Contracting Frictions in Global Sourcing: Implications for Welfare

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Backdrop

Contracting frictions matter:

- ▶ for the pattern of trade (e.g., Levchenko 2007; Nunn 2007); and
- for the global sourcing of inputs (e.g., Antràs & Helpman 2004, 2008; Nunn & Trefler 2008, 2013; Bernard et al. 2010; Corcos et al. 2013; Defever & Toubal 2013).

We now have:

- ► Frameworks that spotlight how decisions over organizational mode i.e., integration vs outsourcing can help firms to cope with contracting frictions and holdup problems when they source from suppliers.
- Supporting empirical evidence, often based on the intrafirm trade share (to capture the propensity to integrate vs outsource).

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However: Less is known about *how much* considerations related to contracting frictions in global sourcing matter for aggregate outcomes such as welfare.

(Some exceptions: Fally & Hillberry 2018; Startz 2018; Boehm 2018; Oberfield & Boehm 2020)



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 - ... and the severity of contracting frictions, specifically: (i) the inherent contractibility of inputs; and (ii) the extent to which firm-supplier bargaining constrains production outcomes (a la Grossman-Hart-Moore)
- Adopt a nested-Fréchet specification for the joint distribution of supplier productivities across sourcing modes,
 - which facilitates aggregation (c.f., Lind and Ramondo 2019)

The model delivers:

- Sourcing: An EK type expression for sourcing shares by country-mode, but modified by the presence of contracting frictions
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 - Interpretation: Contracting frictions retard the effective state of technology accessible to input-sourcing firms.
- Gravity: A modified gravity equation for bilateral trade flows by source country and organizational mode
- Welfare: A closed-form expression for welfare change, in response to shifts in trade costs or contracting frictions
 - ▶ Nests ACR (2012) and Costinot and Rodriguez-Clare (2014)
 - ... while highlighting new effects introduced by the presence of contracting frictions.

Propose an estimation strategy.

- Based on:
 - a structural estimating equation where the dependent variable is the intrafirm trade share; and
 - (ii) a functional form for how country variables (such as rule of law) or industry characteristics (such as contractibility) map into the contractibility and bargaining parameters that underlie the contracting frictions.

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 - Intrafirm trade shares at the industry level (e.g., from the U.S. Related Party Database), with key parameters estimated via NLLS

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- Relatively low data requirements for implementation:
 - Intrafirm trade shares at the industry level (e.g., from the U.S. Related Party Database), with key parameters estimated via NLLS
- Provides all the pieces we need to evaluate welfare counterfactuals. E.g.:
 - a hypothetical removal of contracting frictions in global sourcing
 - an improvement in the institutional rule of law that alleviates frictions faced in input sourcing for a particular country



Remarks

- Model has a good number of building blocks.
 - At the expense of over-simplifying: Think Grossman & Hart (1986), Antràs & Helpman (2008, with partial contractibility) meets quantitative trade.
- Rich counterfactuals. Today's exercises:
 - A global removal of contracting frictions in input sourcing: Average welfare gain of 3.5%.
 - Contracting frictions and the gains from trade.
 - An improvement in rule of law in China.
- ► Caveat: Production structure is more of a "spider".

(For GVC "snakes", see: Costinot et al. 2013; Antràs & Chor 2013; Alfaro et al. 2019; Antràs & de Gortari 2020; etc.)

Roadmap for this talk

- 1. Motivation and Introduction
- 2. Model: Contracting Frictions and Global Sourcing meets Quantitative Trade
- 3. Taking the Model to the Data
- 4. Estimation and Counterfactuals
- 5. Concluding remarks and next steps

Setup Preliminaries Sourcing Decisions Aggregation and Welfare

Contracting Frictions and Global Sourcing in a Quantitative Trade Model

Utility

J countries (indexed by j).

Representative consumer derives utility from final-good varieties (indexed by ω):

$$U_j = \left(\int_{\omega \in \Omega} c_j(\omega)^{
ho} d\omega
ight)^{rac{1}{
ho}}$$
 , $ho \in (0,1).$

Assume a fixed measure of firms, N_j . Associate each ω with a final-good firm whose core productivity ϕ is an iid draw from $G_j(\phi)$.

We have:

$$q_j(\phi) = A_j p_j(\phi)^{-\frac{1}{1-\rho}},$$

 $R_j(\phi) = A_i^{1-\rho} q_j(\phi)^{\rho}.$

where $A_j = I_j P_j^{\frac{\rho}{1-\rho}}$ is a function of total country-j income, I_j .

Final-good Production

- ► Each final-good variety is produced using inputs from *K* industries (a la CDK 2012), and assembled with domestic labor. (Final-goods are not traded.)
- ▶ Within each industry k, input varieties ℓ are sourced globally.

$$y_j(\phi) = \phi \left(\prod_{k=1}^K \left(X_j^k(\phi) \right)^{\eta^k} \right)^{1-\alpha} L_j(\phi)^{\alpha}, \text{ where}$$
 (2)

$$X_j^k(\phi) = \left(\int_{\ell=0}^1 \tilde{x}_j^k(\phi;\ell)^{\rho^k} d\ell\right)^{\frac{1}{\rho^k}}.$$

- $X_j^k(\phi)$: Composite industry-k input, from a unit measure of input varieties, $\tilde{x}_i^k(\phi;\ell)$. (c.f., Tintelnot 2017, Antràs et al. 2017)
- $ightharpoonup L_i(\phi)$: Labor used in final assembly.
- Assume: $0 < \alpha < 1$; $0 < \eta^k < 1$; $\sum_k \eta^k = 1$; $0 < \rho < \rho^k < 1$.

Final-good Production

$$X_j^k(\phi) = \left(\int_{\ell=0}^1 \tilde{x}_j^k(\phi;\ell)^{\rho^k} d\ell\right)^{\frac{1}{\rho^k}}$$

▶ Each input variety combines firm headquarter services, $h_j^k(\phi; \ell)$, and supplier inputs, $x_j^k(\phi; \ell)$, both of which are relationship-specific:

$$\tilde{x}_j^k(\phi;\ell) = \left[h_j^k(\phi;\ell)\right]^{\alpha^k} \left[x_j^k(\phi;\ell)\right]^{1-\alpha^k}, \ 0 < \alpha^k < 1.$$

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 $h_j^k(\phi;\ell)$ (resp., $x_j^k(\phi;\ell)$) comprises a measure $\mu_{hij}^k \in [0,1]$ (resp., $\mu_{xij}^k \in [0,1]$) of contractible tasks. (Acemoglu et al. 2007, Antràs and Helpman 2008)

$$\begin{split} & h_j^k(\phi;\ell) = \exp\left\{\int_{\iota=0}^{\mu_{hij}^k} \log h_j^k(\iota;\phi,\ell) d\iota + \int_{\iota=\mu_{hij}^k}^1 \log h_j^k(\iota;\phi,\ell) d\iota \right\}, \\ & x_j^k(\phi;\ell) = \exp\left\{\int_{\iota=0}^{\mu_{xij}^k} \log x_j^k(\iota;\phi,\ell) d\iota + \int_{\iota=\mu_{xij}^k}^1 \log x_j^k(\iota;\phi,\ell) d\iota \right\}. \end{split}$$

Input Sourcing and Bargaining

For each input variety, ℓ :

- Let source country be i and organizational mode be $\chi \in \{V, O\}$ (V: integration; O: outsourcing)
- \triangleright 2*J* possible "sourcing modes", (i, χ)
- Firm obtains a set of 2J productivity draws associated with a given input variety ℓ for each of the possible sourcing modes
- ▶ In each sourcing country i, \exists a large number of potential suppliers that can deliver the input using the (i, χ) productivity draw
- Based on these draws, firm decides on the optimal sourcing mode for each input variety ℓ .

Input Sourcing and Bargaining

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- \triangleright 2*J* possible "sourcing modes", (i, χ)
- In this incomplete contracting environment with bilateral holdup, payoffs are determined in ex-post negotiation between the firm and each supplier.
- $\triangleright \beta_{iiv}^k$: Generalized Nash bargaining share that accrues to the firm under sourcing mode (i, χ) . Varies by:
 - Source country i: Rule of law.
 - Industry k: Specificity.
- Assume: $0 < \beta_{iiO}^k < \beta_{iiV}^k < 1$, reflecting the firm's greater residual rights of control when it has ownership over the supplier (Grossman and Hart 1986)

Input Sourcing and Bargaining: Timing

- Firm observes its productivity draws (for all input varieties and sourcing modes)
- ightharpoonup Firm posts contracts for a supplier for each input variety ℓ , specifying:
 - (i) an ex-ante participation fee;
 - (ii) the sourcing mode over ℓ ; and
 - (iii) the investment levels for contractible tasks, $h_j^k(\iota;\phi,\ell)$ for $\iota\in[0,\mu_{hij}^k]$ and $x_j^k(\iota;\phi,\ell)$ for $\iota\in[0,\mu_{xij}^k]$, as well as for $L_j(\phi)$.
- Firm picks a supplier for each ℓ
- Supplier of ℓ chooses how much to invest in providing the non-contractible input services: $x_i^k(\iota; \phi, \ell)$ for $\iota \in (\mu_{hij}^k, 1], \ldots$
- Firm simultaneously chooses how much to invest in the non-contractible headquarter services: $h_j^k(\iota;\phi,\ell)$ for $\iota\in(\mu_{xij}^k,1]$.

