.34)
B. Patent publication	0.016	0.024	0.011	-0.043	0.002	-0.025
	(5.94)	(9.49)	(2.59)	(-10.58)	(0.49)	(-7.45)

Table shows the output of the regression of variants of share turnover  $(x_{t+k} = vol_t/shrout_t)$  on a dummy variable taking the value 1 if a patent was granted to the firm on day t (Panel A), or the USPTO publicized the grant application of the firm on day t (Panel B). Each column in these panels represents a regression. We include firm-year and day-of-week fixed effects. We cluster standard errors by year and report t-statistics in parenthesis. We restrict the sample to firms that have been granted at least one patent.

Table 4: Which firms innovate?

(1)	(2)	(3)	(4)
0.062	0.067	0.076	0.035
(39.55)	(40.40)	(43.12)	(34.17)
	0.035	0.028	0.020
	(19.82)	(14.96)	(20.11)
		0.068	0.030
		(28.38)	(23.07)
			0.742
			(88.33)
141695	141695	65234	65058
0.644	0.671	0.739	1.242
	0.062 (39.55) 141695	0.062	0.062

Table shows Tobit regressions of firm-level innovation  $A_{ft}$  on firm characteristics: log firm size ( $K_{ft}$ , gross PPE), log Tobin's Q and log R&D expenditures to book assets  $\ln RD$ . All specifications include year (T) and industry (I) fixed effects. Standard errors are clustered by firm.

Table 5: Number of future citations and announcement day return: 5-day window

		Five-day window – ([t, t+4])						
		Gran	t Day		Publication Day			
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
$\log(1+N)$			I. Log n	umber of	citations	s plus one	e	
$\log \hat{A}$	0.037	0.195	0.106	0.054	0.030	0.048	0.036	0.013
	(8.99)	(5.79)	(5.72)	(5.21)	(5.77)	(5.79)	(4.40)	(1.17)
$R^2$	0.289	0.295	0.401	0.426	0.244	0.249	0.317	0.355
$\hat{A}$	1.543	0.412	0.102	0.361	0.224	-0.642	-0.323	-0.196
	(8.49)	(2.12)	(1.85)	(4.42)	(1.74)	(-3.99)	(-1.81)	(-1.14)
$R^2$	0.285	0.293	0.400	0.426	0.239	0.248	0.318	0.355
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
N			II	. Number	of citati	ons		
$\log \hat{A}$	0.676	3.212	1.802	1.088	0.249	0.385	0.282	0.217
	(7.75)	(4.54)	(4.72)	(4.13)	(3.96)	(4.38)	(4.28)	(2.17)
$R^2$	0.097	0.104	0.221	0.262	0.322	0.104	0.108	0.186
$\hat{A}$	32.377	17.706	8.328	12.581	4.195	-1.764	-1.553	1.003
	(6.36)	(3.68)	(2.66)	(3.83)	(2.04)	(-1.53)	(-1.73)	(0.82)
$R^2$	0.095	0.103	0.221	0.262	0.099	0.107	0.186	0.233
Controls								
Fixed Effects	Т	Τ	TxC	$_{\mathrm{TxC,F}}$	Т	Τ	TxC	$_{\mathrm{TxC,F}}$
Volatility	-	Y	Y	Y	_	Y	Y	Y
Firm Size	_	Y	Y	Y	_	Y	Y	Y
# patents	-	Y	Y	Y	_	Y	Y	Y
granted same day								

Table is the counterpart to Table 3 in the text, but we now use the five day (t, t+4) stock market reaction around the patent grant day (columns 1-4) or the day the application is publicized by the USPTO (columns 5-8).

