# Taxing Humans: Pitfalls of the Mechanism Design Approach and Potential Resolutions

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September 11, 2017

**Abstract:** A growing body of evidence suggests that psychological biases can lead different implementations of otherwise equivalent tax incentives to result in meaningfully different behaviors. We argue that in the presence of such failures of "implementation invariance," decoupling the question of optimal feasible allocations from the tax system used to induce them—the "mechanism design approach" to taxation—cannot be the right approach to analyzing optimal tax systems. After reviewing the diverse psychologies that lead to failures of implementation invariance, we illustrate our argument by formally deriving three basic lessons that arise in the presence of these biases. First, the mechanism design approach neither estimates nor bounds the welfare computed under psychologically realistic assumptions about individuals' responses to the tax instruments used in practice. Second, the optimal allocations from abstract mechanisms may not be implementable with tax policies, and vice-versa. Third, the integration of these biases may mitigate the importance of informational asymmetries, resulting in optimal tax formulas more closely approximated by classical Ramsey results. We conclude by proposing that a "behavioral" extension of the "sufficient statistics" approach is a more fruitful way forward in the presence of such psychological biases.

## 1 Introduction

A standard assumption in optimal tax policy design is that individuals' behavior is governed only by the choice-sets induced by the tax system—conditional on the choice-set induced, behavior does not vary with the tax system that was used to implement that choice set. This assumption—which we refer to as *implementation invariance*—reduces the question of optimal tax-system design to an optimization problem over a set of feasible consumption bundles satisfying incentive compatibility and government revenue constraints. The abstraction from the practical considerations of tax policy implementation results in a framework that is tractable and fruitful. This "mechanism design approach" to taxation has been broadly applied to characterize the features of optimal policy in both static (for classic examples, see Mirrlees, 1971; Atkinson & Stiglitz, 1976) and, more recently, dynamic settings (for a review, see Golosov *et al.*, 2007).

In this paper, we articulate a challenge to the practical value of this approach: due to the psychologically complex manner in which individuals respond to taxation, the details of the tax system that induces a given choice set can substantially influence the resulting behavior. The growing evidence on the prevalence of taxpayer confusion, of heuristic optimization, and of imperfect attention suggests that the assumption of implementation invariance does not hold in practice. When this assumption fails, a policy analyst can be lead awry by the common two-step procedure of first considering the incentives induced by the optimal mechanism and only later considering its implementation.

In section 1, we summarize a series of recent empirical demonstrations of confusion, inattention, and heuristic use, all of which lead people to suboptimally respond to tax incentives. For each class of biases, we illustrate concretely the violations of implementation invariance that result. We argue that biases in the understanding of taxes are widespread, that these biases affect central economic behaviors, and that these biases are shaped by the idiosyncrasies of different tax mechanisms in complex and subtle ways.

In section 2, we formalize the consequences of violations of implementation invariance for

normative tax analysis. We build on a simple two-type model of optimal income taxation proposed by Stiglitz (1982) in which individuals choose between pairs of before-tax income z (which corresponds to a choice of labor supply) and the resulting after-tax consumption c. Using several behavioral biases as examples, we formalize three implications. First, the presence of these biases prevents the application of the revelation principle, a core result in game theory that allows the analyst to separate the question of analyzing optimal behavior under a "direct mechanism" from the specifics of the tax which implements it. As a result, welfare under a direct mechanism neither estimates nor bounds the welfare attainable at the true optimal policy. Second, we illustrate that there are biases can render the optimal allocation in a direct mechanism is not implementable with taxes, while the allocation resulting from the optimal taxes is not implementable with a direct mechanism. Third, we show that the presence of these biases can mitigate the role of information rents—a central concept of mechanism design—and can ultimately result in tax analysis that more closely resemble that of frameworks that are not tightly centered on understanding information asymmetries, such as the Ramsey approach.

In section 3, we assess the comparative advantages of alternative approaches to tax policy analysis in the presence of psychological biases. We argue that a modification to the "sufficient statistics" approach provides a fruitful way forward (for a review, see Chetty, 2009). This approach works with an allowable set of tax instruments directly, deriving optimal tax formulas involving elasticities and empirically-estimable formulations of bias. In addition to tractability, this approach also transparently highlights deviations from standard optimal tax formulas. We present and discuss the key challenges to this approach, and discuss the comparatively advatanges it faces to the mechanism design formulation.

## 2 Violations of implementation invariance

To focus ideas and define basic concepts, we begin by discussing a recent experiment that cleanly demonstrates a failure of implementation invariance. We then turn to a series of examples demonstrating this phenomenon, and its causes, in the field.

#### 2.1 A stylized lab example

The cleanest possible demonstration of a violation of implementation invariance would consist of a comparison of behavior under two meaningfully different tax instruments that induce the same choice sets. Tax policies in the field are rarely deployed in a manner that offers this comparison directly. However, as pursued in Abeler & Jäger (2015), labor markets may be designed in a laboratory setting that exactly satisfy these constraints.

Abeler & Jäger create a simple approximation to a labor-supply decision within the microcosm of the lab. The participants in their experiment must decide how much labor to provide in order to fund consumption. Labor is measured in the context of a real-effort task adopted from Gill & Prowse (2012), in which the participant may move a series of hundred-point slider scales to prespecified values. When time expires, participants receive a piece-rate wage for each slider that is positioned on its assigned value. This experimental task is arguably tedious, but it provides the participant with a means to trade current leisure for experimental earnings.