Input Sourcing and Bargaining: Timing

- ▶ Firm and each supplier bargain over the incremental revenue contributed by the input variety ℓ, taking the investment levels for other inputs as given
- Incremental revenue $r_j^k(\phi;\ell)$ computed following heuristic from Acemoglu et al. (2007): Details

$$r_j^k(\phi;\ell) = (1 - \alpha) \frac{\rho \eta^k}{\rho^k} R_j(\phi) \left(\frac{\tilde{x}_j^k(\phi;\ell)}{X_j^k(\phi)} \right)^{\rho^k}. \tag{3}$$

Input Sourcing and Bargaining: Setup

Firm chooses $h_j^k(\iota; \phi, \ell)$ to maximize:

$$\beta_{ij\chi}^k r_j^k(\phi;\ell) - s_j \int_{\mu_{hij}^k}^1 h_j^k(\iota;\phi,\ell) d\iota. \tag{4}$$

where the firm's costs are in units of human capital.

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Supplier ℓ chooses $x_j^k(\iota; \phi, \ell)$ to maximize:

$$(1-\beta_{ij\chi}^k)r_j^k(\phi;\ell)-c_{ij\chi}^k(\phi;l)\int_{\mu_{xij}^k}^1 x_j^k(\iota;\phi,l)d\iota, \tag{5}$$

where $c_{ij\chi}^k$ is incurred in units of labor:

$$c_{ij\chi}^k(\phi;\ell) = \frac{d_{ij}^k w_i}{Z_{ij\chi}^k(\phi;\ell)}.$$
 (6)

- ▶ $d_{ij}^k \ge 1$: iceberg trade costs
- $ightharpoonup Z_{iix}^k(\phi;\ell)$: labor productivity

Specify a nested Fréchet for the joint distribution of the $Z_{ij\chi}^k(\phi;\ell)$'s over the 2J possible sourcing modes.

$$\textit{Pr}\left(Z^k_{1jV} \leq z^k_{1jV}, Z^k_{1jO} \leq z^k_{1jO}, \dots, Z^k_{JjO} \leq z^k_{JjO}\right) \text{ is given by:}$$

$$\exp\left\{-\sum_{i=1}^{J} T_{i}^{k} \left(\left(z_{ijV}^{k}\right)^{-\frac{\theta^{k}}{1-\lambda_{i}}} + \left(z_{ijO}^{k}\right)^{-\frac{\theta^{k}}{1-\lambda_{i}}}\right)^{1-\lambda_{i}}\right\},\tag{7}$$

where $\theta^k > 1$ and $0 < \lambda_i < 1$.

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Remarks:

- ► Analogue of the nested logit in discrete choice models.
- ▶ Relaxes the Independence of Irrelevant Alternatives (IIA) assumption inherent in Fréchet, . . . by introducing a correlation parameter λ_i for "within-nest" draws.

 $(\lambda_i = 0 \text{ for all } i \text{ gets us back to iid Fréchet.})$



Sourcing Decisions

- Solve for $h_i^k(\iota; \phi, \ell)$ and $x_i^k(\iota; \phi, \ell)$ for non-contractible input varieties from FOCs of firm and supplier ℓ .
- ▶ Bearing in mind the ex-ante transfer, firm specifies the contractible levels of investment and the sourcing mode to maximize:

$$r_j^k(\phi;\ell) - s_j \int_0^1 h_j^k(\iota;\phi,\ell) d\iota - c_{ij\chi}^k(\phi;l) \int_0^1 x_j^k(\iota;\phi,\ell) d\iota.$$

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Sourcing decision boils down to:

$$\arg\max_{(i,\chi)} \ \Xi_{ij\chi}^k Z_{ij\chi}^k$$

where: Details

$$\Xi_{ij\chi}^{k} = \left(\frac{(1-\alpha)\rho\eta^{k}R_{j}(\phi)}{(X_{j}^{k}(\phi))^{\rho^{k}}}\right)^{\frac{1}{\rho^{k}(1-\alpha^{k})}} \times \left(\frac{1-\rho^{k}}{\rho^{k}}\right)^{\frac{1-\rho^{k}}{\rho^{k}(1-\alpha^{k})}} \left(\frac{\zeta_{ij\chi}^{k}}{\zeta_{ij}^{k}}\right)^{\frac{\zeta_{ij}^{k}}{\rho^{k}(1-\alpha^{k})}} \times \left(\frac{\alpha^{k}}{s_{j}}\right)^{\frac{\alpha^{k}}{1-\alpha^{k}}} \left(\frac{1-\alpha^{k}}{d_{ij}^{k}w_{i}}\right) \left(\beta_{ij\chi}^{k}\right)^{\frac{\alpha^{k}(1-\mu_{hij}^{k})}{1-\alpha^{k}}} \left(1-\beta_{ij\chi}^{k}\right)^{1-\mu_{xij}^{k}}.$$
(8)

Share of inputs sourced under mode (i, χ) is equal to $\pi_{ii}^k \pi_{\chi | ii}^k$.

 $\triangleright \pi_{ii}^{k}$: Probability of sourcing from country i

$$\pi_{ij}^{k} = \frac{T_{i}^{k}(d_{ij}^{k}w_{i})^{-\theta^{k}}(B_{ij}^{k})^{\theta^{k}}}{\sum_{i'=1}^{J}T_{i'}^{k}(d_{i'j}^{k}w_{i'})^{-\theta^{k}}(B_{ij}^{k})^{\theta^{k}}} = \frac{T_{i}^{k}(d_{ij}^{k}w_{i})^{-\theta^{k}}(B_{ij}^{k})^{\theta^{k}}}{\Phi_{j}^{k}}, \qquad (9)$$

where: $\Phi_i^k \equiv \sum_{i'=1}^J T_{i'}^k (d_{i'i}^k w_{i'})^{-\theta^k} (B_{ii}^k)^{\theta^k}$ is the sourcing capability.

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where: $\Phi_j^k \equiv \sum_{i'=1}^J T_{i'}^k (d_{i'j}^k w_{i'})^{-\theta^k} (B_{ij}^k)^{\theta^k}$ is the sourcing capability.

▶ Compare with EK2002: Contracting frictions – the $(B_{ij}^k)^{\theta^k}$'s – distort the effective state of technology available to sourcing firms.

$$B_{ij}^{k} = \left(\frac{1}{2} \left[\left(B_{ijV}^{k}\right)^{\frac{\theta^{k}}{1-\lambda_{i}}} + \left(B_{ijO}^{k}\right)^{\frac{\theta^{k}}{1-\lambda_{i}}} \right] \right)^{\frac{1-\lambda_{i}}{\theta^{k}}}, \text{ where}$$
 (10)

$$B_{ij\chi}^k = \left(\zeta_{ij\chi}^k/\zeta_{ij}^k\right)^{\frac{\zeta_{ij}^k}{\rho^k(1-\alpha^k)}} \left(\beta_{ij\chi}^k\right)^{\frac{\alpha^k\left(1-\mu_{hij}^k\right)}{\left(1-\alpha^k\right)}} \left(1-\beta_{ij\chi}^k\right)^{\left(1-\mu_{\chi ij}^k\right)}.$$



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where: $\Phi_i^k \equiv \sum_{i'=1}^J T_{i'}^k (d_{i'i}^k w_{i'})^{-\theta^k} (B_{ii}^k)^{\theta^k}$ is the sourcing capability.

- Quick Lemma: B_{ii}^k is increasing in μ_{hii}^k and μ_{xii}^k . $B_{ii}^k \leq 1$, with equality iff $\mu_{hii}^k = \mu_{xii}^k = 1$ (i.e., full contractibility).
- Interpretation: B_{ii}^k terms capture the effect of contracting frictions on sourcing capability (of final-good firms in country i)

Share of inputs sourced under mode (i,χ) is equal to $\pi^k_{ij}\pi^k_{\chi|ij}$.

• $\pi^k_{\chi|j}$: probability of sourcing under organizational mode χ conditional on selecting country i

$$\pi_{\chi|ij}^{k} = \frac{\left(B_{ij\chi}^{k}\right)^{\frac{\theta^{k}}{1-\lambda_{i}}}}{\left(B_{ijV}^{k}\right)^{\frac{\theta^{k}}{1-\lambda_{i}}} + \left(B_{ijO}^{k}\right)^{\frac{\theta^{k}}{1-\lambda_{i}}}}.$$

- ► Conditional probability is a function of the $\beta^k_{ij\chi}$'s and other deep model parameters. (In particular: Does not depend on T^k_i , d^k_{ii} or w_i .)
- As in Antràs and Helpman (2008), propensity to integrate $(\pi^k_{V|ii})$ is:
 - increasing in μ_{xii}^k (supplier contractibility); and
 - decreasing in μ_{hii}^{k} (hq contractibility).