Table 6: Firm-level reallocation: raw stock market reaction

$i_{t+1}$		I.	Investme	nt	
	(1)	(2)	(3)	(4)	(5)
$ar{A}_{It}$	0.500	0.441	0.738	-0.982	-0.990
	(2.75)	(2.43)	(4.29)	(-4.53)	(-4.56)
$ar{A}_{ft}$	1.073	0.831	0.930	-0.302	-0.323
	(7.12)	(5.49)	(6.37)	(-2.08)	(-2.23)
$R^2$	0.084	0.091	0.220	0.259	0.260
$n_{t+1}$		II.	Labor hir	ing	
	(1)	(2)	(3)	(4)	(5)
$ar{A}_{It}$	2.274	2.210	2.317	0.251	0.226
	(7.18)	(7.02)	(7.32)	(0.73)	(0.66)
$ar{A}_{ft}$	2.637	2.375	2.198	0.556	0.510
	(10.31)	(9.32)	(8.72)	(2.21)	(2.03)
$R^2$	0.039	0.044	0.053	0.086	0.088
$e_{t+1}$		III. F	inancial ii	nflows	
	(1)	(2)	(3)	(4)	(5)
$ar{A}_{It}$	1.809	1.853	2.017	1.160	1.122
	(6.71)	(6.88)	(7.36)	(4.30)	(3.97)
$ar{A}_{ft}$	-0.020	0.159	0.150	-0.937	-0.808
	(-0.07)	(0.58)	(0.55)	(-3.41)	(-2.96)
$R^2$	0.114	0.117	0.155	0.184	0.219
Observations	126727	126727	126727	126727	126727
Fixed Effects	I,T	$_{\rm I,T}$	$_{\rm I,T}$	$_{\rm I,T}$	$_{\mathrm{I,T}}$
(Size)	Y	Y	Y	Y	Y
$(\sigma)$	-	Y	Y	Y	Y
$(x_t)$	-	-	Y	Y	Y
$(R_f, R_I, Q)$	-	-	-	Y	Y
(ROA)	-	-	-	-	Y

Table is the counterpart to firm level real location tables in main text, but we now construct our innovation measure using the raw stock market reaction  $\bar{A}$  instead of  $\hat{A}$ .

Table 7: Firm-level reallocation: number of patents

$i_{t+1}$		I.	Investme	nt	
	(1)	(2)	(3)	(4)	(5)
$P_{It}$	-0.365	-0.399	-0.266	-0.280	-0.281
	(-5.63)	(-6.05)	(-5.68)	(-5.99)	(-6.02)
$P_{ft}$	0.243	0.239	0.231	0.197	0.204
	(9.63)	(9.19)	(12.03)	(9.81)	(10.12)
$R^2$	0.085	0.092	0.220	0.260	0.261
$n_{t+1}$		II.	Labor hir	ing	
	(1)	(2)	(3)	(4)	(5)
$P_{It}$	-0.118	-0.163	-0.157	-0.167	-0.166
	(-1.42)	(-1.96)	(-1.98)	(-2.13)	(-2.14)
$P_{ft}$	0.166	0.152	0.196	0.142	0.156
	(5.52)	(5.10)	(6.94)	(4.65)	(5.12)
$R^2$	0.038	0.044	0.053	0.086	0.088
$e_{t+1}$		III. F	inancial ii	nflows	
	(1)	(2)	(3)	(4)	(5)
$P_{It}$	-0.432	-0.407	-0.336	-0.380	-0.376
	(-5.11)	(-4.87)	(-4.85)	(-5.39)	(-6.11)
$P_{ft}$	0.182	0.184	0.174	0.118	0.054
	(5.04)	(5.23)	(6.12)	(3.60)	(1.82)
$R^2$	0.114	0.117	0.155	0.182	0.219
Observations	126727	126727	126727	126727	126727
Fixed Effects	I,T	$_{\rm I,T}$	$_{\rm I,T}$	$_{\rm I,T}$	$_{\mathrm{I,T}}$
(Size)	Y	Y	Y	Y	Y
$(\sigma)$	-	Y	Y	Y	Y
$(x_t)$	-	-	Y	Y	Y
$(R_f, R_I, Q)$	-	-	-	Y	Y
(ROA)	-	-	-	-	Y

Table is the counterpart to firm level real location tables in main text, but we now construct our innovation measure using the total number of patents P granted to firm f in year t.

Table 8: Firm-level reallocation: Number of patents, weighted by citations

$i_{t+1}$		I.	Investme	nt	<u></u>
	(1)	(2)	(3)	(4)	(5)
$\hat{P}_{It}$	-0.028	-0.025	-0.016	-0.033	-0.034
	(-3.47)	(-3.16)	(-2.84)	(-5.76)	(-5.82)
$\hat{P}_{ft}$	0.028	0.028	0.026	0.019	0.020
	(10.46)	(10.01)	(12.88)	(9.77)	(10.08)
$R^2$	0.085	0.092	0.220	0.260	0.261
$n_{t+1}$		II.	Labor hir	ring	
	(1)	(2)	(3)	(4)	(5)
$\hat{P}_{It}$	-0.042	-0.040	-0.038	-0.060	-0.061
	(-3.80)	(-3.63)	(-3.57)	(-5.75)	(-5.82)
$\hat{P}_{ft}$	0.015	0.014	0.018	0.008	0.009
	(4.90)	(4.52)	(6.36)	(2.82)	(3.28)
$R^2$	0.039	0.044	0.053	0.086	0.088
$e_{t+1}$		III. F	inancial i	nflows	
	(1)	(2)	(3)	(4)	(5)
$\hat{P}_{It}$	-0.019	-0.020	-0.019	-0.033	-0.034
	(-1.93)	(-2.12)	(-2.28)	(-4.01)	(-4.52)
$\hat{P}_{ft}$	0.018	0.018	0.017	0.008	0.001
	(4.80)	(4.97)	(5.72)	(2.22)	(0.39)
$R^2$	0.114	0.117	0.155	0.181	0.219
Observations	126727	126727	126727	126727	126727
Fixed Effects	I,T	$_{\rm I,T}$	$_{\rm I,T}$	$_{\rm I,T}$	$_{\mathrm{I,T}}$
(Size)	Y	Y	Y	Y	Y
$(\sigma)$	-	Y	Y	Y	Y
$(x_t)$	-	-	Y	Y	Y
$(R_f, R_I, Q)$	-	-	-	Y	Y
(ROA)	_	-	-	-	Y