In the experiment, earnings from this task are subject to a progressive tax. Across treatment arms, the experimenters apply two tax systems that induce similar choice sets, but are of significantly differing complexity. In the "simple treatment", the progressive tax is implemented with two simply-articulated rules. The tax schedule traced by these rules can be calculated with relatively little effort. In the "complex treatment", the progressive tax is implemented with 22 tax rules. The tax schedule traced by these rules closely approximates that in the "simple treatment"—and thus induces the same choices sets—but the calculation

of this tax schedule is substantially more cognitively demanding.

While the traditional mechanism design approach would treat these experimental taxes as interchangeable tools for achieving the same behavior, Abeler & Jäger document substantially different behavior across treatment arms. When nearly identical tax incentives were induced through the complex system, subjects were less likely to choose the payoff-maximizing output level, and on average earned 23% less than subjects in the simple treatment arm. Furthermore, as new tax rules were introduced across rounds in the experiment, subjects were systematically less responsive to tax changes in the complex frame. In short, these mechanisms had differing effects on the distortionary impact of taxation, despite the near equivalence of the choice-sets that the policies induced.

The mechanism design approach takes as given that we may use arbitrarily complex tools to induce the choice sets, and thus choices, that the mechanism designer views as desirable. In practice, however, the quality of decision-making might decline if the choice environment is imperfectly understood. This worry is undoubtedly relevant for behavior in the current U.S. income tax system, commonly lamented for its extraordinary complexity.

#### 2.2 Field evidence

Laboratory experiments such as those of Abeler & Jäger provide compelling evidence of failures of implementation invariance, but do not inform us about the biases that shape people's responses to the actual tax systems used in practice. We now discuss the evidence on biased responses to tax incentives in the field. We focus on biases caused by confusion, by heuristic adoption, and by differential salience of different tax provisions.

#### 2.2.1 Confusion

Perhaps the most straightforward and psychologically uncomplicated manner in which psychological realism might influence our tax policy analysis is through the serious treatment of confusion. If a taxpayer misunderstands the provisions of the tax, he will come to believe he faces a different choice-set than he actually does. Under such circumstances, even an otherwise-optimizing agent would appear to generate violations of implementation invariance if the details of a tax instrument affect the manner in which it might be misunderstood.

Given the dramatic complexity of taxes in the United States, it is perhaps unsurprising that substantial confusion regarding tax provisions has been documented. When directly surveyed about the key parameters characterizing their federal income tax burden—like their marginal tax rate—taxpayers regularly report values with substantial individual error (Fujii & Hawley, 1988; Blaufus et al., 2013; Gideon, 2015; Rees-Jones & Taubinsky, 2016). Analysis of observational data reveals that there are large differences in knowledge of taxpayers' understanding of the tax code: Chetty et al. (2013) find significant differences in bunching at the refund-maximizing kink of the earned income tax credit (EITC), and that individuals who move from low-bunching neighborhoods to high bunching neighborhoods increase their EITC refunds due to new information diffusion. Moreover, significant amounts of tax benefits are "left on the table" every tax year through, e.g., failures to claim itemized deductions (Benzarti, 2016) or failures to claim the EITC (Bhargava & Manoli, 2015). The difficulty individuals face in understanding the complex tax code is argued to have generated the large professional-tax-preparation industry in the United States (Slemrod & Bakija, 2008), and indeed attempts to "teach the tax code" have been shown to be ineffective, on average, but can be effective when paired with expert advice (as in, e.g., Chetty & Saez, 2013).

To concretely illustrate the potential for confusion to generate violations of implementation invariance, we focus on recent evidence of taxpayer confusion arising from the work of Feldman *et al.* (2016a). The authors present a clear test of the possibility that taxpayers mistake predictable changes in lump-sum transfers for changes in marginal tax incentives.

Feldman *et al.* examine the effect of the Child Tax Credit (CTC), a transfer given to households with a child younger than 17 in the calendar year. While the size of this transfer varies with income, virtually all filers with adjusted gross income between \$30,000 and \$100,000 were able to claim the maximum \$1,000 credit in the window studied by the authors. For this group, a loss of the CTC constitutes a lump-sum change in tax liability.

The requirement that a household have a child under 17 at the end of the calendar year introduces a discontinuity in the average tax credit received. A household whose child "ages out" on December 31, 2010 could not claim the CTC for 2010, whereas a household whose child "ages out" on January 1, 2011 could. This distinction is perfectly predictable. Furthermore, the distinction does not change the marginal tax rate, and thus should not influence marginal tax incentives except through small income effects. However, using a regression discontinuity design, the authors document that the loss of the CTC is associated with an approximately 0.5 percent decline in reported wage income relative to households who have just retained the credit for another year. The authors document that this effect is not driven by strategic timing of earnings, nor by direct effects of a child aging. They interpret their result as evidence that at least some households confuse factors that influence average tax rates with those that determine marginal tax rates.

Under the assumption that households with a child born in late December do not hold meaningfully different preferences than those with a child born in early January, these results illustrate a clear violation of implementation invariance. Given that the CTC does not mechanically affect marginal tax rates, the loss of this credit does not meaningfully induce different tradeoffs between lesiure and consumption. But by nevertheless changing labor supply, the CTC must therefore have shaped taxpayers misunderstanding of the tax system. Upon observing an increase in their tax bill, the taxpayer incorrectly infers that marginal tax rates have gone up, and changes choice behavior.

#### 2.2.2 Heuristic Adoption

As documented by a large literature in psychology, decision makers often adopt simple heuristics to approximate complex decision-rules when cognitively effortful decisions must be quickly and regularly made. In an influential paper, Liebman & Zeckhauser (2004) consider and formalize two heuristics that they argue are sensible, and potentially common, means of approximating a convex schedule like the US income tax. These heuristics are presented in figure 1, and are described below.