From Firm-level Decisions to Aggregate Variables

(i) Composite industry-k input, $X_j^k(\phi)$:

$$X_j^k(\phi)^{\rho^k} = \mathbb{E}_{\ell}\left[\tilde{x}_j^k(\phi;l)^{\rho^k}\right] \propto \mathbb{E}_{\ell}\left[\tilde{Z}_{ij\chi}^k(\phi;\ell)^{\frac{(1-\alpha^k)\rho^k}{1-\rho^k}}\right],$$

where $ilde{Z}^k_{ij\chi}(\phi;\ell)$ is the productivity from the optimal sourcing mode.



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▶ Details

(ii) Assembly labor, $L_j(\phi)$: Chosen to maximize the firm's overall payoff (after aggregating over the revenue and costs contributed by each input variety)

Upshot: $X_j^k(\phi)$, $L_j(\phi)$, and hence $q_j(\phi)$ are linear in $R_j(\phi)$.



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Details

(iii) Revenue, $R_j(\phi)$: After aggregation,

$$R_j(\phi) = I_j(\phi/\overline{\phi})^{\frac{\rho}{1-\rho}}$$
,

where
$$\bar{\phi} = \left(\int \phi^{\frac{1}{1-\rho}} dG_j(\phi)\right)^{\frac{1-\rho}{\rho}}$$
 and $I_j = \frac{w_j \bar{L}_j + s_j \bar{H}_j}{1 - (1-\alpha\rho)\hat{\Upsilon}_j}$.

Welfare

Plugging the expression for $q_i(\phi)$ into the utility function:

$$U_{j} = (N_{j})^{\frac{1-\rho}{\rho}} \rho I_{j} \frac{\alpha^{\alpha} (1-\alpha)^{1-\alpha}}{(w_{j})^{\alpha}} (\bar{\Upsilon}_{j})^{\alpha} \bar{\phi}$$

$$\times \prod_{k=1}^{K} \left[\left(\frac{\alpha^{k}}{\mathfrak{s}_{j}} \right)^{\alpha^{k}} \left(\frac{1-\alpha^{k}}{w_{j}} \right)^{1-\alpha^{k}} \eta^{k} \left(\frac{\bar{\Gamma}}{\Upsilon_{j}^{k}} \right)^{\frac{1-\rho^{k}}{\rho^{k}}} \left(\frac{T_{j}^{k}}{\pi_{jj}^{k}} \right)^{\frac{1-\alpha^{k}}{\theta^{k}}} (B_{jj}^{k})^{1-\alpha^{k}} \right]^{\eta^{k}(1-\alpha)}$$

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Will proceed to work instead with hat changes:

- ▶ Let $\hat{X} \equiv X'/X$.
- Consider shocks to either trade costs (the d_{ij}^k 's) or to contracting frictions (the μ_{hij}^k 's, μ_{xij}^k 's).

$$\widehat{U}_{j} = \widehat{I}_{j} (\widehat{w}_{j})^{-\alpha} \left(\prod_{k=1}^{K} \left[(\widehat{w}_{j})^{-(1-\alpha^{k})} (\widehat{s}_{j})^{-\alpha^{k}} \right]^{\eta^{k}(1-\alpha)} \right) (\widehat{\widehat{\Upsilon}}_{j})^{\alpha}$$

$$\times \prod_{k=1}^{K} \left[(\widehat{\Upsilon}_{j}^{k})^{-\frac{1-\rho^{k}}{\rho^{k}}} (\widehat{\pi_{jj}^{k}})^{-\frac{1-\alpha^{k}}{\rho^{k}}} (\widehat{B}_{jj}^{k})^{1-\alpha^{k}} \right]^{\eta^{k}(1-\alpha)}$$

(i)
$$\prod_{k=1}^{K} (\widehat{\pi_{jj}^{k}})^{-\frac{1-\alpha^{K}}{\theta^{k}}} \eta^{k} (1-\alpha)$$
: As in ACR (2012) and CR (2014)

$$\widehat{U_{j}} = \widehat{I_{j}} (\widehat{w_{j}})^{-\alpha} \left(\prod_{k=1}^{K} \left[(\widehat{w_{j}})^{-(1-\alpha^{k})} (\widehat{s_{j}})^{-\alpha^{k}} \right]^{\eta^{k}(1-\alpha)} \right) (\widehat{\widehat{\Upsilon}_{j}})^{\alpha}$$

$$\times \prod_{k=1}^{K} \left[(\widehat{\Upsilon_{j}^{k}})^{-\frac{1-\rho^{k}}{\rho^{k}}} (\widehat{\pi_{jj}^{k}})^{-\frac{1-\alpha^{k}}{\theta^{k}}} (\widehat{B_{jj}^{k}})^{1-\alpha^{k}} \right]^{\eta^{k}(1-\alpha)}$$

- (i) $\prod_{k=1}^K \widehat{(\pi_{ij}^k)}^{-\frac{1-\alpha^k}{\theta^k} \eta^k (1-\alpha)}$: As in ACR (2012) and CR (2014)
- (ii) $\prod_{k=1}^K (\widehat{B_{jj}^k})^{(1-\alpha^k)\eta^k(1-\alpha)}$: Contracting frictions' effect on sourcing capability

$$\widehat{U_{j}} = \widehat{I_{j}} (\widehat{w_{j}})^{-\alpha} \left(\prod_{k=1}^{K} \left[(\widehat{w_{j}})^{-(1-\alpha^{k})} (\widehat{s_{j}})^{-\alpha^{k}} \right]^{\eta^{k}(1-\alpha)} \right) (\widehat{\widehat{\gamma}_{j}})^{\alpha}$$

$$\times \prod_{k=1}^{K} \left[(\widehat{\gamma_{j}^{k}})^{-\frac{1-\rho^{k}}{\rho^{k}}} (\widehat{\pi_{jj}^{k}})^{-\frac{1-\alpha^{k}}{\theta^{k}}} (\widehat{B_{jj}^{k}})^{1-\alpha^{k}} \right]^{\eta^{k}(1-\alpha)}$$

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- (iii) $\prod_{k=1}^K \left(\widehat{\Upsilon_j^k}\right)^{-\frac{1-\rho^k}{\rho^k}\eta^k(1-\alpha)}$: Holding sourcing capability constant, contracting frictions' effect on relationship-specific input investments
- (iv) $\left(\widehat{\widehat{\Upsilon}_{j}}\right)^{\alpha}$: Contracting frictions' effect on choice of assembly labor

$$\widehat{U_{j}} = \widehat{I_{j}} (\widehat{w_{j}})^{-\alpha} \left(\prod_{k=1}^{K} \left[(\widehat{w_{j}})^{-(1-\alpha^{k})} (\widehat{s_{j}})^{-\alpha^{k}} \right]^{\eta^{k}(1-\alpha)} \right) (\widehat{\widehat{\Upsilon}_{j}})^{\alpha}$$

$$\times \prod_{k=1}^{K} \left[(\widehat{\Upsilon_{j}^{k}})^{-\frac{1-\alpha^{k}}{\rho^{k}}} (\widehat{\pi_{jj}^{k}})^{-\frac{1-\alpha^{k}}{\theta^{k}}} (\widehat{B_{jj}^{k}})^{1-\alpha^{k}} \right]^{\eta^{k}(1-\alpha)}$$

- (i) $\prod_{k=1}^K \widehat{(\pi_{ii}^k)}^{-\frac{1-\alpha^k}{\theta^k}} \eta^k (1-\alpha)$: As in ACR (2012) and CR (2014)
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- (iv) $\left(\widehat{\Upsilon}_{j}\right)^{\alpha}$: Contracting frictions' effect on choice of assembly labor
- (v) \widehat{w}_i , \widehat{s}_i , \widehat{l}_i terms: Factor price effects (in general equilibrium)

Trade flows by sourcing mode

Assume trade flows observed are valued at costs, and thus equal to factor payments to suppliers. Summing over all suppliers by sourcing mode (i, χ) :

$$t_{ij\chi}^{k} = \frac{(1-\alpha)\rho\eta^{k}}{\rho^{k}} \frac{\Upsilon_{j}^{k}}{\Phi_{j}^{k}} I_{j} \rho^{k} (1-\alpha^{k}) \mathcal{T}_{i}^{k} (w_{i})^{-\theta^{k}} \left(B_{ij}^{k}\right)^{-\frac{\theta^{k} \lambda_{i}}{1-\lambda_{i}}} \left(d_{ij}^{k}\right)^{-\theta^{k}}$$

$$\times \left(\mu_{xij}^{k} + (1-\mu_{xij}^{k})(1-\beta_{ij\chi}^{k}) \frac{\zeta_{ij}^{k}}{\zeta_{ij\chi}^{k}}\right) \frac{1}{2} \left(B_{ij\chi}^{k}\right)^{\frac{\theta^{k} \lambda_{i}}{1-\lambda_{i}}}.$$
 (11)

A gravity-like decomposition of terms into:

- ▶ a destination-country-by-industry component
- a source-country-by-industry component
- bilateral trade costs
- ightharpoonup a country-pair-by-industry-by-organizational-mode (χ) component

om Model to Estimation Strateg timates ounterfactuals

Taking the Model to the Data

Estimation: Framework

Empirical setting: U.S. Related Party Trade Database

- $ilde{t}_{ij\chi}^k$: Observed value of industry-k trade from country i to j, under mode $\chi \in \{V, O\}$. (Stack both the import j = US and export i = US data.)
- ▶ Map *k* to NAICS 3-digit industries.