Table is the counterpart to firm level real location tables in main text, but we now construct our innovation measure using  $\hat{P}$ , the total number of patents granted to firm f in year t weighted by the number of forward citations.

Table 9: Firm-level productivity

			I. Raw	Measure		
$z_{t+1}^k,z_{t+1}^l$		Capital			Labor	
	(1)	(2)	(3)	(4)	(5)	(6)
$ar{A}_{It}$	5.923	5.801	2.368	5.860	5.744	3.293
	(10.49)	(10.36)	(3.90)	(11.33)	(11.17)	(6.00)
$ar{A}_{ft}$	3.671	3.205	1.555	2.088	1.700	0.691
	(5.76)	(5.03)	(2.46)	(3.55)	(2.89)	(1.18)
$R^2$	0.844	0.845	0.847	0.847	0.848	0.849
		I	I. Number	of paten	ts	
$z_{t+1}^k,z_{t+1}^l$		Capital			Labor	
	(1)	(2)	(3)	(4)	(5)	(6)
$P_{It}$	0.064	-0.002	0.002	-0.179	-0.239	-0.241
	(0.48)	(-0.02)	(0.02)	(-1.53)	(-2.04)	(-2.04)
$P_{ft}$	0.629	0.626	0.640	0.726	0.713	0.716
	(11.90)	(11.45)	(11.63)	(14.35)	(13.76)	(13.64)
$R^2$	0.844	0.845	0.847	0.847	0.848	0.850
	III.	Number o	of patents	, weighte	d by citat	ions
$z_{t+1}^k,z_{t+1}^l$		Capital			Labor	
	(1)	(2)	(3)	(4)	(5)	(6)
$\hat{P}_{It}$	-0.026	-0.020	-0.041	-0.010	-0.004	-0.021
	(-1.72)	(-1.30)	(-2.67)	(-0.70)	(-0.32)	(-1.56)
$\hat{P}_{ft}$	0.062	0.062	0.061	0.076	0.075	0.074
	(13.17)	(12.87)	(12.73)	(16.49)	(16.04)	(15.64)
$R^2$	0.844	0.845	0.847	0.848	0.849	0.850
Observations	125678	125678	125678	120020	120020	120020
Fixed Effects	I,T	$_{\mathrm{I,T}}$	$_{\rm I,T}$	I,T	$_{\rm I,T}$	$_{\rm I,T}$
(Size, $x_{t-1}$ )	Y	Y	Y	Y	Y	Y
$(\sigma)$	-	Y	Y	-	Y	Y
$(R_f, R_I, q)$	-	-	Y	-	-	Y

Table is the counterpart to productivity regressions in the main text, but we now construct our innovation measure using a)  $\bar{A}$ , raw stock market reaction; b) P, the total number of patents granted to firm f in year t; c)  $\hat{P}$ , the total number of patents granted to firm f in year t, weighted by the number of forward citations .