The first heuristic, *ironing*, is applied by individuals who know the average tax rate they face, and forecast tax liability by applying their average tax rate to all incomes. Using the ironing heuristic, the forecasted tax at income z is given by  $\tilde{T}_I(z|z^*,\theta) = A(z^*|\theta) * z$ , where  $z^*$  denotes the individual's own income,  $\theta$  denotes all individual-specific characteristics that determine the applicable tax schedule, and  $A(z^*|\theta)$  denotes the individual's average tax rate. This heuristic has the practical benefit that it leads to reasonably accurate beliefs about the *levels* of taxes when considering small deviations from one's current income. Thus for decisions about how to budget one's annual income, this heuristic leads to minimal errors. However, when used to infer the leisure/consumption combinations that form an individual's choice set, this heuristic leads to meaningful errors. Specifically, it leads to overestimation of the tax burden for comparatively low incomes and underestimation of the tax burden for comparatively high incomes. This heuristic directly generates inaccurate beliefs about marginal tax rates: because the tax schedule is convex, average tax rates are systematically smaller than marginal tax rates, and thus the application of this heuristic generates a "flattening" of perceived schedules. Feldman et al. (2016a) argue that this heuristic potentially generates the confusion over marginal tax rates they document, and similar responsiveness to shocks to average tax rates have been documented in lab settings (de Bartolome, 1995). In a recent survey experiment directly eliciting perceptions of tax schedules, Rees-Jones & Taubinsky (2016) find evidence that the ironing heuristic is adopted by 30-40% of US tax filers.

The second heuristic, *spotlighting*, is applied by individuals who know their own tax and own *marginal* tax rate, and forecast tax liability by applying their marginal rate to the difference between their own income and the income amount under consideration. Using the spotlighting heuristic, the forecasted tax at income z is given by  $\tilde{T}_S(z|z^*,\theta) = T(z^*|\theta) +$  $MTR(z^*|\theta) * (z - z^*)$ , where  $z^*$  again denotes the individual's own income,  $MTR(z^*|\theta)$  denotes the marginal tax rate at that income, and  $T(z^*|\theta)$  denotes the true tax due at that income. Within one's own tax bracket, this heuristic leads to correct beliefs about the level and slope of the tax schedule; as a result, under the assumption that leisure/consumption pairs falling under other tax brackets are irrelevant alternatives in the choice set, this heuristic does not meaningfully violate mechanism dependence. While this heuristic has received some theoretical attention, Rees-Jones & Taubinsky (2016) find little evidence of its adoption in their forecasting experiment.

The apparent widespread adoption of the ironing heuristic provides another channel through which the assumption of implementation invariance will be violated. This heuristic essentially constitutes a structural model of how choice-sets will be misinferred, drawing on potentially irrelevant cues in the implementation of the mechanism. Since ironers use the average tax rate to approximate their marginal tax rate, different tax mechanism which induce the same marginal incentives, but with different average rates, will induce different behavior. More broadly, heuristics for approximating the tax schedule may draw upon subtle and otherwise-irrelevant cues from the implementation of the tax mechanism to inform behavior. To the extent that this occurs, assuming that behavior is invariant to these details of implementation has the potential to miss the changes in behavior that result from heuristic use.

#### 2.2.3 Salience

A recent and growing literature has demonstrated that the visibility of taxes substantially influences behavioral response, and that this feature can be incorporated into standard tax formulae with appropriate care. In two pioneering studies, Chetty *et al.* (2009) demonstrated that experimentally manipulated integration of taxes into posted prices for groceries and alcohol meaningfully influenced the resulting demand curves, and Finkelstein (2009) demonstrated that the reduced visibility of road-use tax induced by the adoption of "EZpass" reduced taxes' (dis)incentive effect on road use. Other recent advancements have studied how issues of salience affect the regressivity of commodity taxes (Goldin & Homonoff, 2013), how a social planner would optimally choose between differentially salient tax instruments (Goldin, 2015), and how issues of endogenous salience might affect tax policy analysis (Taubinsky & Rees-Jones, 2016; Feldman *et al.*, 2015). In short, in the context of commodity taxation, salience has come to be viewed as an increasingly well-understood policy instrument that shapes the welfare evaluation of tax policy.

While the tax salience literature has often focused on commodity taxation, its core findings appear to apply to tax incentives administered through the income tax as well. Miller & Mumford (2015) examine a change to the Child and Dependent Care Credit introduced in 2003; this change affected the direct, visible value that could be claimed for this credit that, considered in isolation, increased the subsidization of child and dependent care administered through the income tax. However, this policy change also interacted with provisions of the existing Child Tax Credit in a non-salient but offsetting manner. They demonstrate that taxpayer response was most consistent with reaction to the salient direct incentives of the tax, and with complete ignorance of the arguably non-salient interactions with other provisions of the tax code. As summarized by the authors, "taxpayers increased their expenditure on child care in response to the expansion of the CDCC regardless of whether the actual after-tax price of child care increased or decreased."

Under reasonably mild assumptions on the demand for child care, these results imply a violation of implementation invariance. For consumers facing an increase in the after-subsidy price of childcare, the larger amount of childcare demanded post-reform was available in their choice set prior to the tax change. Under the assumption that this change in subsidies does not introduce implausibly large income effects, this necessitates a violation of our key assumption. As a concrete illustration of the failure of implementation invariance, one may consider the predicted effect of a completely transparent price change as contrasted with the price-change introduced through interactions with multiple price interactions. If one believes that transparently raising the price of child care would lower its demand—i.e., that child

care is not a Giffen good—then behavior under these two choice-set-equivalent instruments would be expected to vary.