Posit that trade flows from (11) are observed with error:

$$\tilde{t}_{ij\chi}^{k} = t_{ij\chi}^{k} \cdot \epsilon_{ij\chi}^{k} = \mathbf{a}_{ij\chi}^{k} \cdot \mathbf{a}_{ij}^{k} \cdot \epsilon_{ij\chi}^{k}, \tag{12}$$

where:

- $ightharpoonup a_{ij}^k$ collects terms that are specific to the country-pair-by-industry;
- ▶ Details
- $ightharpoonup a_{ij\chi}^k$ collects terms that further vary by organizational mode; and
- $ightharpoonup \epsilon_{ij\chi}^k$ is an iid Poisson noise term with unit mean (consistent with presence of zeros)

Implies a moment condition:

$$E\left[\frac{\tilde{t}_{ijV}^{k}}{\tilde{t}_{ij}^{k}}\left|\tilde{t}_{ij}^{k}\right.\right] = \frac{a_{ijV}^{k}a_{ij}^{k}}{\sum_{\chi=\{V,O\}}a_{ij\chi}^{k}a_{ij}^{k}} = \frac{a_{ijV}^{k}}{\sum_{\chi=\{V,O\}}a_{ij\chi}^{k}}.$$
 (13)

▶ Why? Under the Poisson assumption, $\tilde{t}^k_{ijV}/\tilde{t}^k_{ij}$ conditional on \tilde{t}^k_{ij} follows a Bernoulli distribution with success probability: $a^k_{ijV}a^k_{ij}/\sum_{\chi=\{V,O\}}a^k_{ij\chi}a^k_{ij}$.

▶ Alternative foundation: Replacing a_{ij}^k with its quasi-maximum likelihood estimator yields the same moment condition (Santos Silva and Tenreyro 2006; Fally 2015) ▶ Details

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Upshot: A structural estimating equation in which:

- the intrafirm trade share is the dependent variable; and
- ightharpoonup a_{ij\chi_x} on the RHS is a function of parameters: $eta_{ij\chi_x}^k$, μ_{hij}^k , μ_{xij}^k , α^k , θ^k , λ_i , ρ^k .

Estimation: Mapping the μ_{hij}^k 's, μ_{xij}^k 's to observables

▶ Since $\mu_{hij}^k, \mu_{xij}^k \in [0, 1]$, adopt a logistic function specification:

$$\mu_{hij}^k = \frac{e^{\mathbf{h}(i,k)}}{1 + e^{\mathbf{h}(i,k)}}, \quad \text{and} \quad \mu_{xij}^k = \frac{e^{\mathbf{x}(i,k)}}{1 + e^{\mathbf{x}(i,k)}}.$$

- ▶ h(i, k): full 2nd-order polynomial in HQContractibility^k, ROL_i, and ROL_j.
- ightharpoonup x(i,k): full 2nd-order polynomial in SSContractibility^k, ROL_i, and ROL_j.

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- $ightharpoonup \mathbf{x}(i,k)$: full 2nd-order polynomial in SSContractibility^k, ROL_i, and ROL_j.
- Distinguishing between hq and supplier contractibility:
 - Order industries according to their capital-intensity
 - HQContractibility^k: Weighted-average contractibility of inputs from NAICS industries with above-median capital-intensity (c.f., Nunn 2007).
 - SSContractibility^k: Analogous weighted-average contractibility of inputs from NAICS input industries with below-median capital-intensity
- ▶ ROL: Country rule-of-law index from the World Governance Indicators.



Estimation: Mapping the $\beta_{ij\chi}^k$'s to observables

- ▶ Set: $\beta_{ijV}^k = (1 \delta_{ij}^k)\beta_{ijO}^k + \delta_{ij}^k$, where $\delta_{ij}^k \in [0,1]$ is the share of bilateral surplus over which the firm has residual rights of control.
- Specify: $\beta_{ijO}^k = \beta_O$ (to be estimated)
- ▶ Since $\delta_{ij}^k \in [0,1]$:

$$\delta_i^k = \frac{e^{\mathbf{d}(i,k)}}{1 + e^{\mathbf{d}(i,k)}},$$

where $\mathbf{d}(i, k)$ is a full 2nd-order polynomial in Specificity^k, ROL_i, and ROL_j.

► Specificity^k: Industry specificity based on Rauch (1999)

Estimation: Mapping the α^k 's to observables

▶ For the α^k 's:

$$lpha^k = rac{e^{\mathbf{a}(i,k)}}{1 + e^{\mathbf{a}(i,k)}}$$
 ,

where $\mathbf{a}(i, k)$ is a quadratic in $\log(K/L)^k$.

▶ $log(K/L)^k$: Industry capital-labor ratio from the NBER CES Dataset (c.f., Antràs 2003)

$$m(\Theta) = \mathbb{E}\left[\frac{\tilde{t}_{ij\chi}^k}{\sum_{\chi \in \{V,O\}} \tilde{t}_{ij\chi}^k} - \frac{a_{ij\chi}^k}{\sum_{\chi \in \{V,O\}} a_{ij\chi}^k} \left| \mathbf{X}_{ij}^k \right| \right] = 0.$$
 (14)

 \mathbf{X}_{ij}^{k} : collects the country and industry observables that enter into $\mathbf{a}(i,k)$, $\mathbf{d}(i,k)$, $\mathbf{h}(i,k)$, and $\mathbf{x}(i,k)$.

Weighted non-linear least squares (NLLS): $\Theta^* = \operatorname{argmin}_{\Theta} (m(\Theta))^T \Omega (m(\Theta))$

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Top 50 U.S. trade partners (less HKG, SAU, VEN and IRQ).

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- ▶ Pinned down externally: ρ^k (Soderbery 2015).
- ▶ Remaining parameters to be estimated: $\Theta = \{\theta^k, \lambda, \beta_0, \gamma_1, \ldots\}$.

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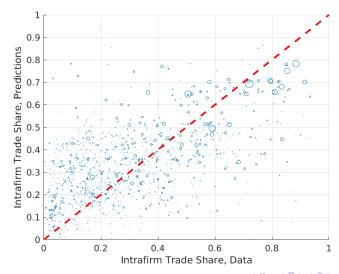
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- ► Algorithm: Levenberg-Marquardt (with theoretical restrictions) Standard errors: Gauss-Newton regressions



Predicted vs actual: Intrafirm trade shares



Point estimates

| name | est. | se | 95% CI |
|--------------------------------------|--------|-------|------------------|
| $\alpha^k \ln(K/L)$ | 0.414 | 0.009 | [0.40, 0.43] |
| $\alpha^k \left(\ln(K/L) \right)^2$ | -0.134 | 0.003 | [-0.14, -0.13] |
| β_{O} | 0.678 | 0.007 | [0.66, 0.69] |
| λ_{01} | 0.921 | 0.001 | [0.92, 0.92] |
| λ_{02} | 0.884 | 0.002 | [0.88, 0.89] |
| λ_{03} | 0.782 | 0.004 | [0.77, 0.79] |
| F-val | 56.58 | - | - |

$\rightarrow \theta^{k}$'s, α^{k} 's, ρ^{k} 's

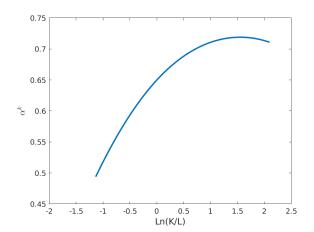
 μ_{xii}^{k} 's, μ_{hii}^{k} 's, δ_{ii}^{k} 's

- ▶ Some normalizations: $\theta^1 = 4$; α^k constant targets an average α^k of 0.65.
- ightharpoonup Separate λ 's for lower-middle, upper-middle, and high income countries:

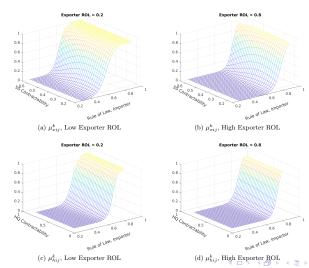
Estimates point to the relevance of within-"nest" correlation in productivity draws.

Estimates

 $\triangleright \alpha^k$: Increasing in the capital-labor ratio.

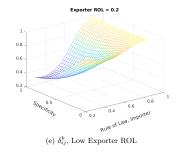


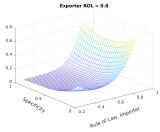
▶ For μ_{hij}^k and μ_{xij}^k : Both increasing in Importer ROL_j



 δ_{ii}^k : Firm's residual rights-of-control weakest when industry specificity is high and importer ROL is low.