Table 10: Innovation and aggregate variables, OLS specifications

I. TFP growth									
$\Delta x_{t+T}$	T=1	T=2	T=3	T=4	T=5	T=6			
$\Delta \ln A_t$	0.0027	0.0054	-0.0004	0.0014	0.0004	-0.0015			
	(2.42)	(2.62)	(-0.20)	(0.56)	(0.17)	(-0.68)			
$R^2$	0.021	0.089	0.000	0.007	0.001	0.007			
$\Delta \ln A_t$	0.0031	0.0045	0.0006	0.0041	0.0010	-0.0005			
	(2.92)	(2.68)	(0.34)	(4.05)	(0.42)	(-0.22)			
$\Delta x_t$	0.2334	0.0144	0.1485	0.1964	0.0400	0.0643			
	(3.33)	(0.17)	(1.73)	(3.04)	(0.40)	(1.13)			
$R^2$	0.074	0.067	0.024	0.079	0.004	0.007			
		II. (	Output gro	owth					
$\Delta y_{t+T}$	T=1	T=2	T=3	T=4	T=5	T=6			
$\Delta \ln A_t$	-0.0106	-0.0060	-0.0035	0.0066	0.0093	0.0059			
	(-1.93)	(-0.67)	(-0.54)	(1.81)	(2.26)	(1.23)			
$R^2$	0.038	0.012	0.004	0.016	0.038	0.016			
$\Delta \ln A_t$	-0.0058	-0.0027	0.0021	0.0076	0.0042	0.0056			
	(-1.19)	(-0.29)	(0.57)	(2.02)	(1.87)	(1.02)			
$\Delta y_t$	0.4550	0.0631	-0.1702	-0.2828	-0.1515	0.0062			
	(5.34)	(0.51)	(-2.88)	(-3.07)	(-2.24)	(0.07)			
$R^2$	0.234	0.007	0.040	0.139	0.044	0.014			
		III. Cor	sumption	growth					
$\Delta c_{t+T}$	T=1	T=2	T=3	T=4	T=5	T=6			
$\Delta \ln A_t$	-0.0081	-0.0043	-0.0024	0.0008	0.0034	0.0031			
	(-2.75)	(-0.98)	(-0.74)	(0.41)	(2.03)	(1.96)			
$R^2$	0.131	0.037	0.013	0.002	0.040	0.038			
$\Delta \ln A_t$	-0.0060	-0.0031	0.0011	0.0021	0.0021	0.0032			
	(-2.43)	(-0.76)	(0.77)	(1.43)	(1.42)	(1.55)			
$\Delta c_t$	0.4687	0.1733	-0.0829	-0.2460	-0.0221	-0.0270			
	(5.82)	(1.82)	(-1.47)	(-2.77)	(-0.37)	(-0.58)			
$R^2$	0.327	0.057	0.015	0.131	0.017	0.039			

Table shows regressions of 1-period growth rate in z, T periods from now,  $\Delta z_{t+T} \equiv z_{t+T} - z_{t+T-1}$  on log changes in our innovation aggregate measure A. We show results for log TFP, output and consumption,  $z \in \{x, y, c\}$ . We standardize changes in  $\ln A$  to unit standard deviation. Standard errors are Newey-West, with automatic lag length selection.

Figure 1: Number of Patents with Matched Assignees

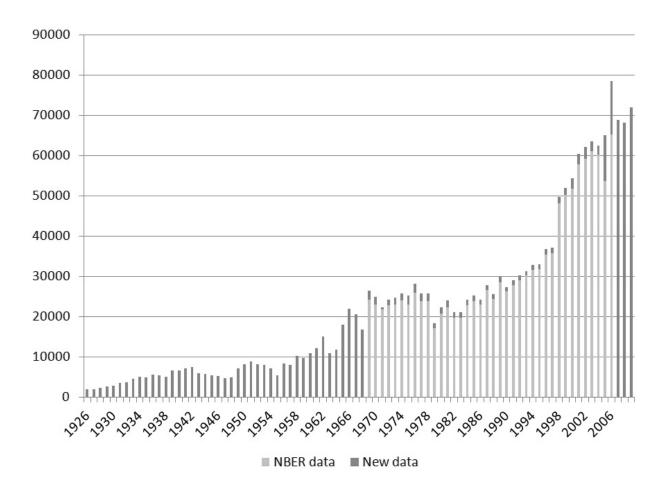


Figure shows the number of patents matched to CRSP firms by year of patent grant. Light shading denotes patents included in the NBER patent data set, while dark shading denotes patents that are new in our paper.

Figure 2: Firm innovation measures – Tail distribution

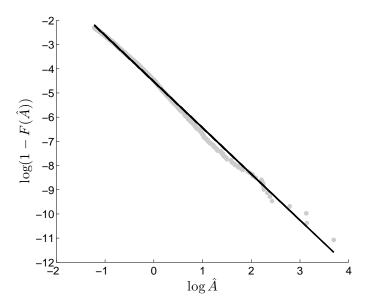


Figure plots the log complementary empirical cdf,  $\log(1 - F(A))$ , versus the log value of the firm-level innovation measure,  $\log A$ , for the top 10 percent of the distribution.