## 3 Consequences of the failure of implementation invariance

In this section, we illustrate several key consequences of the failure of implementation invariance for the formal analysis of tax policy. While the lessons we present are quite general, we illustrate these lessons in the context of a standard, but simple, two-type model of income taxation. We proceed by presenting the model, describing the mechanism-design approach to its analysis, and then illustrating the key complications that arise when biases depend on tax instruments.

#### 3.1 A standard optimal income tax model

We consider a simple model of income taxation based on Stiglitz (1982).

There are two "types" of individuals in the economy, indexed by their earnings ability  $\theta \in \{L, H\}$ . Those of low earnings ability  $(\theta = L)$  earn a wage w(L) per unit of labor and those of high earnings ability  $(\theta = H)$  earn a wage w(H) per unit of labor, where w(H) > w(L). The fraction of each type in the population is denoted by  $\alpha(\theta)$ . An agent with wage w generates gross income of  $z = w \cdot l$  when he supplies l units of labor. All post-tax income is spent on consumption c which, together with the labor output l, generates utility U(c, l). This utility is typically assumed to be concave, increasing in consumption, and decreasing in labor. In some of the analysis that follows, we make the simplifying assumption that  $U(c, l) = c - \psi(l)$ , where  $\psi', \psi'' > 0$ .

The government's objective is to maximize social welfare:

$$W = \sum_{\theta} \alpha(\theta) \cdot G(U(c(\theta), l(\theta)))$$
(1)

We assume that the government's evaluation of individual utility, G, is a smooth and concave function.

The policy decision faced by the government is to specify a tax-and-transfer system that maximizes social welfare. The assumption that G is concave reflects the government's disfavor of inequality, and thus the optimal tax system would redistribute income from those with high earnings ability to those with low earnings ability. Ability is not observed, however, and so the tax must depend on the signal of ability contained in observable earnings  $(z(\theta))$ .

In contrast to taxing ability, taxing earnings is distortionary. When those with high earnings are taxed and those with low earnings are subsidized, a high-earnings-ability worker might choose to reduce his labor supply in order to represent himself as a low-earnings-ability worker.

#### 3.2 A two-step approach to solving the optimal tax problem

This formulation of the social welfare problem illustrates a key trade-off in tax policy design. On one hand, the tax system must redistribute income from those of high earnings ability to those of low earnings ability. On the other hand, this tax system must simultaneously account the fact that such redistribution can lead workers to misrepresent their ability type through the earnings that they choose. Simultaneously mathematically accommodating both the policy motives of the government and the misrepresentation motives of the individual can be challenging. However, a powerful result from mechanism design—the revelation principle–can dramatically simplify the necessary analysis, and forms the heart of what we term "the mechanism design approach" to tax policy.

The revelation principle, as originally articulated in Myerson (1979), states that any equilibrium allocation that can arise among fully optimizing agents can be achieved as an equilibrium allocation in a *direct mechanism*—that is, a mechanism that induces agents to truthfully report their type. In the context of our model, the application of the revelation principle implies that a policy designer can restrict their attention to tax systems that do not induce misrepresentation of earnings ability without reducing the set of equilibrium outcomes that could be achieved. This allows analysis to be divided into two simplified steps: first, characterizing behavior in a world where agents are incentivized to report their type, and second, characterizing the tax system that induces those incentives. We illustrate these two steps in the context of our simple model below.

Step 1: characterizing the direct mechanism. Rather than assuming that the government only observes earnings, now assume that agents "announce" their type,  $\theta \in \{L, H\}$ . The planner assigns an allocation that depends on that announcement,  $(z(\theta), c(\theta))$ . The set of allocations must satisfy incentive compatibility (IC) constraints—which ensure that individuals are incentivized to announce their types honestly—and a budget balance (B) constraint—which ensures that total consumption in the economy does not exceed total earnings. Formally, the government maximizes

$$\max_{(c(\theta), z(\theta))} \sum_{\theta} \alpha(\theta) G(U(c(\theta), \frac{z(\theta)}{w(\theta)}))$$
(2)

subject to the constraints

$$c(H) - \psi(z(H)/w(H)) \ge c(L) - \psi(z(L)/w(H)) \quad \text{(IC-}H: \text{ no incentive for } H \text{ types to lie})$$
$$c(L) - \psi(z(L)/w(L)) \ge c(H) - \psi(z(H)/w(L)) \quad \text{(IC-}L: \text{ no incentive for } L \text{ types to lie})$$
$$z(H) + z(L) \ge c(H) + c(L) \quad \text{(B)}$$

Typically, only conditions IC-H and B are binding at the optimum. If high-ability taxpayers are indifferent between their allocation and the allocation of the low-ability taxpayers, then low-ability taxpayers will strictly prefer the allocation that entails less consumption since generating income is more costly for them.

Step 2: implementing the direct mechanism. Once the optimal direct mechanism is characterized, the second step is to reverse-engineer the tax system that would implement the incentives in that optimum. In the simple optimal taxation model presented here, this is straightforward. The income tax function must satisfy  $T(z(\theta)) = z(\theta) - c(\theta)$ , and it must assign sufficiently high punishments to deviations from earning z(H) or z(L). A smooth tax function would, for example, have to satisfy  $(1 - T'(z(\theta)))U_c(c(\theta), z(\theta)/w(\theta)) + \frac{1}{w(\theta)}U_l(c(\theta), z(\theta)/w(\theta)) = 0$  to ensure that individuals do not want to deviate slightly from their assigned allocations  $(c(\theta), z(\theta))$ . Generally, while the optimal direct mechanism is unique, it can be implemented with many different kinds of tax functions.

