# Discussion of "O-Ring Production Networks" by Demir, Fieler, Xu, Yang

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### Firms that pay high wages have suppliers that pay high wages



Figure: Turkish manufacturing firm-to-firm (VAT) data, 2011-2015

#### DFXY empirical facts

- strong positive assortative matching: high-wage firms have high-wage suppliers
- decomposition: extensive margin  $\sim 60\%$ , intensive margin  $\sim 40\%$
- shift-share regressions: increase in foreign demand for high quality goods (from rich foreign country)
  - exporting firm's own wage increases
  - suppliers' wages increase
- in DFXY quantitative model: firm's wage reflects latent variable "quality"
  - positive assortative matching in quality: extensive & intensive
  - increase in foreign demand for high quality goods  $\rightarrow$  exporting firms upgrade quality

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### Extremely stripped-down version of DFXY model

#### Firms

• mass of firms  $i \in [0,1]$  with qualities

$$q_i \in Q \subseteq \mathbb{R}_+$$

• distribution of firms over qualities

j(q)

production function

$$X_i = z_i F(L_i, Y(q_i))$$

 ${\ensuremath{\bullet}}$  input bundle CES over supplier qualities q'

$$Y(q_i) = \left[\int y(q')^{\frac{\sigma-1}{\sigma}} \phi_y(q_i,q')^{1/\sigma} dq'\right]^{\sigma/(\sigma-1)}$$

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#### Firm Problem: intensive margin

cost minimization

$$C(q_i) = \min \int p(q') y(q') dq'$$

subject to

$$Y(q_i) = \left[\int y(q')^{\frac{\sigma-1}{\sigma}} \phi_y(q_i,q')^{1/\sigma} dq'\right]^{\sigma/(\sigma-1)}$$

• FOC implies CES demand for firm of quality  $q_i$ 

$$\frac{y(q_1')}{y(q_2')} = \left[\frac{p(q_1')}{p(q_2')}\right]^{-\sigma} \underbrace{\frac{\phi_y(q_i, q_1')}{\phi_y(q_i, q_2')}}_{\text{intensive}}$$

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#### Intensive margin

• intensive margin governed by

$$\frac{\phi_y(q_i,q_1')}{\phi_y(q_i,q_2')}$$

- increasing in quality of firm  $q_i$  iff  $q_1' > q_2'$
- a.k.a.  $\phi_y$  is log-supermodular
- quality complementarity: high quality firms buy more from high quality suppliers

### Intensive Margin

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Figure:  $\phi_y(q,q')$ 

## High q firms buy more from high q suppliers



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#### Firm Problem: extensive margin

• firms must post mass of ads in order to attract suppliers (m) and buyers (v)

 $\max_{v,m} \pi(q_i,v,m) - c^m(m) - c^v(v)$ 

• determines optimal mass of ads

 $m(q_i)$  and  $v(q_i)$ 

• buyers of quality q: passive, just posts ads m(q)

• sellers of quality q': posts ads v(q') directed towards buyers of quality q according to

$$\phi_{\scriptscriptstyle \! V}(q,q') \qquad {\sf pdf} \; {\sf of} \; \; {\cal N}(q',\sigma_{\scriptscriptstyle \! V}^2)$$



suppliers

buyers

Figure: supplier network formation



suppliers



buyers

Figure: supplier network formation

#### Search & Matching



buyers

#### Search & Matching



buyers

#### Search & Matching



buyers

### Consider a buyer of quality $q_i$

• buyer's ratio of matches with suppliers of quality  $q_1'$  and  $q_2'$ 

$$\underbrace{\frac{j(q_1')\nu(q_1')}{j(q_2')\nu(q_2')}}_{(q_2')\nu(q_2')}\underbrace{\frac{\phi_{\nu}(q_i,q_1')}{\phi_{\nu}(q_i,q_2')}}_{(q_1')\nu(q_1')\nu(q_1')}$$

extensive

#### Extensive margin



suppliers

buyers

#### Extensive margin



suppliers

#### buyers

High q firms have relatively more matches with high q suppliers

extensive margin governed by

$$\frac{\phi_v(q_i,q_1')}{\phi_v(q_i,q_2')}$$

- increasing in quality of firm  $q_i$  iff  $q'_1 > q'_2$ ,
- a.k.a.  $\phi_v$  is log-supermodular
- one-sided directed search leads to positive assortative matching

### Endogenous Quality Choice

• firm's quality q is actually endogenous:

 $\max_{q \in \mathcal{Q}} \Pi(q, z(q), \delta)$ 

- ▶ z(q) is Hicks-neutral productivity (recall production function  $X_i = z_i F(L_i, Y_i)$ )
- let  $\delta$  parameterize foreign demand shock

#### Endogenous Quality Choice

 $\max_{q \in Q} \Pi(q, z(q), \delta)$ 

FOC

$$\frac{\partial \Pi(\cdot)}{\partial q} + \frac{\partial \Pi(\cdot)}{\partial z} \frac{\partial z(q)}{\partial q} = 0$$

• why an interior  $q^* \in Q$ ?

• trade-off between quality q and productivity z

$$\exists ilde{Q} \subseteq Q \qquad ext{ s.t. } \qquad rac{\partial z(q)}{\partial q} < 0, \quad \forall q \in ilde{Q}$$

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### How does firm's quality choice respond to foreign demand shock?

 $\bullet\,$  Let  $q^*(\delta)$  denote firm's optimal quality choice for given foreign demand  $\delta\,$ 

#### Proposition

The firm's optimal choice  $q^*(\delta)$  is strictly increasing in  $\delta$  if and only if

 $\frac{\partial^2 \Pi(\cdot)}{\partial \delta \partial q} > 0$ 

i.e. foreign demand shock increases demand more for high quality goods than for low quality.

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#### Sketch of proof/intuition

• firm's optimal choice of  $q^*(\delta)$  determined implicitly by FOC

$$\frac{\partial \Pi(\cdot)}{\partial q} + z^{\gamma(\sigma-1)-1} \frac{\partial z(q)}{\partial q} = 0$$

• by the implicit function theorem,

$$\frac{dq^*}{d\delta} = -\left.\frac{\partial^2 \Pi(\cdot)}{\partial \delta \partial q}\right/ \frac{\partial^2 \Pi(\cdot)}{\partial q^2}$$

• as long as profits are concave in quality,

$$rac{dq^*}{d\delta} > 0 \qquad ext{iff} \qquad rac{\partial^2 \Pi(\cdot)}{\partial \delta \partial q} > 0$$

• firm upgrades quality in response to demand shock iff demand shock is complementary to quality

#### Conclusion

- Very impressive paper
  - novel and rich data set, interesting new empirical facts
  - quantitative model that fits facts/can be used for counterfactual exercises
- Comments on theory exposition:
  - intuition and theory for the trade-off firm faces when choosing quality
  - intuition and theory for upgrading quality in response to demand
  - intuition for why earnings-per-worker are increasing in quality
- I really enjoyed reading and thinking about this paper, and I learned a lot!