Figure 3: Impulse responses, controlling for volatility

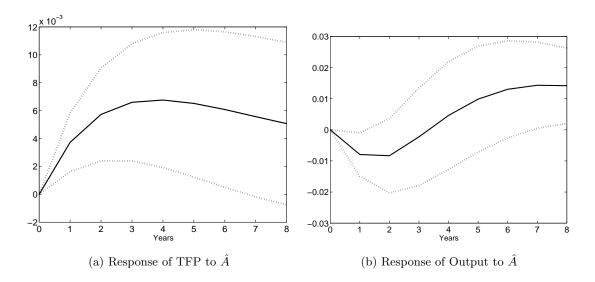


Figure shows impulse response of total factor productivity (Panel a) and gross domestic product (Panel b) from a VAR including  $[\log X, \log \sigma, \log \hat{A}]$ . We include the log cross-sectional average of idiosyncratic volatility  $\sigma$ . We include a deterministic trend in all specifications. We select lag length based on the AIC criterion. Dotted lines represent 90% confidence intervals using standard errors are computed using 500 bootstrap simulations.

Figure 4: Impulse responses, controlling for level of stock prices

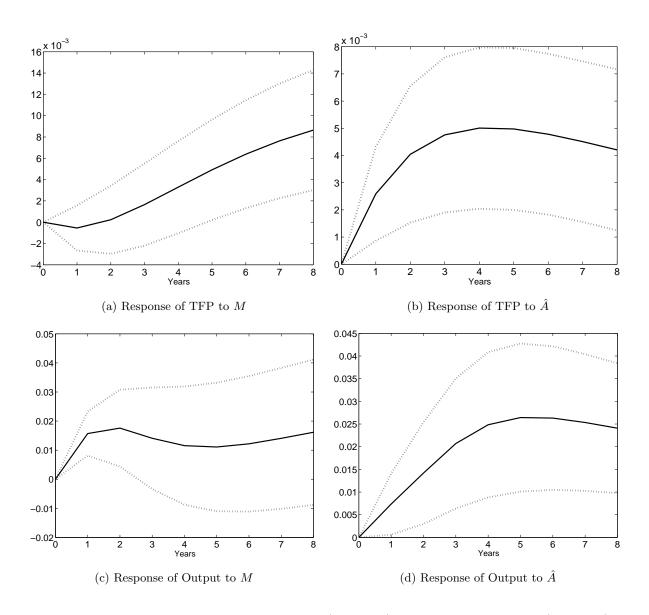
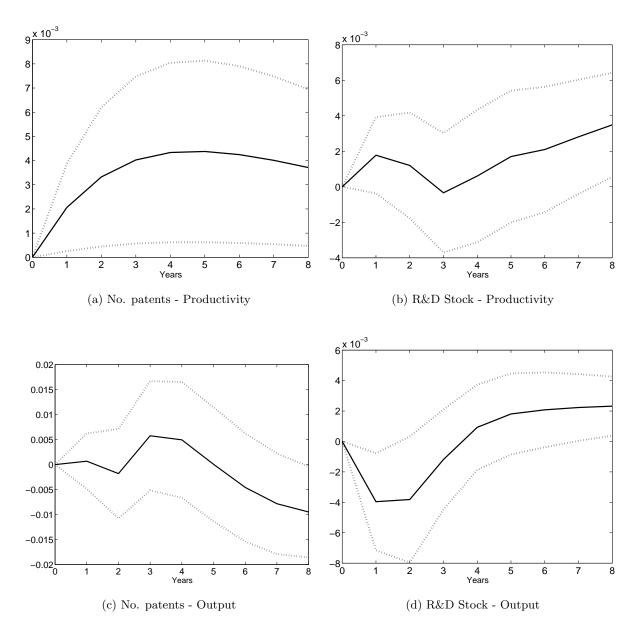


Figure shows impulse response of total factor productivity (Panels a-b) and gross domestic product (Panels c-d) from a VAR including  $[\log X, \log M, \log \hat{A}]$ , where M is the stock market level deflated by the price deflator and population growth, following Beaudry and Portier (2006). Right panel shows impulse response to our innovation measures. Left panel shows response to per-capita real stock market level. We include a deterministic trend in all specifications. We select lag length based on the AIC criterion. Dotted lines represent 90% confidence intervals using standard errors are computed using 500 bootstrap simulations.

Figure 5: Impulse responses using Number of Patents and R&D Stock



Left panel shows impulse response of log productivity and output from a bi-variate VAR  $[\log X_t, \log N_t]$  with a deterministic trend. Right panel shows impulse response of log productivity and output from a bi-variate VAR  $[\log X_t, \log RD_t]$  with a deterministic trend. Dotted lines represent 90% confidence intervals.

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