#### **3.3** Implementation invariance and its failure

In the context of this simple model, we may define implementation invariance as a restriction that taxpayers' preferences over consumption and labor cannot be influenced by the steptwo tax system induced. Consider an individual who chooses a consumption-earnings bundle (c, z) over (c', z') when both options are available. This decision is implementation invariant if any tax system T satisfying z - T(z) = c and z' - T(z') = c' results in the same behavior. The literature reviewed in the previous section suggests violations of this principle arise in situations where inattention, misperception, or heuristics guide decisions.

Notice that individuals whose decisions are not implementation invariant violate basic tenents of optimization appealed to in the statement of the revelation principle. As a result, use of the two-stage proceedure in the previous section is no longer ensured to be valid. This failure may be understood to be generated by a disjoint between the incentivecompatability constraints that restrict a fully-optimal decision maker and the *perceived* incentive-compatibility constraints that govern a biased decision-maker. Stated informally, the incentive-compatability constraint generates a threshold on "how much" you can tax an individual before inducing a misrepresentation of type. If different tax systems generate different natures of misunderstanding, then they similarly generate different such thresholds. This complicates analysis, but also introduces new tools to the policy maker.

It is worth noting that many commonly-studied biases do not operate through this channel of misunderstood incentive compatibility constraints. For example, behavioral models of prospect theory or sophisticated present bias are better understood as cases where the decision maker does accurately understand the constraints faced, but holds an individual utility function that is viewed as normatively undesirable by the social planner (e.g., attending to "irrelevant" reference comparisons or applying impatient time discounting). Cases such as these need not generate violations of implementation invariance; indeed, variants of the mechanism design approach have been successfully applied to these biases (see, e.g., Kanbur *et al.*, 2008; Lockwood, 2015).

#### 3.4 Consequences of the failure of implementation invariance

We use a series of examples to illustrate some broad implications of the violation of implementation invariance. While the consequences we highlight are exposited under highly stylized assumptions, we believe they illustrate the the broader point that the welfare analysis of tax policies can lead to meaningfully different conclusions in the presence of this class of biases. Lesson 1: The optimal tax system may induce a consumption-labor allocation that is different than the one implemented with the optimal direct mechanism. The allocation induced by the optimal tax system may generate higher or lower welfare than would be induced by optimizers under the direct mechanism.

To demonstrate Lesson 1, consider the consequences of the salience of an income tax. Suppose that when individuals choose labor supply, they make decisions based on a perception of the tax represented by  $\tilde{T} = \sigma T$ . When  $\sigma = 1$ , individuals correctly attend to the taxes in place. When  $\sigma > 1$ , taxes are overly salient. When  $\sigma < 1$ , taxes are partially ignored.

To illustrate the impact of salience on welfare, consider first the extreme case where individuals choose labor supply as if there is no tax in place ( $\sigma = 0$ ). In this case, the tax is entirely ignored, and as a result it does not distort behavior: regardless of the tax, individuals choose the efficient level of labor supply satisfying  $\psi'(l(\theta)) = w(\theta)$ . This means that it is possible to achieve full redistribution without creating inefficiencies, simply by choosing a tax function that satisfies z(H) - T(z(H)) = z(L) - T(z(L)). In constrast, under the approach taken in the mechanism design problem of section 3.2, this first-best level of labor supply would be viewed as unobtainable. The presence of this bias facilitates the maximization of our social welfare function.

In contrast, when taxes are overly salient ( $\sigma > 1$ ), the disortionary consequences of a tax are even greater than they would be under the assumption of optimal behavior. Since distortionary motives are the primary cost of redistribution, in this case the presence of this bias hinders the maximization of our social welfare function.

This may be summarized in the following formal result:

**Proposition 1.** At the optimal tax system, the social welfare function expressed in equation 1 is decreasing in scaling parameter  $\sigma$ . When  $\sigma < 1$ , the welfare that results in the optimal tax system is higher than would be obtained by optimizers under the optimal direct mechanism. When  $\sigma > 1$ , the welfare that results in the optimal tax system is lower than would be obtained by optimizers under the optimal direct mechanism. Lesson 2: The allocation implemented by the optimal direct mechanism may not be implementable by any income tax. Conversely, equilibrium allocations obtainable under some biases may not be implementable by a direct mechanism among optimizers.

We illustrate this point by a simple example of a taxpayer who adopts the ironing heuristic. As reviewed in section 2.2.2, this taxpayer perceives the tax schedule to be linear, with slope  $\tau(z(\theta)) = T(z(\theta))/z(\theta)$ . Further suppose that  $\psi(l) = l^2/2$ .

Under the direct mechanism, the binding IC constraint is given by

$$c_H - c_L = \frac{z_H^2 - z_L^2}{2w_H^2} \quad \text{(Direct Mechanism IC)} \tag{3}$$

Under ironing, the misperception of the tax schedule leads to the different first-order condition  $1 - T(z_{\theta})/z_{\theta} = z_{\theta}/w_{\theta}^2$ . Since  $c_{\theta} = z_{\theta} - T(z_{\theta})$ , this implies that  $c_{\theta}/z_{\theta} = z_{\theta}/w_{\theta}^2$ , and thus that  $c_{\theta} = z_{\theta}^2/w_{\theta}^2$ . Thus under ironing, the consumption allocations must satisfy

$$c_H - c_L = \frac{z_H^2}{w_H^2} - \frac{z_L^2}{w_L^2} \quad \text{(Ironing IC)} \tag{4}$$

Generically, it cannot be the case that  $\frac{z_H^2}{w_H^2} - \frac{z_L^2}{w_L^2} = \frac{z_H^2 - z_L^2}{2w_H^2}$ , which yields the result. More generally, in Proposition 2 below we show that the result holds without the assumption that  $\psi(l) = l^2/2$ .