Moreover, δ_{ii}^k tends to be increasing in importer ROL_i





(f) δ_{ij}^k , High Exporter ROL

Closing the Model and Implementing Counterfactuals

- ► Factor-market clearing conditions in each country to close the model:
 - Labor endowment \bar{L}_j equals the sum of factor demand from: (i) final-good assembly; and (ii) country-j input suppliers.
 - lackbox Skill endowment $ar{H}_j$ equals the sum of factor demand from firms headquartered in country j
 - Firm profits accrue back to consumers via holdings in a domestic asset market. No international trade in assets; take deficits as fixed from the data.

Closing the Model and Implementing Counterfactuals

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 - Firm profits accrue back to consumers via holdings in a domestic asset market. No international trade in assets; take deficits as fixed from the data.
- Counterfactual changes computed via a "hat algebra" system, following Dekle et al. (2008)
- To operationalize: need initial trade shares across countries (which we take from the ICIO), and calibrated/estimated model parameters
 - Perform a correction on trade shares to map them to the π 's in the model.

 Details
 - Upper-tier parameters: η^k , $\alpha = 0.66$, $\rho = 0.75$
 - Pin down $s_i \bar{H}_i$ in initial equilibrium, rather than take it from data.



Counterfactuals: Global improvement in μ^k_{hij} and μ^k_{xij}

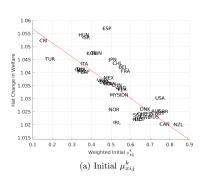
Shift all μ_{hij}^k 's and μ_{xij}^k 's to 1 globally, to get to the full contractibility world:

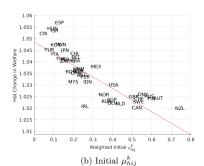
- ▶ Yields a mean country welfare increase of 3.5%
- lackbox Gains driven by the contracting frictions terms: \widehat{B}^k_{jj} , $\widehat{\Upsilon}^k_j$

| | Total Effect | $\widehat{\pi}^k_{jj}$ | \widehat{B}_{jj}^{k} | $\widehat{\Upsilon}_{j}^{k}$ | $\widehat{\widehat{f {	au}}}_{j}$ | Factor Price Effects |
|---------------------------------------|--------------|------------------------|------------------------|------------------------------|-----------------------------------|----------------------|
| $\mu_{hij}^k = \mu_{\times ij}^k = 1$ | 0.035 | 0.003 | 0.079 | 0.052 | -0.046 | -0.044 |
| ,, | (0.011) | (0.008) | (0.055) | (0.038) | (0.036) | (0.036) |
| $\mu_{xij}^k = 1$ | 0.026 | 0.001 | 0.069 | 0.038 | -0.038 | -0.039 |
| • | (800.0) | (0.005) | (0.050) | (0.030) | (0.031) | (0.033) |
| $\mu_{\mathit{hij}}^{\mathit{k}} = 1$ | 0.014 | 0.001 | 0.039 | 0.038 | -0.038 | -0.023 |
| • | (0.013) | (0.003) | (0.028) | (0.028) | (0.029) | (0.021) |
| $\delta_{ii}^k = 0$ | 0.001 | -0.000 | 0.001 | -0.000 | 0.000 | 0.000 |
| | (0.001) | (0.000) | (0.000) | (0.001) | (0.001) | (0.001) |

Counterfactuals: Global improvement in μ_{hij}^k and μ_{xij}^k (cont.)

ightharpoonup Greater welfare gains for countries with lower initial μ 's.





Counterfactuals: Removing integration as an organizational mode

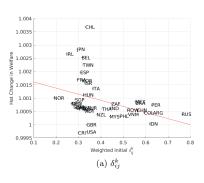
Set $\delta^k_{ij}=0$ globally, so all final-good firms are indifferent between integration and outsourcing:

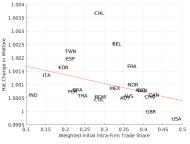
▶ Modest effect on average country welfare: +0.1%

| | Total Effect | $\widehat{\pi}^{k}_{jj}$ | \widehat{B}_{jj}^{k} | $\widehat{\Upsilon}_{j}^{k}$ | $\widehat{\widehat{ar{\Upsilon}}}_{j}$ | Factor Price Effects |
|---------------------------------------|--------------|--------------------------|------------------------|------------------------------|--|----------------------|
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| | (0.001) | (0.000) | (0.000) | (0.001) | (0.001) | (0.001) |

Counterfactuals: Removing integration as an organizational mode (cont.)

Welfare effects negatively correlated with countries' initial propensity to adopt integration.

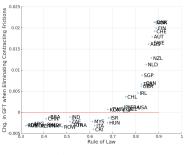




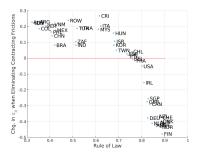
Counterfactuals: Gains from Trade and Contracting Frictions

When contracting frictions are removed (i.e., all μ_{hij}^k 's and μ_{xij}^k 's are set to 1):

- the gains from trade (relative to autarky) increase for high ROL countries,
- while decreasing for low ROL countries.



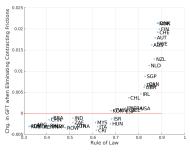
(a) Gains from Trade



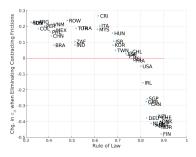
(b) Domestic Absorption Ratio

Counterfactuals: Gains from Trade and Contracting Frictions

- Intuition: Low ROL countries see large improvements in contractibility when these frictions are removed \Rightarrow They end up sourcing more, particularly from themselves (i.e., $\pi_{jj} \uparrow$).
- ▶ This dampens the gains from trade.



(a) Gains from Trade

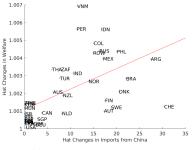


(b) Domestic Absorption Ratio

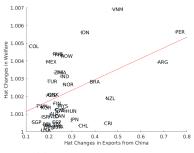
Counterfactuals: Improving CHN Rule of Law

Raise ROL in CHN to the world frontier (FIN):

- ► CHN's welfare gain: +3.1%
- lacktriangle All other countries gain too, with an average of +0.2%
- Countries who see their trade with China rise more experience a larger welfare increase



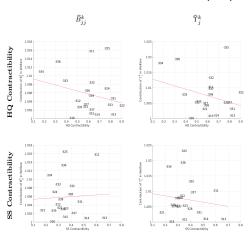
(a) Changes in Imports from China



(b) Changes in Exports To China

Counterfactuals: Improving CHN Rule of Law

Raise ROL in CHN to the world frontier (FIN):



Bigger contribution to aggregate welfare change in CHN from industries with lower hq contractibility or lower ss contractibility.

From Model to Estimation Strate Estimates Counterfactuals

Concluding Remarks

Wrapping Up

- Developed a bridge between: (i) models of contracting frictions with bilateral holdup; and (ii) the quantitative trade literature.
- ► The model delivers:
 - Tractable expressions for sourcing shares and a modified gains-from-trade formula, that reflect the effects of contracting frictions
 - A structural estimating equation for the intrafirm trade share
- Quantification allows us to address such issues as:
 - How much do contracting fictions in global sourcing impinge on country welfare?
 - ► How much would a country stand to gain from an improvement in institutions (e.g., related to the rule of law) that alleviates these frictions in input sourcing?

Supplementary Slides

Incremental revenue: Derivation

▶ Details

Compute for discrete number of suppliers, L, each in charge of $\epsilon=1/L$ inputs.

$$\begin{split} \widetilde{r}(\ell;\epsilon) \; &= \; A_{j}^{1-\rho} \phi^{\rho} L_{j}(\phi)^{\alpha \rho} \left[\prod_{k' \neq k} \left(X_{j}^{k'}(\phi) \right)^{\eta^{k'}(1-\alpha)\rho} \right] \times \\ & \left\{ \left[\left(\sum_{\ell' \neq \ell} x_{j}^{k}(\phi;\ell')^{\rho^{k}} \epsilon' \right) + x_{j}^{k}(\phi;\ell)^{\rho^{k}} \epsilon \right]^{\frac{\eta^{k}(1-\alpha)\rho}{\rho^{k}}} - \left[\left(\sum_{\ell' \neq \ell} x_{j}^{k}(\phi;\ell')^{\rho^{k}} \epsilon' \right) \right]^{\frac{\eta^{k}(1-\alpha)\rho}{\rho^{k}}} \right\}. \end{split}$$

Approximate the term in the curly braces via a first-order Taylor expansion about $\epsilon=0$. Then, evaluate the limit as $L\to\infty$.

$$\begin{split} \frac{\widetilde{r}(\ell;\epsilon)}{\epsilon} \; &\approx \; A_{j}^{1-\rho} \, \phi^{\rho} L_{j}(\phi)^{\alpha\rho} \left[\prod_{k' \neq k} \left(X_{j}^{k'}(\phi) \right)^{\eta^{k'}(1-\alpha)\rho} \right] \times \\ & \left[\left(\sum_{\ell' \neq \ell} x_{j}^{k}(\phi;\ell')^{\rho^{k}} \epsilon' \right) + x_{j}^{k}(\phi;\ell)^{\rho^{k}} \epsilon \right]^{\frac{\eta^{k}(1-\alpha)\rho}{\rho^{k}} - 1} \left(\frac{\eta^{k}(1-\alpha)\rho}{\rho^{k}} \right) x_{j}^{k}(\phi;\ell)^{\rho^{k}} \\ \Rightarrow \quad r_{j}^{k}(\phi;\ell) \; &= \; \lim_{L \to \infty} \frac{\widetilde{r}(\epsilon)}{\epsilon} \; = \; (1-\alpha) \frac{\rho \eta^{k}}{\rho^{k}} R_{j}(\phi) \left(\frac{x_{j}^{k}(\phi;\ell)}{X^{k}(\phi)} \right)^{\rho^{k}} \, . \end{split}$$