**Proposition 2.** Consider the social welfare function expressed in equation 1 and suppose individuals are ironers. Generically, there does not exist a tax function T that implements the allocation of the optimal direct mechanism. Moreover, the resulting allocation of consumption that is obtained from directly solving for the optimal tax function T cannot be implemented using a direct mechanism.

This leads to the broader lesson that the set of allocations that are are feasible when taxpayers are perfect optimizers might not be feasible when considering taxpayers' imperfect reactions to "real-world" policy tools. Conversely, desirable "real-world" outcomes may seem infeasible when analyzed under the assumption of perfect optimization.

## Lesson 3: The reaction to information asymmetries that generates the key tension of the mechanism design approach may be mitigated or eliminated.

Recall that in the standard model, perfect redistribution is not possible because the high type must have incentives that are high enough to not imitate the low type. With  $\psi(l) = l^2/2$ , this incentive compatibility constraint is presented in equation (3). The constraint captures the key innovation of optimal tax analysis in the spirit of Mirrlees (1971): because of asymmetric information, taxes can still be distortionary even without any "arbitrary" constraints such as linearity. The optimal taxation problem thus builds on broader principles of mechanism design of maximizing transfers from the high types by paying them minimal "information rents."

Misperceptions of taxes can fundamentally change the principles of optimal tax analysis, and may completely eliminate the role of concepts such as "information rents." Indeed, this outcome has already been demonstrated when discussing Lesson 1 above, in which distortionary behavior was eliminated in the case where perceived taxes were scaled to zero. Intuitively, these findings mirror the growing set of demonstrations that behavioral biases can mitigate the negative consequences of information asymmetries in insurance markets, for the similar reason that agents cannot claim rent for information that they have ignored (Handel, 2013; Handel & Kolstad, 2015; Handel *et al.*, 2015; Spinnewijn, 2017). While the assumptions of the illustration in Lesson 1 are extreme, more generally the impact of heuristics and biases can be to mitigate the role of information rents and to push optimal tax analysis more towards the mechanics represented in models of Ramsey taxation.

We illustrate this idea by demonstrating the reversal of a core principle of taxation: that

in the presence of income taxation, commodity taxes should only be used if they help to target taxes to those of high earnings ability.

Consider, following Stiglitz (1982), and extension to the model of section 3.1, in which individuals choose before-tax income z and a consumption bundle  $(c_1, c_2)$ . One interpretation is that  $c_1$  and  $c_2$  are different commodities. Another interpretation is that  $c_1$  is period 1 consumption and  $c_2$  is period 2 consumption. For simplicity, assume that  $U(c_1, c_2, l, \theta) =$  $u(c_1) + v(c_2, \theta) - \psi(l)$ .

In the standard model, when both types L and H have the same subutility  $v(c_2, \theta) \equiv v(c_2)$ , the optimal allocation must always satisfy  $v'(c_2(\theta)) = u'(c_1(\theta))$  for each type (Stiglitz, 1982). This means that linear, nonlinear, or means-tested taxes on  $c_2$  are *not* justified when different types' preferences are homogeneous. This result is not specific to a two-type model and holds more generally for a continuum of types (Atkinson & Stiglitz, 1976; Saez, 2002; Golosov *et al.*, 2013).

For unbiased consumers, taxes (or subsidies) on  $c_2$  are justified only when they can be used to better screen between low and high types. When those of higher earnings ability have a greater preference for  $c_2$  (i.e.,  $\frac{v_{c_2(c_2,\theta)}}{u'(c_1)}$  is increasing in  $\theta$ ), it then becomes optimal to have some form of a tax on  $c_2$ .<sup>1</sup> Greater consumption of  $c_2$  now serves as an additional signal that an individual has high earnings ability, and thus taxing these individuals can efficiently increase the redistributive properties of the tax system. Explicit formulae for optimal taxes on  $c_2$  are complex, however, as they depend intricately on the informational advantages that the commodity taxes have over the income tax.

The case for commodity taxation can be fundamentally affected by the presence of more realistic psychological assumptions. In particular, the psychological assumption that individuals perfectly compute the labor-supply incentives induced by commodity taxes is quite demanding; more realistically, consumers might at least partially neglect the labor-supply incentives induced by taxes on  $c_2$ . This leads to optimal tax formulas that are closer to the

<sup>&</sup>lt;sup>1</sup>Conversely, when higher types have a lower preference for  $c_2$ , it is optimal to have some form of a subsidy on  $c_2$  (Atkinson & Stiglitz, 1976; Saez, 2002; Golosov *et al.*, 2013).

Ramsey case, and rely less on the extent to which consumption of  $c_2$  serves as a tag for an individual being a high type.

To illustrate formally, suppose the government chooses an income tax T(z) on before-tax earnings and a linear commodity tax t on  $c_2$ . The individual first chooses earnings z and a consumption bundle  $c_1$  and  $c_2$  such that  $c_1 + (1 + t)c_2 \leq z - T(z)$ . Suppose, however, that individuals neglect to consider the tax t on  $c_2$  when choosing their labor supply, and only react to the commodity tax after they have generated their income and are observing the after-tax prices of both  $c_1$  and  $c_2$ . Letting  $g(\theta)$  denote the social marginal utility of income to a type  $\theta$ , the effects of increasing the commodity tax are now as follows:

- A decrease in revenue following a substitution away from  $c_2$ , given by  $tdc_2 = -t\zeta \frac{\bar{c}_2}{1+t}dt$ , where  $\bar{c}_2$  denote aggregate consumption of  $c_2$  and  $\zeta$  is the price elasticity of (aggregate) demand for  $c_2$ .
- A mechanical revenue effect given by  $\bar{c}_2 dt$
- A mechanical welfare effect given by  $-E[g(\theta)c_2(\theta)]dt$

The sum of these effects must be zero at the optimum:

$$-t\zeta \frac{\bar{c}_2}{1+t}dt + \bar{c}_2dt - E[g(\theta)c_2(\theta)] = 0.$$

Solving the above equation for t then yields the following result:

**Proposition 3.** When individuals are inattentive to the commodity tax on the labor supply margin, the optimal commodity tax t satisfies

$$\frac{t}{1+t} = \frac{\lambda - E[g(\theta)\tilde{c}_2(\theta)]}{\lambda\zeta}$$
(5)

where  $\tilde{c}_2(\theta) = c_2(\theta)/\bar{c}_2$  is the share of  $c_2$  consumption by type  $\theta$ , and  $\lambda$  is the marginal value of public funds.

There are several noteworthy features of formula (5). First, notice that it is the standard Ramsey formula with redistributive concerns (Diamond, 1975). Second, notice that the formula holds regardless of the extent to which preferences for  $c_2$  differ between high and low types: whether the Engel curve for  $c_2$  is driven by income effects or heterogeneous preferences correlated with earnings ability does not matter. In contrast to the core lessons from mechanism design, the formula for the optimal commodity tax here does not depend at all on the extent to which introducing distortions to  $\frac{v_{c_2(c_2,\theta)}}{u'(c_1)}$  allows the designer to reduce the information rents that must be payed to the high types. This is because individuals ignore the tax t on the labor supply margin, and thus the presence of the income tax does not fundamentally change the basic logic fleshed out in the classical Ramsey approach.

## 4 Discussion

We have argued that the growing body of evidence supporting the failure of implementation invariance poses significant problems for the mechanism design approach to tax analysis. If the manner in which taxes are implemented is fundamentally intertwined with the manner in which decisions are made, the two-stage procedure of separating the question of optimal behavior under direct mechanisms from the question of implementing the direct mechanism poses a difficult foundation for the integration of psychological realism. Instead, the two questions of computing optimal feasible allocations and the implementation of these allocations must be considered simultaneously.

The simultaneous consideration of these two questions is implicit in the alternative approach summarized by Diamond & Saez (2011), which is to to first write down a limited set of possible tax instruments and then to optimize over those instruments. Within this framework, a particularly fruitful technique has been to express optimal tax formulas in terms of measurable "sufficient statistics" such as elasticities or social marginal welfare weights. Because of the emphasis on measurable responses to actual tax instruments, this approach is

more easily extended to incorporate psychological biases. The key additional statistic needed to compute optimal tax policy is a price-metric measure of bias: a monetized measure of the difference between what people would optimally do and what they actually do.

#### 4.1 A concrete illustration of the sufficient statistics approach

To provide a more concrete illustration of the sufficient statistics approach, we summarize the formula provided by Farhi & Gabaix (2015) for a nonlinear income tax with a continuum of productivity types, and for utility functions of the form  $U(c, l) = c - \psi(l)$ . In particular, assume that individuals perceive the actual income tax T to be  $\tilde{T}$ , where  $\tilde{T}(z)$  depends the actual income tax T(z) on earnings z, as well as the the individual's actual earnings  $z^*$  and the tax paid on those earnings  $T(z^*)$ .

This formulation captures both the salience and ironing examples studied in the previous section. In the case of salience,  $\tilde{T}(z) = \sigma T(z)$ . In the case of ironing,  $\tilde{T}(z) = T(z^*) + (z - z^*) \frac{T(z^*)}{z^*}$ .

Farhi & Gabaix (2015) show that for this broad class of misperceptions, the optimal tax rates depend on the sum of two terms. The first term is just the standard optimal tax formula for rational consumers, as characterized by Saez (2001). This depends on the governments' redistributive preferences as well as the usual measurable statistics: the distribution of earned income and the elasticity of taxable income with respect to the marginal tax rate.<sup>2</sup>

The second term, denoted  $\tilde{\tau}^b(z)$  is essentially a price metric for consumers biases. This terms answers the following question: If consumers were fully debiased, by what percent would the marginal keep rate, 1 - T'(z), need to be increased so that consumers choose the same amount of labor as they do in the biased state. Formally,  $\tilde{\tau}^b(z) = \frac{(1-T'(z))-\frac{1}{2}\psi'(z/w)}{1-T'}$ .

$$\frac{T'(z)}{1 - T'(z)}$$

<sup>&</sup>lt;sup>2</sup>To define this term formally, let H be the cumulative density function of income, with a probability density h. Let  $\zeta$  be the elasticity of taxable income with respect to the keep rate 1 - T'(z). Let  $h^*$  be the "virtual density"  $h^*(z) := \frac{h(z)}{1 - T'(z) + \zeta z T''(z)}$ . Then the optimal income tax satisfies

where  $\lambda$  is the marginal value of public funds and g(z) is the social marginal utility of income to a z-earner.