Ξ_{ii}^{k} : Details • Return

$$\begin{split} \Xi^k_{ij\chi} &= \left(\frac{(1-\alpha)\rho\eta^k R_j(\phi)}{(X^k_j(\phi))^{\rho^k}}\right)^{\frac{1}{\rho^k(1-\alpha^k)}} \times \left(\frac{1-\rho^k}{\rho^k}\right)^{\frac{1-\rho^k}{\rho^k(1-\alpha^k)}} \left(\frac{\zeta^k_{ij\chi}}{\zeta^k_{ij}}\right)^{\frac{\zeta^k_{ij}}{\rho^k(1-\alpha^k)}} \\ &\times \left(\frac{\alpha^k}{\mathbf{s}_j}\right)^{\frac{\alpha^k}{1-\alpha^k}} \left(\frac{1-\alpha^k}{d^k_{ij}w_i}\right) \left(\beta^k_{ij\chi}\right)^{\frac{\alpha^k(1-\mu^k_{hij})}{1-\alpha^k}} \left(1-\beta^k_{ij\chi}\right)^{1-\mu^k_{\chi ij}}, \end{split}$$

where:

$$\zeta_{ij\chi}^{k} = 1 - \rho^{k} \alpha^{k} \left(1 - \mu_{hij}^{k} \right) \beta_{ij\chi}^{k} - \rho^{k} \left(1 - \alpha^{k} \right) \left(1 - \mu_{xij}^{k} \right) \left(1 - \beta_{ij\chi}^{k} \right), \text{ and}$$
 (15)

$$\zeta_{ij}^{k} = 1 - \rho^{k} \alpha^{k} \left(1 - \mu_{hij}^{k} \right) - \rho^{k} \left(1 - \alpha^{k} \right) \left(1 - \mu_{xij}^{k} \right). \tag{16}$$

Note: $\zeta_{ij\chi}^k \geq \zeta_{ij}^k$, with equality if and only if $\mu_{hij}^k = \mu_{xij}^k = 1$ (i.e., in the full contractibility case).

$X_i^k(\phi)$: Details Return

(i) Composite industry-k input:

Assuming $heta^k > rac{(1-lpha^k)
ho^k}{1ho^k}$, can be evaluated explicitly as:

$$\mathbb{E}_{\ell}\left[\tilde{Z}_{ij\chi}^{k}(\phi;\ell)^{\frac{(1-\alpha^{k})\rho^{k}}{1-\rho^{k}}}\right] = \bar{\Gamma}^{k} \times \pi_{ij}^{k} \pi_{\chi|ij}^{k}\left(\Phi_{j}^{k}\right)^{\frac{1}{\theta^{k}}} \frac{\rho^{k}(1-\alpha^{k})}{1-\rho^{k}} \frac{\left(d_{ij}^{k}w_{i}\right)^{\frac{\rho^{k}(1-\alpha^{k})}{1-\rho^{k}}}}{\left(B_{ij\chi}^{k}\right)^{\frac{\rho^{k}(1-\alpha^{k})}{1-\rho^{k}}}}.$$

where $\bar{\Gamma}^k \equiv \Gamma\left(1-\frac{1}{\theta^k}\frac{(1-\alpha^k)\rho^k}{1-\rho^k}\right)$, and $\Gamma(\cdot)$ is the Gamma function.

$L_j(\phi)$: Details ightharpoonup

(ii) Full solution to the firm's problem.

Firm's overall payoff (with ex-ante transfers):

$$F_{j}(\phi) = R_{j}(\phi) - \sum_{k=1}^{K} \int_{\ell=0}^{1} s_{j} h_{j}^{k}(\phi, \ell) d\ell - \sum_{k=1}^{K} \int_{\ell=0}^{1} c_{ij\chi}^{k}(\phi, \ell) x_{j}^{k}(\phi, \ell) d\ell - w_{j} L_{j}(\phi),$$
(17)

- From this, solve for $L_j(\phi)$ (final-good assembly labor)
- After simplification: $X_j^k(\phi)$, $L_j(\phi)$, and hence $q_j(\phi)$ are all linear functions of $R_j(\phi)$.

$L_i(\phi)$: Details • Return

(ii) Full solution to the firm's problem.

In particular:

$$\begin{split} X_j^k(\phi) &= (1-\alpha)\rho\eta^k R_j(\phi) \left(\frac{\alpha^k}{s_j}\right)^{\alpha^k} \left(1-\alpha^k\right)^{1-\alpha^k} \left(\Phi_j^k\right)^{\frac{1-\alpha^k}{\theta^k}} \left(\bar{\Gamma}^k\right)^{\frac{1-\rho^k}{\rho^k}} \left(\Upsilon_j^k\right)^{-\frac{1-\rho^k}{\rho^k}}, \\ L_j(\phi) &= \frac{\alpha\rho}{w} \bar{\Upsilon}_j R_j(\phi). \end{split}$$

 $ightharpoonup \Upsilon_i^k$ and $\bar{\Upsilon}_i$ depend on the underlying parameters, including the $eta_{ij\chi}^k$ bargaining shares

In particular, \hat{T}_i is the share of revenue that accrues to the firm (after accounting for payments to factors other than assembly labor)

Υ_j^k and $\bar{\Upsilon}_j$: Details

 $ar{\Upsilon}_j$: Share of revenues that accrue to the firm (after accounting for the ex-ante transfer and payments to factors)

$$\Upsilon_j^k \quad = \quad \left(\sum_{i=1}^J \sum_{\chi \in \{V,O\}} \frac{\zeta_{ij}^k}{\zeta_{ij\chi}^k} \pi_{ij}^k \pi_{\chi|ij}^k\right)^{-1} \text{, and}$$

$$\tilde{\Upsilon}_j = 1 - (1 - lpha) \sum_{k=1}^K rac{
ho \eta^k}{
ho^k} \left(1 - (1 -
ho^k) \Upsilon_j^k
ight).$$

In the full-contractibility case $(\mu_{\mathit{hij}}^k = \mu_{\mathit{xij}}^k = 1)$, we have: $\Upsilon_j^k = 1$ and $\bar{\Upsilon}_j = 1 - \rho(1 - \alpha)$.

From Model to Data: Details

$$\tilde{t}^k_{ij\chi} = t^k_{ij\chi} \cdot \epsilon^k_{ij\chi} \ = \ \mathbf{a}^k_{ij\chi} \cdot \mathbf{a}^k_{ij} \cdot \epsilon^k_{ij\chi},$$

$$\begin{split} a_{ij}^k &= (1-\alpha)\rho\eta^k \frac{\Upsilon_j^k}{\Phi_j^k} I_j \left(1-\alpha^k\right) T_i^k (w_i)^{-\theta^k} \left(B_{ij}^k\right)^{-\frac{\theta^k \lambda_j}{1-\lambda_i}} \left(d_{ij}^k\right)^{-\theta^k} \frac{1}{2} \left(\frac{1}{\zeta_{ij}^k}\right)^{\frac{\zeta_{ij}^k}{\rho^k (1-\alpha^k)}} \frac{\theta^k}{1-\lambda_i} \\ a_{ij\chi}^k &= \left(\zeta_{ij\chi}^k\right)^{\frac{\zeta_{ij}^k}{\rho^k (1-\alpha^k)}} \frac{\theta^k}{1-\lambda_i} \left(1-\beta_{ij\chi}^k\right)^{\frac{\theta^k}{1-\lambda_i}} \left(1-\mu_{xij}^k\right) \left(\beta_{ij\chi}^k\right)^{\left(1-\mu_{hij}^k\right)} \frac{\alpha^k}{1-\alpha^k} \frac{\theta^k}{1-\lambda_i} \\ &\times \left(\mu_{xij}^k + (1-\mu_{xij}^k)(1-\beta_{ij\chi}^k) \frac{\zeta_{ij}^k}{\zeta_{ij\chi}^k}\right) \end{split}$$

Moment Condition: Details



- lacksquare $ilde{t}^k_{ij}$ is the sum of two independent Poisson random variables, $ilde{t}^k_{ijV} + ilde{t}^k_{ijO} = ilde{t}^k_{ij}$.
- ▶ Property: Conditional on the realized value of \tilde{t}^k_{ij} , the distribution of \tilde{t}^k_{ijV} is a binomial distribution where:
 - $ightharpoonup ilde{t}_{ij}^k$ is the number of the trials; and
 - $ightharpoonup a_{ijV}^k a_{ij}^k / \left(\sum_{\chi=\{V,O\}} a_{ij\chi}^k a_{ij}^k\right)$ is the success probability.
- It follows that the distribution of $\tilde{t}^k_{ijV}/\tilde{t}^k_{ij}$ conditional on \tilde{t}^k_{ij} , is Bernoulli with the same success probability.
- This yields the following moment condition for estimation; compare to (14):

$$E\left[\frac{\tilde{t}_{ijV}^k}{\tilde{t}_{ij}^k}\left|\tilde{t}_{ij}^k\right.\right] = \frac{a_{ijV}^k a_{ij}^k}{\sum_{\chi = \{V,O\}} a_{ij\chi}^k a_{ij}^k} = \frac{a_{ijV}^k}{\sum_{\chi = \{V,O\}} a_{ij\chi}^k}$$



Moment Condition: Quasi-MLE Approach

▶ Return

Treat a_{ij}^k as a source-by-industry fixed effect. Writing down the quasi-maximum likelihood function, the FOC with respect to a_{ij}^k implies:

$$\begin{aligned} a^k_{ij} & \sum_{\chi \in \{V,O\}} a^k_{ij\chi} = \sum_{\chi \in \{V,O\}} \tilde{t}^k_{ij\chi} \\ \Rightarrow & a^k_{ij} = \frac{\sum_{\chi = V,O} \tilde{t}^k_{ij\chi}}{\sum_{\chi = V,O} a^k_{ij\chi}} \quad \text{(c.f., Fally 2015)} \end{aligned}$$

Substituting this back into the expression for $\tilde{t}^k_{ij\chi}$ from (12), we have:

$$\frac{\tilde{t}_{ijV}^k}{\sum_{\chi \in \{V,O\}} \tilde{t}_{ij\chi}^k} = \frac{a_{ijV}^k}{\sum_{\chi \in \{V,O\}} a_{ij\chi}^k} \varepsilon_{ijV}^k. \tag{18}$$

Industry Parameters PReturn



| ID | NAICS3 | Desc | α^k | θ^k | $ ho^k$ | $1 - \frac{(1-\alpha^k)\rho^k}{\theta^k(1-\rho^k)}$ |
|----|--------|---------------------------|------------|------------|---------|---|
| 1 | 311 | Food Manufacturing | 0.646 | 4.000 | 0.886 | 0.315 |
| 2 | 312 | Beverage and Tobacco Prod | 0.701 | 16.223 | 0.788 | 0.932 |
| 3 | 313 | Textile Mills | 0.659 | 3.805 | 0.821 | 0.590 |
| 4 | 314 | Textile Product Mills | 0.539 | 8.432 | 0.768 | 0.820 |
| 5 | 315 | Apparel Manufacturing | 0.521 | 9.478 | 0.852 | 0.708 |
| 6 | 316 | Leather and Allied Produc | 0.555 | 12.714 | 0.781 | 0.875 |
| 7 | 321 | Wood Product Manufacturin | 0.560 | 8.858 | 0.777 | 0.827 |
| 8 | 322 | Paper Manufacturing | 0.698 | 8.641 | 0.580 | 0.952 |
| 9 | 323 | Printing and Related Supp | 0.587 | 16.020 | 0.688 | 0.943 |
| 10 | 324 | Petroleum and Coal Produc | 0.707 | 11.193 | 0.881 | 0.806 |
| 11 | 325 | Chemical Manufacturing | 0.708 | 21.514 | 0.771 | 0.954 |
| 12 | 326 | Plastics and Rubber Produ | 0.626 | 13.045 | 0.879 | 0.791 |
| 13 | 327 | Nonmetallic Mineral Produ | 0.656 | 39.243 | 0.738 | 0.975 |
| 14 | 331 | Primary Metal Manufacturi | 0.700 | 36.932 | 0.891 | 0.934 |
| 15 | 332 | Fabricated Metal Product | 0.607 | 10.690 | 0.708 | 0.911 |
| 16 | 333 | Machinery Manufacturing | 0.639 | 18.377 | 0.841 | 0.897 |
| 17 | 334 | Computer and Electronic P | 0.687 | 15.771 | 0.728 | 0.947 |
| 18 | 335 | Electrical Equipment Appl | 0.625 | 1.835 | 0.632 | 0.650 |
| 19 | 336 | Transportation Equipment | 0.664 | 23.198 | 0.749 | 0.957 |
| 20 | 337 | Furniture and Related Pro | 0.494 | 9.246 | 0.297 | 0.977 |
| 21 | 339 | Miscellaneous Manufacturi | 0.575 | 7.802 | 0.714 | 0.864 |
| - | - | Mean | 0.626 | 14.144 | 0.751 | 0.839 |

Estimates for bargaining parameters Return



| name | est. | se | 95% CI |
|---|---------|-------|--------------------|
| $\gamma_1: \mu_{\mathit{xij}}^k$ constant | -7.154 | 0.987 | [-9.09, -5.22] |
| $\gamma_2: \mu_{xij}^k$ SSCont ^k | 4.856 | 0.286 | [4.30, 5.42] |
| $\gamma_3: \mu_{x i j}^k \left(SSCont^k ight)^2$ | -18.223 | 0.160 | [-18.54, -17.91] |
| $\gamma_4:\mu_{xij}^k$ ROL_i | -9.843 | 0.296 | [-10.42, -9.26] |
| $\gamma_5: \mu_{xij}^k \; (ROL_i)^2$ | 2.624 | 0.245 | [2.14, 3.10] |
| $\gamma_6 : \mu_{xij}^k ROL_j$ | 6.853 | 2.485 | [1.98, 11.72] |
| $\gamma_7: \mu_{xij}^{k^*} (ROL_j)^2$ | 11.132 | 1.588 | [8.02, 14.24] |
| $\gamma_8: \mu_{xij}^k \; SSCont^k \times ROL_i$ | -3.744 | 0.067 | [-3.88, -3.61] |
| $\gamma_9: \mu_{xij}^k SSCont^k \times ROL_j$ | 12.949 | 0.296 | [12.37, 13.53] |
| $\gamma_{11}: \mu^{\check{k}}_{hij}$ constant | -17.156 | 2.106 | [-21.28, -13.03] |
| $\gamma_{12}:\mu_{hij}^{k}$ HQCont k | 8.760 | 0.877 | [7.04, 10.48] |
| $\gamma_{13}: \mu_{hij}^k \left({\sf HQCont}^k ight)^2$ | -0.527 | 0.035 | [-0.60, -0.46] |
| $\gamma_{14}: \mu_{hij}^k \ ROL_i$ | -6.376 | 0.232 | [-6.83, -5.92] |
| $\gamma_{15}: \mu_{hij}^{k} (ROL_i)^2$ | 1.661 | 0.210 | [1.25, 2.07] |
| $\gamma_{16}: \mu_{hij}^{k'} \; ROL_{j}$ | 11.580 | 4.696 | [2.38, 20.78] |
| $\gamma_{17}: \mu_{hij}^{k} (ROL_{j})^{2}$ | 16.951 | 2.693 | [11.67, 22.23] |
| $\gamma_{18}: \mu_{hij}^k \ HQCont^k \times ROL_i$ | 0.229 | 0.050 | [0.13, 0.33] |
| $\gamma_{19} : \mu_{hij}^{k'} HQCont^k \times ROL_j$ | -9.446 | 1.093 | [-11.59, -7.30] |

Estimates for bargaining parameters Return



| name | est. | se | 95% CI |
|---|---------|-------|--------------------|
| $\gamma_{21}:\delta^k_{ij}$ constant | 6.394 | 0.066 | [6.26, 6.52] |
| $\gamma_{22}:\delta^k_{ij}$ Speci k | -7.824 | 0.056 | [-7.93, -7.72] |
| $\gamma_{23}:\delta_{ij}^{k}\left(Speci^{k}\right)^{2}$ | 2.746 | 0.051 | [2.65, 2.85] |
| $\gamma_{24}: \delta_{ij}^k \ ROL_i$ | 1.930 | 0.271 | [1.40, 2.46] |
| $\gamma_{25}: \delta_{ij}^{k} (ROL_i)^2$ | -7.522 | 0.242 | [-8.00, -7.05] |
| $\gamma_{26} : \delta_{ij}^k ROL_j$ | -17.544 | 0.140 | [-17.82, -17.27] |
| $\gamma_{27}:\delta_{ij}^{\check{k}}\;(ROL_j)^2$ | 17.369 | 0.153 | [17.07, 17.67] |
| $\gamma_{28}: \delta_i^k \; Speci^k \times ROL_i$ | 0.224 | 0.038 | [0.15, 0.30] |
| $\gamma_{29}: \delta_i^k Speci^k \times ROL_j$ | 4.742 | 0.044 | [4.66, 4.83] |