With these two terms in hand, Farhi & Gabaix (2015) show that the optimal income tax satisfies

$$\frac{T'(z)}{1 - T'(z)} = \frac{T'(z)}{1 - T'(z)} \tag{6}$$

Formula (6) provides an immediate characterization of the optimal income taxes for the salience and ironing biases we have discussed. In the case of salience, we have  $\tilde{\tau}^b(z) = -(1-\sigma)\frac{T'(z)}{1-T'(z)}$ , which leads to the simple formula  $\frac{T'(z)}{1-T'(z)} = \frac{1}{\sigma} \cdot \frac{T'(z)}{1-T'(z)}$ . In the case of ironing, we have  $\tilde{\tau}^b(z) = 1 - \frac{A(z)}{1-T'(z)}$ , which can also be plugged into (6) to obtain a formula for the optimal income tax.

An under-appreciated insight is that while  $\tilde{\tau}^b(z)$  could be the result of many different psychologies, the empirical strategy used to quantify  $\tilde{\tau}$  does not have to depend on the psychology in play, and can be largely an extension of standard revealed preference methods. Once the "welfare-relevant domain" (Bernheim & Rangel, 2009) is identified, the bias measure is constructed as the wedge between choices in the welfare relevant domain and the choices normally observed.

In the case of sales taxes, Chetty *et al.* (2009) and Taubinsky & Rees-Jones (2017) compute such price metrics of bias directly. The basic idea of the empirical strategy is to compute the change in upfront prices that would alter demand as much as a debiasing intervention that displays tax-inclusive final prices.

A simple example of empirically quantifying such bias price-metrics in a non-income tax domain is provided by Allcott & Taubinsky (2015), who run an experiment that provides a direct estimate of bias for each consumer's valuation of energy efficient lightbulbs (CFLs). They compute willingness to pay (WTP) for more versus less energy efficient lightbulbs in a standard market frame, and then measure how the distribution of WTP changes when biases arising from inattention or incorrect beliefs are eliminated via an informational intervention that directs attention.

In some cases, such direct experiments may not be possible to run, as is the case for

income taxes. However, other strategies for measuring bias are still available. For example, Rees-Jones & Taubinsky (2016) run a survey experiment eliciting individual's perceptions of the US income tax and find evidence that the ironing heuristic is adopted by 30-40% of US tax filers.

These empirical strategies illustrate that sufficient statistics formulas such as (6) are fully implementable using standard methods for estimating elasticities, and extensions of standard revealed preference methods for computing price-metric measures of bias.

#### 4.2 Challenges for future work

An important challenge with extending the sufficient statistics approach to incorporating individuals' mistakes is the critical need to have individual-level measures of biases, rather than just population means. Allcott & Taubinsky (2015) point out that in evaluating the welfare impact of tax change, it is necessary to know the bias of the consumers who are marginal to that tax change, which may be very different from the population average. They show that without restrictive assumptions, the only way to obtain the bias of marginal consumers at different levels of the policy is to estimate bias at the individual level. Taubinsky & Rees-Jones (2017) show that without homogeneity assumptions, Chetty et al.'s (2009) measure of aggregate underreaction to taxes is not actually a sufficient statistic for computing efficiency costs. Rather, Taubinsky & Rees-Jones (2017) show that both the mean and the variance of consumers' misreaction are together necessary and sufficient for computing efficiency costs—i.e., that some knowledge of heterogeneity across individuals is necessary for understanding welfare effects.

The broad principle behind this additional challenge is that in a standard model of optimizing consumers, marginal benefits must equal the marginal costs or the price at the margin. Thus, even if consumers are heterogeneous, their valuations for, e.g., the product they are buying are homogeneous on the margin. This "marginal homogeneity" is what makes it possible to calculate welfare by observing only aggregate changes in behavior. In the presence of behavioral biases, however, marginal benefits do not equal marginal costs, and this wedge will be heterogeneous when consumers are heterogeneous in their bias. The greater the heterogeneity on the margin, the lower is welfare.

The need for individual-level measurement does not fundamentally change the principles by which the standard sufficient statistics approach must be adapted, nor does it fundamentally change the strategies for how bias should be measured. However, it does require especially rich data sets that allow for robust measurement at the individual level. Observational or quasi-experimental data of this type is not always available, requiring researchers to design new experiments that allow more granular measurement (Taubinsky & Rees-Jones, 2017). As the literature progresses, an iterative application of the sufficient statistics approach to welfare, paired with local measurement of heterogeneous biases used to inform improvements to tax policy, appears to be both a conceptually justified and practically implementable approach to the development of empirically informed tax policy.

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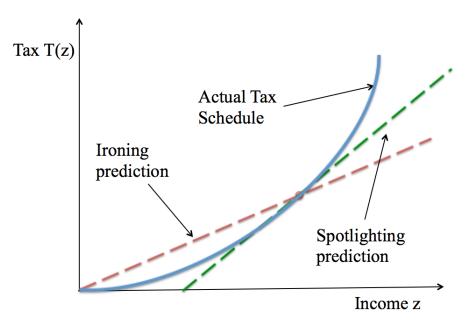
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Figure 1: Heuristics for approximating a tax schedule



*Notes:* This figure presents an illustration of the ironing and spotlighting heuristics applied to a generic convex schedule. When using these heuristics, the taxpayer linearizes the convex schedule according to parameters local to his own position on the schedule, indicated by the red dot. Under the ironing heuristic, the taxpayer forecasts by applying his average tax rate at all points, resulting in the observed secant line. Under the spotlighting heuristic, the taxpayer forecasts by applying his marginal tax rate to the change in income that would occur, resulting in the observed tangent line.

Source: Rees-Jones & Taubinsky (2016).