Hat algebra: Details



$$\left(\zeta_{ij}^{k}\right)' = 1 - \rho^{k} + \rho^{k} \alpha^{k} \left(\mu_{hij}^{k}\right)' + \rho^{k} \left(1 - \alpha^{k}\right) \left(\mu_{xij}^{k}\right)' \tag{19}$$

$$\left(\zeta_{ij\chi}^{k}\right)' = 1 - \rho^{k} \alpha^{k} \left[1 - \left(\mu_{hij}^{k}\right)'\right] \left(\beta_{ij\chi}^{k}\right)' - \rho^{k} \left(1 - \alpha^{k}\right) \left(1 - \left(\mu_{xij}^{k}\right)'\right) \left(1 - \left(\beta_{ij\chi}^{k}\right)'\right). \tag{20}$$

$$\left(B_{ij\chi}^{k}\right)' = \left[1 - \left(\beta_{ij\chi}^{k}\right)'\right]^{1 - \left(\mu_{xij}^{k}\right)'} \left[\left(\beta_{ij\chi}^{k}\right)'\right]^{\left(1 - \left(\mu_{hij}^{k}\right)'\right)} \frac{\alpha^{k}}{1 - \alpha^{k}} \left[\frac{\left(\zeta_{ij\chi}^{k}\right)'}{\left(\zeta_{ij}^{k}\right)'}\right]^{\frac{\left(\zeta_{ij}^{k}\right)'}{\rho^{k}\left(1 - \alpha^{k}\right)}}$$
(21)

$$\left(B_{ij}^{k}\right)' = \left(\frac{1}{2}\left[\left(\left(B_{ijV}^{k}\right)'\right)^{\frac{\theta^{k}}{1-\lambda_{i}}} + \left(\left(B_{ijO}^{k}\right)'\right)^{\frac{\theta^{k}}{1-\lambda_{i}}}\right]\right)^{\frac{1-\lambda_{i}}{\theta^{k}}}.$$
(22)



$$\left(\pi_{\chi|ij}^{k}\right)' = \frac{\left(\left(B_{ij\chi}^{k}\right)'\right)^{\frac{\theta^{k}}{1-\lambda_{i}}}}{\left(\left(B_{ijV}^{k}\right)'\right)^{\frac{\theta^{k}}{1-\lambda_{i}}} + \left(\left(B_{ijO}^{k}\right)'\right)^{\frac{\theta^{k}}{1-\lambda_{i}}}}.$$
(23)

$$\widehat{\pi_{ij}^k} = \frac{\left(\widehat{d_{ij}^k}\widehat{w_i}\right)^{-\theta^k} \left(\widehat{B_{ij}^k}\right)^{\theta^k}}{\widehat{\Phi_{j}^k}}$$
(24)

$$\widehat{\Phi_j^k} \equiv \sum_{i=1}^J \pi_{ij}^k (\widehat{d_{ij}^k} \widehat{w_i})^{-\theta^k} \left(\widehat{B_{ij}^k}\right)^{\theta^k}$$
(25)

$$\left(v_{ij\chi}^{k}\right)' = \frac{\left(\pi_{ij}^{k}\right)'\left(\pi_{\chi|ij}^{k}\right)'}{\frac{\left(\varsigma_{ij\chi}^{k}\right)'}{\left(\varsigma_{ij}^{k}\right)'}} \tag{26}$$

$$\left(\Upsilon_{j}^{k}\right)' = \left\{ \sum_{i=1}^{J} \sum_{\chi \in \{V,O\}} \frac{\left(\pi_{ij}^{k}\right)' \left(\pi_{\chi|ij}^{k}\right)'}{\frac{\left(\zeta_{ij\chi}^{k}\right)'}{\left(\zeta_{ij}^{k}\right)'}} \right\}^{-1} = \left\{ \sum_{i=1}^{J} \sum_{\chi = \{V,O\}} \left(v_{ij\chi}^{k}\right)' \right\}^{-1}$$
 (27)

$$(\tilde{\Upsilon}_{j})' = 1 - (1 - \alpha) \sum_{k=1}^{K} \frac{\rho \eta^{k}}{\rho^{k}} \left[1 - (1 - \rho^{k}) \left(\Upsilon_{j}^{k} \right)' \right]. \tag{28}$$

$$(I_j)' = \frac{\widehat{w}_j w_j \bar{L}_j + \widehat{s}_j s_j \bar{H}_j}{1 - (1 - \alpha \rho) (\bar{\Upsilon}_j)'}$$
(29)

$$\widetilde{w_{j}}\widetilde{w_{j}}\widetilde{L_{j}} = \rho\alpha\left(\widehat{\Upsilon}_{j}\right)'\left(l_{j}\right)' + \rho\left(1 - \alpha\right) \\
\times \sum_{k=1}^{K} \left(1 - \alpha^{k}\right)\eta^{k} \sum_{m=1}^{J} (l_{m})'\left(\Upsilon_{m}^{k}\right)' \sum_{\chi \in \{V, O\}} \left(v_{jm\chi}^{k}\right)' \left[\frac{\left(\mu_{xjm}^{k}\right)'\left(\zeta_{jm\chi}^{k}\right)'}{\left(\zeta_{jm}^{k}\right)'} + \left(1 - \left(\mu_{xjm}^{k}\right)'\right)\left[1 - \left(\beta_{jm\chi}^{k}\right)'\right]\right] \tag{30}$$

$$\widehat{s_{j}^{k}} s_{j}^{k} \bar{H_{j}} = \rho (1 - \alpha) \left(I_{j} \right)' \sum_{k=1}^{K} \alpha^{k} \eta^{k} \left(\Upsilon_{j}^{k} \right)' \sum_{i=1}^{J} \sum_{\chi = V, O} \left(\upsilon_{ij\chi}^{k} \right)' \left[\frac{\left(\mu_{hij}^{k} \right)' \left(\varsigma_{ij\chi}^{k} \right)'}{\left(\varsigma_{ij}^{k} \right)'} + \left(\beta_{ij\chi}^{k} \right)' \left(1 - \left(\mu_{hij}^{k} \right)' \right) \right]$$

$$(31)$$

Note: Data for $w_j \bar{L}_j$ are from the Penn World Tables. Value of $s_j \bar{H}_j$ is inferred from the Cobb-Douglas condition in the initial equilibrium.

The algorithm:

- 1. Given $(\mu_{hij}^k)'$, $(\mu_{hij}^k)'$ and $(\beta_{ij\chi}^k)'$, use equation (22) to solve for $(B_{ij\chi}^k)'$.
- 2. Use equation (23) and $(B^k_{ij\chi})'$ to get $\left(\pi^k_{\chi|ij}\right)'$ and $\widehat{\pi^k_{\chi|ij}}.$
- 3. Guess a vector of \widehat{w}_j and \widehat{s}_j .
- 4. Conditional on the guessed \widehat{w}_j and \widehat{s}_j , use equation (25) to solve for $\widehat{\Phi_j^k}$.
- 5. Use $\widehat{\Phi_j^k}$ and equation (24) to solve for $\widehat{\pi_{ij}^k}$ and $\left(\pi_{ij}^k\right)'$.
- 6. With $\left(\pi_{ij}^k\right)'$, we can use equation (27) and (28) to get $\left(\Upsilon_m^k\right)'$ and $\left(\bar{\Upsilon}_m\right)'$.
- 7. With $(\bar{\Upsilon}_j)'$, use equation (29) to solve for $(I_j)'$.
- 8. With all the above information, invert equation (30) to get a new $\widetilde{w_j}$ Similarly, we can update the price of capital, $\widetilde{s_j}$ by inverting equation (31):
- 9. Update $(\widehat{w_i}, \widehat{s_i})$ with $(\widetilde{w_i}, \widetilde{s_i})$, and iterate from step 3 until convergence.

Trade Share Correction Term: Details

Denote the correction term as σ_{ij}^k :

$$\sigma_{ij}^k = \left(\mathcal{B}_{ij}^k\right)^{-\frac{\theta^k}{1-\lambda_i}} \sum_{\chi \in \{V,O\}} \left(\mu_{\mathrm{x}ij}^k + (1-\mu_{\mathrm{x}ij}^k)(1-\beta_{ij\chi}^k) \frac{\zeta_{ij}^k}{\zeta_{ij\chi}^k}\right) \frac{1}{2} \left(\mathcal{B}_{ij\chi}^k\right)^{\frac{\theta^k}{1-\lambda_i}}.$$

Applying this correction term to the observed bilateral trade flows, \tilde{t}^k_{ij} , in the data allows us to recover the model-implied sourcing probabilities, π_{ij} , since:

$$\frac{\tilde{t}_{ij}^{k}/\sigma_{ij}^{k}}{\sum_{i'=1}^{J}\tilde{t}_{i'j}^{k}/\sigma_{i'j}^{k}} = \frac{T_{i}^{k}\left(w_{i}d_{ij}^{k}\right)^{-\theta^{k}}\left(B_{ij}^{k}\right)^{-\frac{\theta^{k}\lambda_{i}}{1-\lambda_{i}}}\left(B_{ij}^{k}\right)^{\frac{\theta^{k}}{1-\lambda_{i}}}}{\sum_{i'=1}^{J}T_{i'}^{k}\left(w_{i'}d_{i'j}^{k}\right)^{-\theta^{k}}\left(B_{i'j}^{k}\right)^{-\frac{\theta^{k}\lambda_{i'}}{1-\lambda_{i'}}}\left(B_{i'j}^{k}\right)^{\frac{\theta^{k}}{1-\lambda_{i'}}}} = \pi_{ij}^{k}.$$